

All-optical probes of quantum vacuum nonlinearity

Felix Karbstein

Helmholtz-Institut Jena & Friedrich-Schiller-Universität Jena



Helmholtz-Institut Jena



Probing quantum vacuum nonlinearity with high-intensity lasers

Felix Karbstein

Helmholtz-Institut Jena & Friedrich-Schiller-Universität Jena



Helmholtz-Institut Jena



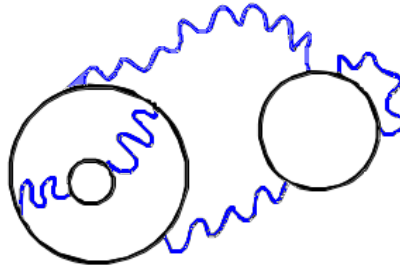
Outline

- (i) Introduction
- (ii) Our approach
- (iii) Vacuum birefringence
- (iv) Conclusions & Outlook

(i) Introduction

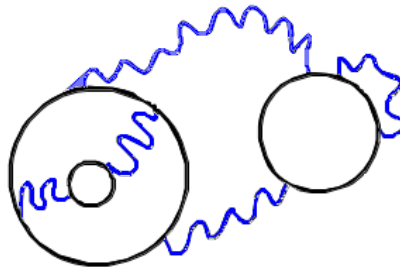
(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.



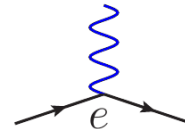
(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.



- knows about particle content and interactions of the theory,

in QED: e^- , e^+ , γ interacting via



e : electron charge

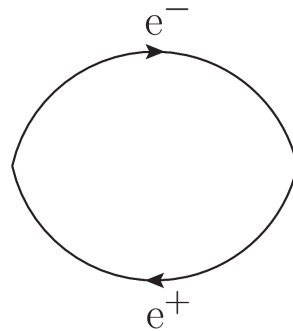
- particle-antiparticle fluctuations, virtual (= off-shell) particles

- happens everywhere/all the time

(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.

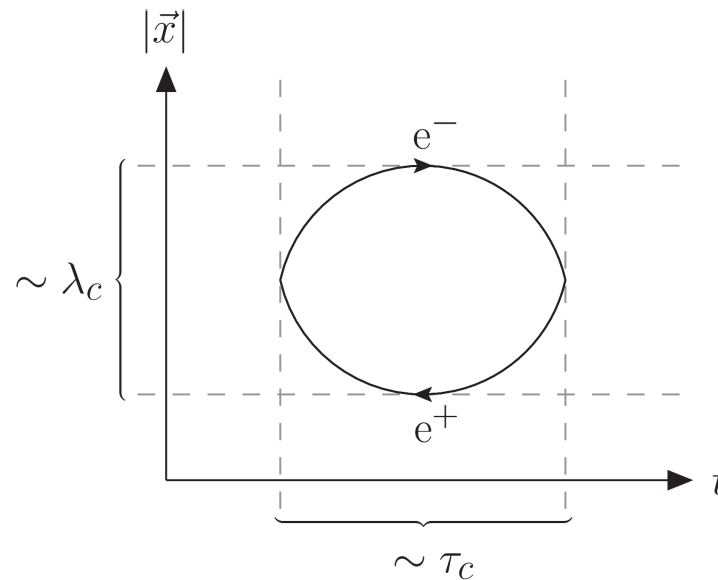
At 1-loop level:



(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.

At 1-loop level:



$$\lambda_c \sim \tau_c \sim \frac{1}{m_e}$$

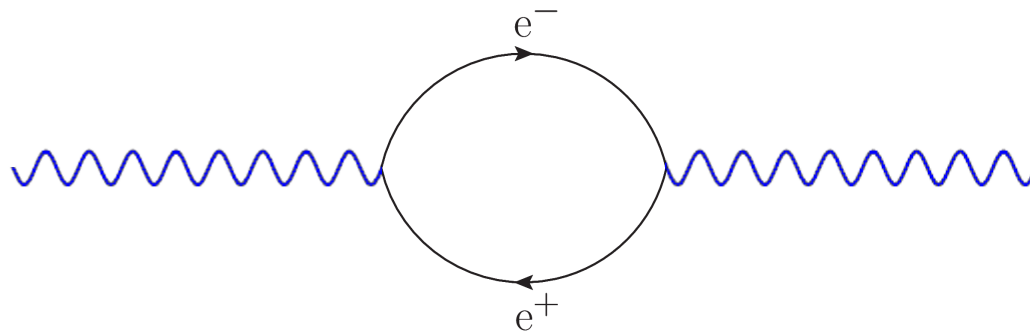
$$\lambda_c = 3.9 \cdot 10^{-13} \text{m}$$

$$\tau_c = 1.3 \cdot 10^{-21} \text{s}$$

(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.

At 1-loop level:

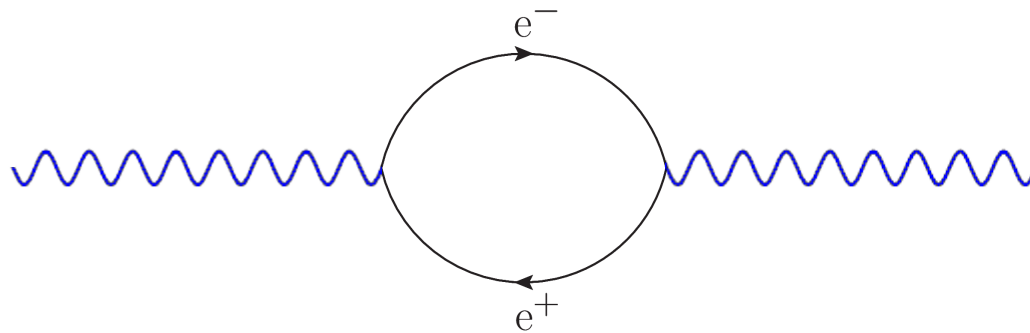


- in particular affects **photon propagation**

(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.

At 1-loop level:

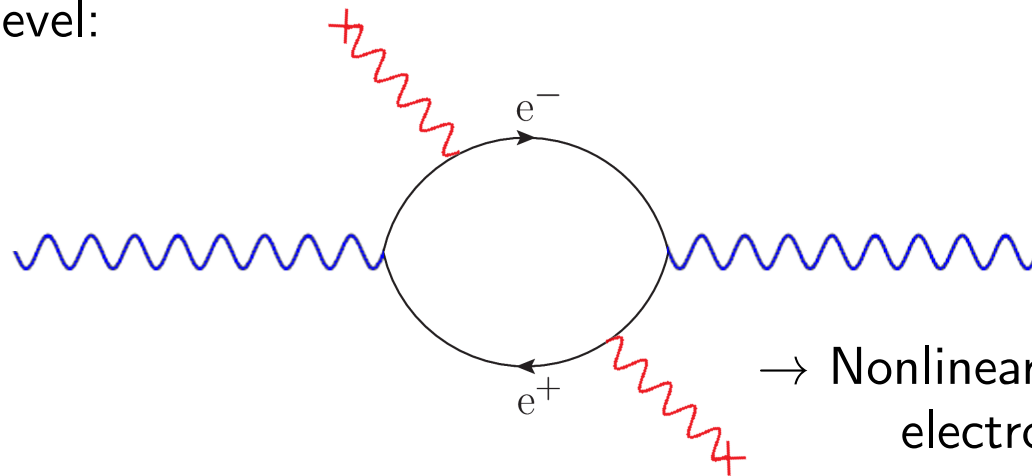


- in particular affects **photon propagation**; **no** measurable consequences

(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.

At 1-loop level:



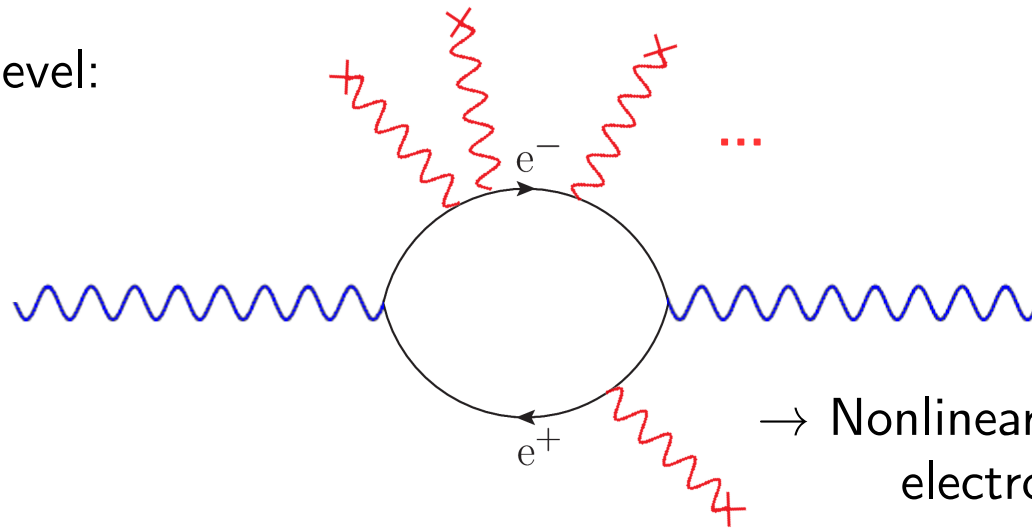
→ Nonlinear couplings between electromagnetic fields.

- in particular affects **photon propagation**; ~~no~~ measurable consequences
- vacuum has to be distorted, e.g., by external **electromagnetic field**

(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.

At 1-loop level:



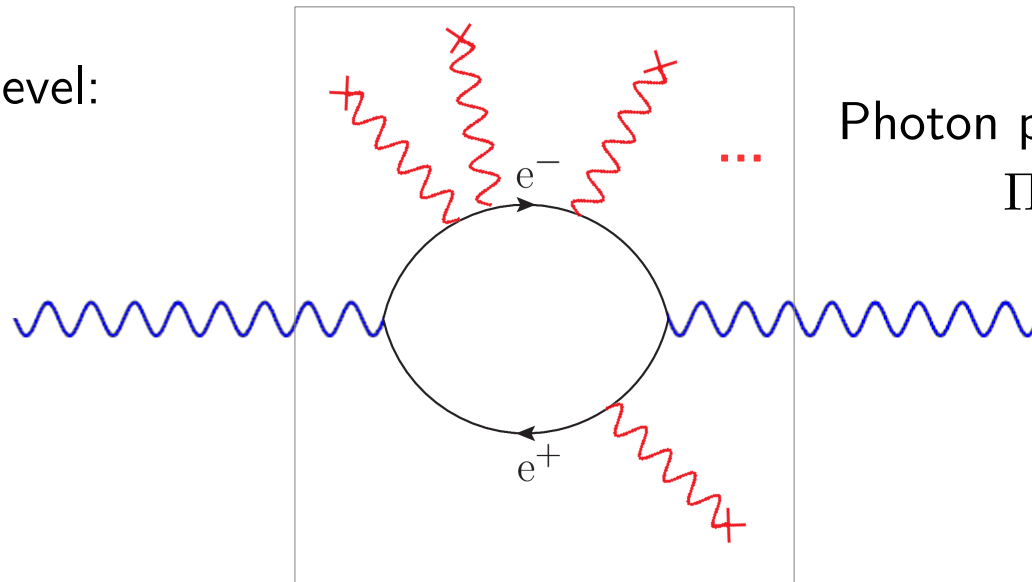
→ Nonlinear couplings between electromagnetic fields.

- in particular affects **photon propagation**; ~~no~~ measurable consequences
- vacuum has to be distorted, e.g., by external **electromagnetic field**

(i) Introduction

The **quantum** vacuum is not empty and boring, but rather a highly nontrivial interacting medium.

At 1-loop level:



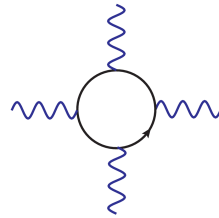
Photon polarization tensor:
 $\Pi^{\mu\nu}(x, x' | \mathcal{A})$

- in particular affects **photon propagation**; ~~no~~ measurable consequences
- vacuum has to be distorted, e.g., by external **electromagnetic field**

(i) Introduction

Quantum vacuum nonlinearity manifests itself in various effects, e.g.,

- direct light-by-light scattering



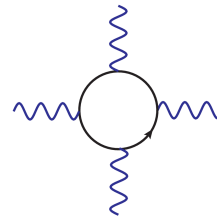
[Euler, Kockel: Naturwiss. 1935]

[Karplus, Neuman: Phys. Rev. 1950]

(i) Introduction

Quantum vacuum nonlinearity manifests itself in various effects, e.g.,

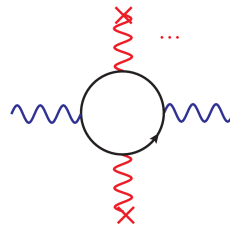
- direct light-by-light scattering



[Euler, Kockel: Naturwiss. 1935]

[Karplus, Neuman: Phys. Rev. 1950]

- vacuum birefringence



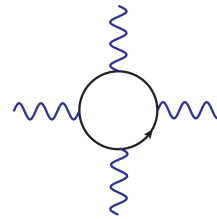
[Toll: PhD thesis 1952]

[Baier, Breitenlohner: Act. Phys. Austriaca & Nuov. Cim. 1967]

(i) Introduction

Quantum vacuum nonlinearity manifests itself in various effects, e.g.,

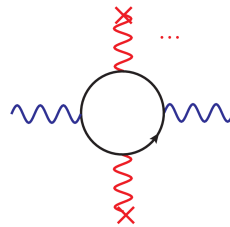
- direct light-by-light scattering



[Euler, Kockel: Naturwiss. 1935]

[Karplus, Neuman: Phys. Rev. 1950]

- vacuum birefringence



[Toll: PhD thesis 1952]

[Baier, Breitenlohner: Act. Phys. Austriaca & Nuov. Cim. 1967]

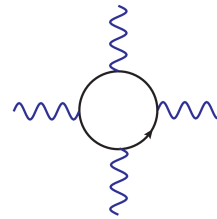
- quantum reflection

[Gies, FK, Seegert: New J. Phys. 2013 & 2015]

(i) Introduction

Quantum vacuum nonlinearity manifests itself in various effects, e.g.,

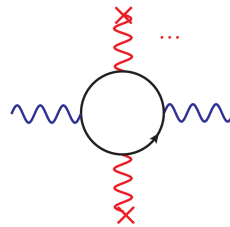
- direct light-by-light scattering



[Euler, Kockel: Naturwiss. 1935]

[Karplus, Neuman: Phys. Rev. 1950]

- vacuum birefringence



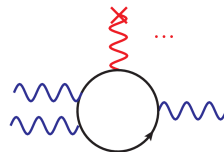
[Toll: PhD thesis 1952]

[Baier, Breitenlohner: Act. Phys. Austriaca & Nuov. Cim. 1967]

- quantum reflection

[Gies, FK, Seegert: New J. Phys. 2013 & 2015]

- photon splitting



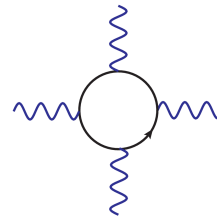
[Adler: Ann. Phys. 1971]

[Papayan, Ritus: JETP 1971]

(i) Introduction

Quantum vacuum nonlinearity manifests itself in various effects, e.g.,

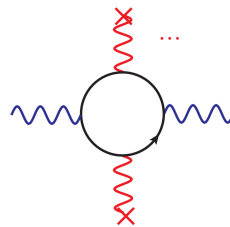
- direct light-by-light scattering



[Euler, Kockel: Naturwiss. 1935]

[Karplus, Neuman: Phys. Rev. 1950]

- vacuum birefringence



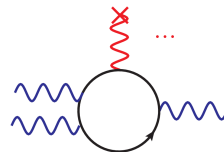
[Toll: PhD thesis 1952]

[Baier, Breitenlohner: Act. Phys. Austriaca & Nuov. Cim. 1967]

- quantum reflection

[Gies, FK, Seegert: New J. Phys. 2013 & 2015]

- photon splitting



[Adler: Ann. Phys. 1971]

[Papanyan, Ritus: JETP 1971]

- photon merging

[Gies, FK, Shaisultanov: Phys. Rev. D 2014]

(ii) Our approach

(ii) Our approach

Problem: Most analytical calculations have been performed either for uniform, constant or planewave **backgrounds** (null-fields).

- Photon polarization tensor [\[Batalin, Shabad: JETP 1971\]](#)
[\[Baier, Milshtein, Strakhovenko: JETP 1975\]](#)
[\[Becker, Mitter: J. Phys. A 1975\]](#)

↔ the electromagnetic fields delivered by focused high-intensity lasers are highly inhomogeneous

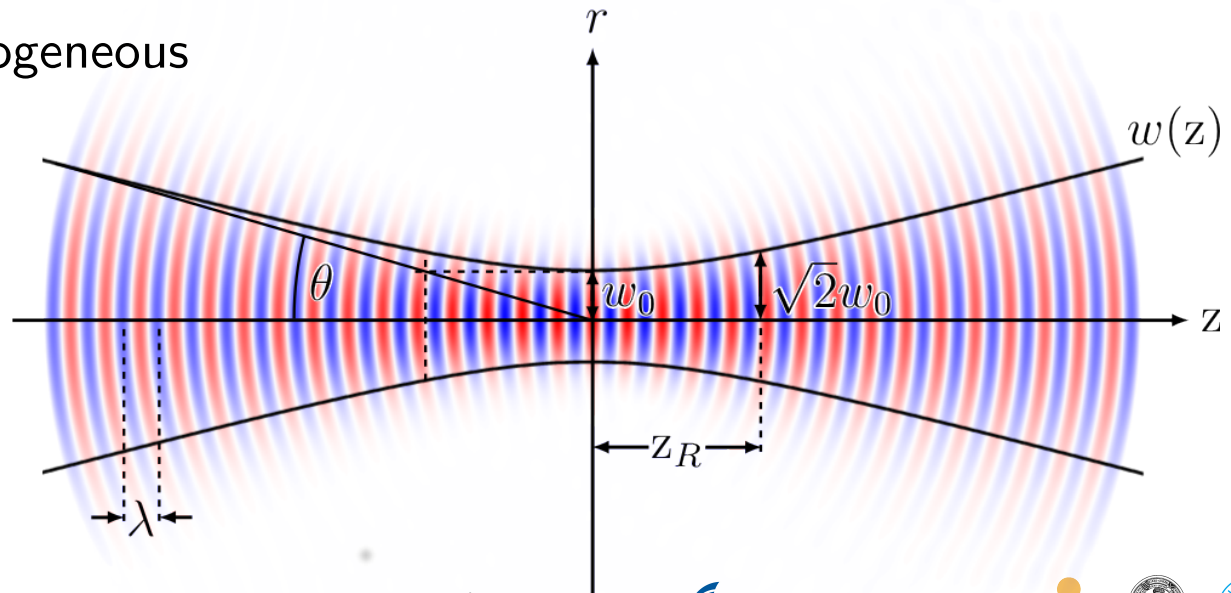
(ii) Our approach

Problem: Most analytical calculations have been performed either for uniform, constant or planewave **backgrounds** (null-fields).

- Photon polarization tensor [\[Batalin, Shabad: JETP 1971\]](#)
[\[Baier, Milshtein, Strakhovenko: JETP 1975\]](#)
[\[Becker, Mitter: J. Phys. A 1975\]](#)

↔ the electromagnetic fields delivered by focused high-intensity lasers are highly inhomogeneous

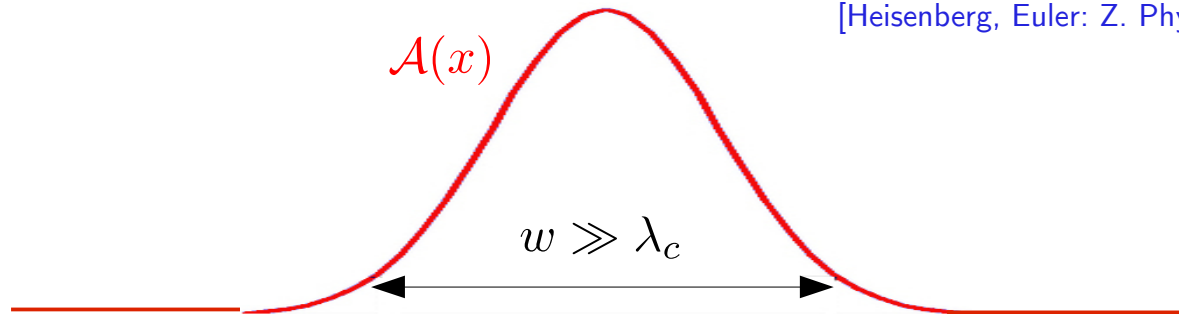
- Pulsed, focused Gaussian beams



(ii) Our approach

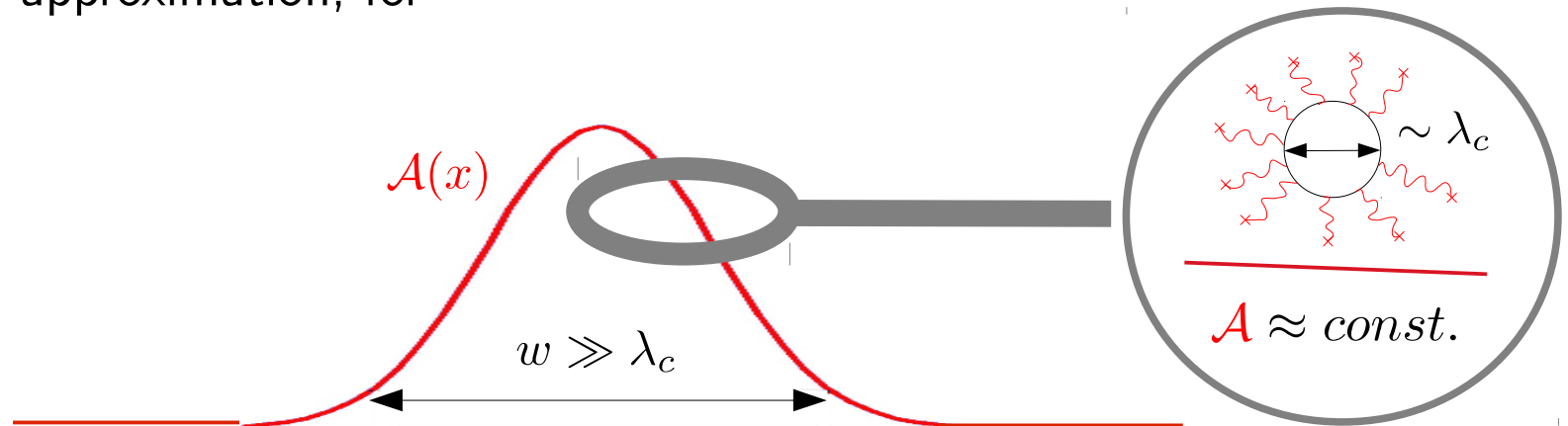
Our approach: The locally constant field approximation constitutes a good approximation, for [...] den speziellen Fall [...], in dem keine wirklichen Elektronen und Positronen vorhanden sind, und in dem sich das Feld auf Strecken der Compton-Wellenlänge nur wenig ändert.

[Heisenberg, Euler: Z. Phys. 1936]



(ii) Our approach

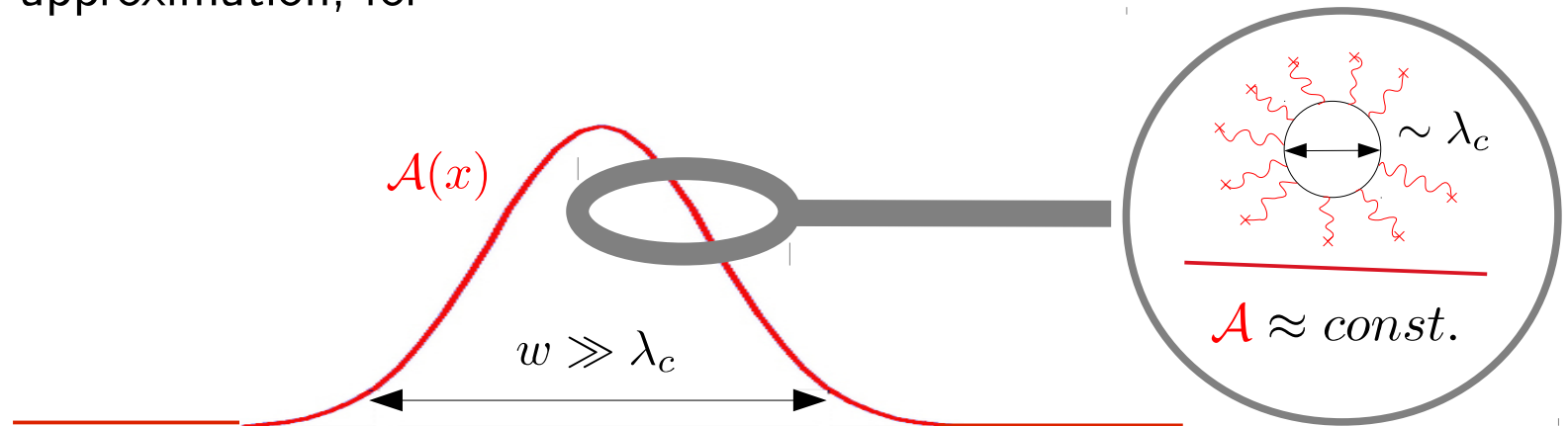
Our approach: The locally constant field approximation constitutes a good approximation, for



- analytical insights possible without having to solve the problem for the exact, inhomogeneous **background field** configuration.

(ii) Our approach

Our approach: The locally constant field approximation constitutes a good approximation, for



- analytical insights possible without having to solve the problem for the exact, inhomogeneous **background field** configuration.

→ Polarization tensor in pulsed, focused Gaussian beams

$$\Pi^{\rho\sigma}(k, k' | \mathcal{A}) = (g^{\rho\beta} k^\alpha - g^{\rho\alpha} k^\beta) \left[\int_x e^{i(k+k')x} \frac{\partial^2 \mathcal{L}[\mathcal{A}]}{\partial F^{\alpha\beta} \partial F^{\mu\nu}}(x) \right] (k'^\mu g^{\nu\sigma} - k'^\nu g^{\mu\sigma})$$

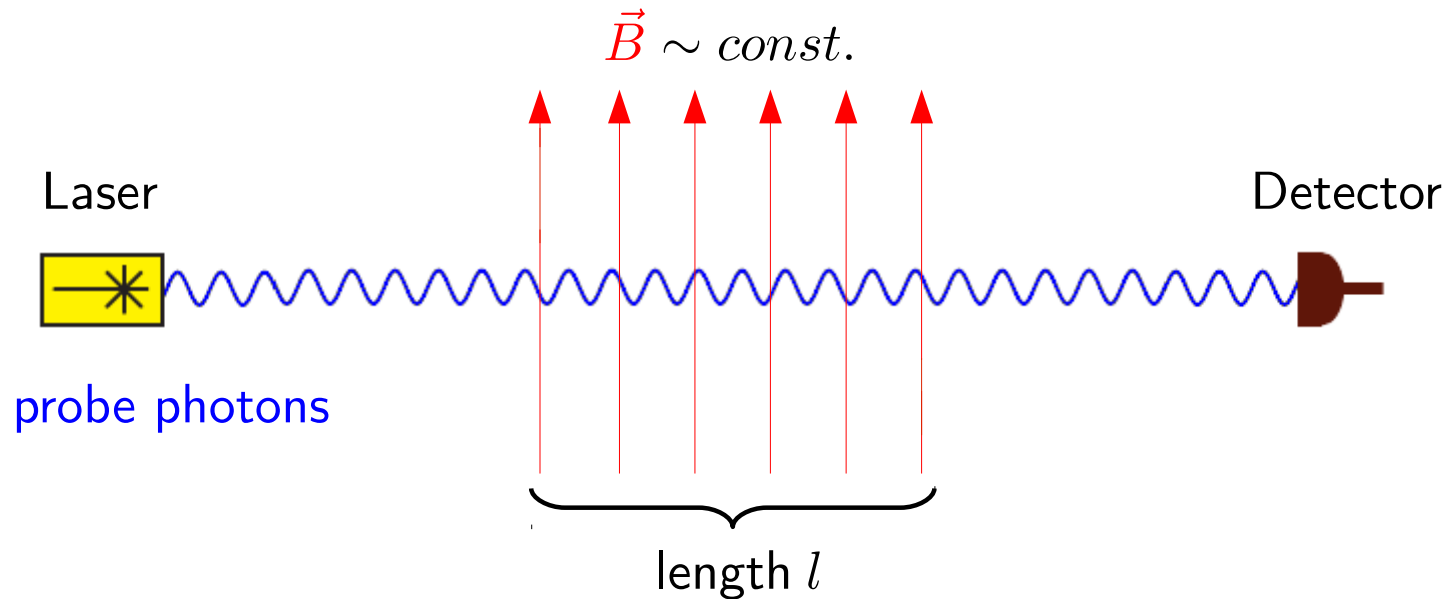
(iii) Vacuum birefringence

(iii) Vacuum birefringence

Conventional scenario:

[BMV (Biréfringence Magnétique du Vide) experiment, Toulouse]

[PVLAS (Polarizzazione del Vuoto con Laser) experiment, Padova/Ferrara]

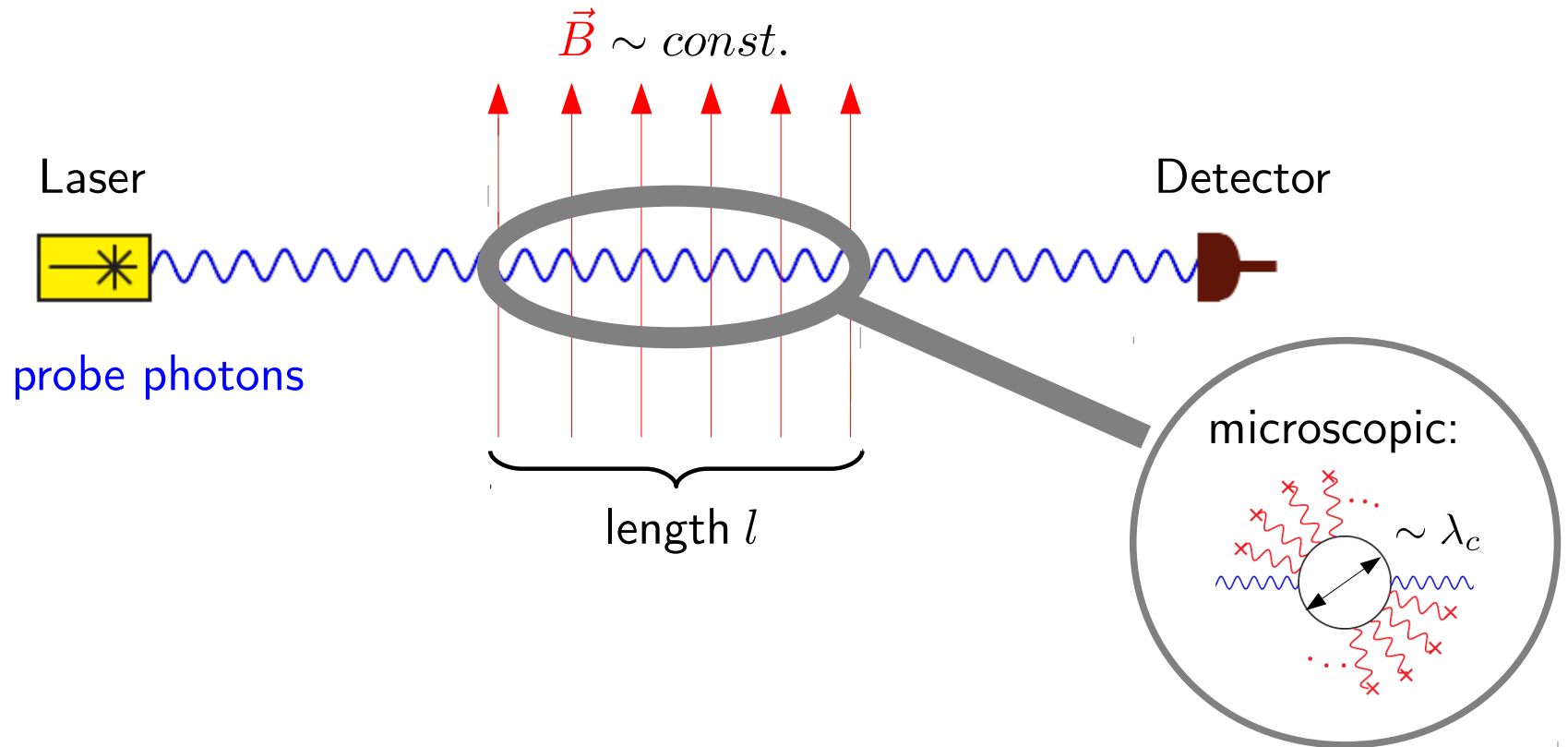


(iii) Vacuum birefringence

Conventional scenario:

[BMV (Biréfringence Magnétique du Vide) experiment, Toulouse]

[PVLAS (Polarizzazione del Vuoto con Laser) experiment, Padova/Ferrara]

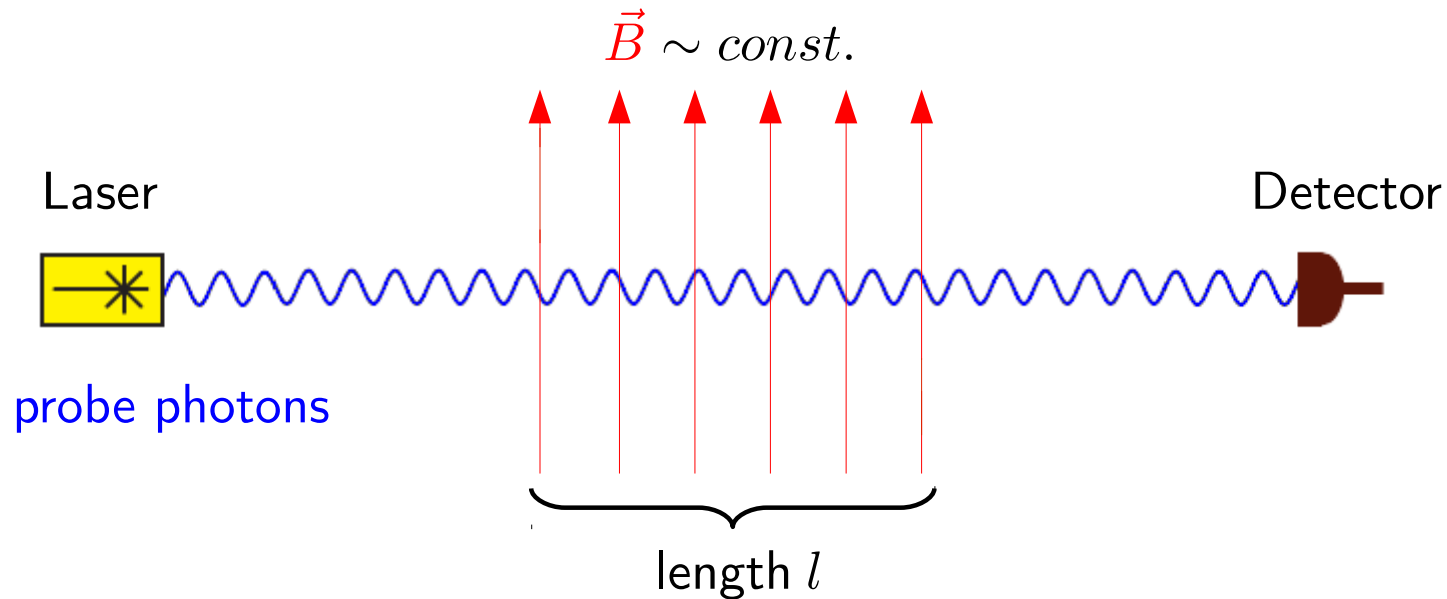


(iii) Vacuum birefringence

Conventional scenario:

[BMV (Biréfringence Magnétique du Vide) experiment, Toulouse]

[PVLAS (Polarizzazione del Vuoto con Laser) experiment, Padova/Ferrara]

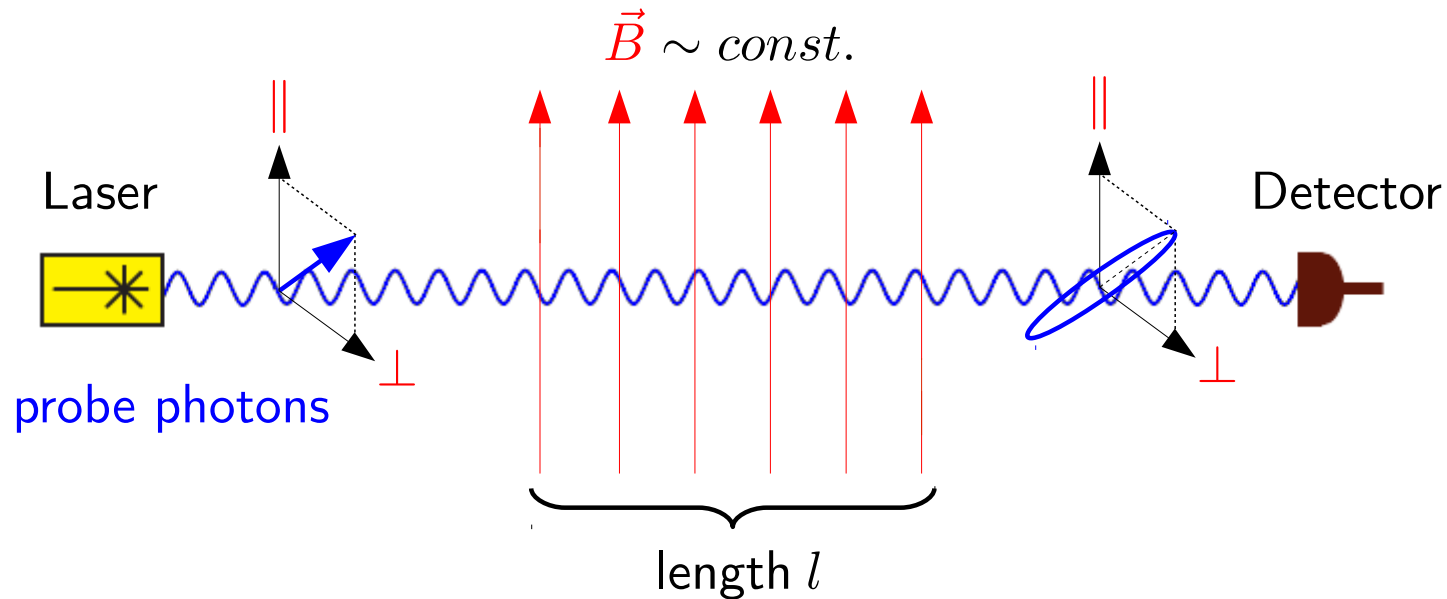


(iii) Vacuum birefringence

Conventional scenario:

[BMV (Biréfringence Magnétique du Vide) experiment, Toulouse]

[PVLAS (Polarizzazione del Vuoto con Laser) experiment, Padova/Ferrara]



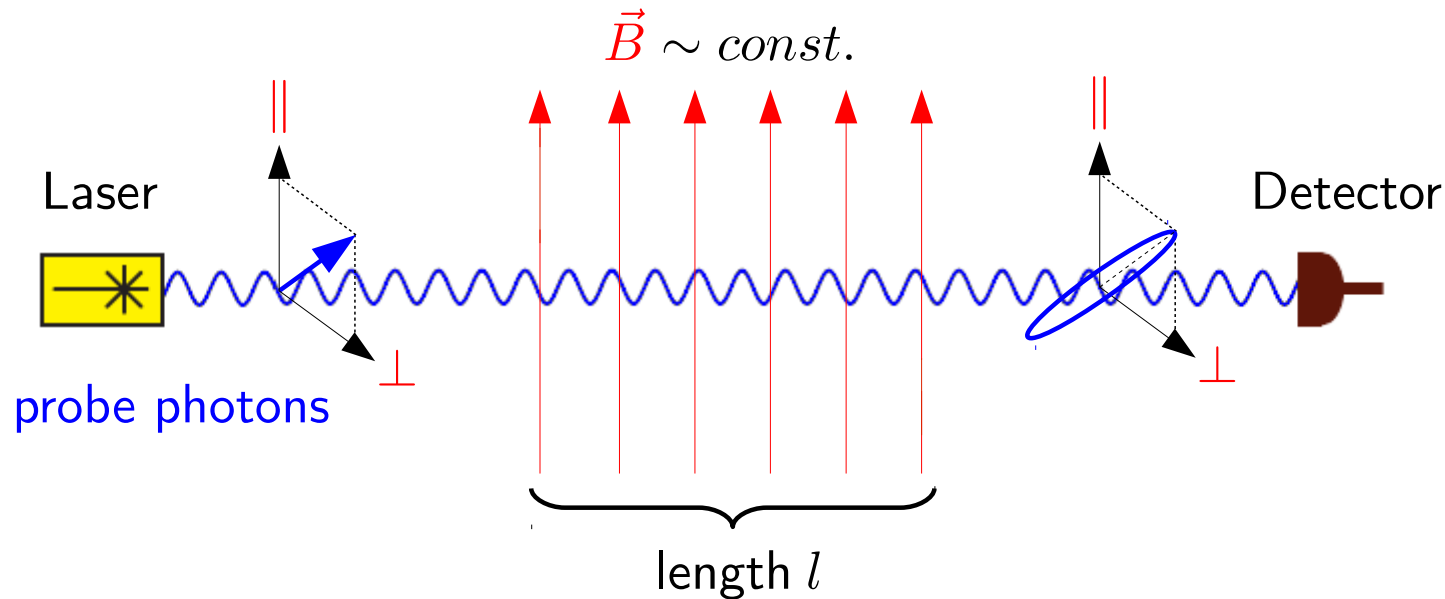
- vacuum birefringence $\rightarrow$ ellipticity: $\Delta\phi \sim \alpha \frac{l}{\lambda} \left(\frac{eB}{m_e^2} \right)^2$ $\leftarrow$ relative phase shift between $\parallel$ and $\perp$ modes

(iii) Vacuum birefringence

Conventional scenario:

[BMV (Biréfringence Magnétique du Vide) experiment, Toulouse]

[PVLAS (Polarizzazione del Vuoto con Laser) experiment, Padova/Ferrara]



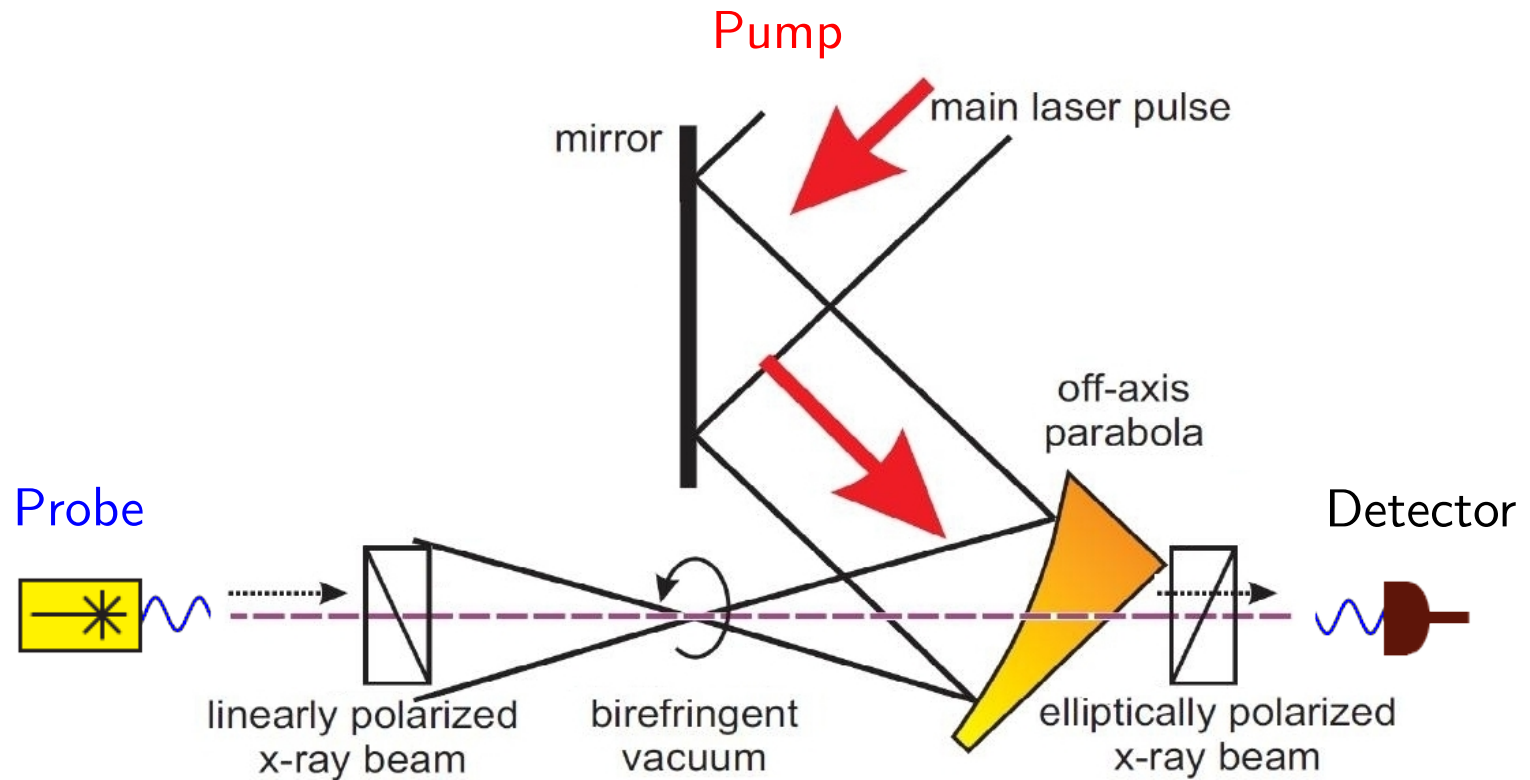
- vacuum birefringence $\rightarrow$ ellipticity: $\Delta\phi \sim \alpha \frac{l}{\lambda} \left(\frac{eB}{m_e^2} \right)^2$ $\leftarrow$ relative phase shift between $\parallel$ and $\perp$ modes

$\leftrightarrow$ photons in $\perp$ polarization mode induced: $N_{\perp} \simeq \left(\frac{\Delta\phi}{2} \right)^2 N_{\text{in}}$

(iii) Vacuum birefringence

Analogous scenario with **pump = high-intensity laser**:

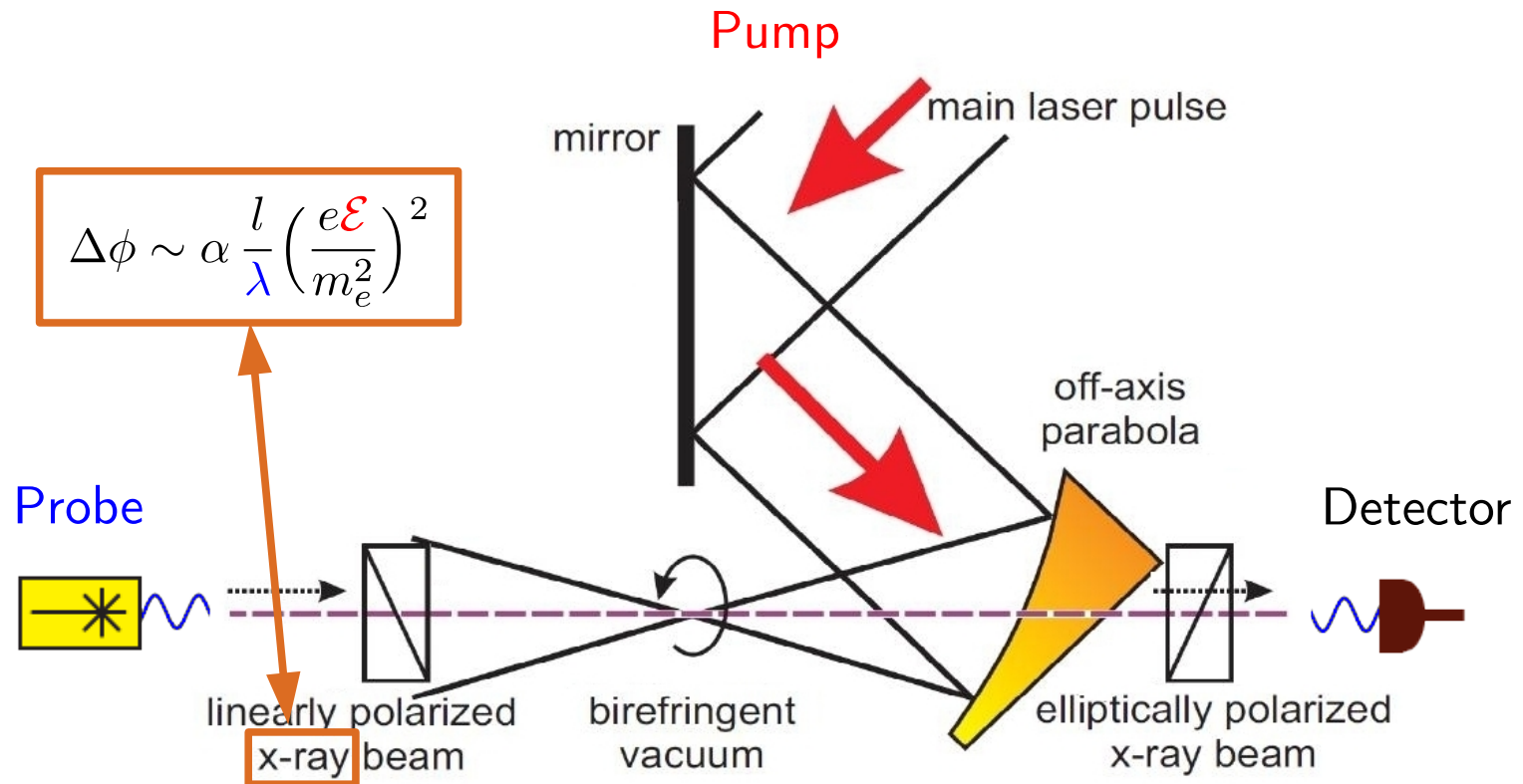
[Heinzl, Liesfeld, Amthor, Schworer, Sauerbrey, Wipf: Opt. Comm. 2006]



(iii) Vacuum birefringence

Analogous scenario with **pump = high-intensity laser**:

[Heinzl, Liesfeld, Amthor, Schworer, Sauerbrey, Wipf: Opt. Comm. 2006]

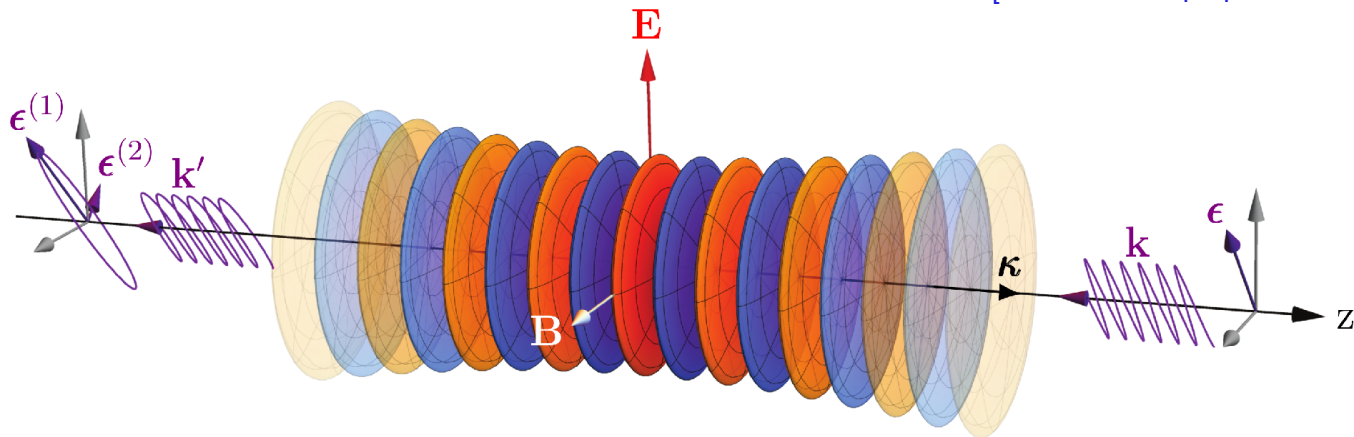


(iii) Vacuum birefringence

Analogous scenario with **pump = high-intensity laser**:

- in a recent study we account for the full inhomogeneous field profile of a linearly polarized, pulsed Gaussian laser beam

[FK, et al.: in preparation 2015]

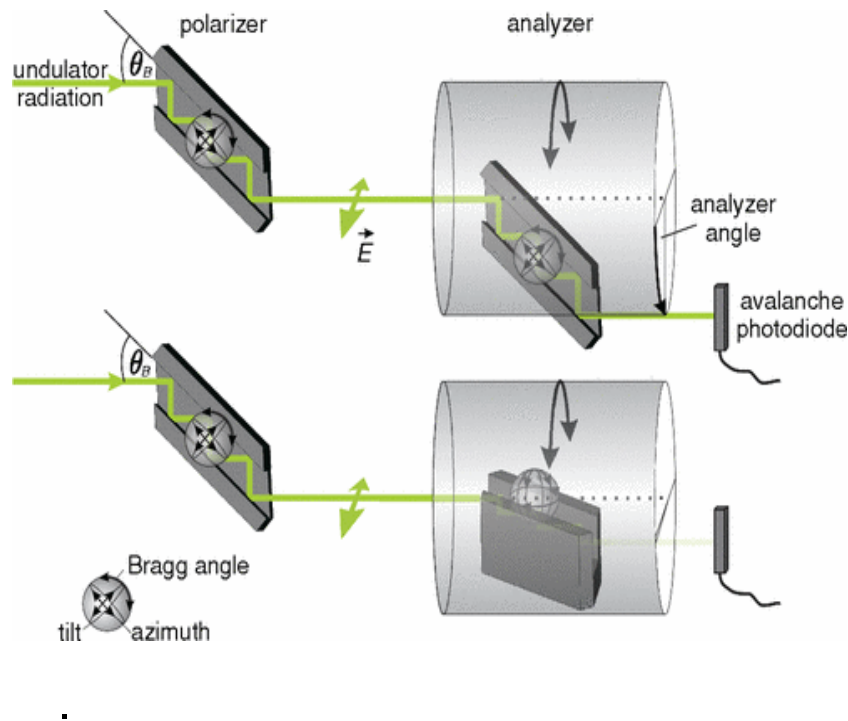


- **pump**: 1PW class laser ($W = 30\text{J}$, $\tau = 30\text{fs}$, $\lambda = 800\text{nm}$, $w_0 = 1\mu\text{m}$)
- **probe**: x-ray beam from FEL ($\omega = 12914\text{eV}$, $N_{\text{in}} \simeq 10^{12}$)

(iii) Vacuum birefringence

Analogous scenario with **pump = high-intensity laser**:

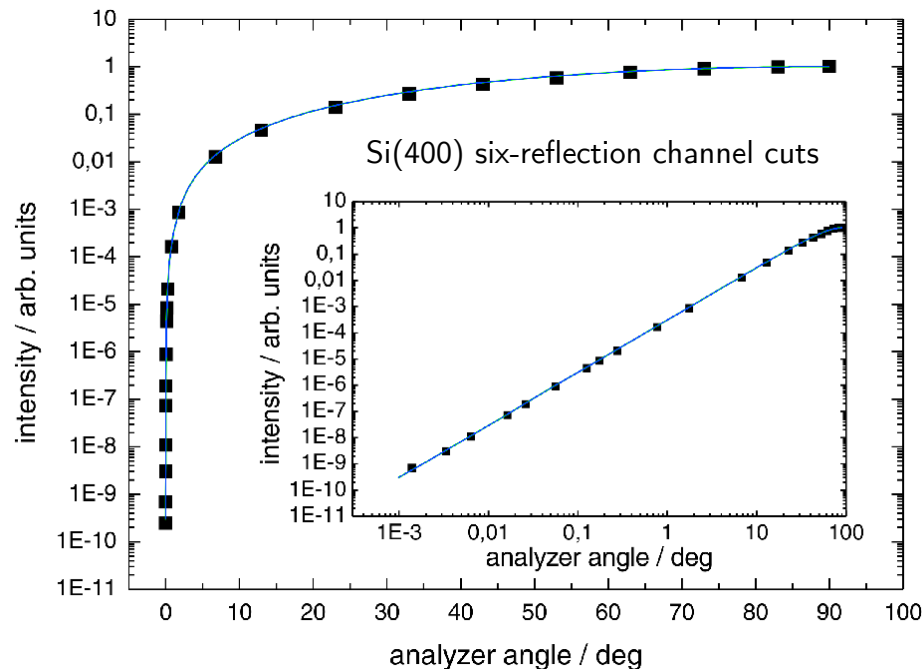
→ demand for high-purity x-ray polarimetry [Marx et al.: Phys. Rev. Lett. 2013]



(iii) Vacuum birefringence

Analogous scenario with **pump = high-intensity laser**:

→ demand for high-purity x-ray polarimetry [Marx et al.: Phys. Rev. Lett. 2013]



Polarization purity
record @ $\omega = 12914\text{eV}$:

$$\mathcal{P} = 5.7 \cdot 10^{-10}$$

- experimental confirmation of vacuum birefringence requires $\frac{N_{\perp}}{N_{\text{in}}} > \mathcal{P}$.

(iii) Vacuum birefringence

Our theoretical approach:

Idea: Interpret vacuum birefringence as **vacuum emission process:**

[FK, Shaisultanov: Phys. Rev. D **91** 113002 (2015)]

- laser fields correspond to macroscopic electromagnetic fields
- taking this literally means not to resolve the individual photons constituting the beams

(iii) Vacuum birefringence

Our theoretical approach:

Idea: Interpret vacuum birefringence as **vacuum emission process**:

[FK, Shaisultanov: Phys. Rev. D **91** 113002 (2015)]

- laser fields correspond to macroscopic electromagnetic fields
- taking this literally means not to resolve the individual photons constituting the beams

↔ vacuum in the presence of **pump** and **probe** beams = $|0\rangle$

- the signal of quantum vacuum nonlinearity is encoded in (single) photons = $|\gamma_{(p)}(\vec{k})\rangle$ emitted from the strong field region

→ amplitude: $\mathcal{S}_{(p)}(\vec{k}) = \langle \gamma_p(\vec{k}) | \int_x a_\mu(x) j^\mu(x) | 0 \rangle.$

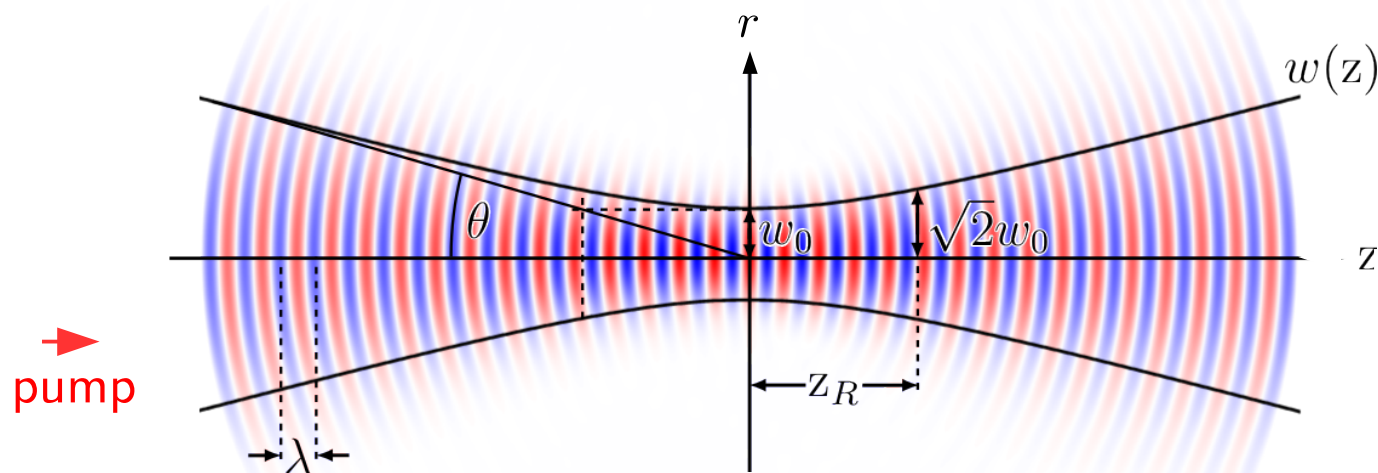
(iii) Vacuum birefringence

Our theoretical approach:

Idea: Interpret vacuum birefringence as **vacuum emission process**:

[FK, Shaisultanov: Phys. Rev. D **91** 113002 (2015)]

→ amplitude: $\mathcal{S}_{(p)}(\vec{k}) = \langle \gamma_p(\vec{k}) | \int_x a_\mu(x) j^\mu(x) | 0 \rangle.$



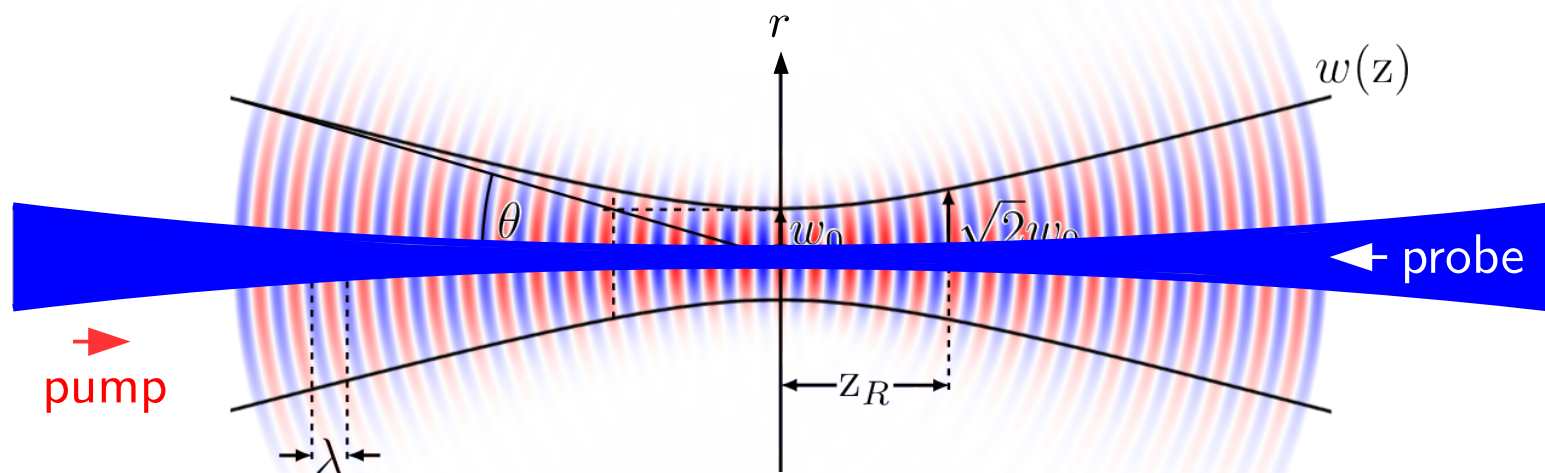
(iii) Vacuum birefringence

Our theoretical approach:

Idea: Interpret vacuum birefringence as **vacuum emission process**:

[FK, Shaisultanov: Phys. Rev. D **91** 113002 (2015)]

→ amplitude: $\mathcal{S}_{(p)}(\vec{k}) = \langle \gamma_p(\vec{k}) | \int_x a_\mu(x) j^\mu(x) | 0 \rangle.$



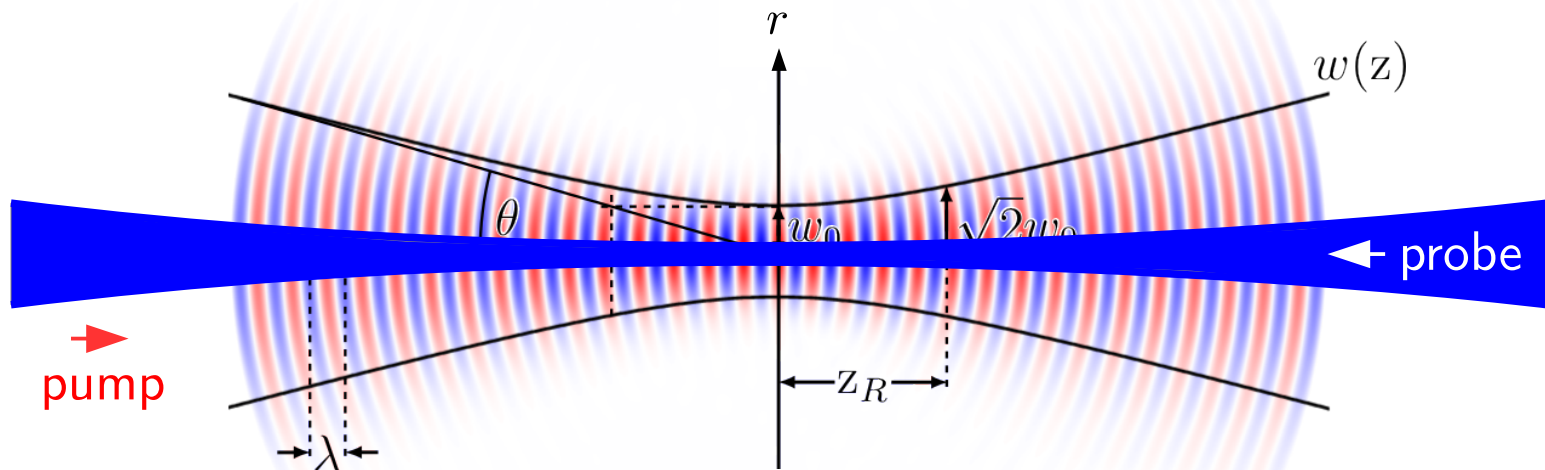
(iii) Vacuum birefringence

Our theoretical approach:

Idea: Interpret vacuum birefringence as **vacuum emission process**:

[FK, Shaisultanov: Phys. Rev. D **91** 113002 (2015)]

→ amplitude: $\mathcal{S}_{(p)}(\vec{k}) = \langle \gamma_p(\vec{k}) | \int_x a_\mu(x) j^\mu(x) | 0 \rangle.$



$$j^\mu(x) = \int_{x'} \Pi^{\mu\nu}(x, x' | \mathcal{A}) A_\nu(x')$$

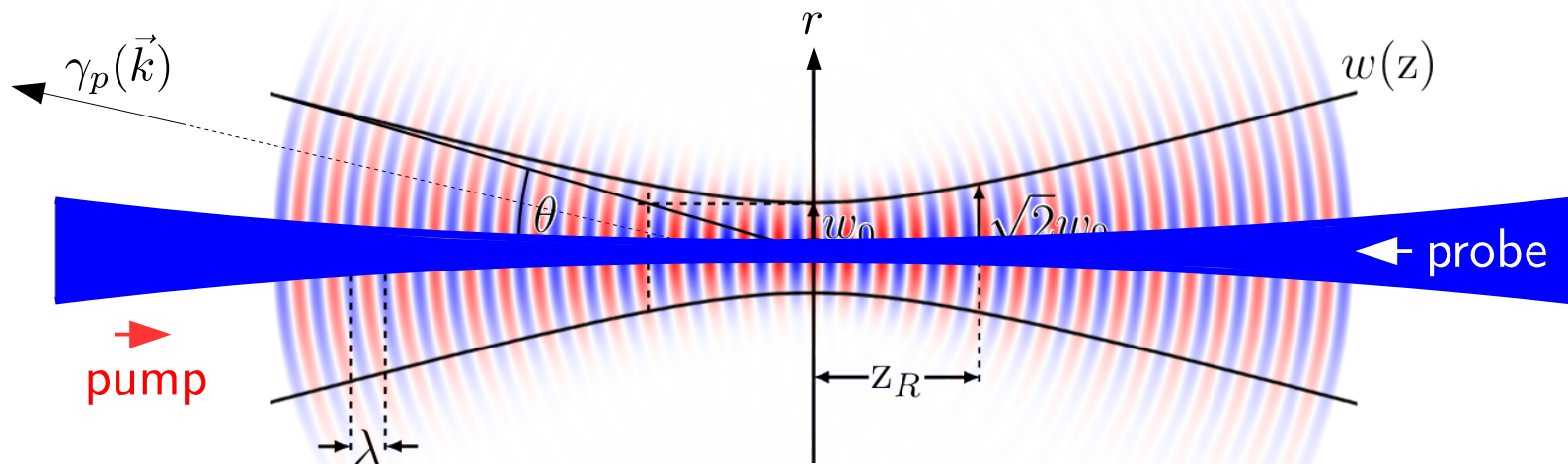
(iii) Vacuum birefringence

Our theoretical approach:

Idea: Interpret vacuum birefringence as **vacuum emission process**:

[FK, Shaisultanov: Phys. Rev. D **91** 113002 (2015)]

→ amplitude: $\mathcal{S}_{(p)}(\vec{k}) = \langle \gamma_p(\vec{k}) | \int_x a_\mu(x) j^\mu(x) | 0 \rangle.$



$$j^\mu(x) = \int_{x'} \Pi^{\mu\nu}(x, x' | \mathcal{A}) A_\nu(x')$$

(iii) Vacuum birefringence

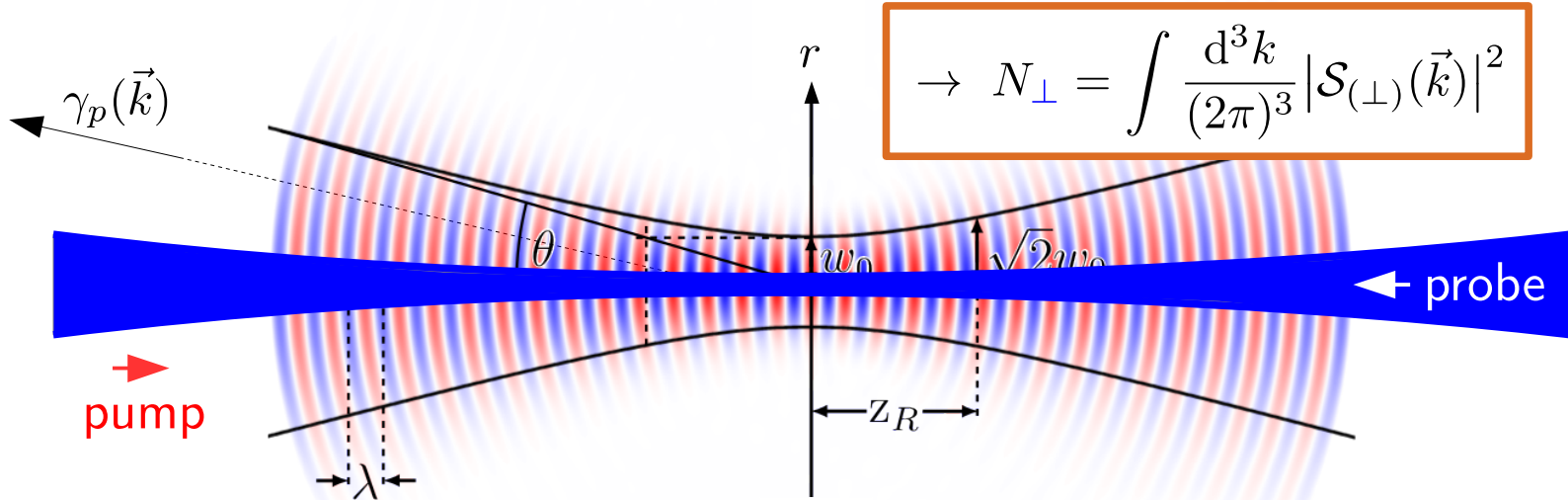
Our theoretical approach:

Idea: Interpret vacuum birefringence as **vacuum emission process**:

[FK, Shaisultanov: Phys. Rev. D **91** 113002 (2015)]

→ amplitude: $\mathcal{S}_{(p)}(\vec{k}) = \langle \gamma_p(\vec{k}) | \int_x a_\mu(x) j^\mu(x) | 0 \rangle.$

$$\rightarrow N_{\perp} = \int \frac{d^3k}{(2\pi)^3} |\mathcal{S}_{(\perp)}(\vec{k})|^2$$



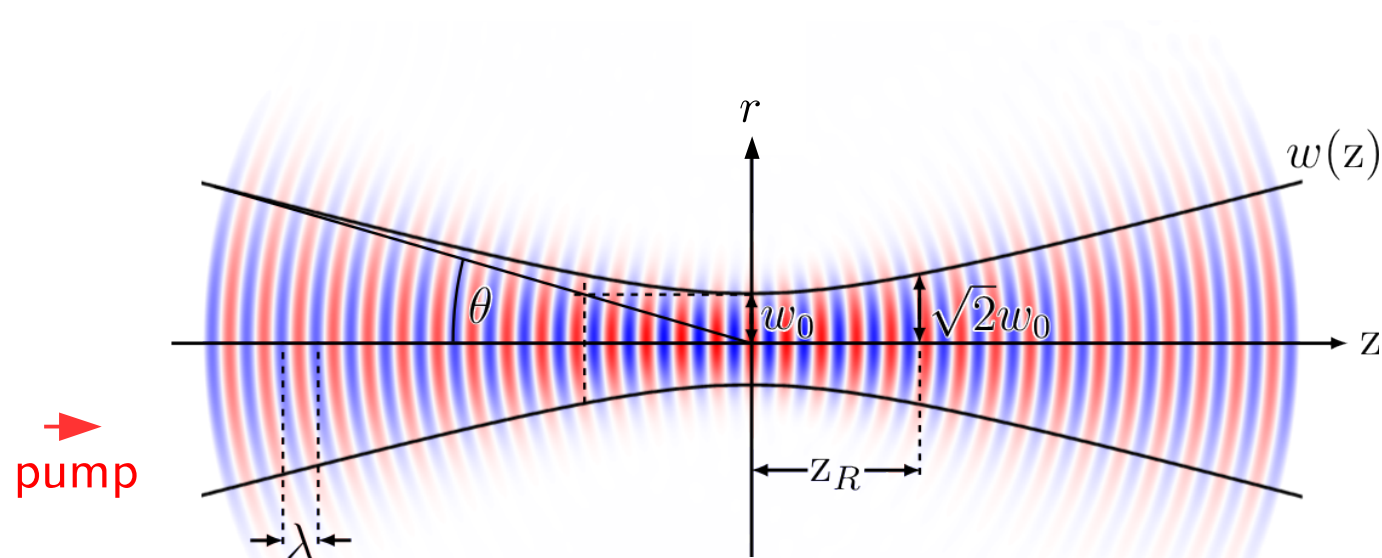
$$j^\mu(x) = \int_{x'} \Pi^{\mu\nu}(x, x' | \mathcal{A}) A_\nu(x')$$

(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases



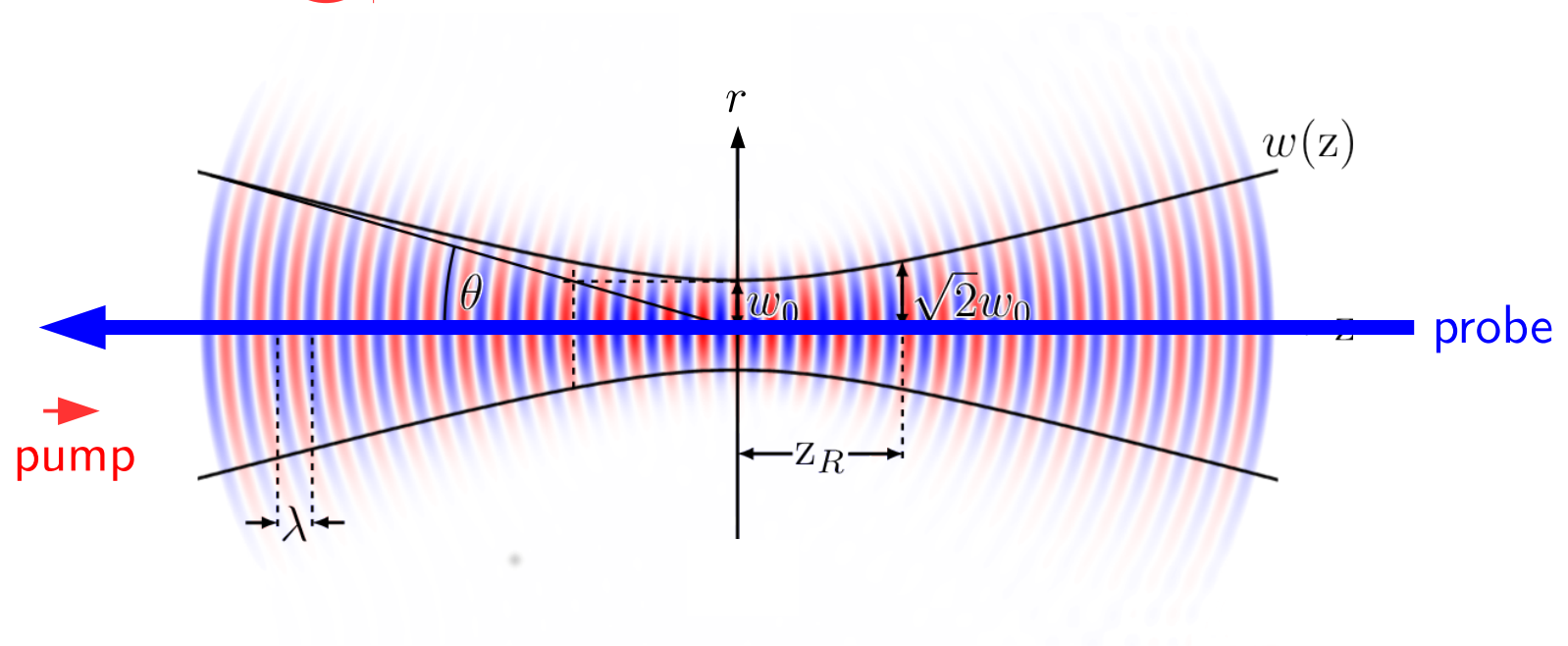
(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (a): 

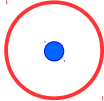


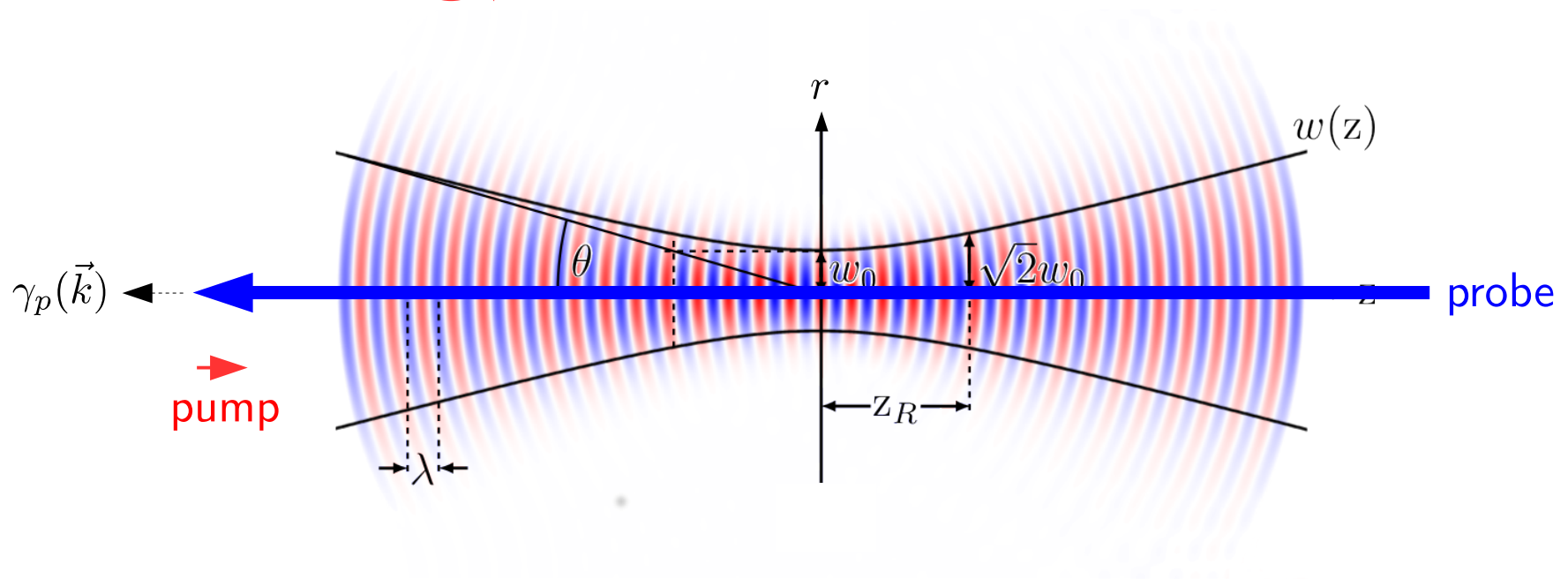
(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (a): 

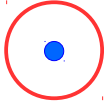


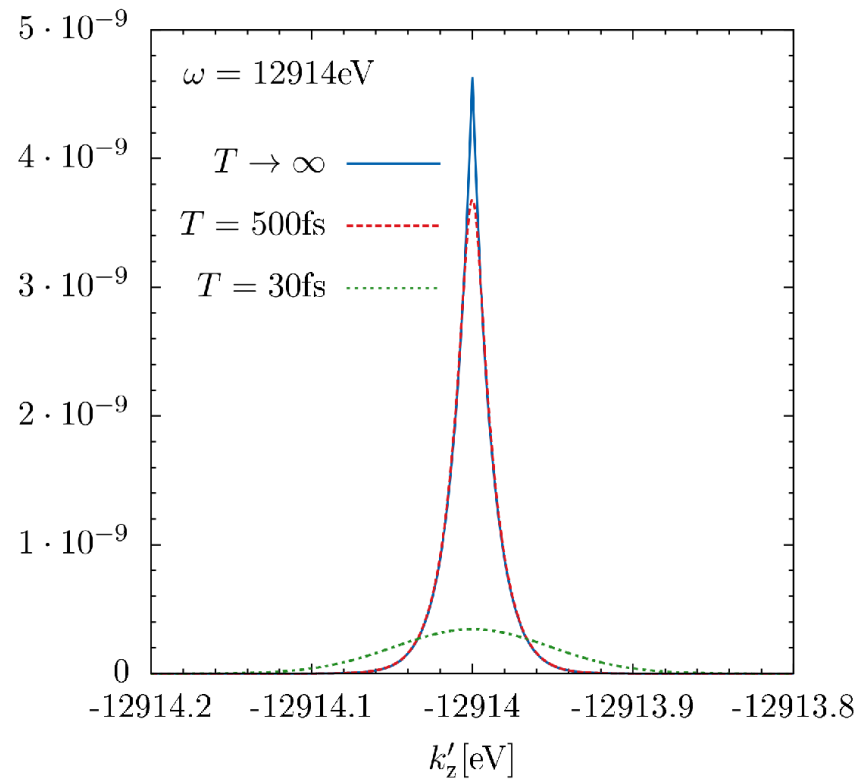
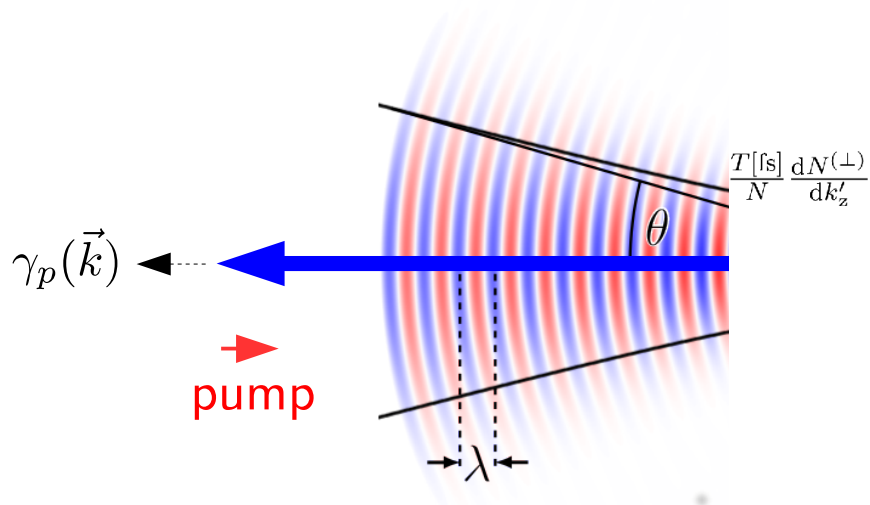
(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (a): 

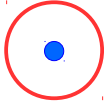


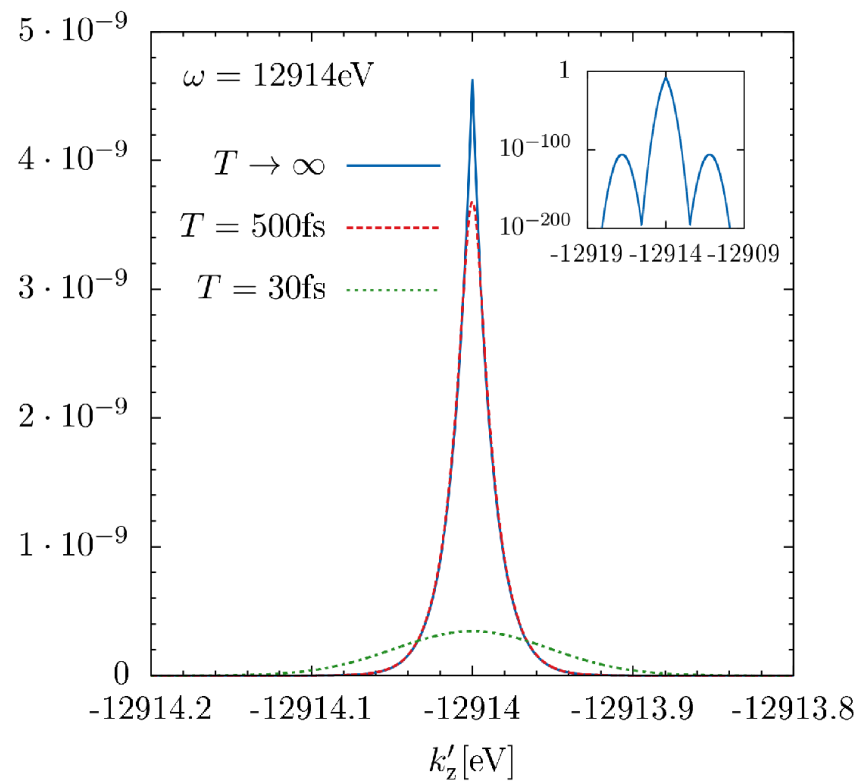
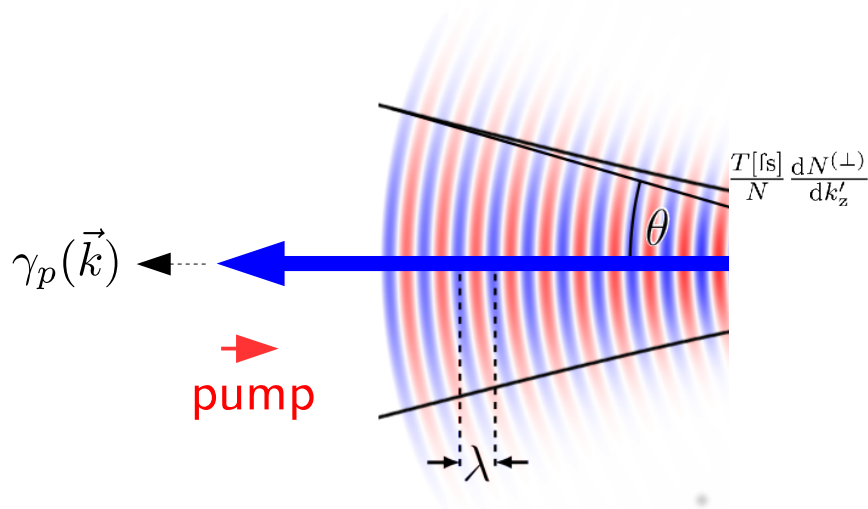
(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (a): 

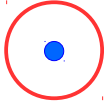


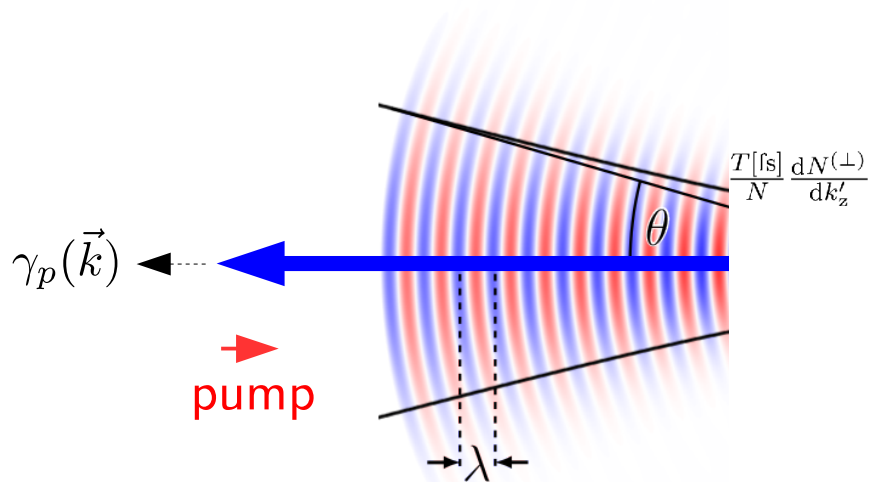
(iii) Vacuum birefringence

Our **results**:

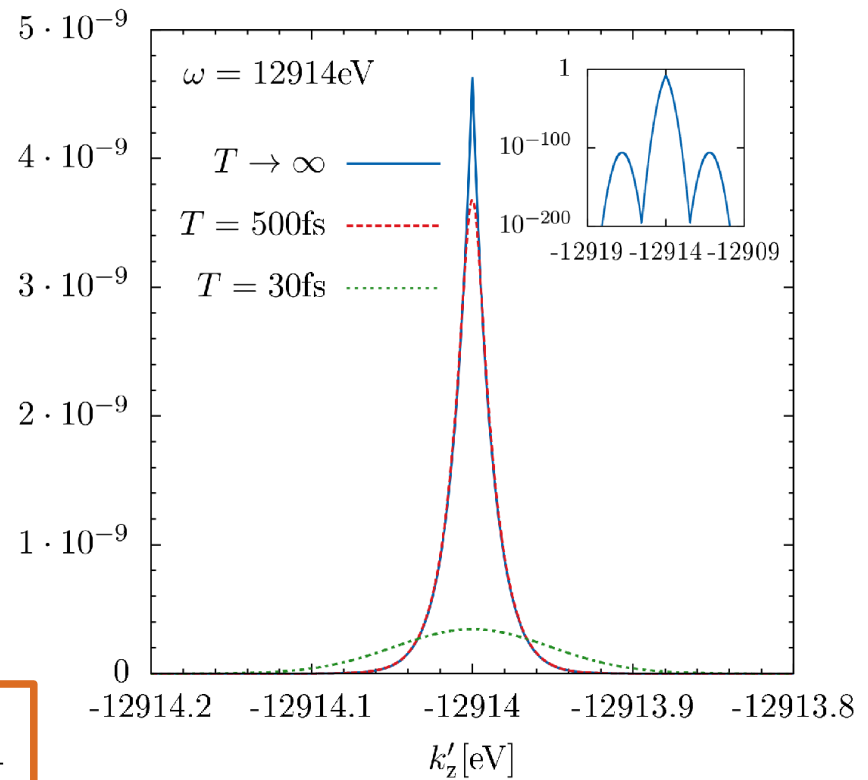
[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (a): 



$$\left. \frac{N_{\perp}}{N_{\text{in}}} \right|_{T=30\text{fs}} = 1.39 \cdot 10^{-12} \approx \frac{\mathcal{P}}{410}$$

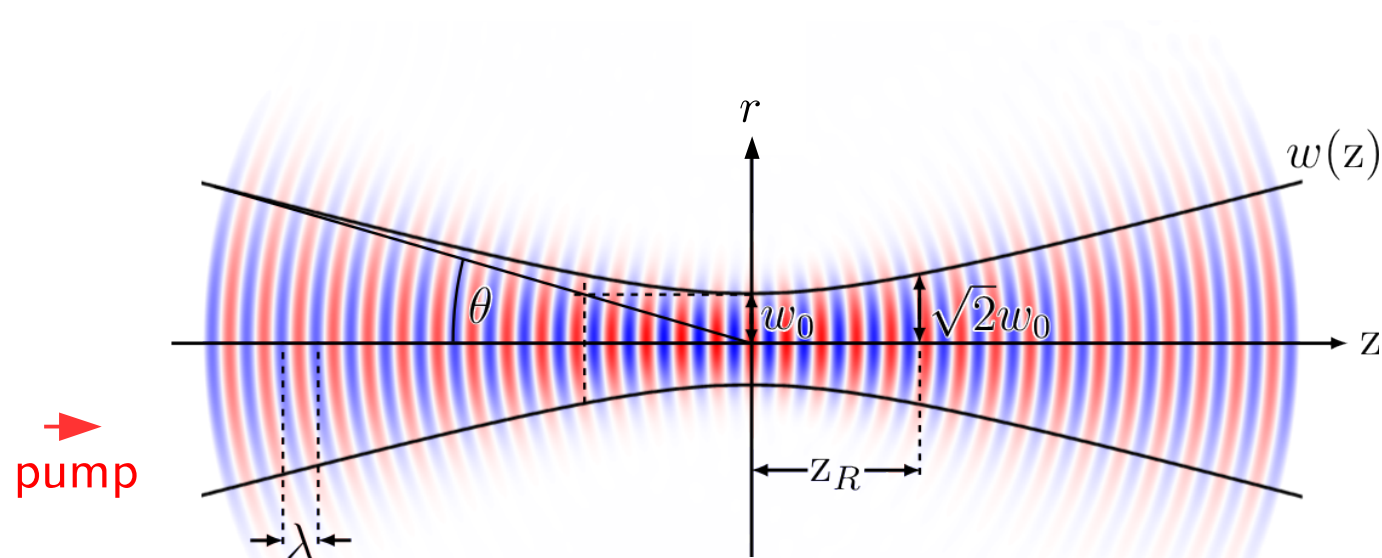


(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases



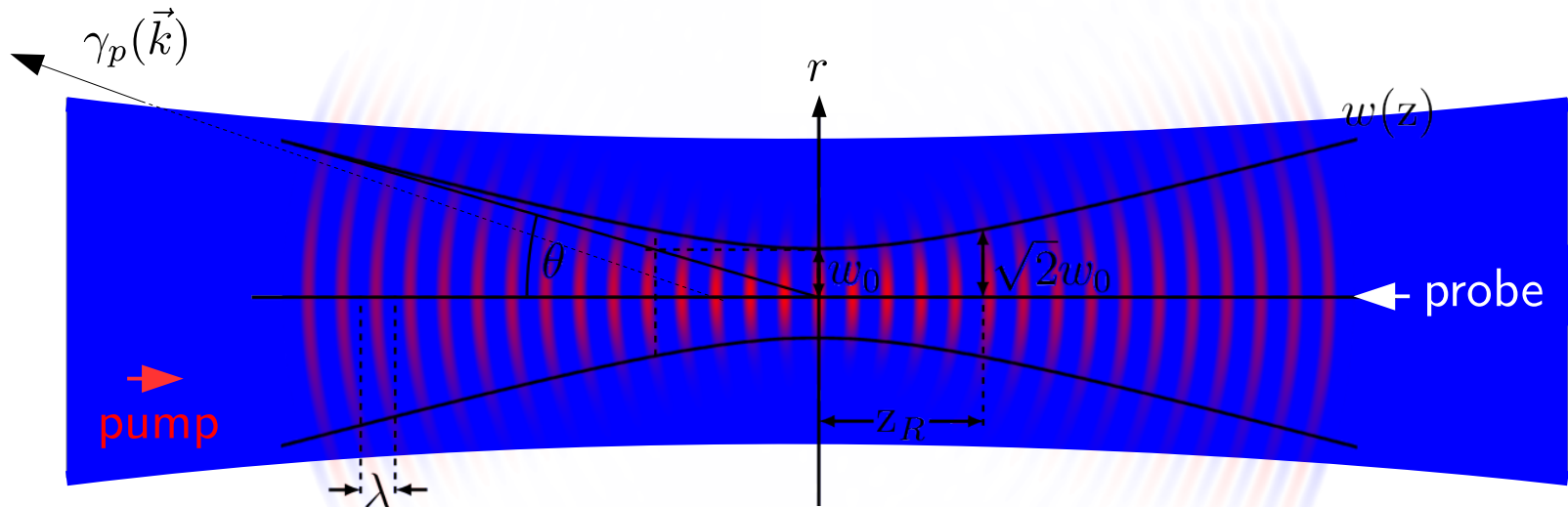
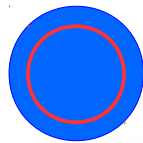
(iii) Vacuum birefringence

Our results:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (b):

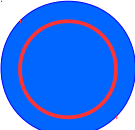
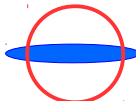


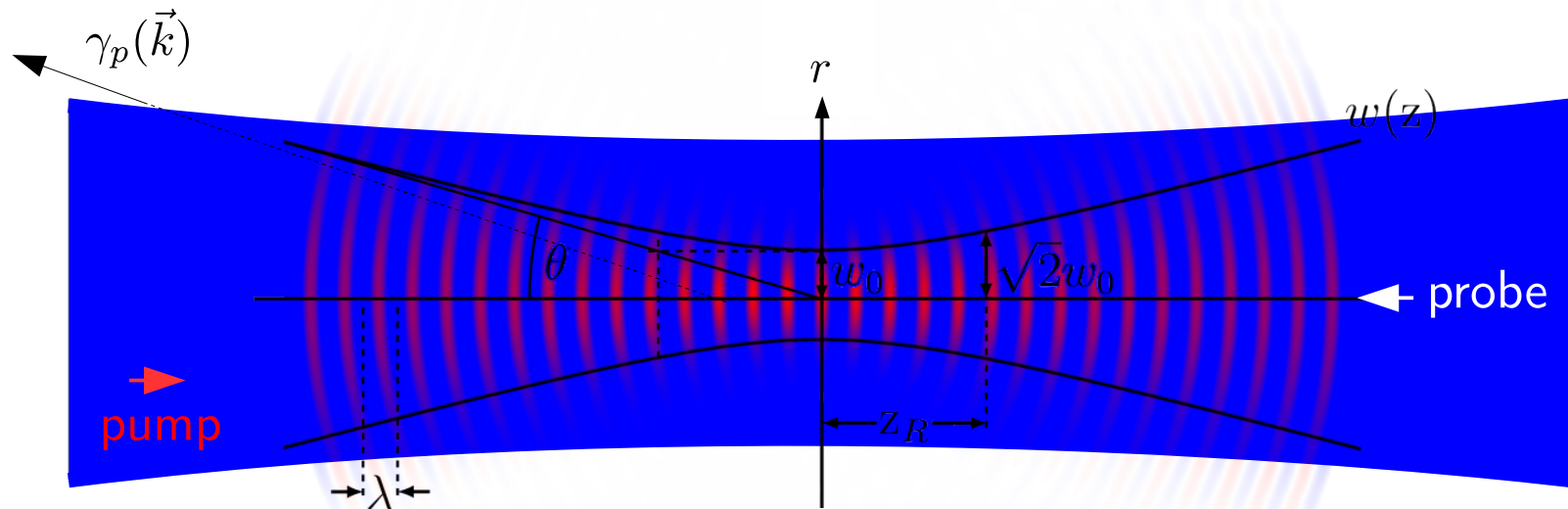
(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (b):  and case (c): 

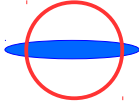


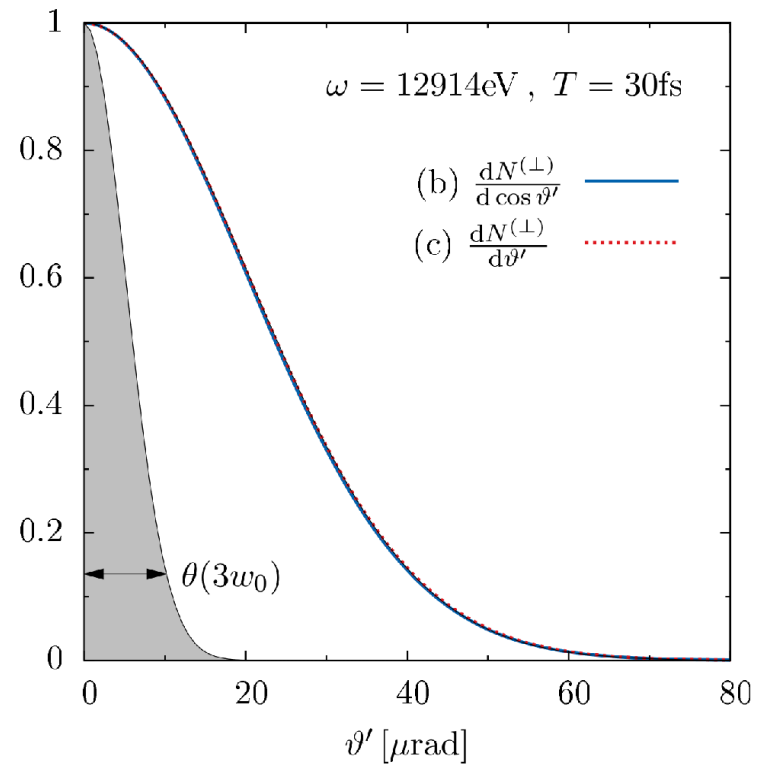
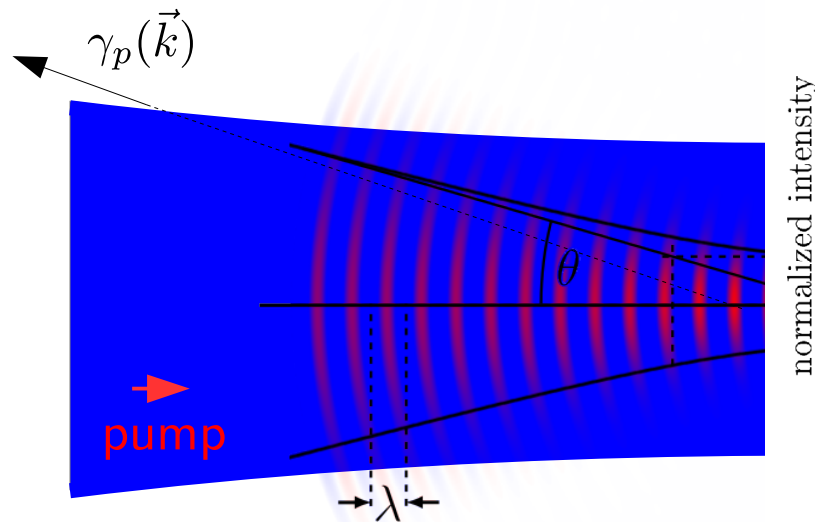
(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (c): 

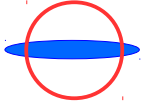


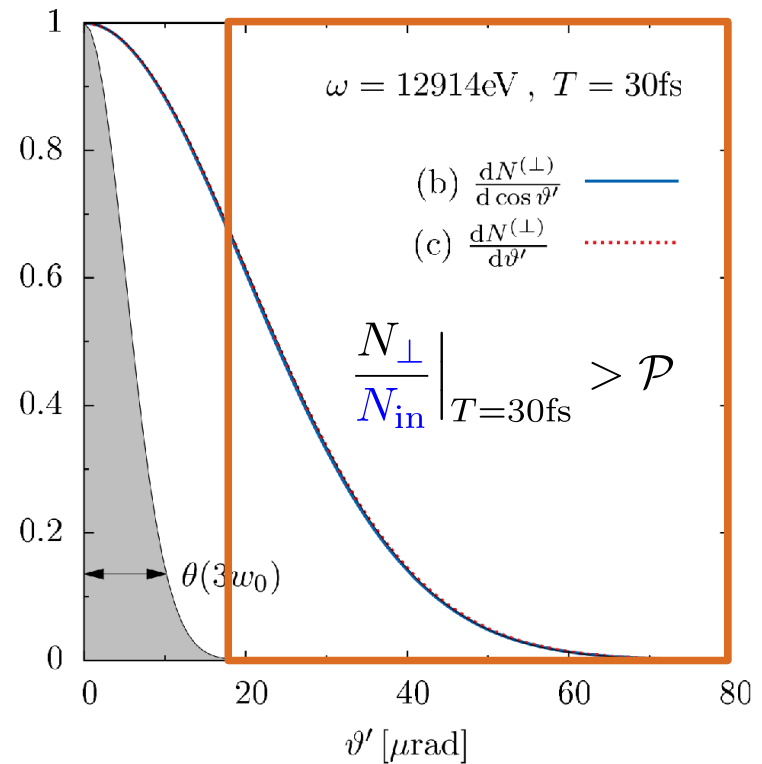
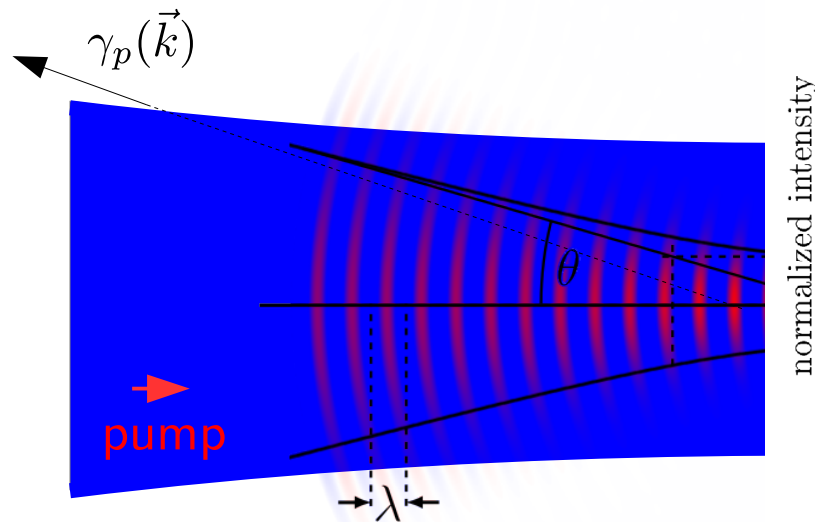
(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (c): 

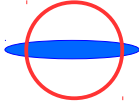


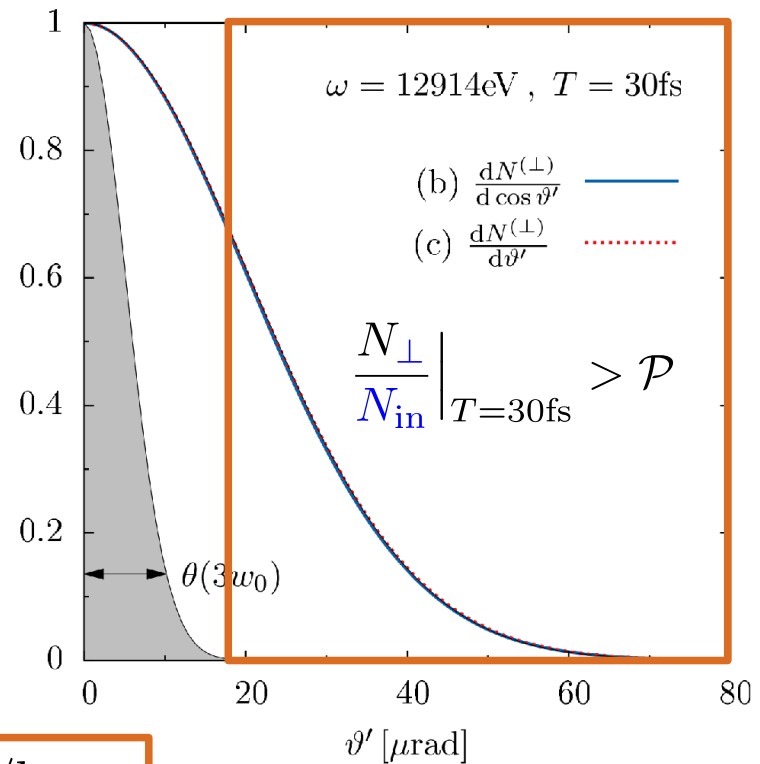
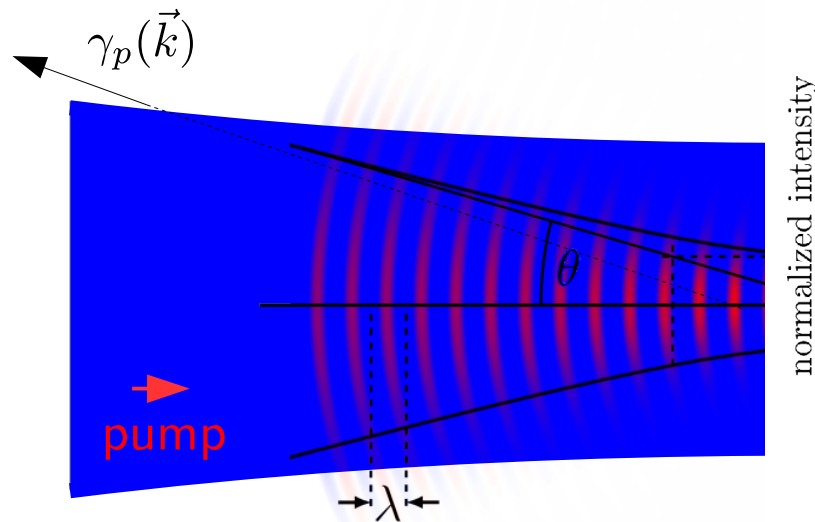
(iii) Vacuum birefringence

Our **results**:

[FK, et al.: in preparation 2015]

- we consider three different cases

→ case (c): 



→ repetition rate 1Hz : $N_{\perp} \approx 265/\text{hour}$

(iv) Conclusions and Outlook

(iv) Conclusions

- I focused on **all-optical probes** of quantum vacuum nonlinearity.
- I presented and advocated a different perspective to analyze optical signatures of **quantum vacuum nonlinearities**.
- I exemplarily discussed **vacuum birefringence**.

(iv) Conclusions & Outlook

- I focused on **all-optical probes** of quantum vacuum nonlinearity.
- I presented and advocated a different perspective to analyze optical signatures of **quantum vacuum nonlinearities**.
- I exemplarily discussed **vacuum birefringence**.
- Our approach can be straightforwardly generalized to the study of other (inhomogeneous) electromagnetic field profiles.
- It can be easily adopted to various other optical probes.

(iv) Conclusions & Outlook

- I focused on **all-optical probes** of quantum vacuum nonlinearity.
- I presented and advocated a different perspective to analyze optical signatures of **quantum vacuum nonlinearities**.
- I exemplarily discussed **vacuum birefringence**.
- Our approach can be straightforwardly generalized to the study of other (inhomogeneous) electromagnetic field profiles.
- It can be easily adopted to various other optical probes.

Thank you for your attention!