

# Photons Interacting with Pions at COMPASS

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*COMPASS collaboration*



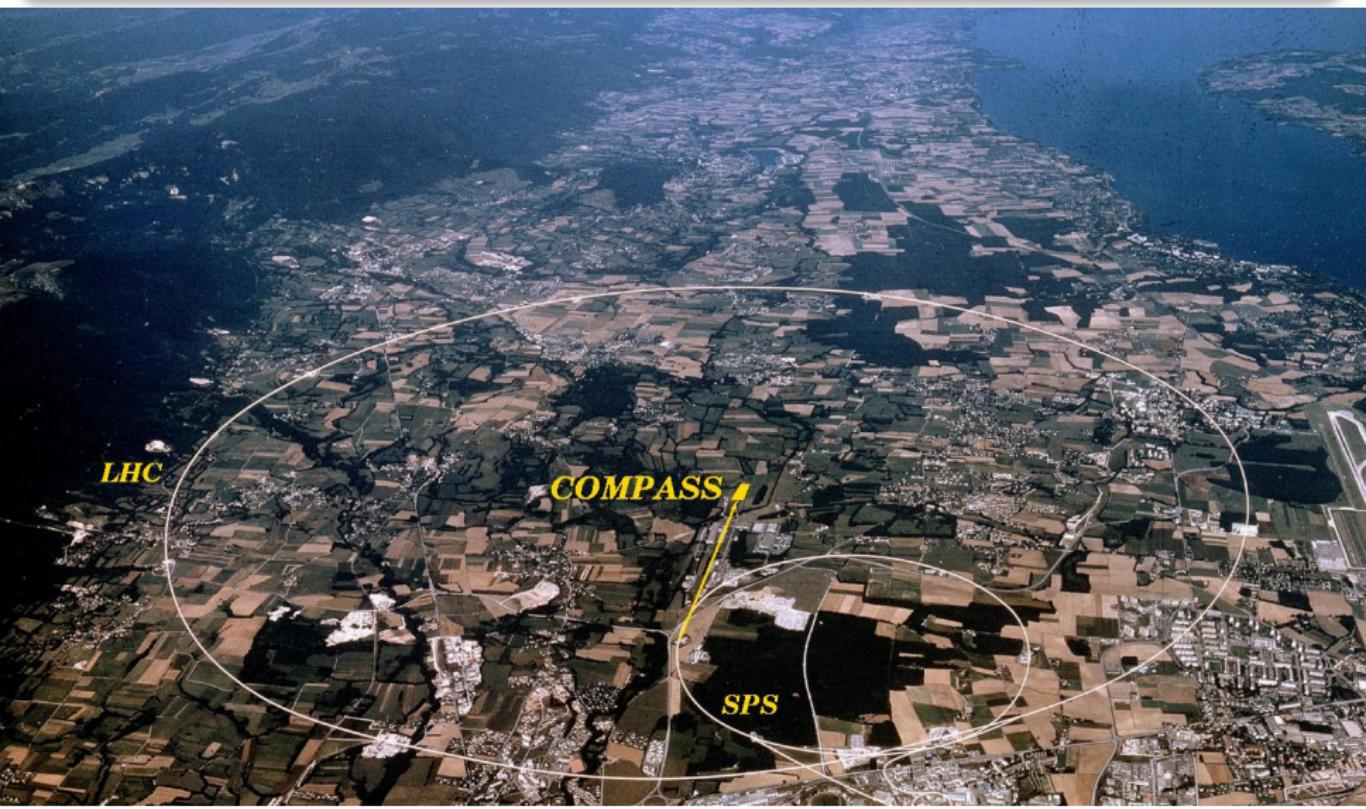
June 18, 2015



Bundesministerium  
für Bildung  
und Forschung



# COCommon Muon and Proton Apparatus for Structure and Spectroscopy

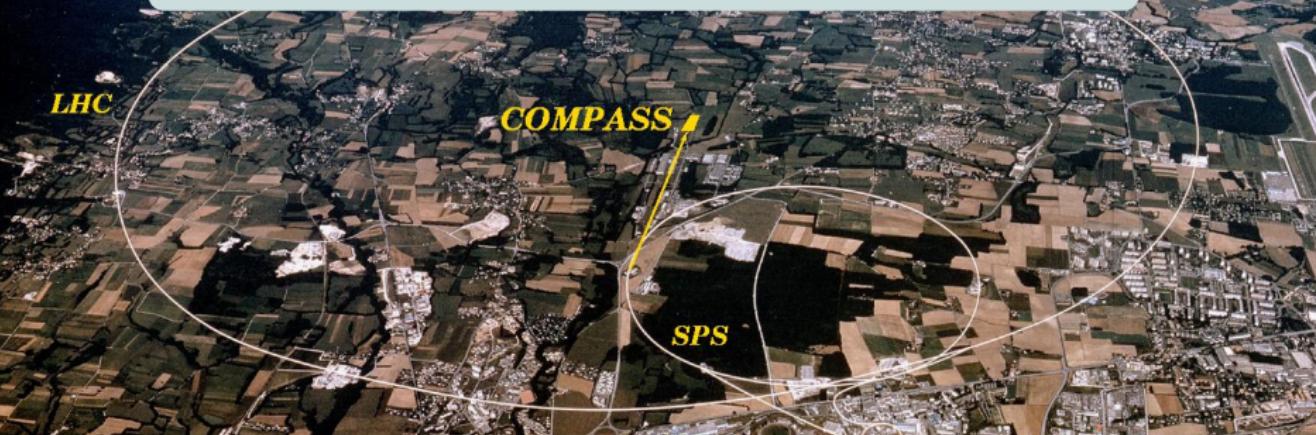




# COCommon Muon and Proton Apparatus for Structure and Spectroscopy

CERN SPS: protons  $\sim 400$  GeV (5 – 10 sec spills)

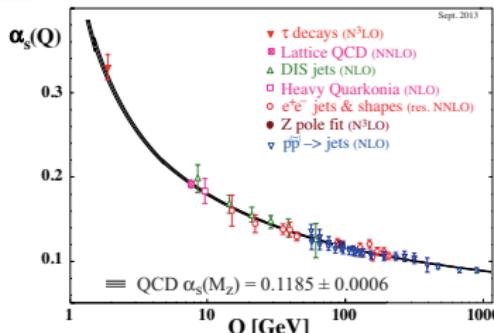
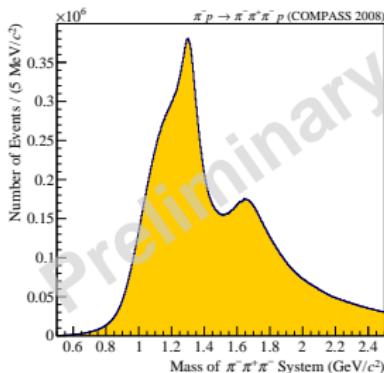
- secondary  $\pi, K, (\bar{p})$ : up to  $2 \cdot 10^7$ /s (typ.  $5 \cdot 10^6$ /s)  
Nov. 2004, 2008-09, 2012:  
hadron spec. & Primakoff reactions
- tertiary muons:  $4 \cdot 10^7$  / s  
2002-04, 2006-07, 2010-11: spin structure of the nucleon





# Physics fields at COMPASS

- lepton scattering  
at high momentum transfer  
→ partonic structure of the nucleons



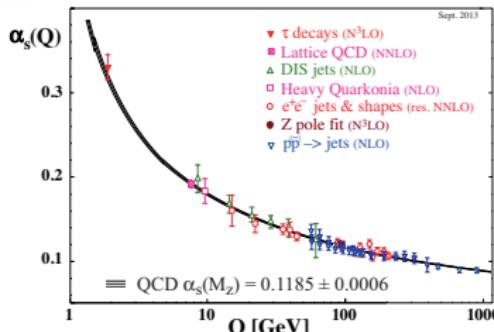
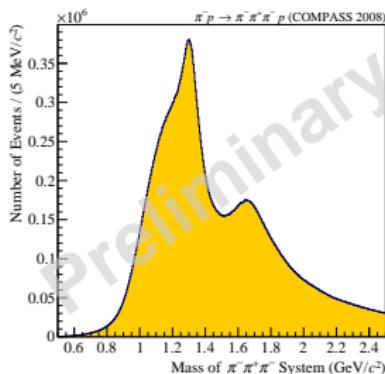
- diffractive dissociation of pions and kaons  
→ meson spectrometry

- scattering of pions (and kaons) in nuclear Coulomb field  
→ low-energetic meson-photon reactions  
 $\pi\gamma \rightarrow \pi\gamma$  (pion polarisability),  $\pi\gamma \rightarrow 3\pi$  (chiral dynamics, radiative couplings)



# Physics fields at COMPASS

- lepton scattering  
at high momentum transfer  
→ partonic structure of the nucleons  
*s. talk tomorrow by A. Ferrero*

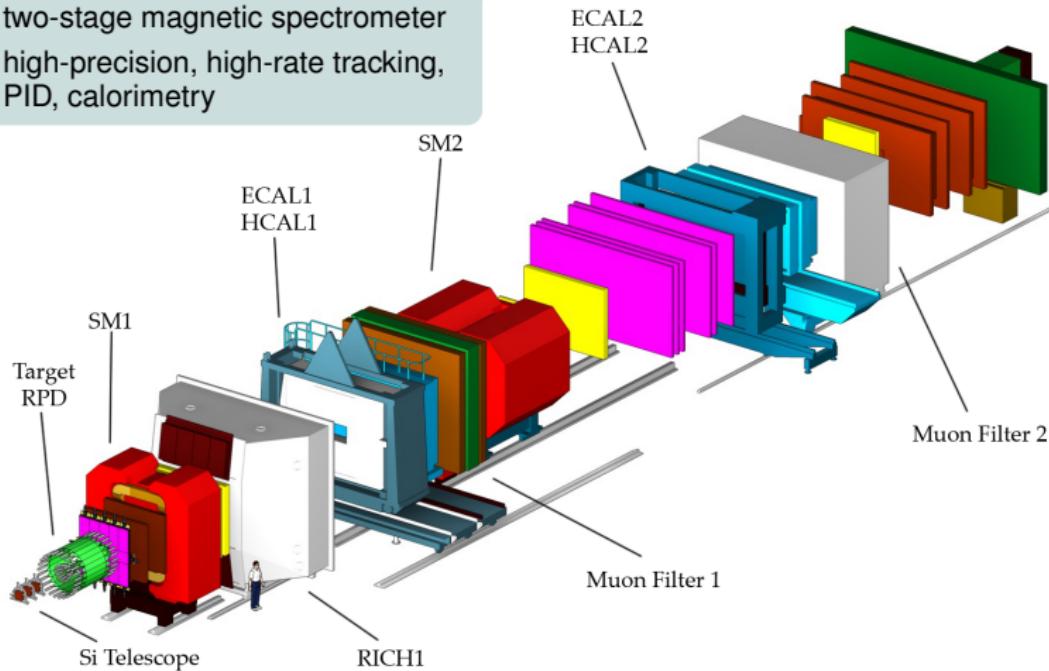


- diffractive dissociation of pions and kaons  
→ meson spectrometry  
*s. following talk by B. Grube*

- scattering of pions (and kaons) in nuclear Coulomb field  
→ low-energetic meson-photon reactions (*this talk*)  
 $\pi\gamma \rightarrow \pi\gamma$  (pion polarisability),  $\pi\gamma \rightarrow 3\pi$  (chiral dynamics, radiative couplings)

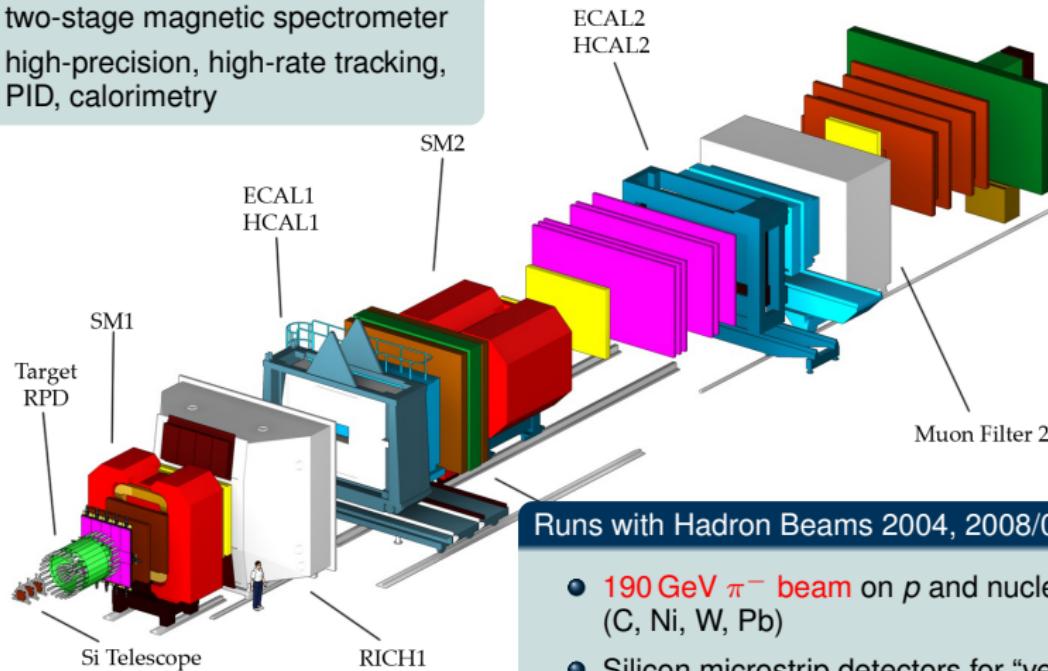
## Fixed-target experiment

- two-stage magnetic spectrometer
- high-precision, high-rate tracking,  
PID, calorimetry



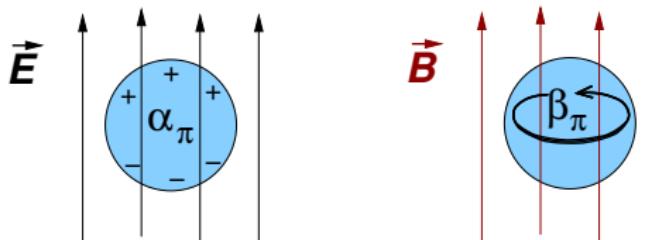
## Fixed-target experiment

- two-stage magnetic spectrometer
- high-precision, high-rate tracking, PID, calorimetry



Runs with Hadron Beams 2004, 2008/09, 2012

- **190 GeV  $\pi^-$  beam** on  $p$  and nuclear targets (C, Ni, W, Pb)
- Silicon microstrip detectors for “vertexing”
- recoil and (digital) ECAL triggers



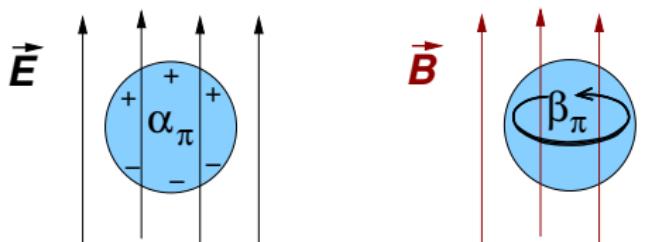
pion polarisabilities  $\alpha_\pi, \beta_\pi$  in units of  $10^{-4} \text{ fm}^3$

size of the pion  $\sim 1 \text{ fm}^3$  [cf. atoms: polarisability  $\approx$  size  $\approx 1 \text{ \AA}^3$ ]

Theory: ChPT (2-loop) prediction:

$\alpha_\pi - \beta_\pi$	$=$	$5.7 \pm 1.0$
$\alpha_\pi + \beta_\pi$	$=$	$0.16 \pm 0.1$

experiments for  $\alpha_\pi - \beta_\pi$  lie in the range  $4 \dots 14$   
 $(\alpha_\pi + \beta_\pi = 0 \text{ assumed})$



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size of the pion  $\sim 1 \text{ fm}^3$  [cf. atoms: polarisability  $\approx$  size  $\approx 1 \text{ \AA}^3$ ]

Theory: ChPT (2-loop) prediction:

$\alpha_\pi$	=	$2.93 \pm 0.5$
$\beta_\pi$	=	$-2.77 \pm 0.5$

experiments for  $\alpha_\pi$  lie in the range  $2 \dots 7$

( $\alpha_\pi + \beta_\pi = 0$  assumed)



# latest publication on the pion polarisability



Technische Universität München



## PHYSICAL REVIEW LETTERS

week ending  
13 FEBRUARY 2015

### Measurement of the Charged-Pion Polarizability

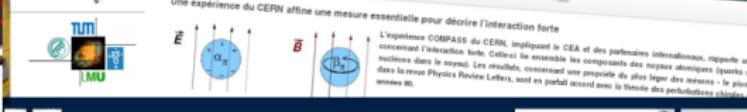
C. Adolph,<sup>8</sup> R. Akhunzyanov,<sup>7</sup> M. G. Alexeev,<sup>27</sup> G. D. Alexeev,<sup>7</sup> A. Amoroso,<sup>27,29</sup> V. Andrieux,<sup>22</sup> V. Anosov,<sup>7</sup>

... [213 authors]

(COMPASS Collaboration)

(Received 2 June 2014; revised manuscript received 24 December 2014; published 10 February 2015)

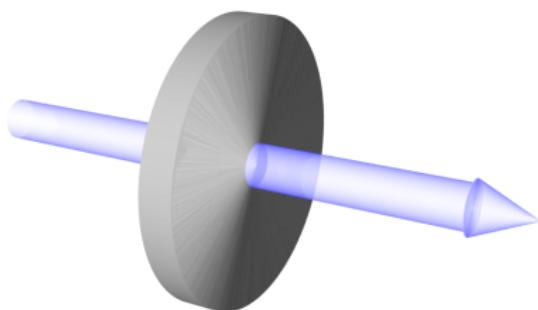
The COMPASS collaboration at CERN has investigated pion Compton scattering,  $\pi^- \gamma \rightarrow \pi^- \gamma$ , at center-of-mass energy below 3.5 pion masses. The process is embedded in the reaction  $\pi^- \text{Ni} \rightarrow \pi^- \gamma \text{Ni}$ , which is initiated by 190 GeV pions impinging on a nickel target. The exchange of quasireal photons is selected by isolating the sharp Coulomb peak observed at smallest momentum transfers,  $Q^2 < 0.0015 \text{ (GeV/c)}^2$ . From a sample of 63 000 events, the pion electric polarizability is determined to be  $\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$  under the assumption  $\alpha_\pi = -\beta_\pi$ , which relates the electric and magnetic dipole polarizabilities. It is the most precise measurement of this fundamental low-energy parameter of strong





# Principle of the COMPASS measurement

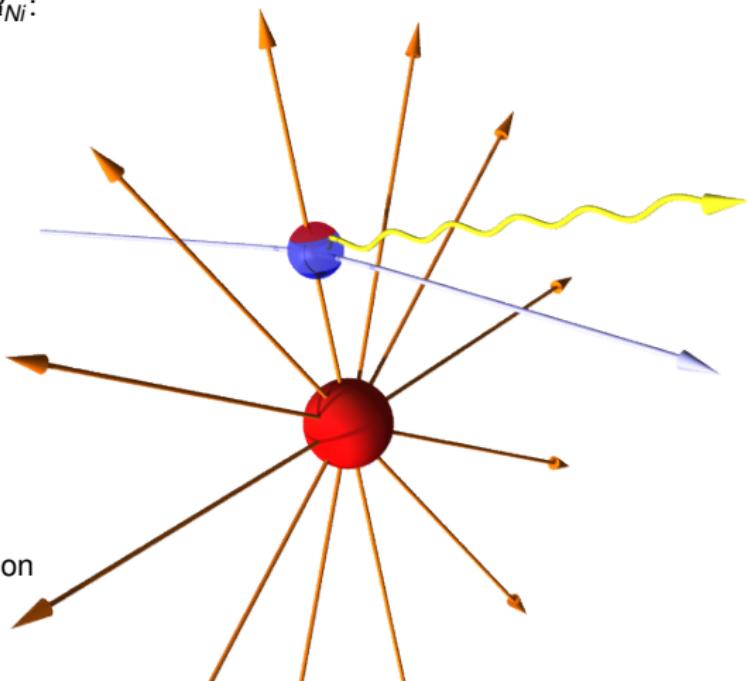
- high-energetic pion beam on 4mm nickel disk
- observe scattered pions in coincidence with produced hard photons
- study of cross-section shape





# Polarisability effect in Primakoff technique

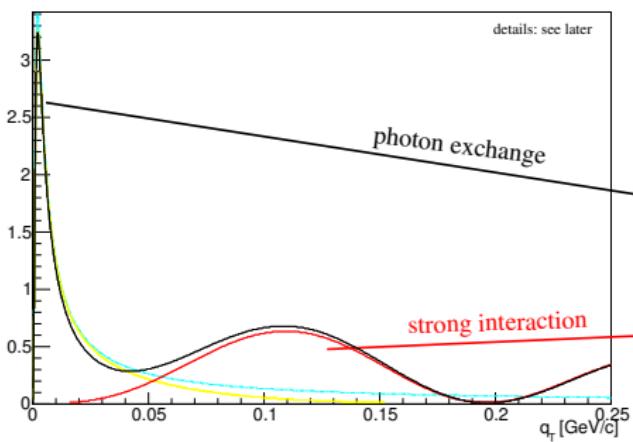
- Charged pions traverse the nuclear **electric field**
  - typical field strength at  $d = 5R_{Ni}$ :  
 $E \approx 300 \text{ kV/fm}$
- Bremsstrahlung process:
  - particles scatter off **equivalent photons**
  - tiny momentum transfer  
 $Q^2 \approx 10^{-5} \text{ GeV}^2/c^2$
  - pion/muon (quasi-)real Compton scattering
- Polarisability contribution
  - Compton cross-section typically diminished
  - corresponding charge separation  
 $\approx 10^{-5} \text{ fm} \cdot e$





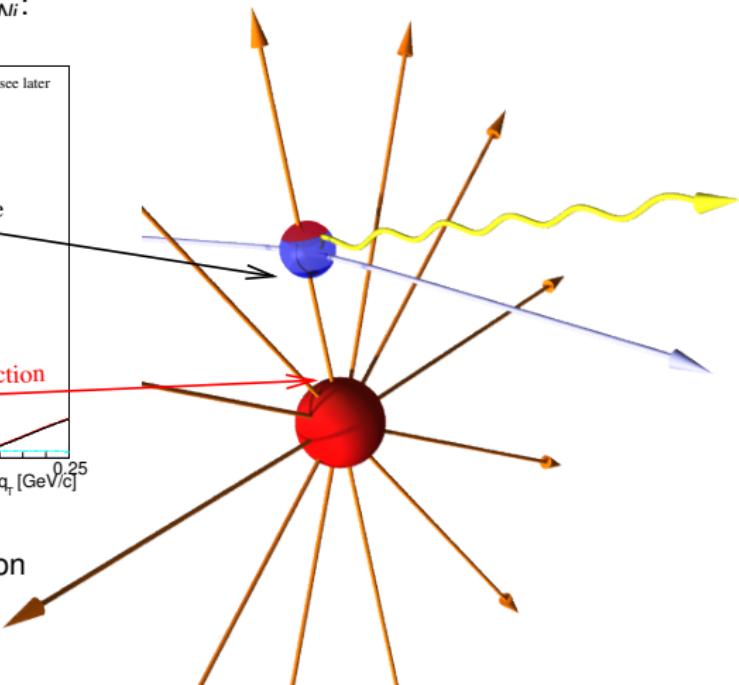
# Polarisability effect in Primakoff technique

- Charged pions traverse the nuclear **electric field**
  - typical field strength at  $d = 5R_{Ni}$ :



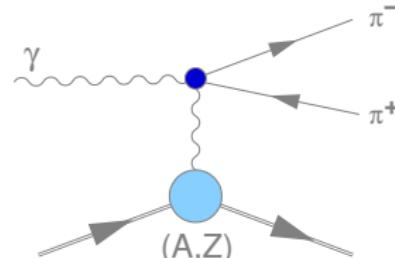
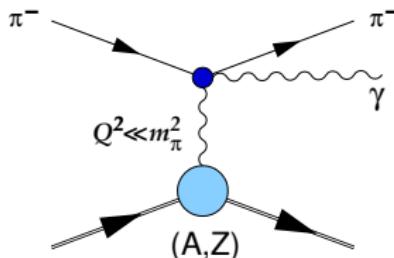
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- corresponding charge separation  
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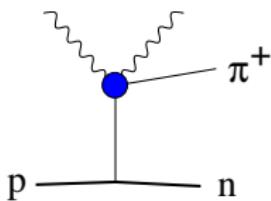




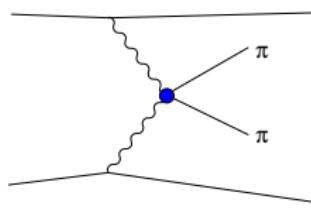
## Pion Compton scattering: embedding the process



Primakoff processes



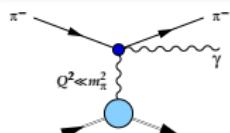
Radiative pion photoproduction



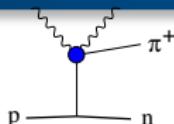
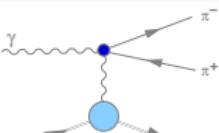
Photon-Photon fusion



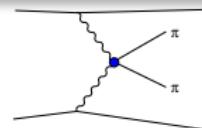
# Pion polarisability: world data before COMPASS



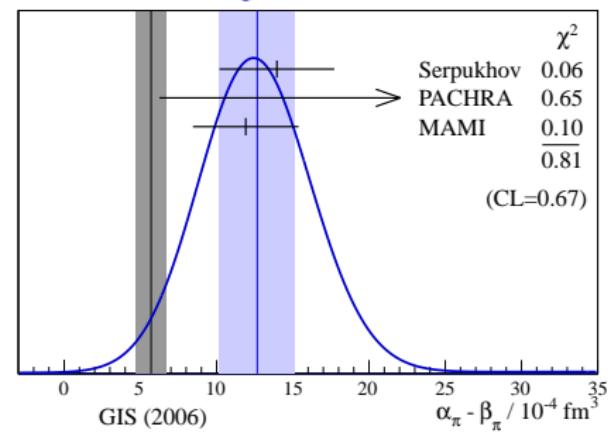
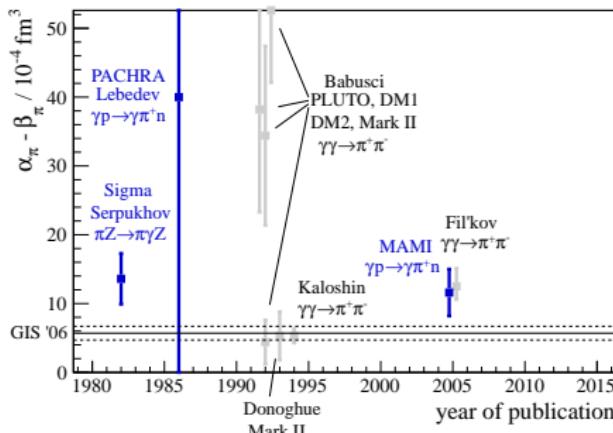
Primakoff processes



Radiative pion photoproduction



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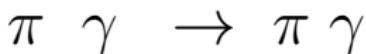


GIS'06: ChPT prediction, Gasser, Ivanov, Sainio, NPB745 (2006), plots: T. Nagel, PhD

Fil'kov analysis objected by Pasquini, Drechsel, Scherer PRC81, 029802 (2010)



# Pion Compton Scattering



- Two kinematic variables, in CM: total energy  $\sqrt{s}$ , scattering angle  $\theta_{cm}$

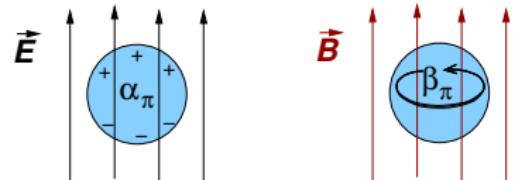
$$\frac{d\sigma_{\pi\gamma}}{d\Omega_{cm}} = \frac{\alpha^2(s^2 z_+^2 + m_\pi^4 z_-^2)}{s(sz_+ + m_\pi^2 z_-)^2} - \frac{\alpha m_\pi^3 (s - m_\pi^2)^2}{4s^2(sz_+ + m_\pi^2 z_-)} \cdot \mathcal{P}$$

$$\mathcal{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2(\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3(\alpha_2 - \beta_2)$$

$$z_\pm = 1 \pm \cos \theta_{cm}$$



# Pion Compton Scattering



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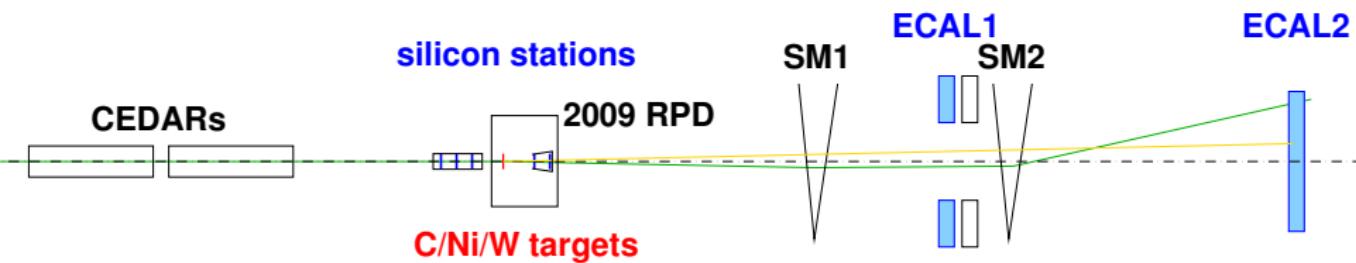
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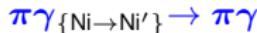
## Principle of the measurement





# Extraction of the pion polarisability

- Identify exclusive reactions



at smallest momentum transfer  $< 0.001 \text{ GeV}^2/c^2$

- Assuming  $\alpha_\pi + \beta_\pi = 0$ , from the cross-section

$$R = \frac{\sigma(x_\gamma)}{\sigma_{\alpha_\pi=0}(x_\gamma)} = \frac{N_{\text{meas}}(x_\gamma)}{N_{\text{sim}}(x_\gamma)} = 1 - \frac{3}{2} \cdot \frac{m_\pi^3}{\alpha} \cdot \frac{x_\gamma^2}{1-x_\gamma} \alpha_\pi$$

is derived, depending on  $x_\gamma = E_{\gamma(\text{lab})}/E_{\text{Beam}}$ .  
Measuring  $R$  the polarisability  $\alpha_\pi$  can be concluded.

- Control systematics by



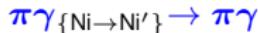
and





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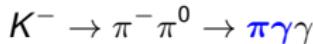
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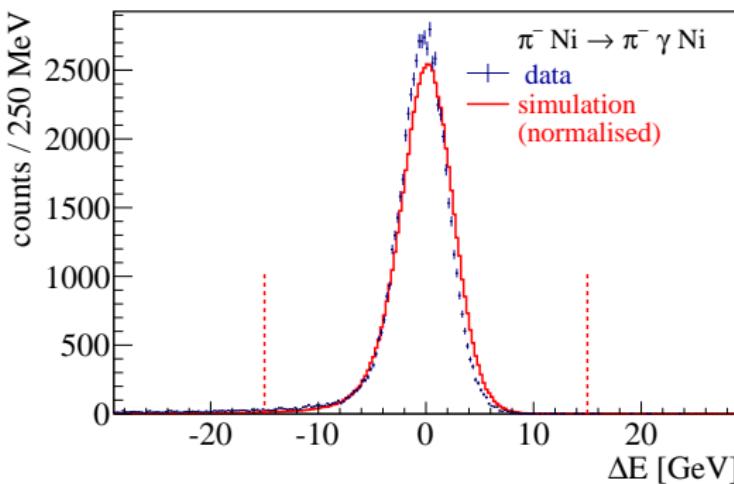


and



# Identifying the $\pi\gamma \rightarrow \pi\gamma$ reaction

Phys. Rev. Lett. 114, 062002 (2015)

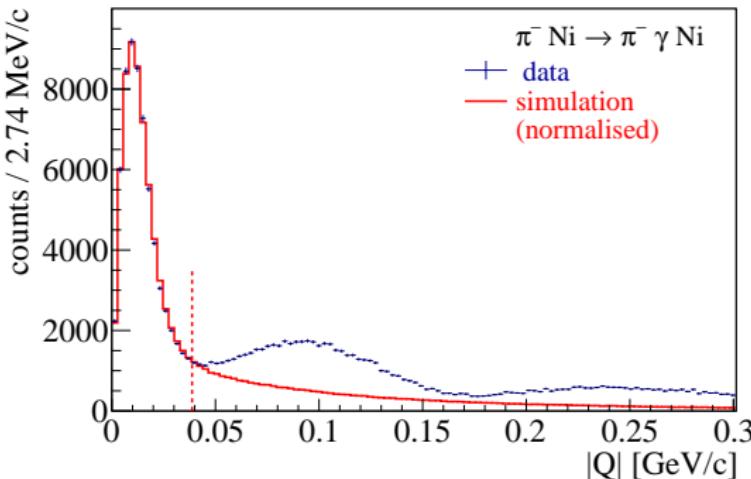


- Energy balance  $\Delta E = E_\pi + E_\gamma - E_{\text{Beam}}$
- Exclusivity peak  $\sigma \approx 2.6 \text{ GeV} (1.4\%)$
- $\sim 63.000$  exclusive events ( $x_\gamma > 0.4$ ) (Serpukhov  $\sim 7000$  for  $x_\gamma > 0.5$ )



## Primakoff peak

Phys. Rev. Lett. 114, 062002 (2015)

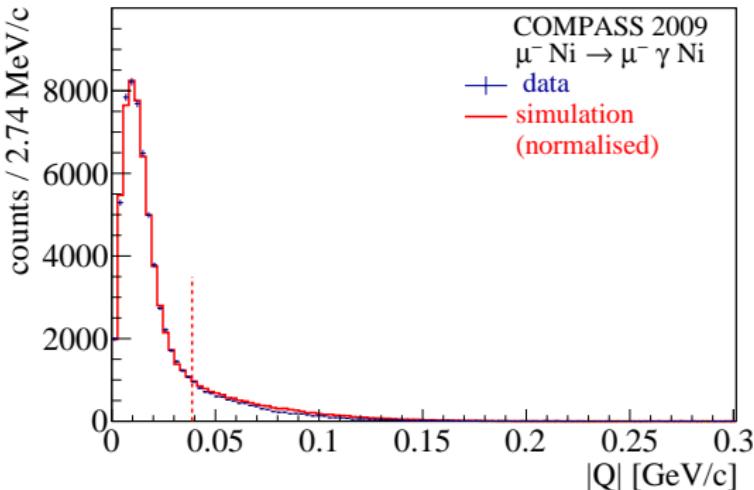


- $\Delta Q_T \approx 12 \text{ MeV}/c$  ( $190 \text{ GeV}/c$  beam  $\rightarrow$  requires few- $\mu\text{rad}$  angular resolution)
- first diffractive minimum on Ni nucleus at  $Q \approx 190 \text{ MeV}/c$
- data a little more narrow than simulation  $\rightarrow$  negative interference?



## Primakoff peak: muon data

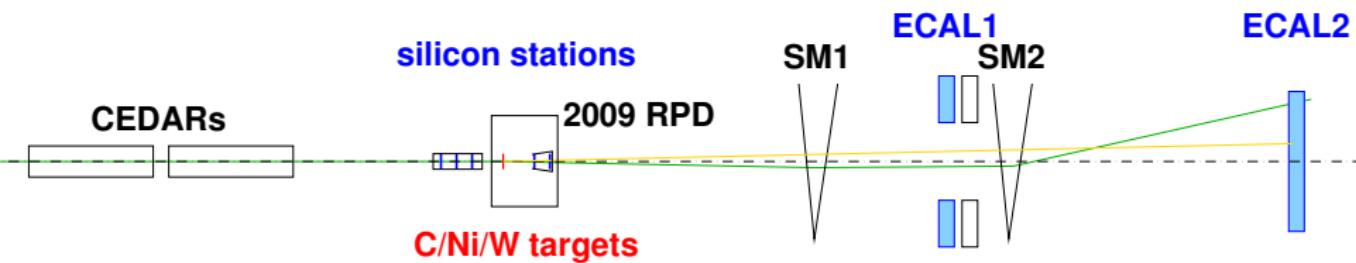
Phys. Rev. Lett. 114, 062002 (2015)



- **muon control measurement:** pure electromagnetic interaction
- e.m. nuclear effects well understood



## Principle of the measurement





# ECAL2: 3000 cells of different types





# ECAL2: the quest for precision

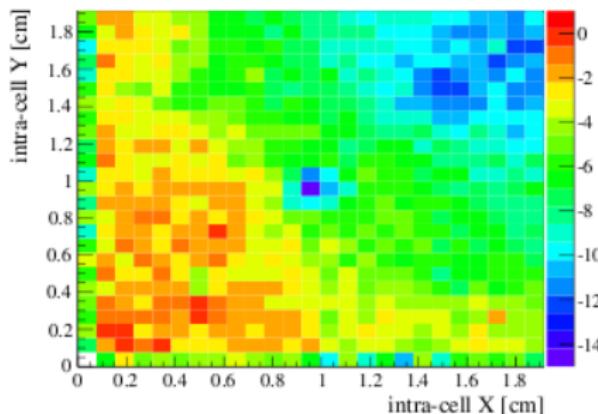


Figure 3.5: Profile of energy deviations shown for 1/4 of a shashlik block and for muon data photons within the range  $133 \text{ GeV} < E_\gamma < 152 \text{ GeV}$ .

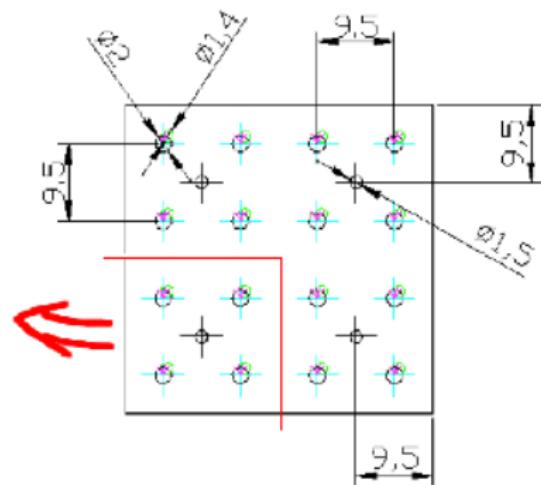


Figure 3.6: Technical drawing of a full shashlik cell to be compared with the figure to the left.

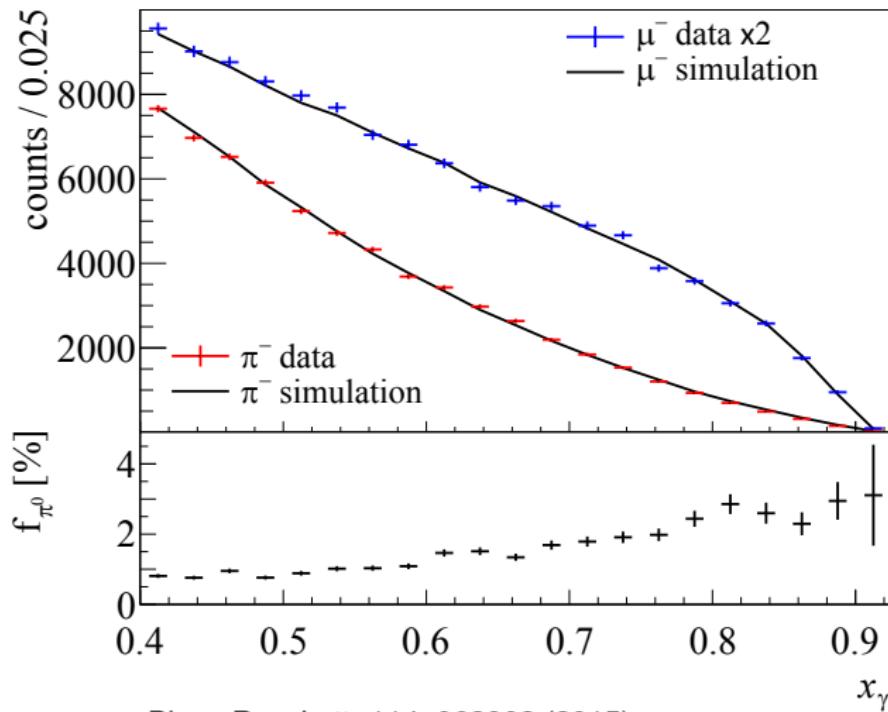
from: Th. Nagel, PhD thesis TUM 2012



## Photon energy spectra for muon and pion beam



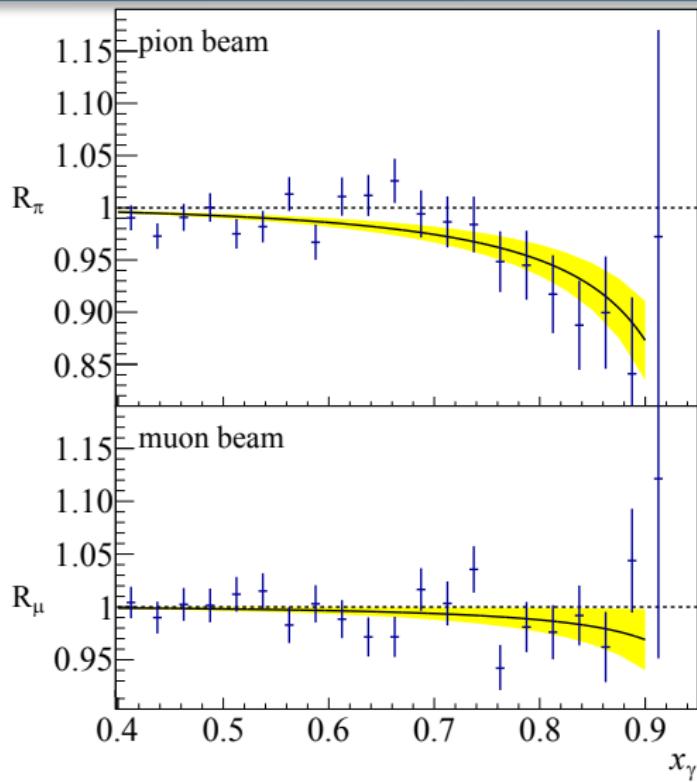
Technische Universität München



Phys. Rev. Lett. 114, 062002 (2015)



## Pion polarisability: COMPASS result



$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

(assuming  $\alpha_\pi = -\beta_\pi$ )

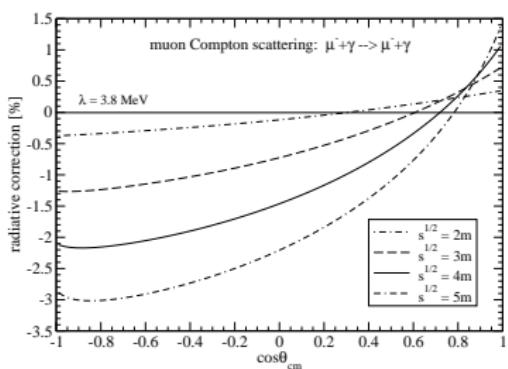
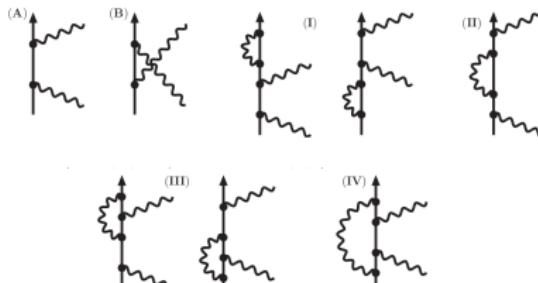
“false polarisability” from muon data:

$$(0.5 \pm 0.5_{\text{stat}}) \times 10^{-4} \text{ fm}^3$$

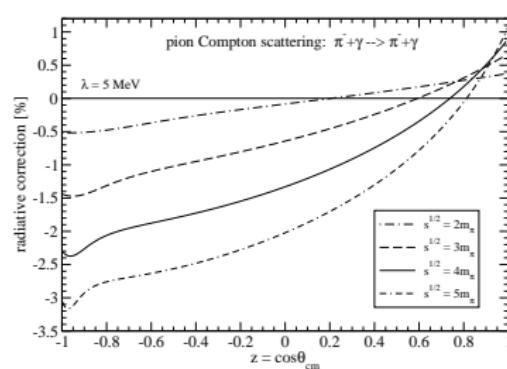
Phys. Rev. Lett. 114, 062002 (2015)



# Radiative corrections (Compton scattering part)



Nucl.Phys. A837 (2010)



Eur.Phys.J. A39 (2009) 71



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source of systematic uncertainty	estimated magnitude CL = 68 % [10 <sup>-4</sup> fm <sup>3</sup> ]
determination of tracking-detector efficiencies	0.5
treatment of radiative corrections	0.3
subtraction of $\pi^0$ background	0.2
strong interaction background	0.2
pion-electron elastic scattering	0.2
contribution of muons in the beam	0.05
quadratic sum	0.7

---



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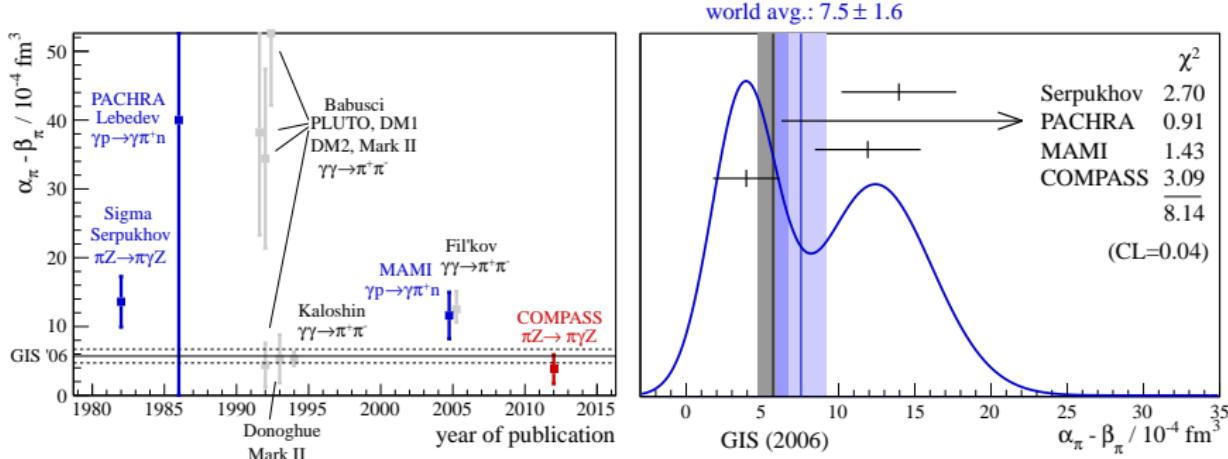
COMPASS result for the pion polarisability:

$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3$$

with  $\alpha_\pi = -\beta_\pi$  assumed



# Pion polarisability: world data including COMPASS



- The new COMPASS result is in significant tension with the earlier measurements of the pion polarisability
- The expectation from ChPT is confirmed within the uncertainties



# Photon-photon fusion process $\gamma\gamma \rightarrow \pi^+ \pi^-$

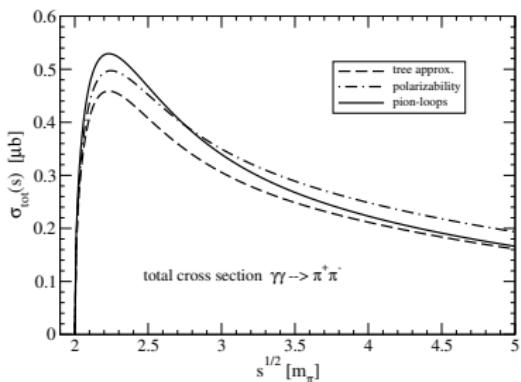


- Planned measurements at ALICE and JLab

$$\sigma_{tot}(s) = \frac{2\pi\alpha^2}{\hat{s}^3 m_\pi^2} \left\{ [4 + \hat{s} + \hat{s}|\mathcal{C}(\hat{s})|^2] \sqrt{\hat{s}(\hat{s}-4)} \right.$$

$$\left. + 8[2 - \hat{s} + \hat{s} \operatorname{Re} \mathcal{C}(\hat{s})] \ln \frac{\sqrt{\hat{s}} + \sqrt{\hat{s}-4}}{2} \right\},$$

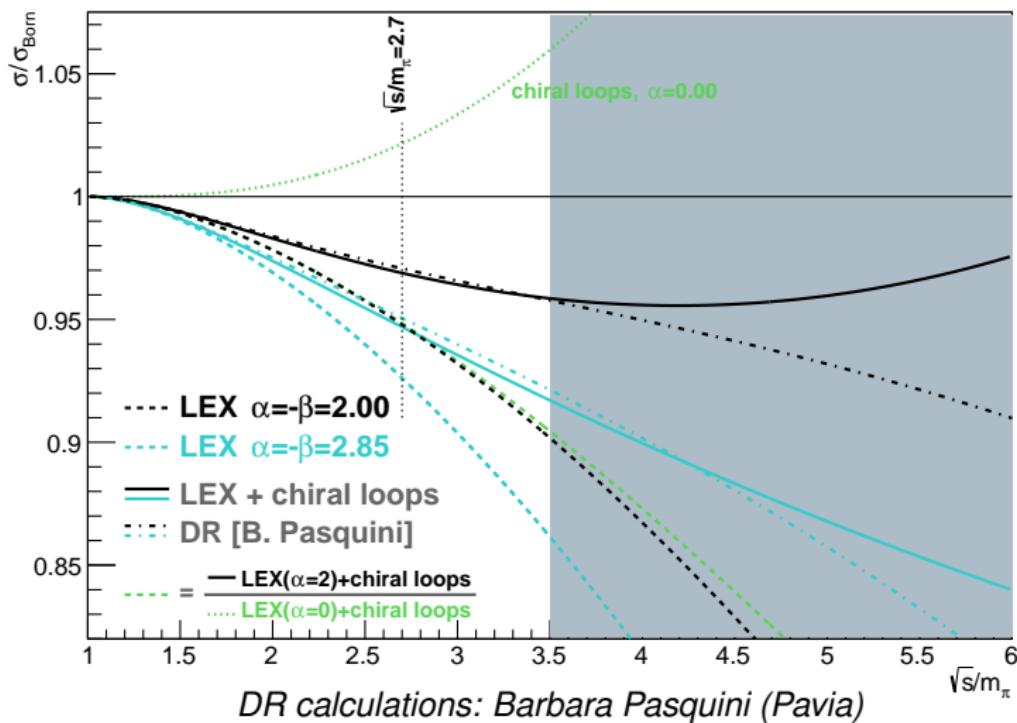
$$\mathcal{C}(\hat{s}) = -\beta_\pi \frac{m_\pi^3}{2\alpha} \hat{s} - \frac{m_\pi^2}{(4\pi f_\pi)^2} \left\{ \frac{\hat{s}}{2} + 2 \left[ \ln \frac{\sqrt{\hat{s}} + \sqrt{\hat{s}-4}}{2} - \frac{i\pi}{2} \right]^2 \right\}$$



courtesy Norbert Kaiser (TUM)

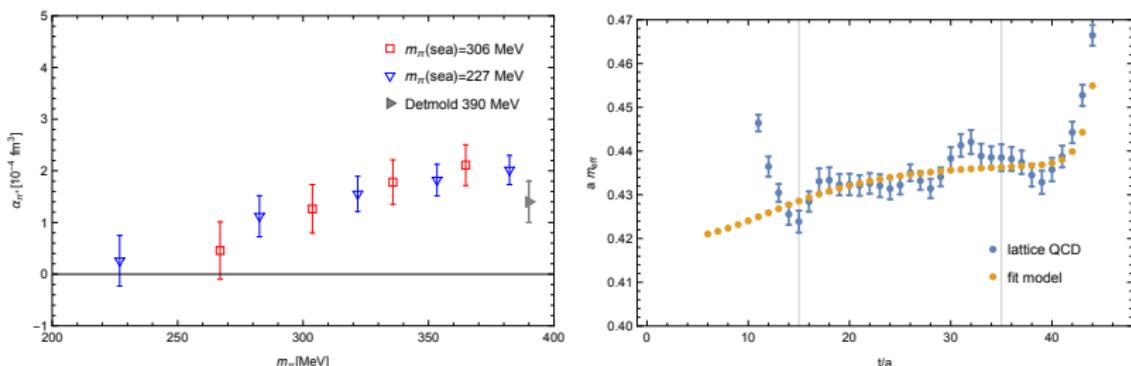
limited sensitivity to the polarisability contribution

## Polarisability and Loop Contributions z=1.0





# Pion polarisability on the lattice



**FIGURE 3.** Left: electric polarizability for the charged pions as a function of the valence quark mass. The data for  $m_\pi = 390 \text{ MeV}$  is taken from [5]. Right: effective mass for a charged pion correlator together with the scalar particle correlator determined from the fit. The fitting range is indicated by the vertical bars.

Alexandru *et al.*, Pion electric polarizability from lattice QCD, arXiv:1501.06516



## Primakoff reactions accessible at COMPASS

Access to  $\pi + \gamma$  reactions via the **Primakoff effect**:

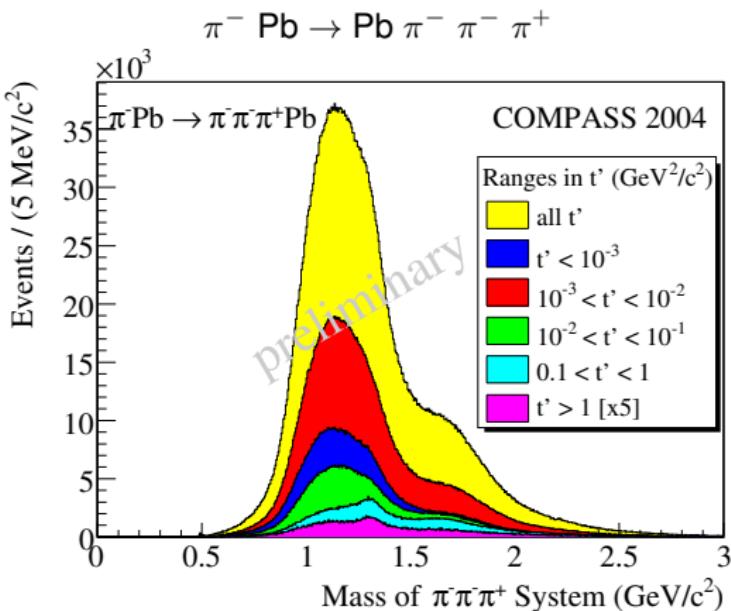
*At smallest momentum transfers* to the nucleus, high-energetic particles scatter predominantly off the **electromagnetic field quanta** ( $\sim Z^2$ )

$$\pi^- + \gamma \rightarrow \left\{ \begin{array}{l} \pi^- + \gamma \\ \pi^- + \pi^0 / \eta \\ \pi^- + \pi^0 + \pi^0 \\ \pi^- + \pi^- + \pi^+ \quad \leftarrow \\ \pi^- + \pi^- + \pi^+ + \pi^- + \pi^+ \\ \pi^- + \dots \end{array} \right.$$

*analogously: Kaon-induced reactions  $K^- + \gamma \rightarrow \dots$*



# 2004 Primakoff results

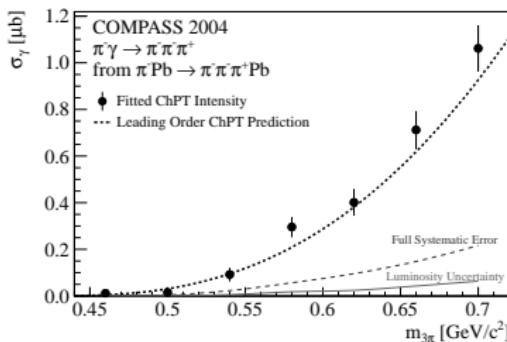
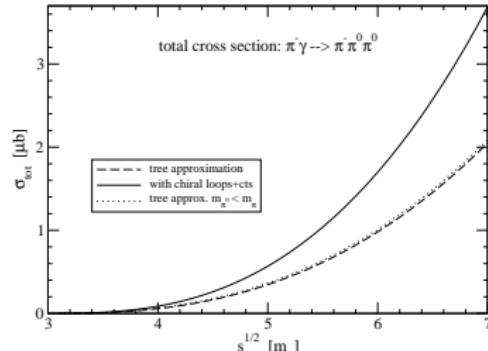
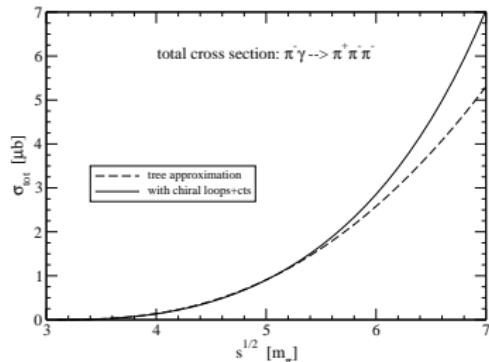


- "Low  $t'$ ":  $10^{-3} (\text{GeV}/c)^2 < t' < 10^{-2} (\text{GeV}/c)^2$   $\sim 2\,000\,000$  events
- "Primakoff region":  $t' < 10^{-3} (\text{GeV}/c)^2$   $\sim 1\,000\,000$  events

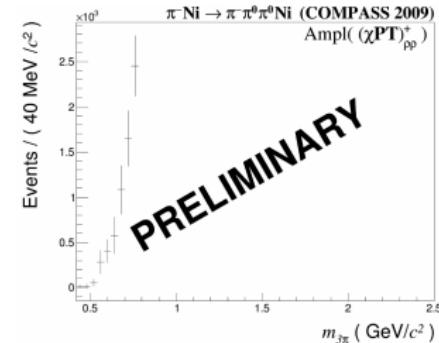


# Chiral dynamics in $\pi\gamma \rightarrow 3\pi$

Technische Universität München



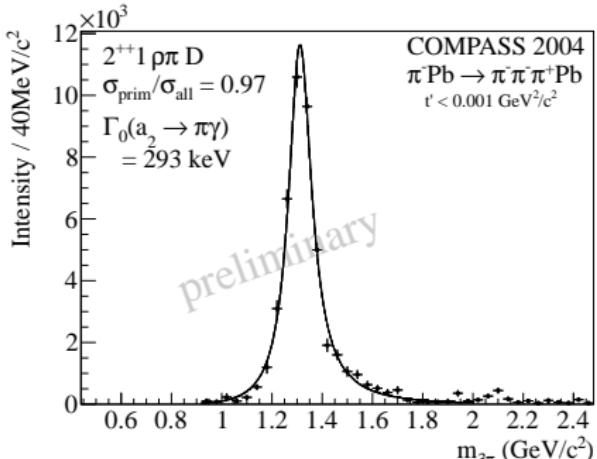
published in PRL 108 (2012) 192001



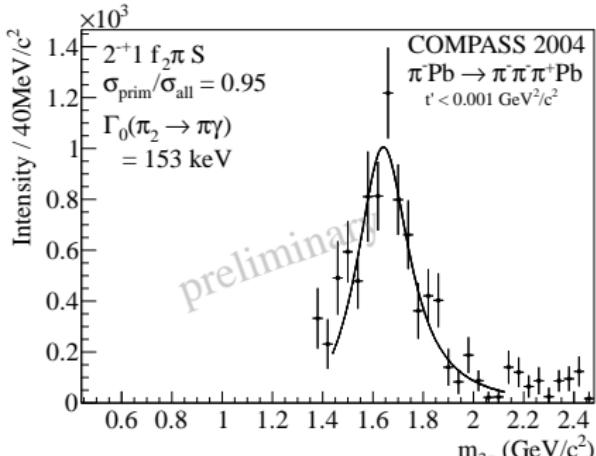
normalization: analysis ongoing



# Radiative Coupling of $a_2(1320)$ and $\pi_2(1670)$



$\Gamma_0(a_2(1320) \rightarrow \pi\gamma)$  M2



$\Gamma_0(\pi_2(1670) \rightarrow \pi\gamma)$  E2

⇒ meson w.f.'s:  $\Gamma_{i \rightarrow f} \propto | \langle \Psi_f | e^{-i\vec{q} \cdot \vec{r}} \hat{\epsilon} \cdot \vec{p} | \Psi_i \rangle |^2$ , VMD

- normalization via beam kaon decays
- large Coulomb correction

published in EPJ A50 (2014) 79



- Measurement of the **pion polarisability** at COMPASS

- Via the Primakoff reaction, COMPASS has determined

$$\alpha_\pi = (2.0 \pm 0.6_{\text{stat}} \pm 0.7_{\text{syst}}) \times 10^{-4} \text{ fm}^3 \quad \text{assuming } \alpha_\pi + \beta_\pi = 0$$

- most direct access to the  $\pi\gamma \rightarrow \pi\gamma$  process
- Most precise experimental determination
- Systematic control:  $\mu\gamma \rightarrow \mu\gamma$ ,  $K^- \rightarrow \pi^-\pi^0$

- COMPASS measures more aspects of chiral dynamics in  $\pi^-\gamma \rightarrow \pi^-\pi^0$  and  $\pi\gamma \rightarrow \pi\pi\pi$  reactions
- High-statistics run 2012

- separate determination of  $\alpha_\pi$  and  $\beta_\pi$
- $s$ -dependent quadrupole polarisabilities
- First measurement of the kaon polarisability



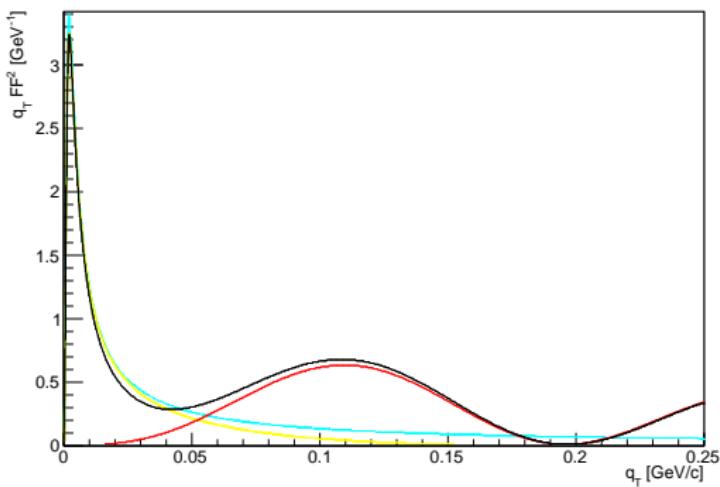
*Thank you for your attention!*



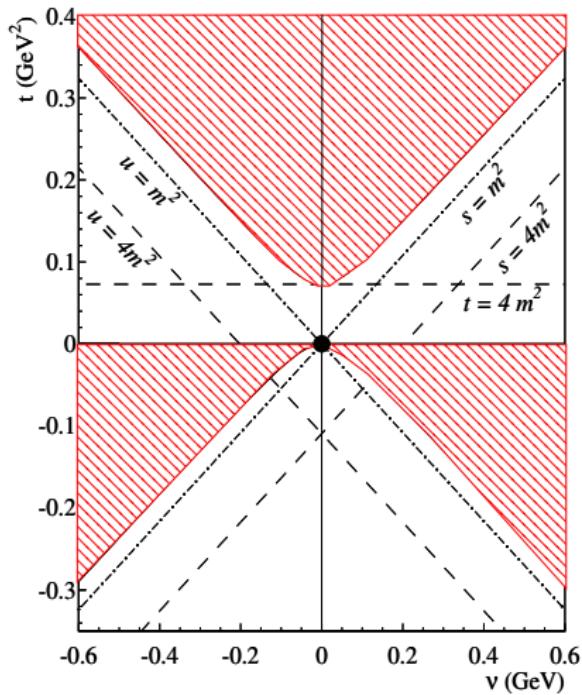
Technische Universität München



Photon density squared form factor

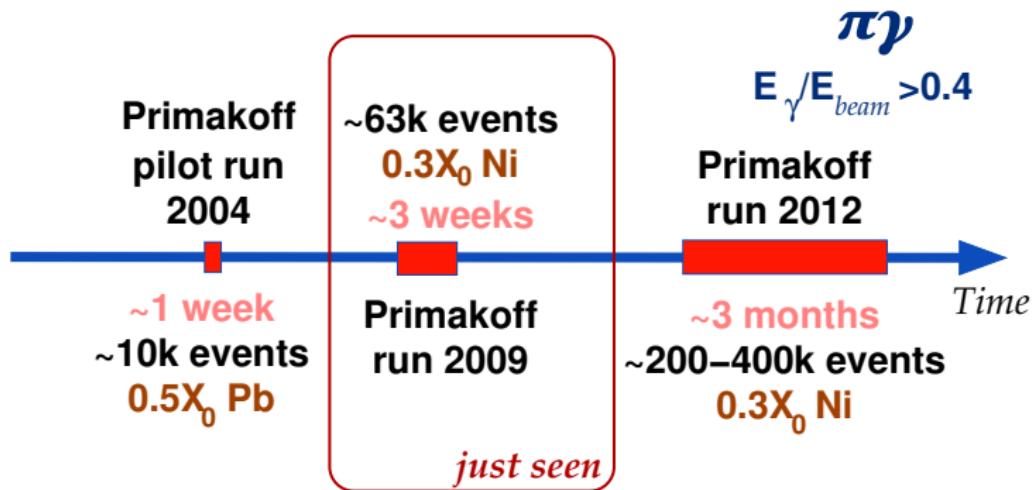


- calculation following G. Fäldt (Phys. Rev. C79, 014607)
- eikonal approximation: pions traverse Coulomb and strong-interaction potentials



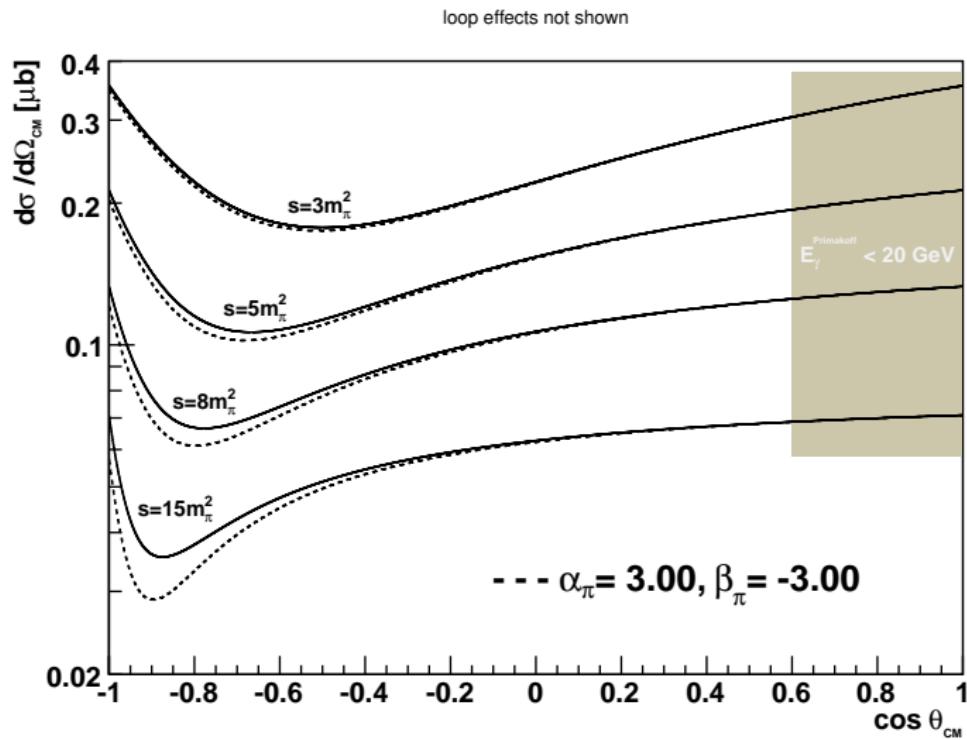
- ▶ red hatched:  
physical regions  
 $\gamma + \gamma \rightarrow \pi + \pi$   
 $\gamma + \pi \rightarrow \gamma + \pi$
- ▶ two-pion thresholds  
at  $s = 4m_\pi^2$ ,  $u = 4m_\pi^2$ ,  
 $t = 4m_\pi^2$
- ▶ DR integration paths  
 $t = 0$  (forward),  
 $\theta = 180^\circ$  (backward)  
 $u = m_\pi^2$ ,  $s = m_\pi^2$ , ...

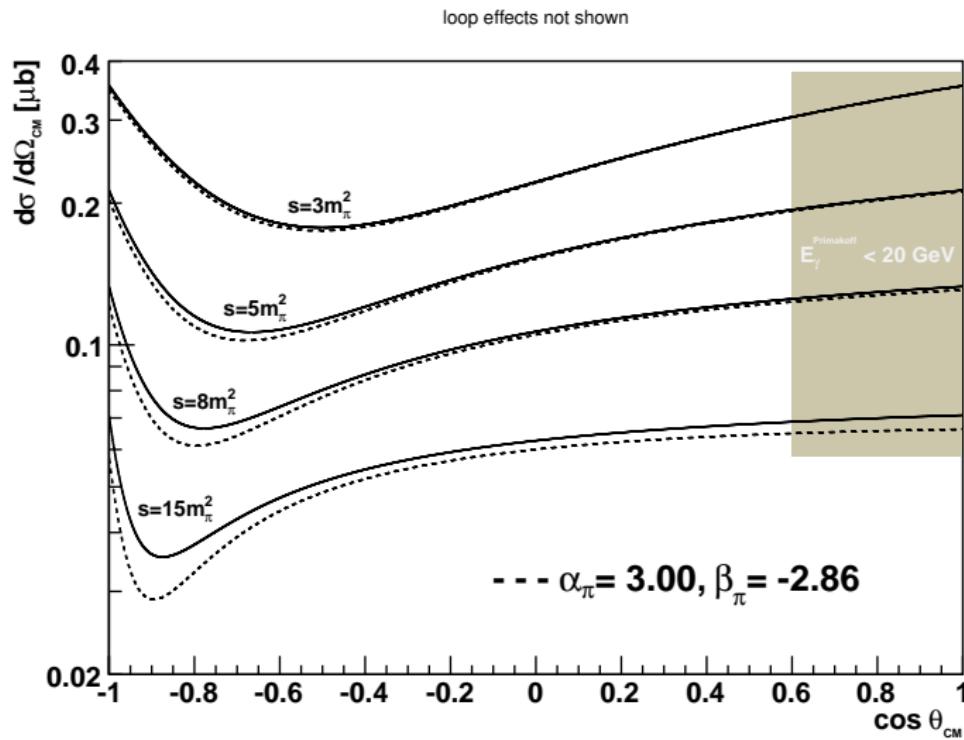
from: D. Drechsel, talk at IWHSS 2011 Paris

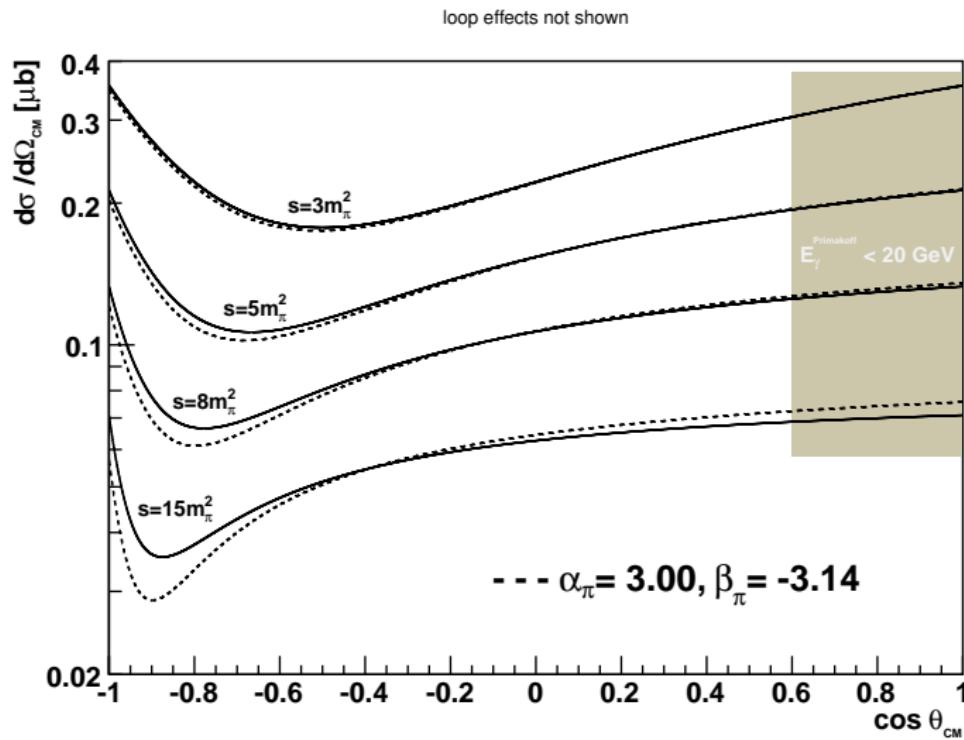


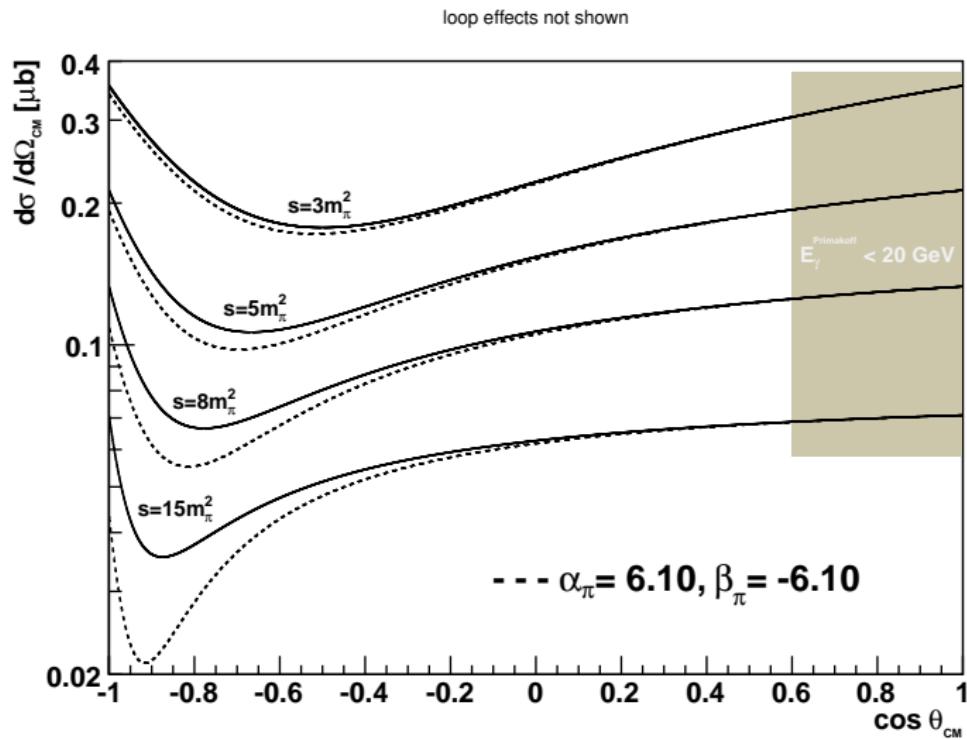
$$\mathcal{P} = z_-^2(\alpha_\pi - \beta_\pi) + \frac{s^2}{m_\pi^4} z_+^2(\alpha_\pi + \beta_\pi) - \frac{(s - m_\pi^2)^2}{24s} z_-^3(\alpha_2 - \beta_2)$$

$$z_\pm = 1 \pm \cos \theta_{cm}$$











- Radiative  $\pi^+$  production on the proton:



Mainz (2005) measurement:  $\alpha_\pi - \beta_\pi = 11.6 \pm 1.5 \pm 3.0 \pm 0.5$

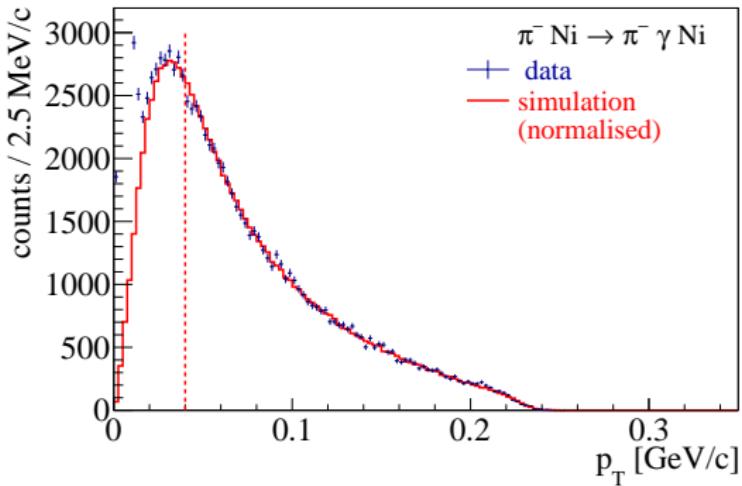
“ $\pm 0.5$ ”: model error *only within the used ansatz,*  
*full systematics not under control*

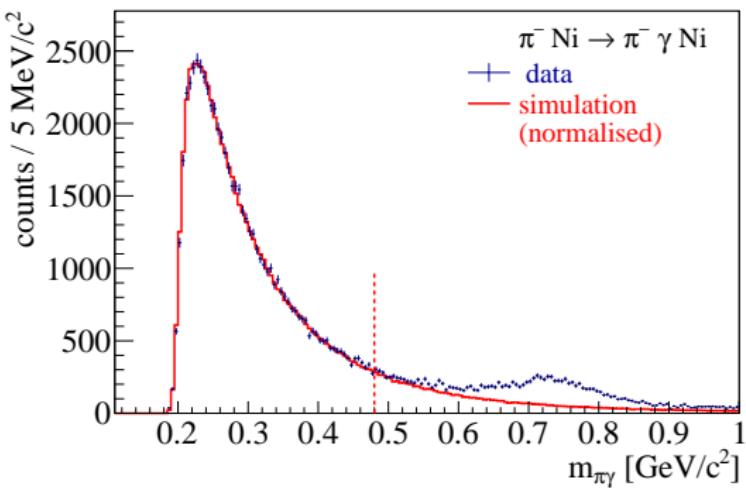
- Primakoff Compton reaction:



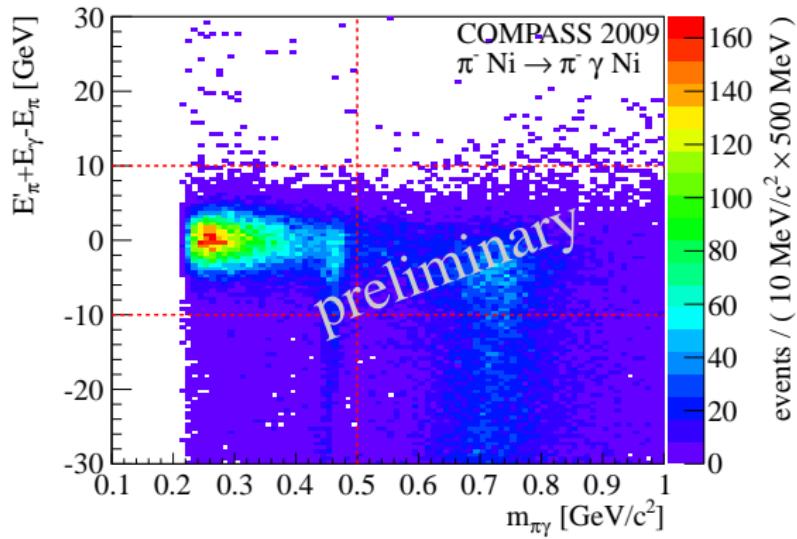
tiny extrapolation  $\gamma^* \rightarrow \gamma \mathcal{O}(10^{-3} m_\pi^2)$   
*fully under theoretical control*

[N. Kaiser, J.F., Nucl. Phys. A 812 (2008) 186]

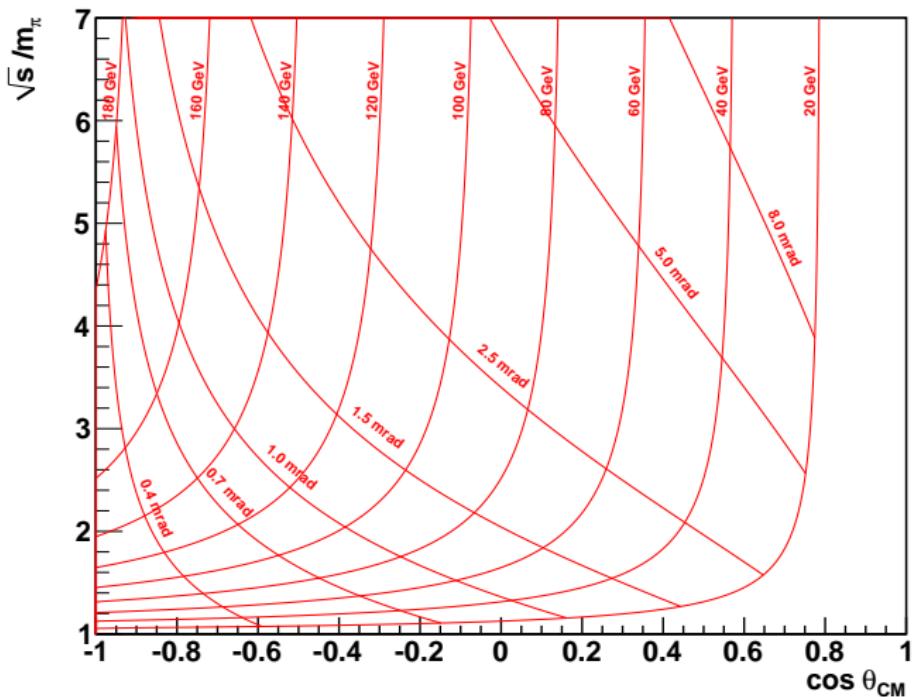


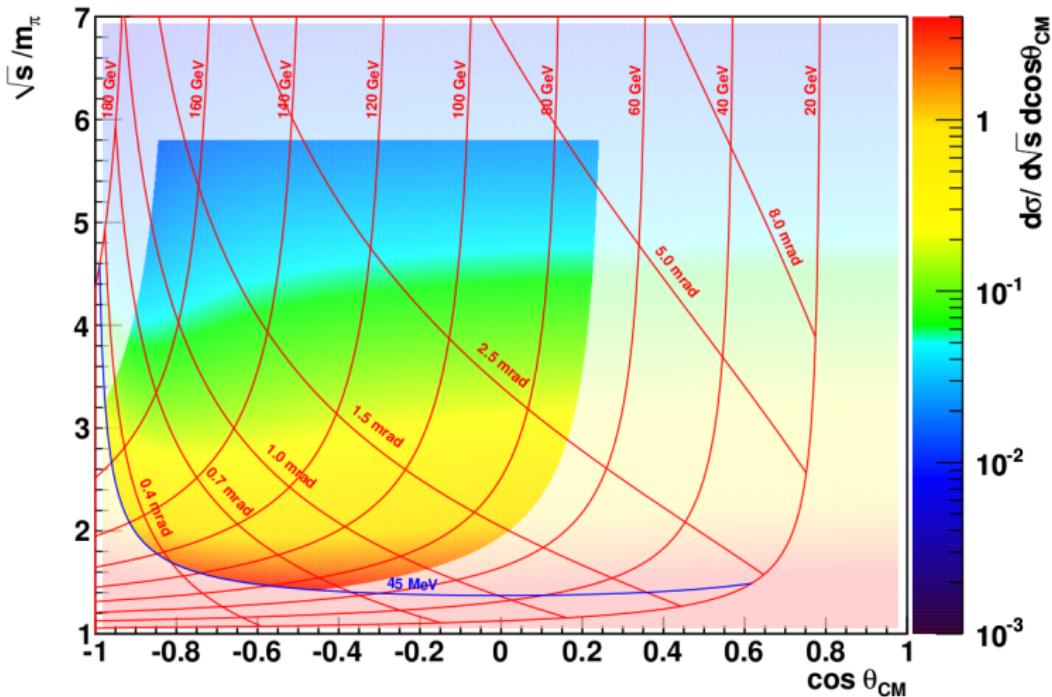


- $\rho$  contribution from  $\pi\gamma \rightarrow \pi\pi^0$



- $\rho$  contribution from  $\pi\gamma \rightarrow \pi\pi^0$

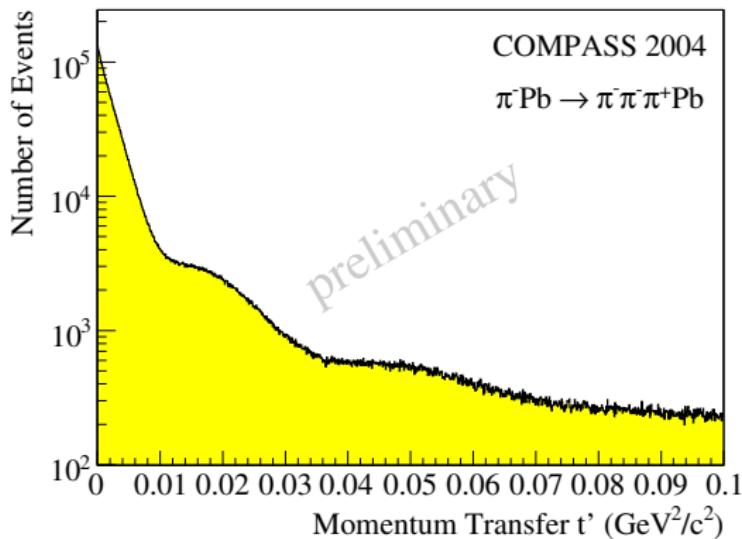




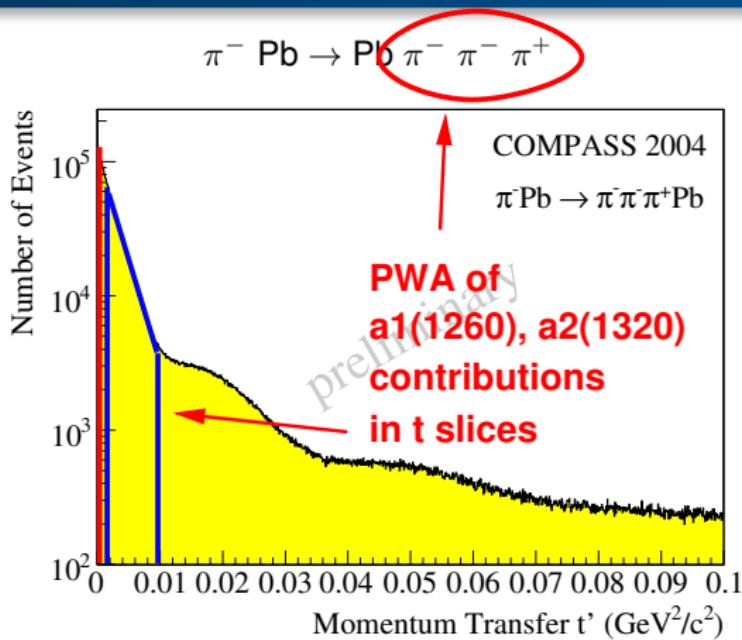


M.R. Pennington in the 2<sup>nd</sup> DAΦNE Physics Handbook,  
“What we learn by measuring  $\gamma\gamma \rightarrow \pi\pi$  at DAΦNE”:

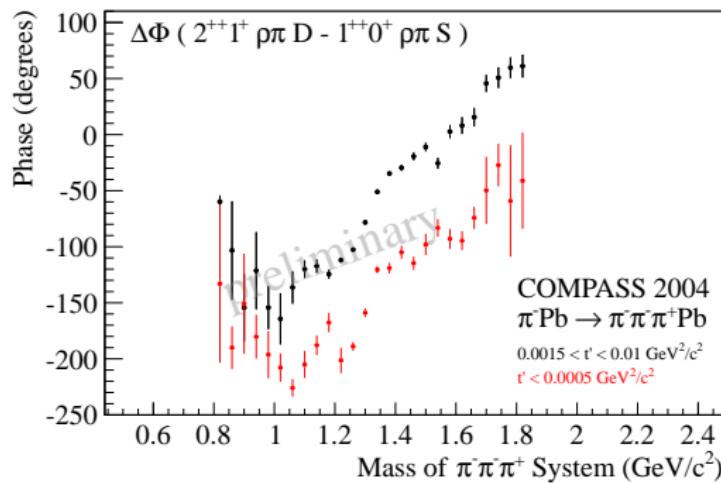
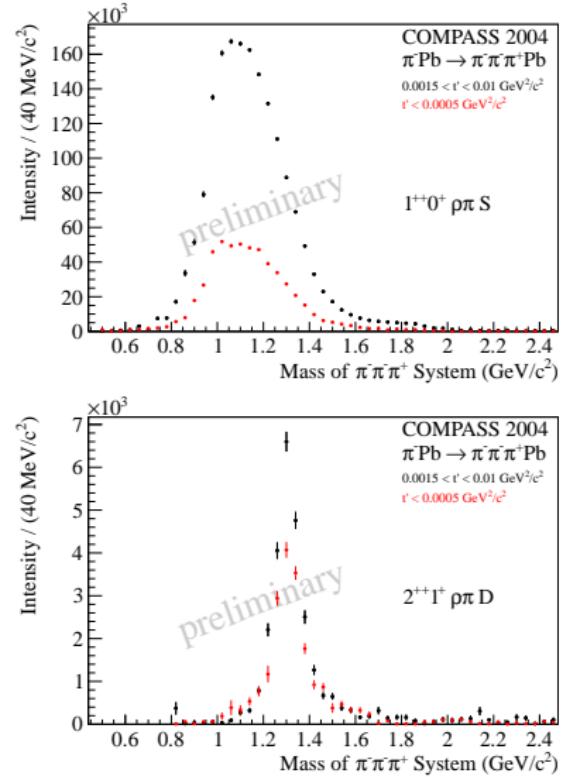
All this means that the only way to measure the pion polarisabilities is in the Compton scattering process near threshold and not in  $\gamma\gamma \rightarrow \pi\pi$ . Though the low energy  $\gamma\gamma \rightarrow \pi\pi$  scattering is seemingly close to the Compton threshold (...) and so the *extrapolation* not very far, the dominance of the pion pole (...) means that the energy scale for this continuation is  $m_\pi$ . Thus the polarisabilities cannot be determined accurately from  $\gamma\gamma$  experiments in a model-independent way and must be measured in the Compton scattering region.

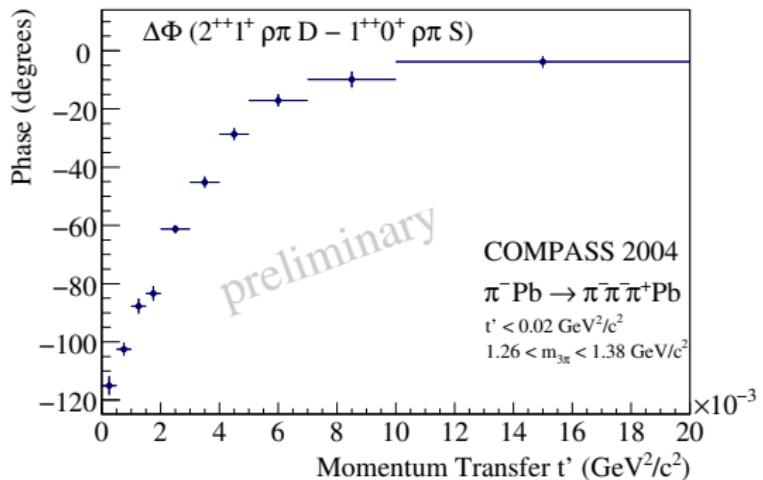
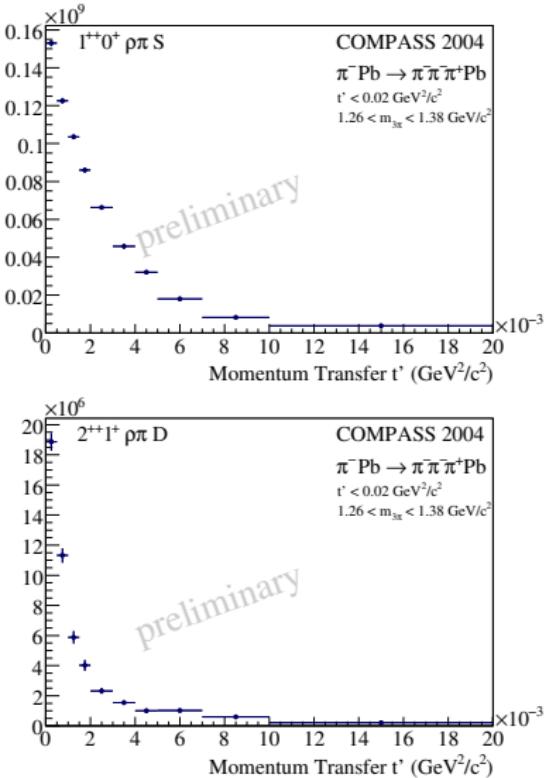


- "Low  $t'$ ":  $10^{-3} (\text{GeV}/\text{c})^2 < t' < 10^{-2} (\text{GeV}/\text{c})^2$   $\sim 2\,000\,000$  events
- "Primakoff region":  $t' < 10^{-3} (\text{GeV}/\text{c})^2$   $\sim 1\,000\,000$  events



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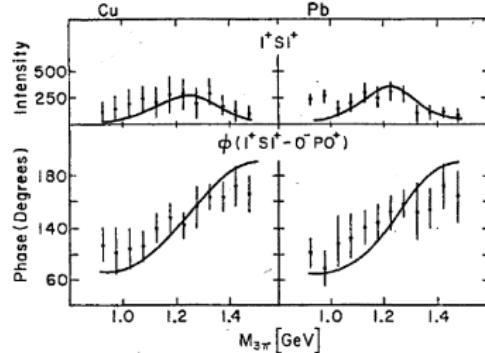
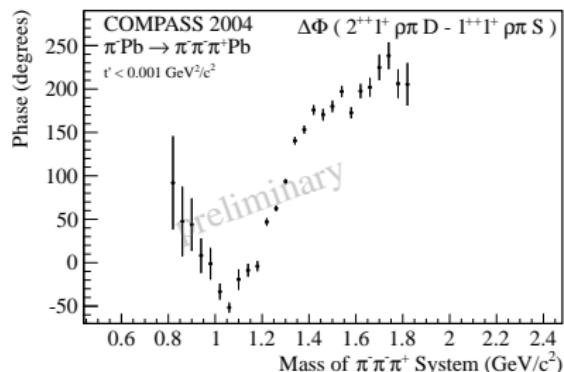
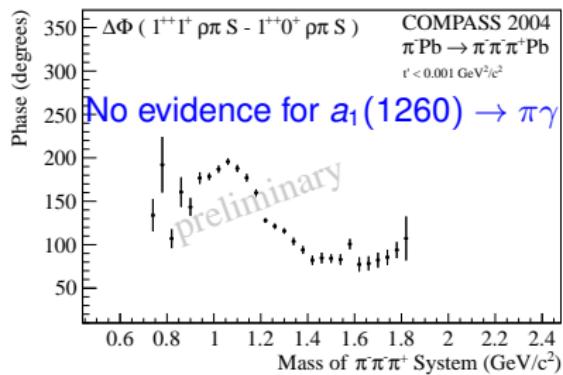
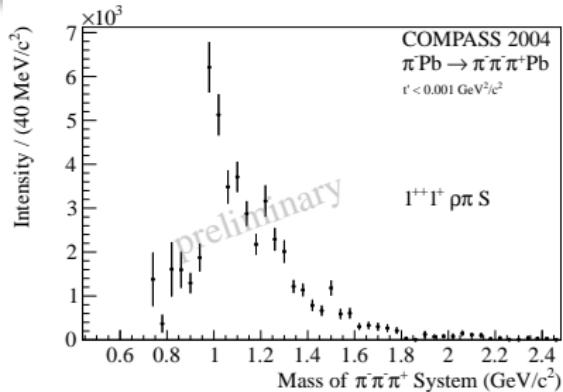




- transition of  $\pi\gamma$  to  $\pi IP \rightarrow a_2$  production
- work in progress
- interference can be used to map details of resonances and production mechanisms



# Primakoff production of $a_1(1260)$ vs. E272 result



M. Zielinski et al, Phys. Rev. Lett 52 (1984) 1195



- Mass-independent PWA (narrow mass bins):

$$\sigma_{\text{indep}}(\tau, m, t') = \sum_{\epsilon=\pm 1} \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^{\epsilon} f_i^{\epsilon}(t') \psi_i^{\epsilon}(\tau, m) \right|^2 / \sqrt{\int |f_i^{\epsilon}(t')|^2 dt'} \sqrt{\int |\psi_i^{\epsilon}(\tau', m)|^2 d\tau'}$$

- Production strength assumed constant in single bins
  - Decay amplitudes  $\psi_i^{\epsilon}(\tau, m)$ , with  $t'$  dependence  $f_i^{\epsilon}(t')$
  - Production amplitudes  $T_{ir}^{\epsilon}$  → Extended log-likelihood fit
  - Acceptance corrections included
- Spin-density matrix:  $\rho_{ij}^{\epsilon} = \sum_r T_{ir}^{\epsilon} T_{jr}^{\epsilon*}$

→ Physical parameters:

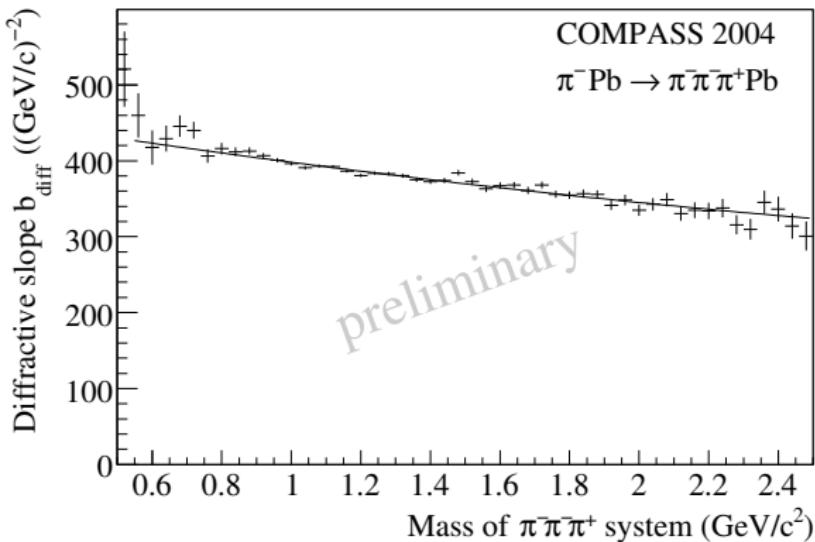
$$\text{Intens}_i^{\epsilon} = \rho_{ii}^{\epsilon},$$

relative phase  $\Phi_{ij}^{\epsilon}$

$$\text{Coh}_{i,j}^{\epsilon} = \sqrt{(\text{Re } \rho_{ij}^{\epsilon})^2 + (\text{Im } \rho_{ij}^{\epsilon})^2} / \sqrt{\rho_{ii}^{\epsilon} \rho_{jj}^{\epsilon}}$$

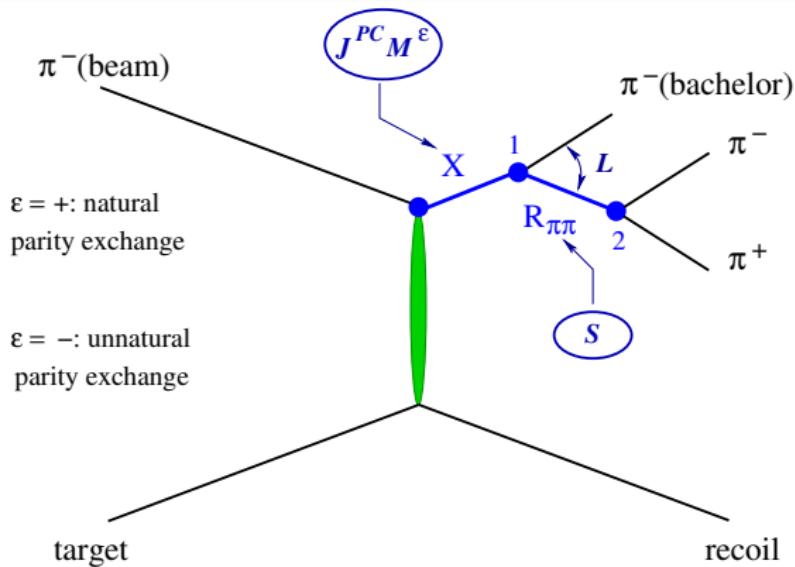
- Mass-dependent  $\chi^2$ -fit (not presented here):

- $X$  parameterized by Breit-Wigner (BW) functions
- Background can be added





## Isobar Model

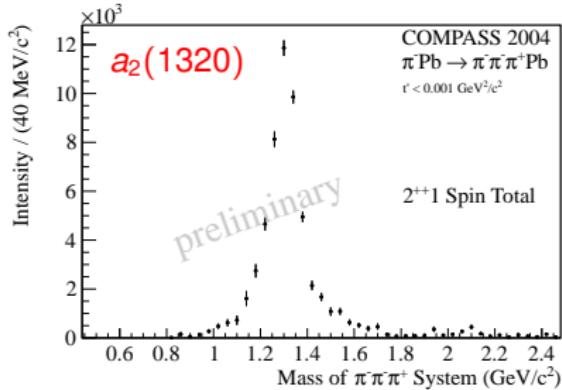
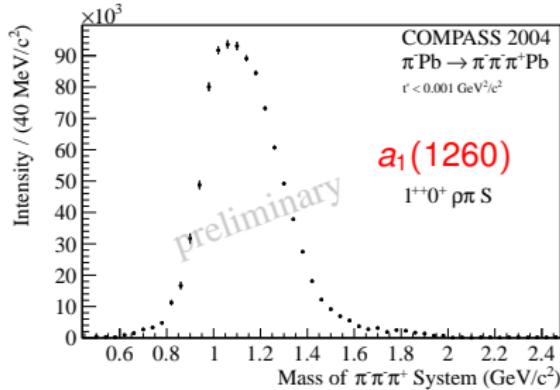
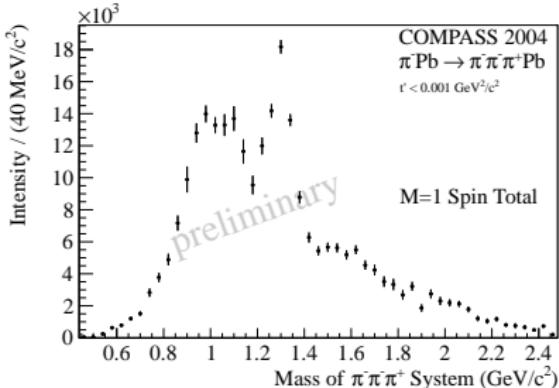
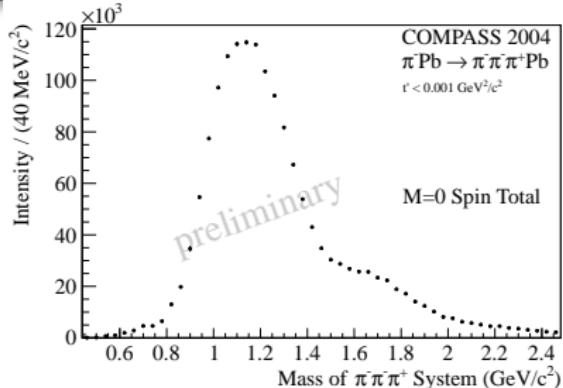


- Isobar model:  
Intermediate  
2-particle decays
- Partial wave in  
reflectivity basis:  
 $J^{PC} M^\epsilon [\text{isobar}] L$

- Mass-independent PWA ( $40 \text{ MeV}/c^2$  mass bins): **38 waves**  
Fit of angular dependence of partial waves, interferences
- Mass-dependent  $\chi^2$ -fit (Not presented here)



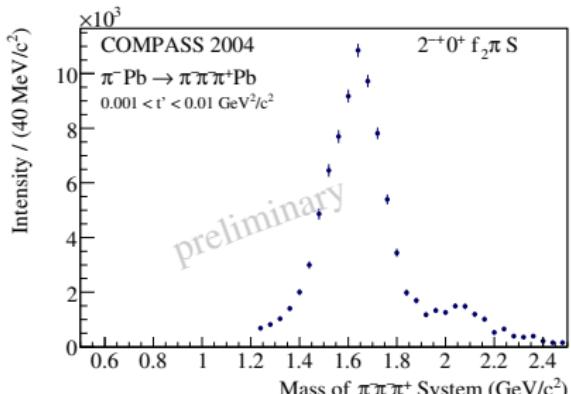
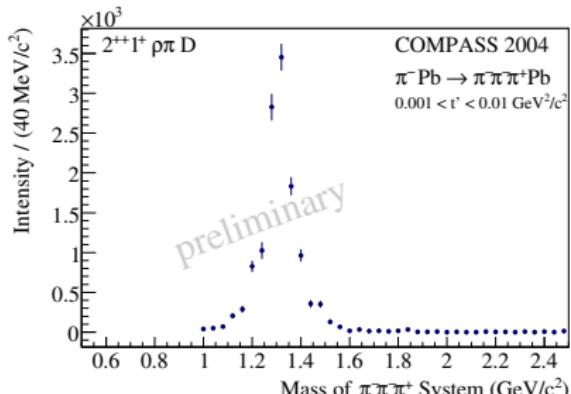
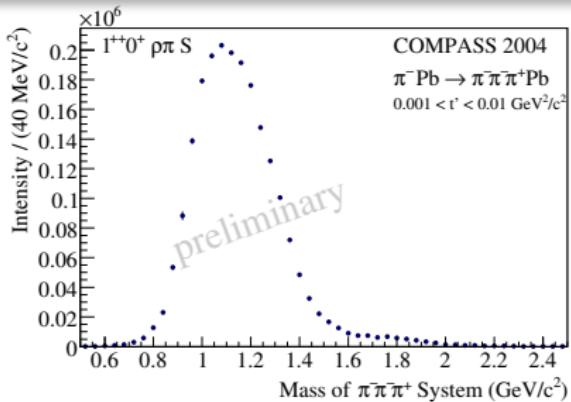
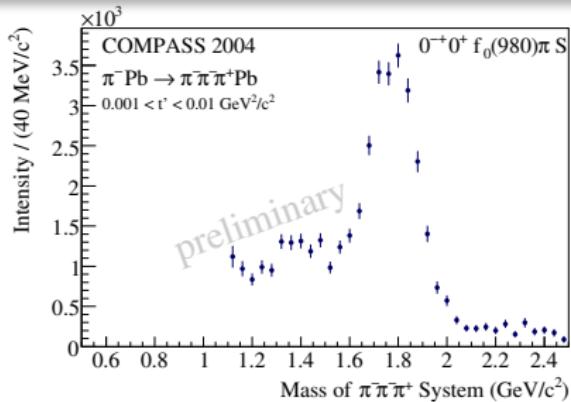
# Major intensities in $m(3\pi)$ -bins (acceptance corrected)





# PWA of data with low $t'$

Intensity of selected waves:  $0^{-+}0^+ f_0(980)\pi S$ ,  $1^{++}0^+ \rho\pi S$ ,  $2^{++}1^+ \rho\pi D$ ,  $2^{-+}0^+ f_2(1270)\pi S$



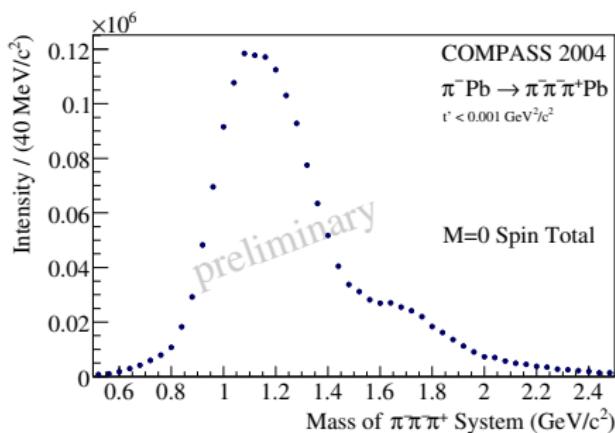
"Spin Totals": Sum of all contributions for given M (i.e. z-projection of J)

$t'$ -dependent amplitudes:

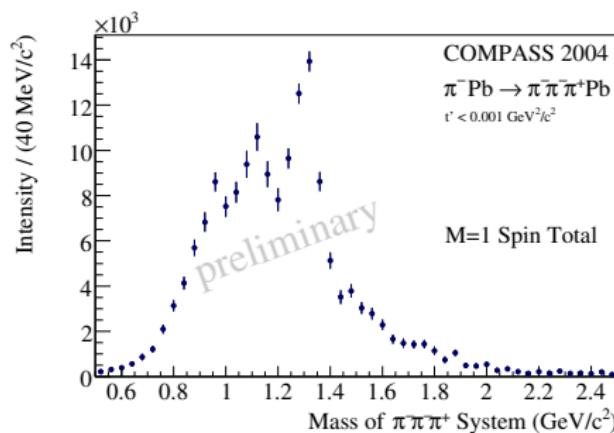
Primakoff production: **M=1**:  $\sigma(t') \propto e^{-b_{\text{Prim}} t'} \rightarrow$  arises at  $t' \approx 0$  (resolved shape!)

Diffractive production: **M=0**:  $\sigma(t') \propto e^{-b_{\text{diff}}(m) t'}$

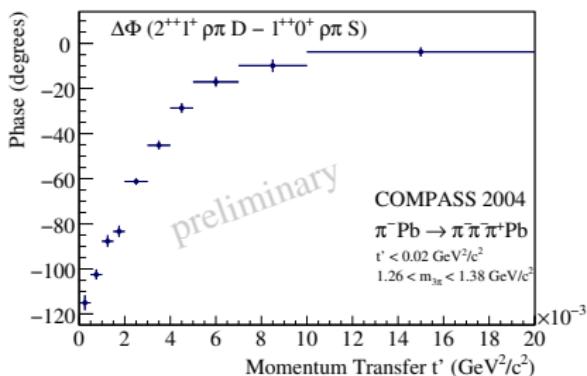
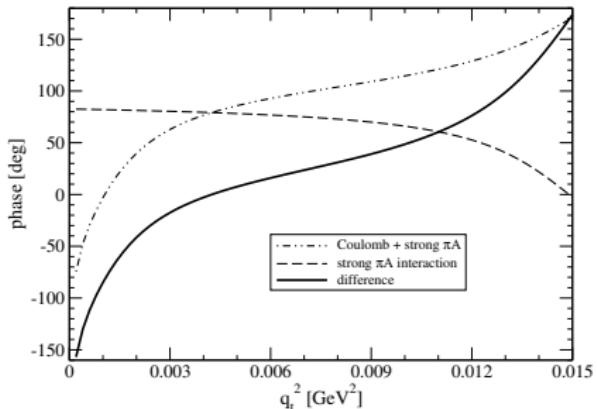
**M=1**:  $\sigma(t') \propto t' e^{-b_{\text{diff}}(m) t'} \rightarrow$  vanishes for  $t' \approx 0$



**M=0**



**M=1**



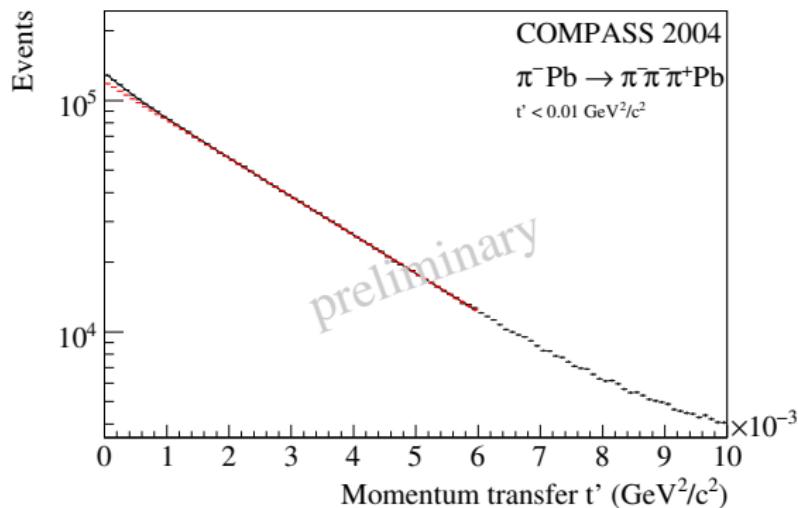
## Glauber modell

G. Fäldt and U. Tengblad, Phys. Rev. C79, 014607 (2009)

Plot: N. Kaiser (TU München)

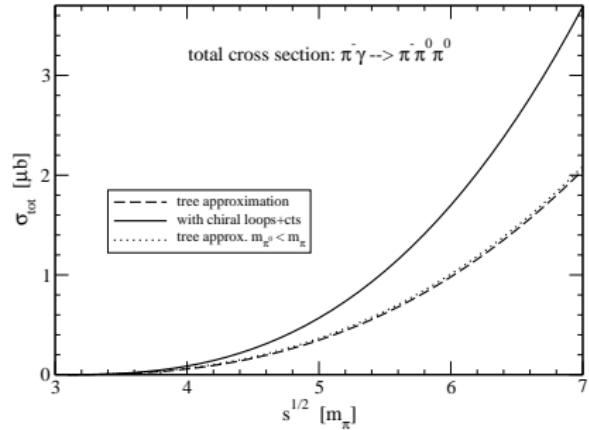
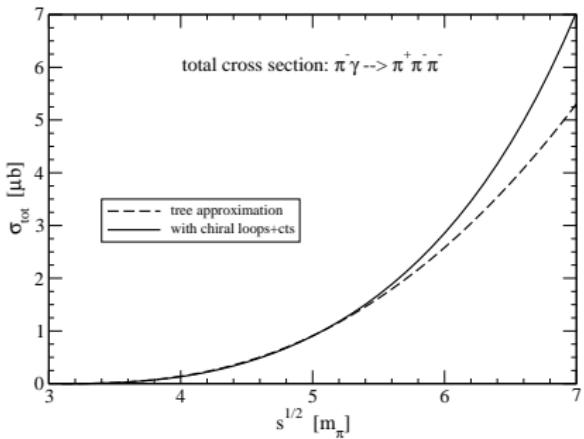
- ⇒ indicates confirmation of interference Coulomb-interaction - strong interaction
- ⇒ detailed studies of the nature of resonances

Primakoff:  $\sigma(t') \propto e^{-b_{\text{Prim}} t'}$ ,  $b_{\text{Prim}} \approx 2000 (\text{GeV}/c)^{-2}$  (mainly resolution)  
Diffractive:  $\sigma(t') \propto e^{-b_{\text{diff}} t'}$ ,  $b_{\text{diff}} \approx 400 (\text{GeV}/c)^{-2}$  for lead target



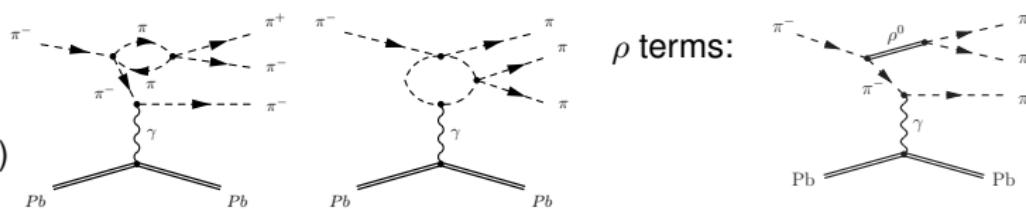
(Mass) spectrum of this Primakoff contribution?

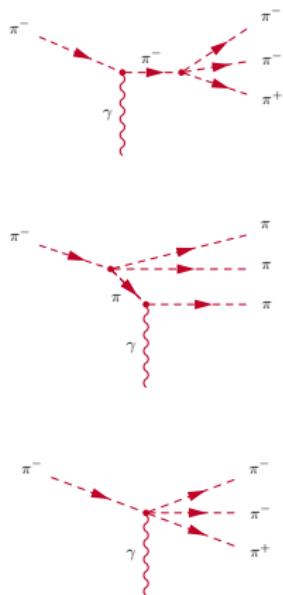
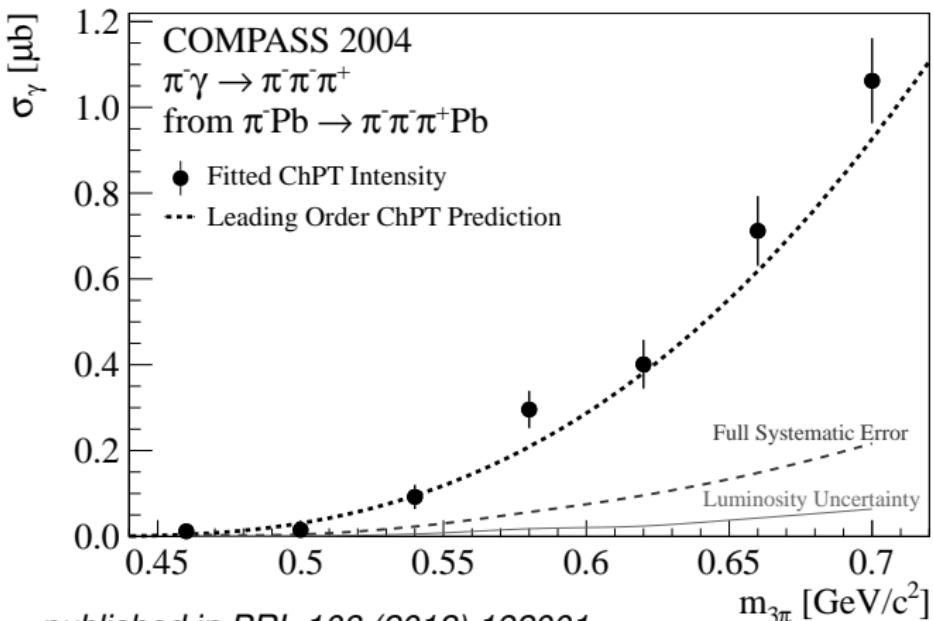
⇒ Statistical subtraction of diffractive background (for bins of  $m_{3\pi}$ )



Chiral loops, e.g.

(N. Kaiser,  
NPA848 (2010) 198)

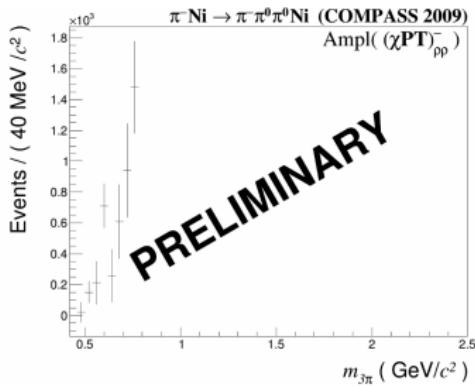
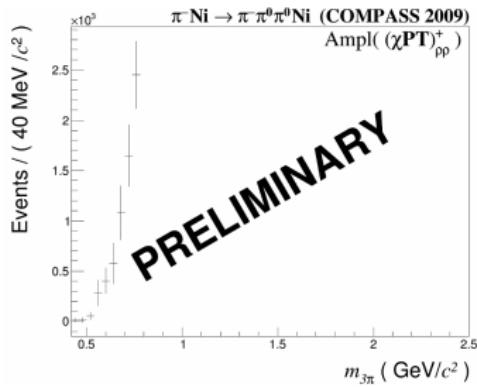


Measured absolute cross-section of  $\pi^-\gamma \rightarrow \pi^-\pi^-\pi^+$ 

published in PRL 108 (2012) 192001

## Partial Wave Analysis

*Isobaric Model – Chiral Wave*



## Partial Wave Analysis

Chiral Model - Amplitudes

