

# Resonance depolarization method

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- 1 Introduction
- 2 The idea of the method
- 3 Radiative polarization
- 4 Polarization measurement
  - Touschek polarimeter at VEPP-4M
  - Laser polarimeter at VEPP-4M
- 5 Summary

# Introduction

- Precision measurement of the mass of the elementary particles in colliding experiments requires precise beam energy calibration

## Resonance depolarization technique

- The most precise method of beam energy measurement
- $\Delta E/E \sim 10^{-6}$
- Suggested and firstly applied in BINP (Novosibirsk) at 1971  
*Baier, Sov. Phys. Usp. 14 695–714 (1972)*
- Used in experiments of precise mass measurement in the wide energy range  
*Skrinskii, Shatunov, Sov. Phys. Usp. 32 548–554 (1989)*
- Energy calibration for some synchrotron light sources: ESSY-I, BESSY-II, ALS, SLS, ANKA, SOLEIL

# Used in experiments of precise mass measurement

Particle	Experiment		Date
$\Phi, K^\pm$	VEPP-2M	OLYA	1975-1979
$J/\psi, \psi(2S)$	VEPP-4	OLYA	1980
$\Upsilon(1S), \Upsilon(2S), \Upsilon(3S)$	VEPP-4	MD-1	1982-1986
$\Upsilon(1S)$	CESR	CUSB	1984
$\Upsilon(2S)$	DORIS II	ARGUS, Crystal Ball	1983
$K^0, \omega$	VEPP-2M	CMD	1987
$Z$	LEP	ALEPH, DELPHI, L3, OPAL	1993
$J/\psi, \psi(2S), \tau, D^0, D^\pm, \psi(3770)$	VEPP-4M	KEDR	2003-2015

# The idea of the method

## Spin precession

Frenkel, Thomas (1926),

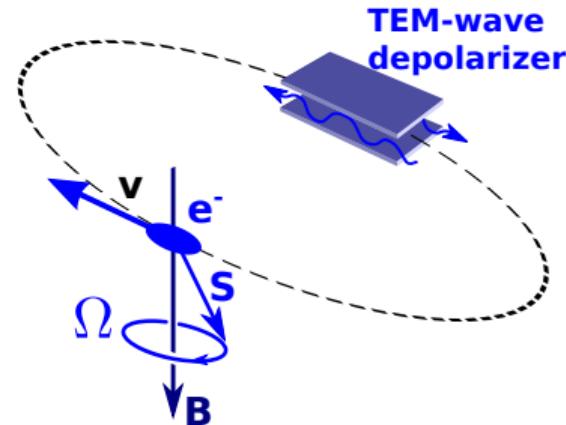
Bargmann, Michel, Telegdi (1959)

$$\frac{ds^i}{d\tau} = 2\mu F^{ij} s_j - 2\mu' u^i F^{jk} u_j s_k$$

$$\frac{d\vec{s}}{dt} = \underbrace{2\mu \frac{\vec{s} \times \vec{B}'}{\gamma}}_{\text{dynamic}} + \underbrace{(\gamma - 1) \frac{\vec{s} \times [\vec{v} \times \dot{\vec{v}}]}{v^2}}_{\text{kinematic (Thomas) precession}} = \vec{\Omega} \times \vec{s}$$

$$\Omega = \omega_0 \left(1 + \gamma \frac{\mu'}{\mu_0}\right) = \omega_0 n \pm \omega_d, \quad n \in \mathbb{Z}$$
$$\delta(\mu'/\mu_0) \approx 2.3 \times 10^{-10} \quad \delta m_e \approx 2.2 \times 10^{-8}$$

$$E = (440.6484431 \pm 0.0000097) [\text{MeV}] \times \left(n - 1 \pm \frac{\omega_d}{\omega_0}\right)$$



# Energy calibration accuracy

- ① Measurement of the spin precession frequency by resonance depolarization ( $\sim 1\text{keV}$ )
- ② Calculation of average beam energy ( $\sim 2\text{keV}$ )
- ③ Calculation of average beam energy at the interaction point ( $\sim 1\text{keV}$ )
- ④ Calculation of luminosity weighted average c.m. energy ( $\sim 1\text{keV}$ )

More about corrections and errors to center of mass energy

*Bogomyagkov, et al., RUPAC-2006-MOAP02.*

*Nikitin, RUPAC-2006-MOAP01.*

*Bogomyagkov, et al., Conf. Proc. C 070625 (2007) 63.*

# Radiative polarization

## Sokolov-Ternov effect (1963)

Sokolov, Ternov, Dokl.Akad.Nauk SSSR 153 (1963) no.5, 1052-1054

Intensity of SR with spin flip

$$W^{\uparrow\downarrow} \approx W_0 \frac{4}{3} \left( \frac{\omega_c}{E} \right)^2$$

$$\tau_p = P_0 \frac{\lambda_c}{\alpha c} \frac{1}{\gamma^2} \left( \frac{H_0}{H} \right)^3 \quad P_0 = \frac{8 \sqrt{3}}{15} \approx 92.4\%$$

First observation

- VEPP-2 (Novosibirsk) in 1970

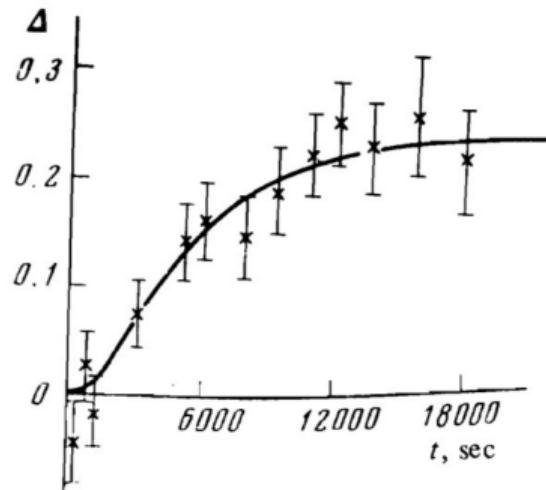
Baier, Sov. Phys. Usp. 14 695–714 (1972)

- ACO storage ring (Orsay) in 1972

Duff, Marin, Masnou, Sommer, Preprint, Orsay 4-73(1973)

Radiative polarization at VEPP-2M observed with Touschek polarimeter,  $\tau = 70$  min (1974)

Serednyakov, Skrinskii, Tumaikin, Shatunov, JETP, V44, No. 6, p.1063 (1976)



$$P(t) = P \frac{\tau}{\tau_p} \left( 1 - e^{-t/\tau} \right); \quad \tau = \frac{\tau_d \tau_p}{\tau_p + \tau_d}$$

# Depolarizing resonances

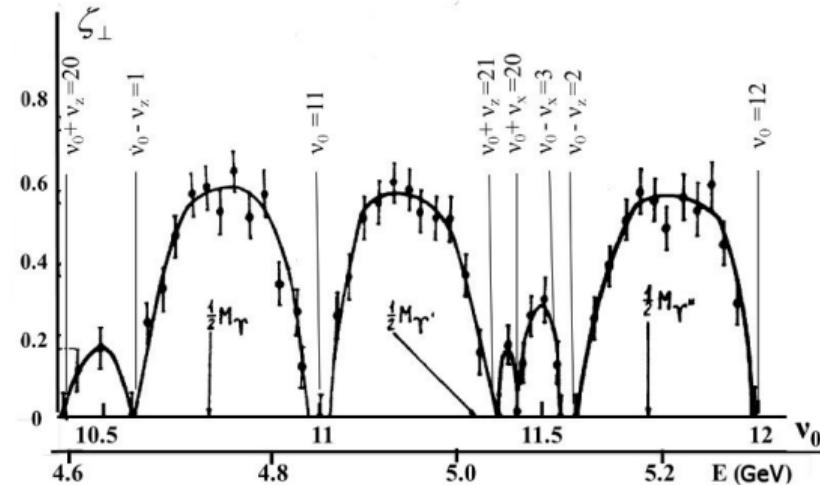
$$\nu = \frac{\Omega}{\omega_0} - 1 = k \cdot \nu_x + l \cdot \nu_y + m \cdot \nu_s + n \quad k, l, m, n \in \mathbb{Z}$$

- Stochastic depolarization

$$\tau_d \sim \left( \nu_0^2 \sum \frac{|w_k|^2}{(\nu_0 - \nu_k)^4} \right)^{-1}$$

- Difficult to accelerate polarized beam due to resonance cross
- Spin precession shift

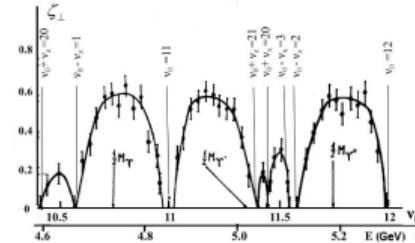
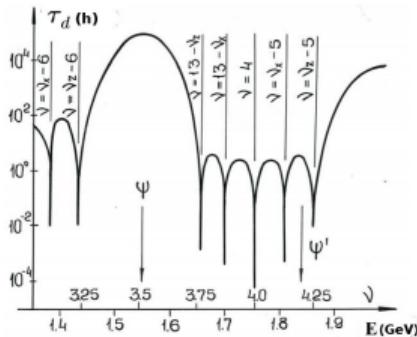
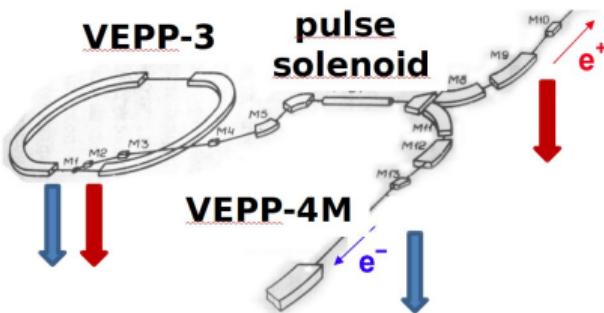
$$\delta\nu \sim \frac{1}{2} \sum \frac{|w_k|^2}{\nu_0 - \nu_k}$$



Equilibrium polarization degree measurement at VEPP-4 with laser polarimeter.

## Obtaining polarization at VEPP-4M

## Polarized beam injection into VEPP-4M ring



## Polarization time

Ring	VEPP-3	VEPP-4M
$\tau_p$ [h]	$\frac{12}{E[\text{GeV}]^5}$	$\frac{1540}{E[\text{GeV}]^5}$
$\tau_p$ @ 1.55 GeV	1.34 h	172 h
$\tau_p$ @ 1.85 GeV	0.56 h	71 h
$\tau_p$ @ 4.1 GeV		80 min
$\tau_p$ @ 4.73 GeV		39 min

- Good beam polarization for  $J/\psi$ ,  $\psi(2S)$ ,  $\Upsilon(1S)$ ,  $\Upsilon(3S)$
  - Problem with  $\tau$  lepton energy region (close to integer  $\nu = 4$  resonance)

# Polarization measurement

- Fixed target
  - Mott scattering (spin orbit coupling,  $100\text{keV} < E < 5 \text{ MeV}$ ): JLab
  - Moller scattering (atomic electron,  $\lesssim 1 \text{ GeV}$ ): JLab, BINP, ...
- Touschek (intrabeam scattering) polarimeter (BINP, BESSY-I/II, ALS, SLS...).  
Best for lower energies  $E < 2 \text{ GeV}$
- Compton backscattering (better for high energies  $E > 5 \text{ GeV}$ )
  - laser: Cornell (CESR), DESY (DORIS), BINP (VEPP-4), SLAC (SLD) ...
  - synchrotron light from clashing (positron) beam: BINP (VEPP-2M, VEPP-4)
- Synchrotron spin-light: BINP (VEPP-4)
- ...

# Touschek polarimeter

- Proposal to use beam lifetime to detect polarization in 1968 (flat beam calculation)

Baier, Khoze, Atomnaya Énergiya, V25, No.5, pp. 440–442 (1968)

- Tumaikin's proposal to use scint. counters (1970)

- Calculation for 2D beam

Serednyakov, Skrinskii, Tumaikin, Shatunov, JETP, V44, No. 6, p.1063 (1976)

- With some relativistic corrections (1978)

Baier, Katkov, Strakhovenko, Dokl.Akad.Nauk SSSR, 1978, V241,No4, P.797–800

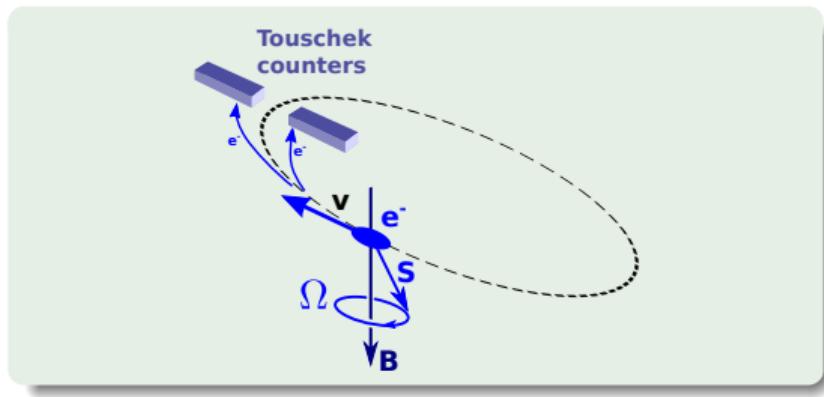
- with Coulomb effects (1978)

Baier, Katkov, Strakhovenko, Dokl.Akad.Nauk SSSR, 1978, V241,No4, P.797–800

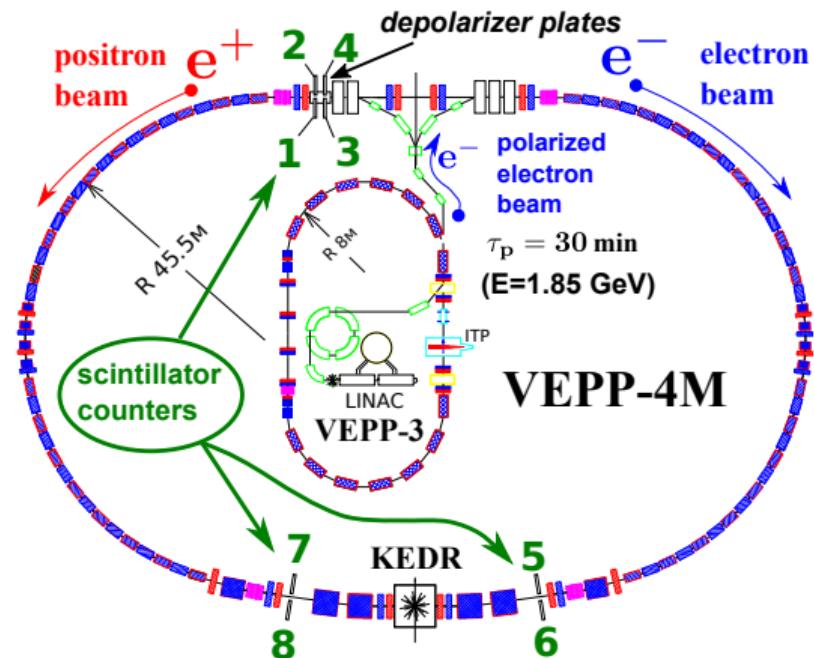
Intra-beam scattering ( $e^-e^- \rightarrow e^-e^-$ ) scattering

$$d\sigma = d\sigma_0 \left( 1 - (\vec{s}_1 \cdot \vec{s}_2) \frac{\sin^2 \theta}{1 + 3 \cos^2 \theta} \right)$$

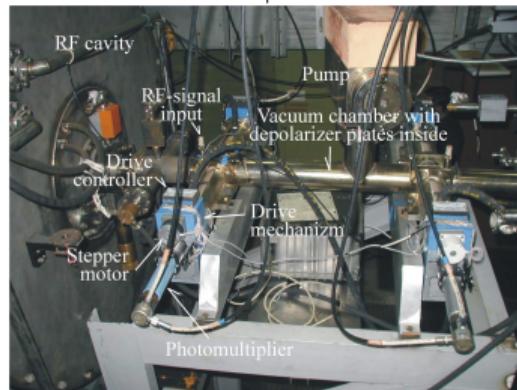
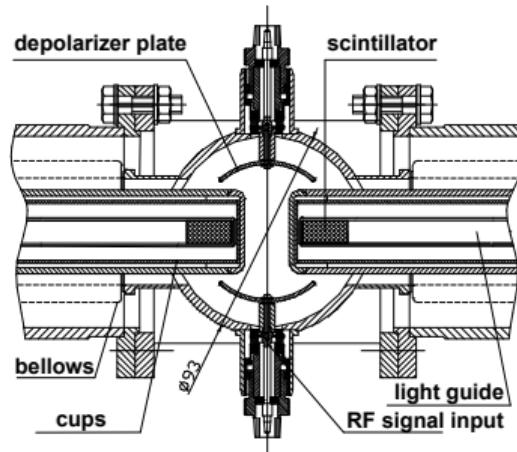
$$\frac{dN}{dt} \approx A \frac{N^2}{V\gamma^2(\Delta p/p)^2} (1 - P^2\eta)$$



# Touschek polarimeter at VEPP-4M



8 movable scintillator counters located inside vacuum chamber at different places of VEPP-4M

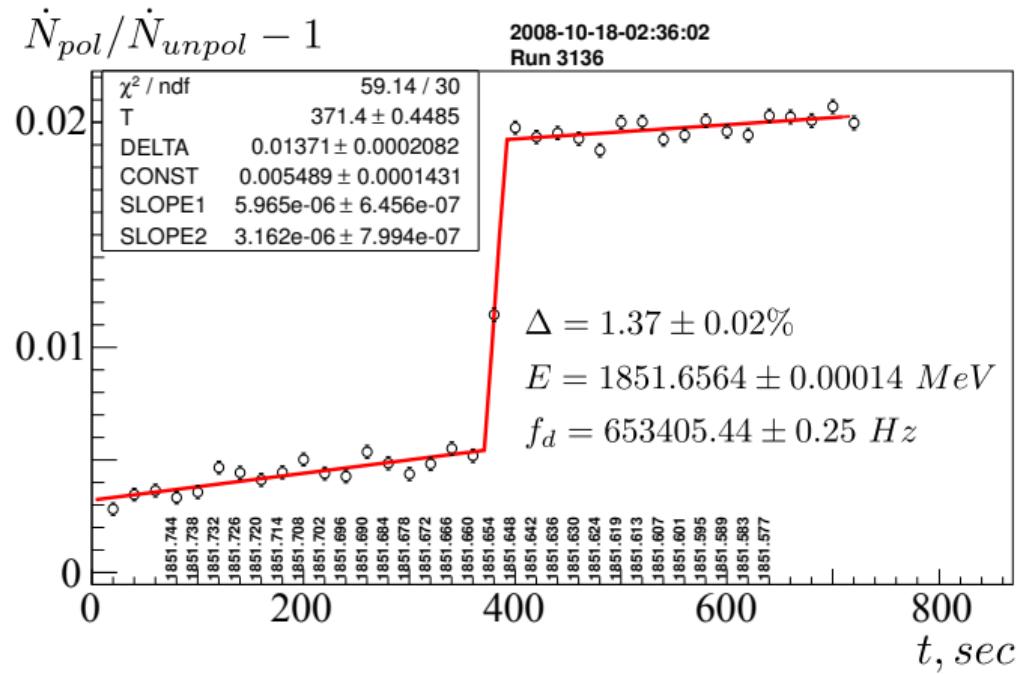


# Touschek polarimeter at VEPP-4M

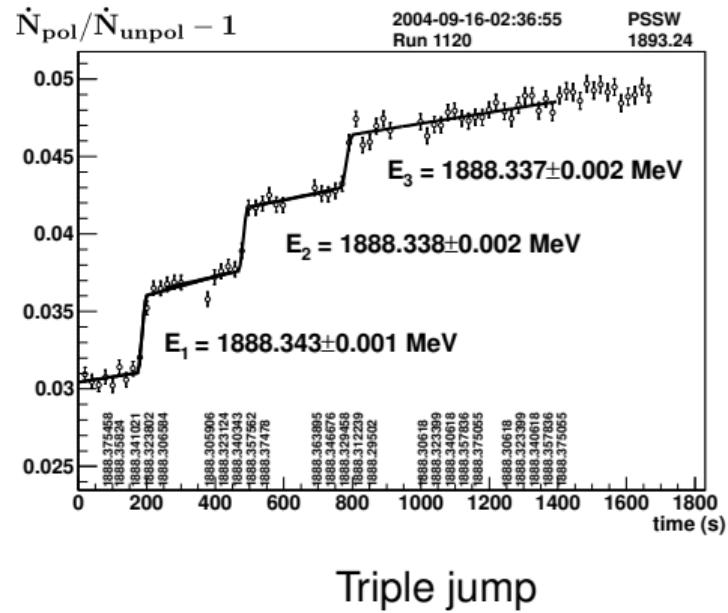
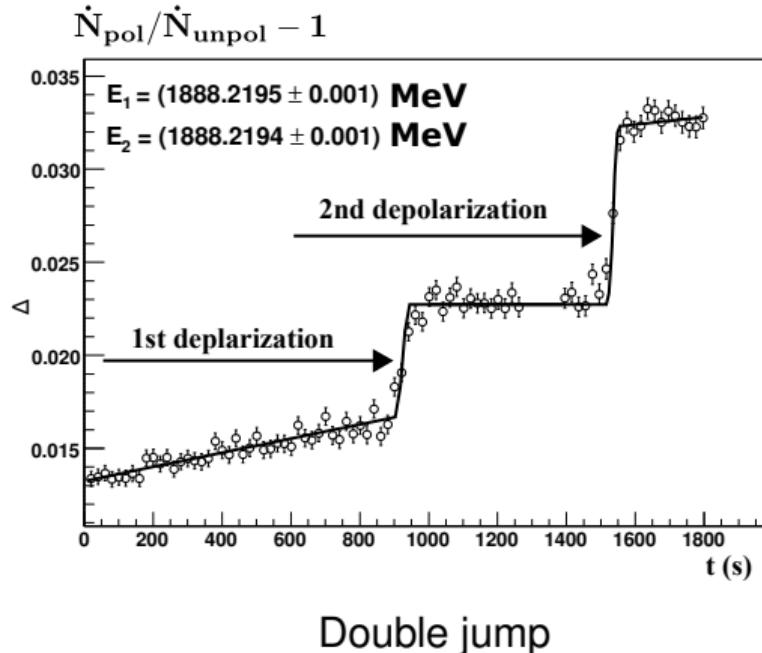
## System performance

Energy range	1.5 ÷ 2.0 GeV
Beam current	> 0.1 mA
Number of bunches (electron or positron)	4
Count rate	1 MHz (50 kHz/mA <sup>2</sup> /counter)
Compensation technique	$\Delta = \dot{N}_{pol}/\dot{N}_{unpol} - 1$
Depolarization effect	$\Delta = 1 \div 3 \%$
Polarization degree	≈ 80%
Stat accuracy	1 keV (10 <sup>-6</sup> )
Number of calibration at same bunches	3
Calibration duration	2 hours
Number of energy calibrations since 2001	≈ 4000

# Energy calibration example



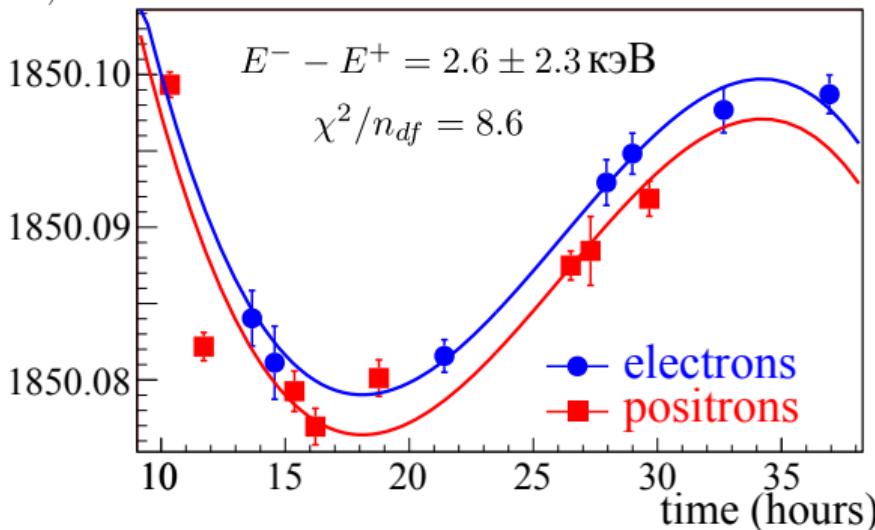
Several calibrations with same polarized bunch



Double up-down scan increase reliability of energy calibration.  
Suppress cases of calibration at side 50 Hz spin resonances

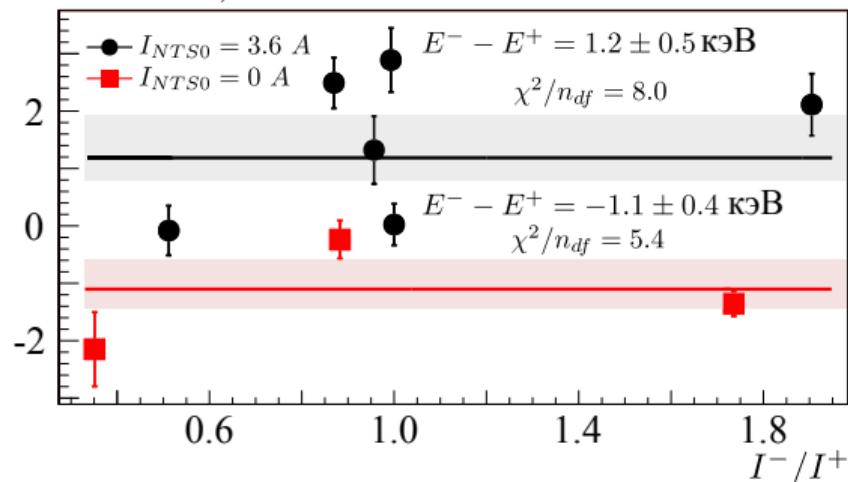
# Electron and positron energy comparison

$E, \text{MeV}$



serial interlaced  $e^-/e^+$  energy calibrations

$E^- - E^+, \text{keV}$



simultaneous  $e^-/e^+$  energy calibrations

Investigating systematics of energy calibration for  $J/\psi, \psi'$  mass measurement experiment

# Energy calibration accuracy

## Single beam energy measurement error

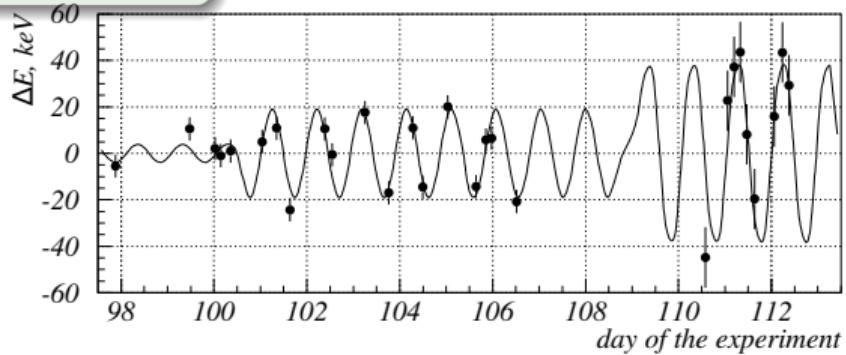
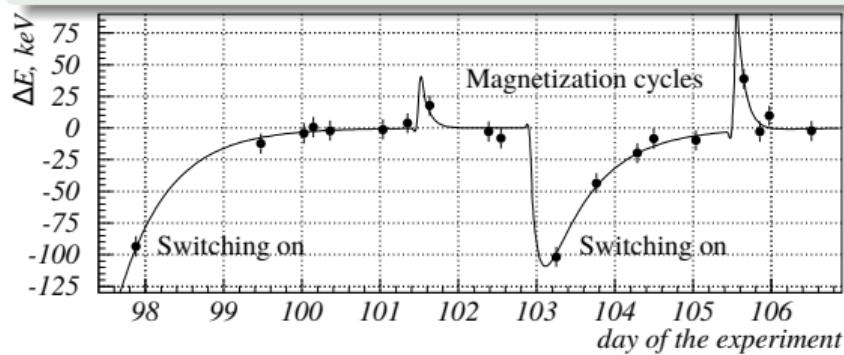
source	$\Delta E$ , keV
Precession frequency measurement	$\pm 1.0$
Spin resonance width	$2.0 \pm 1.0$
Vertical close orbit disturbances	$-0.4 \pm 0.3$
Coherent loss asymmetry	0.1
KEDR longitudinal field compens.	0.1
total	$1.5 \text{ keV ( } 10^{-6} \text{ )}$

# Energy interpolation between calibrations

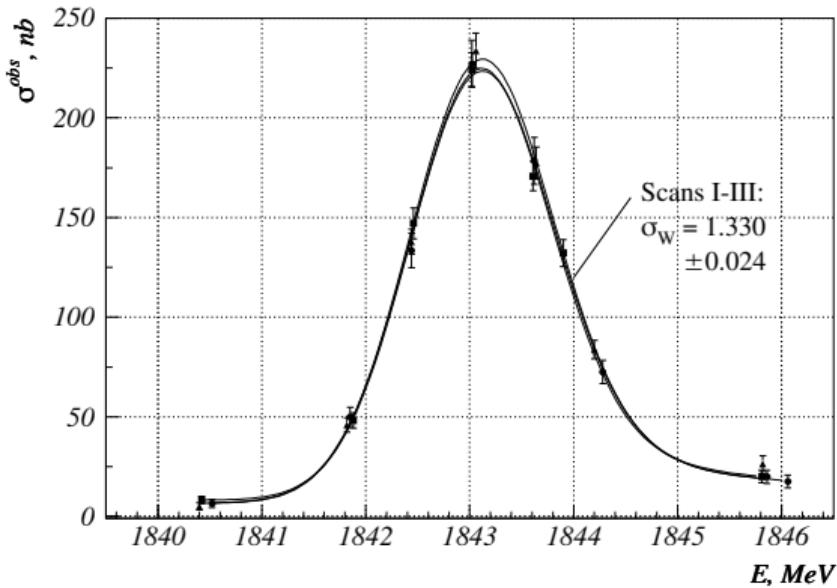
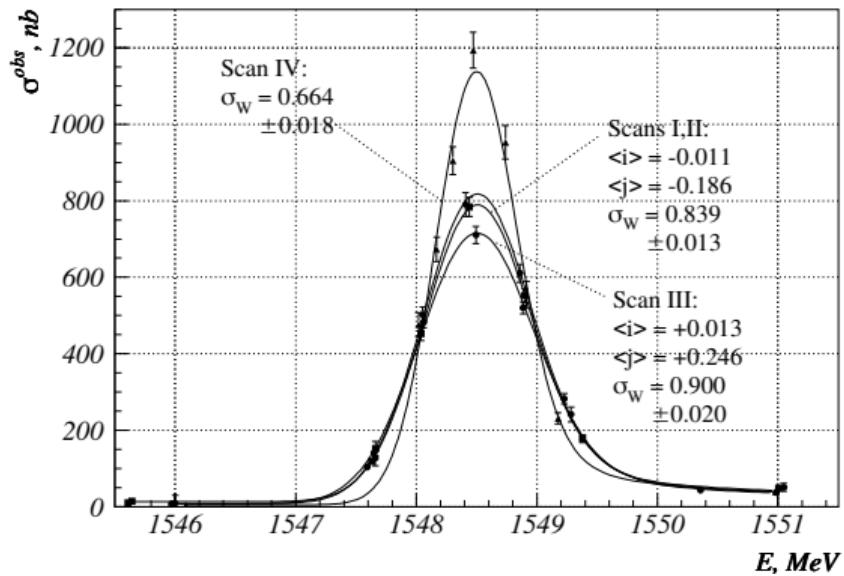
## Energy prediction function

$$E = \alpha_H \cdot H_{\text{NMR}} \cdot (1 + \alpha_T \cdot (T_{\text{ring}} - T_{\text{NMR}})) \times f(T_{\text{ring}}, T_{\text{air}}, T_{\text{water}}) + \\ + A(t) \cdot \cos\left(\frac{2\pi t}{\tau_{\text{day}}} - \varphi(t)\right) + \\ \delta E_{\text{on}} \cdot \exp\left(-\frac{t_{\text{on}}}{\tau_{\text{on}}}\right) + \delta E_{\text{cycle}} \cdot \exp\left(-\frac{t_{\text{cycle}}}{\tau_{\text{cycle}}}\right) + E_0(\Delta i, t),$$

Energy prediction 6 ÷ 8 keV with  
218 energy calibrations



## $J/\psi$ ( $0.7, pb^{-1}$ ), $\psi(2S)$ ( $1.0 pb^{-1}$ ) mass measurement with KEDR detector



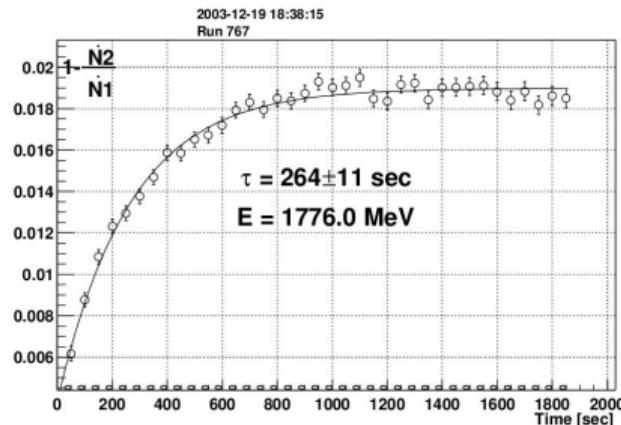
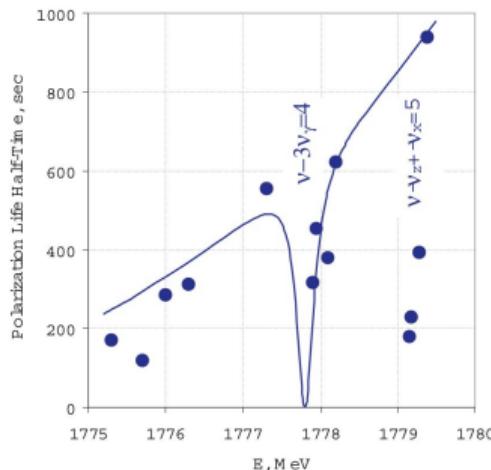
$$M_{J/\psi} = 3096.900 \pm 0.002 \pm 0.006 \text{ MeV}$$

$$M_{\psi(2S)} = 3686.099 \pm 0.004 \pm 0.009 \text{ MeV}$$

KEDR Collaboration / Phys.Lett.B 573 (2003) 63–79  
Anashin et al. / Phys.Lett.B 749 (2015) 50–56

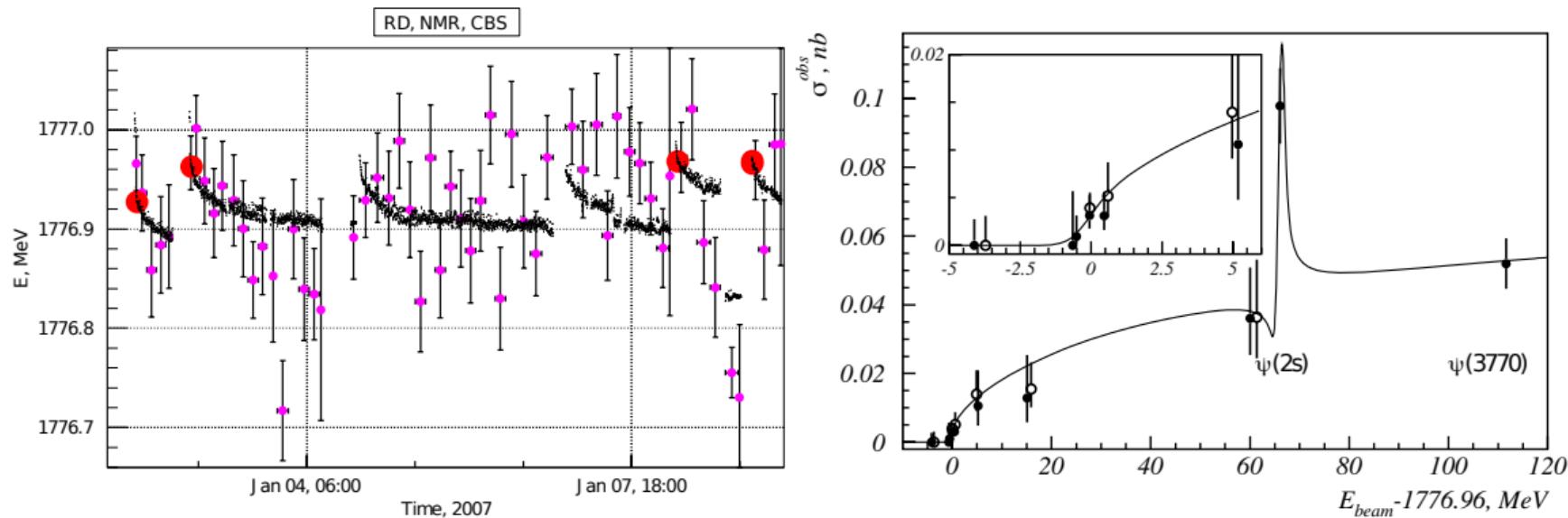
# Energy calibration in tau mass experiment

- Tau threshold (1.78 GeV) close to  $\nu = 4$  integer spin resonance ( $E=1.76$  GeV).  
No polarization in VEPP-3.
- Special effort to increase polarization lifetime at tau threshold were done.



- Polarization at 1.85 GeV and deaccelerate to tau threshold
- Energy calibration after 30 min magnetic field relaxation

# Energy calibration in tau mass experiment

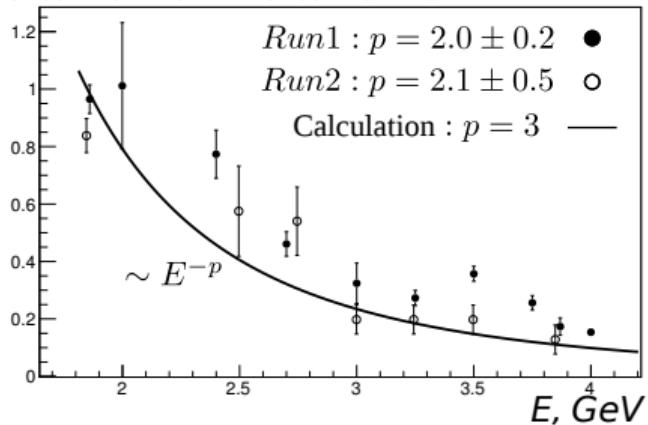


$$M_\tau = 1776.69^{+0.17}_{-0.19} \pm 0.15$$

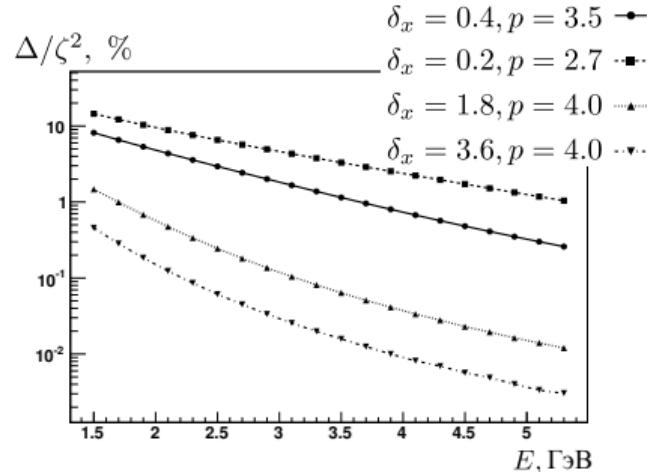
A.G.Shamov / Nuclear Physics B (Proc. Suppl.) 189  
(2009) 21–23

$$\dot{N} \propto \frac{I_{beam}^2}{E^{2/3} V_{beam}} \propto \frac{1}{E^{5/6}}$$

$$\nu_c(E)/\nu_c(1.85) \times V(E)/V(1.85)$$



$$\Delta \approx \frac{0.5\%}{\delta q_x \delta q_y} \zeta^2 \propto \frac{1}{E^4}$$



Small count rate and polarization effect for  $E = 5 \text{ GeV}$

$$\dot{N} \approx 10 \text{ kHz} \quad \text{for} \quad I = 10 \text{ mA}$$

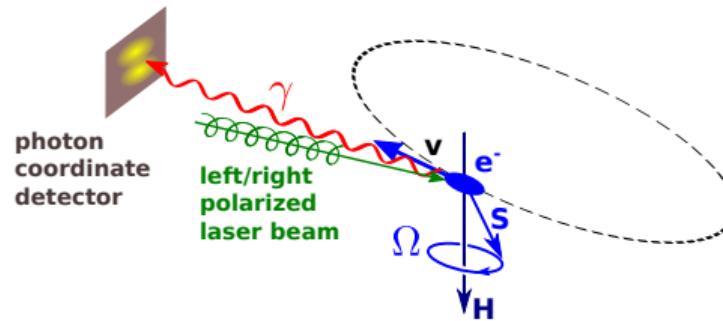
$$\Delta \approx 0.3\%$$

Need alternative method of polarization measurement

# Compton backscattering polarimeter

- Suggested in BINP in 1969:  
*Baier, Khoze, Sov.J.Nucl.Phys. V9, p238 (1969)*
- First implemented at SPEAR (1979)  
*Gustavson et al, NIM, V165, No2, p177 (1979)*
- VEPP-4 (1982)  
*Vorob'ev et al, Proc. All-union conference on charged particle accelerators. (1983)*
- Tikhonov (1982): SR from clashing beam as source of circular polarized light
- at LEP for Z boson mass measurement (1993)

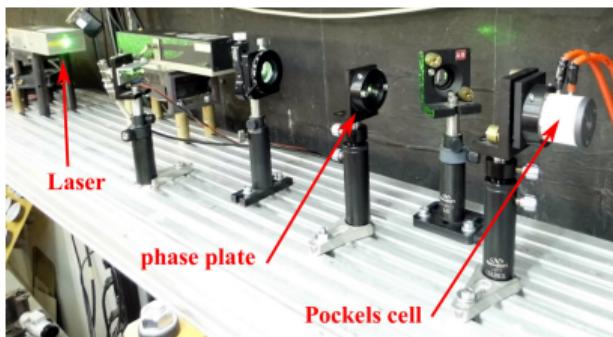
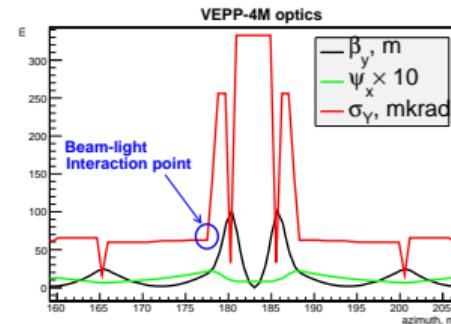
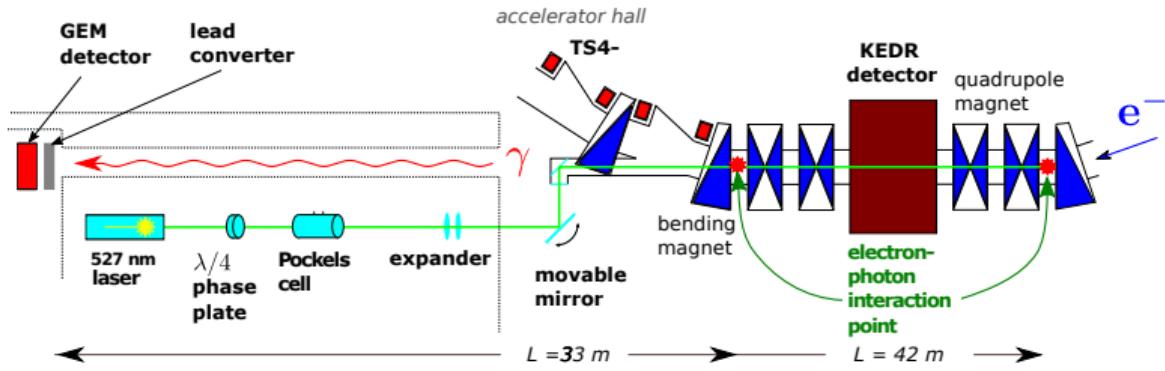
Up-down scattering asymmetry for left-right photon backscattering on vertically polarized electron beam



$$A = \frac{N_{\text{up}} - N_{\text{down}}}{N_{\text{up}} + N_{\text{down}}} \approx -\frac{3}{4} \frac{E\omega_0}{m_e^2} VP$$

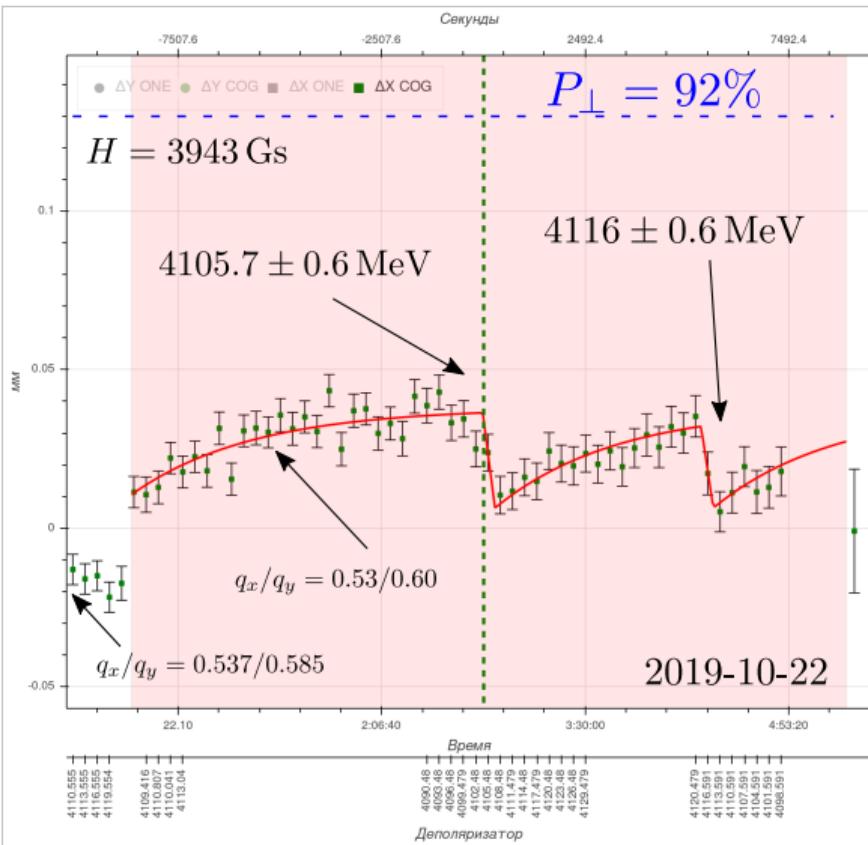
$\omega_0$  is the initial photon energy,  $V$  is the Stokes parameter of circular polarization ( $\pm 1$ )

# Laser polarimeter at VEPP-4M



- 527 nm Nd:YLF solid state laser with  $500\ \mu\text{J}$  pulse energy at 4 kHz, 6ns pulse length
- Circular polarization prepared by KD\*P Pockels cell ( $U_{1/2} = 3.3\text{kV}$ ) or/and by  $\lambda/4$  wave plate. Switched every pulse.
- Two-coordinate GEM detector with  $2X_0$  Pb converter for gamma quanta detection.

# Energy measurements by VEPP-4M laser polarimeter



$$\langle \Delta y \rangle = \frac{\omega_0}{2m_e} L P_{\perp} \Delta V \approx 0.13 \text{ mm}$$

$$\omega_0 \approx 2.35 \text{ eV}, L \approx 33 \text{ m},$$
$$\Delta V = 1.8 \pm 0.1$$

$$\sigma_{\Delta \langle y \rangle} = \sqrt{\frac{2}{N} \left( \frac{L}{\gamma} \oplus L \sigma_Y \oplus \sigma_y \right)} \approx \frac{7 \text{ mm}}{\sqrt{N}}$$

$$\dot{N} \approx 10 \text{ kHz}$$

## Resonace depolarization method

- Most precise method of beam energy calibration ( $10^{-6}$ )
- Requires polarized beam
- Need special time to measure spin precession frequency
  - Need beam energy interpolation between calibrations. NMR,temperatures, moon phase...
- Need c.m. calculation from spin precession.

# THANK YOU

# Synchrotron Spin-light polarimeter

Classical synchrotron light

$$W_0 = \frac{2}{3} \frac{e^2 c}{R^2} \gamma^4$$

Magnet dipole synchrotron light

$$W_{md} = \frac{2}{3} \frac{\mu_0^2}{c^3} \omega_0^4 \zeta^2 \propto \hbar^2$$

Interference between them

$$W_{mixed} = 2 \sqrt{W_0 W_{md}} \propto \hbar$$

For  $\omega/\omega_c > 10$ ,  $B = 1T$ ,  $E = 10 \div 100$  GeV

$$\delta = \frac{W_{mixed}}{W_0} \sim \zeta \omega / E \approx 10^{-4} \div 10^{-3}$$

- Suggested by Korchuganov, Kulipanov, Mezentsev (1977)
- Implemented at BINP (1982) (Belomestnykh, Bondar et al)

