

Theoretical overview of charmonium evolutions in the hot medium

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Xiaojian Du, Jiaying Zhao, Wei Shi

Outline

1. Background:

Quark Gluon Plasma,
Parton inelastic scattering, medium color screening on HQ potential

2. Theoretical models:

Transport models, Coalescence model, potential models (Schrodinger et al)
Co-mover model, et al;

3. Topics:

- 1) **Pb-Pb: charm quark diffusion on Ψ (regeneration, collective flows)**
- 2) **p-Pb : final state interactions on Ψ**
- 3) **Transitions between charmonia by in-medium potential**
- 4) **photoproduction V.S. hadroproduction in semi-central collisions with QGP**
$$\gamma + A \rightarrow J/\psi + A$$

4. Summary

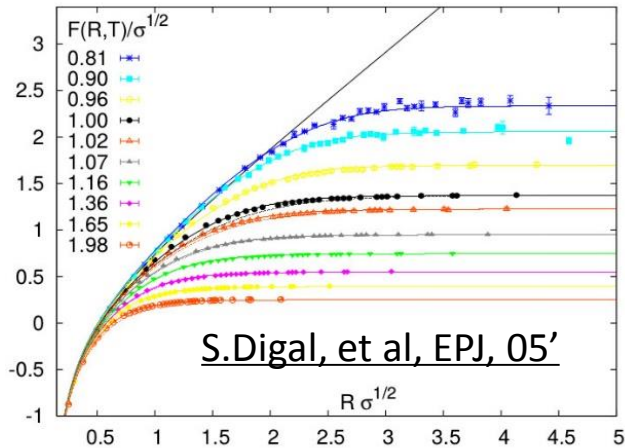
background

J/ψ as a probe of QGP:

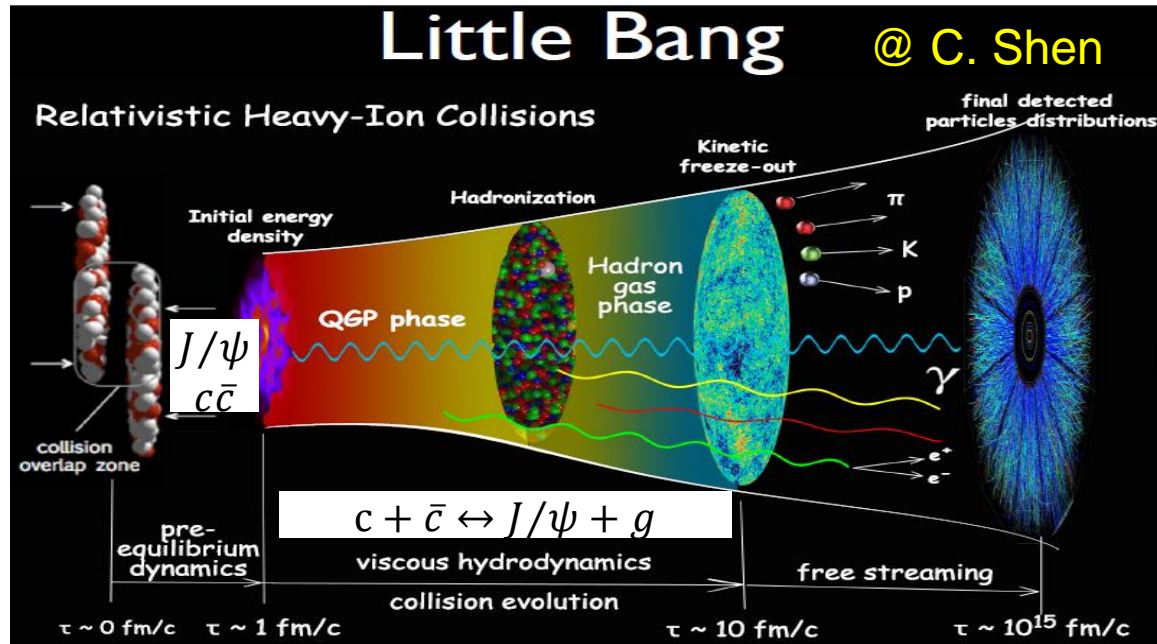
J/ψ suffer color screening end inelastic collisions of partons in QGP

$$R_{AA}^{J/\psi} = \frac{N_{AA}^{J/\psi}}{N_{pp}^{J/\psi} N_{coll}}$$

QGP: color screening on HQ potential; parton scatterings



Heavy quark potential is screened



$V_{c\bar{c}} = U$
Satz, et al

State	$J/\psi(1S)$	$\chi_c(1P)$	$\psi'(2S)$
T_d/T_c	2.10	1.16	1.12

dissociation
temperature

background

J/ψ as a probe of QGP:

J/ψ suffer color screening end inelastic collisions of partons in QGP

NT, J/ψ

The image is a screenshot of a news article on the Nature website. The article is titled "Early Universe was a liquid" and is categorized under "News". The sub-headline is "Quark-gluon blob surprises particle physicists." by Mark Peplow. The article text states that the universe was a perfect liquid in its first moments, based on results from an atom-smashing experiment at RHIC. It mentions that scientists at RHIC have spent five years searching for quark-gluon plasma, which is thought to have filled the universe in the first microseconds. The article concludes that scientists are now convinced they have found it, but it seems to be a liquid rather than the expected hot gas. There is a small image of a "Liquid state" showing a cluster of colorful particles. The article is published online on 19 April 2005. The Nature logo and navigation menu are visible at the top. On the left, there are links for "Comments on this story", "Stories by subject" (Physics, Space and astronomy), and "This article elsewhere" (Blogs linking to this article, Add to Digg, Add to Facebook, Add to Newsvine, Add to Del.icio.us, Add to Twitter). On the right, there are sections for "Related stories" (What's in a name?, Quark soup goes on the menu) and "Naturejobs" (Professor and Faculty Positions at the Academy of Medical Sciences (AMS), Zhengzhou University; Principal Investigator at IDG / McGovern Institute for Brain Research at Peking University).

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[comments on this story](#) Published online 19 April 2005 | Nature | doi:10.1038/news050418-5

News

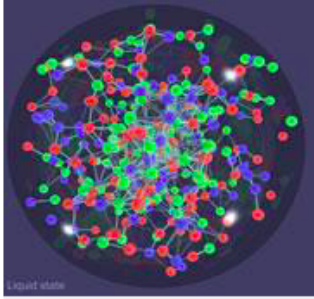
Early Universe was a liquid

Quark-gluon blob surprises particle physicists.

Mark Peplow

The Universe consisted of a perfect liquid in its first moments, according to results from an atom-smashing experiment.

Scientists at the Relativistic Heavy Ion Collider (RHIC) at Brookhaven National Laboratory on Long Island, New York, have spent five years searching for the quark-gluon plasma that is thought to have filled our Universe in the first microseconds of its existence. Most of them are now convinced they have found it. But, strangely, it seems to be a liquid rather than the expected hot gas.



Liquid state

Quarks and gluons have formed a unexpected liquid. [Click here](#) to see animation. © RHIC/BN

Related stories

- [What's in a name?](#)
28 July 2004
- [Quark soup goes on the menu](#)
15 February 2000

Naturejobs

[Professor and Faculty Positions at the Academy of Medical Sciences \(AMS\), Zhengzhou University](#)
The Academy of Medical Sciences of Zhengzhou University

[Principal Investigator at IDG / McGovern Institute for Brain Research at Peking University](#)
Peking University (PKU)

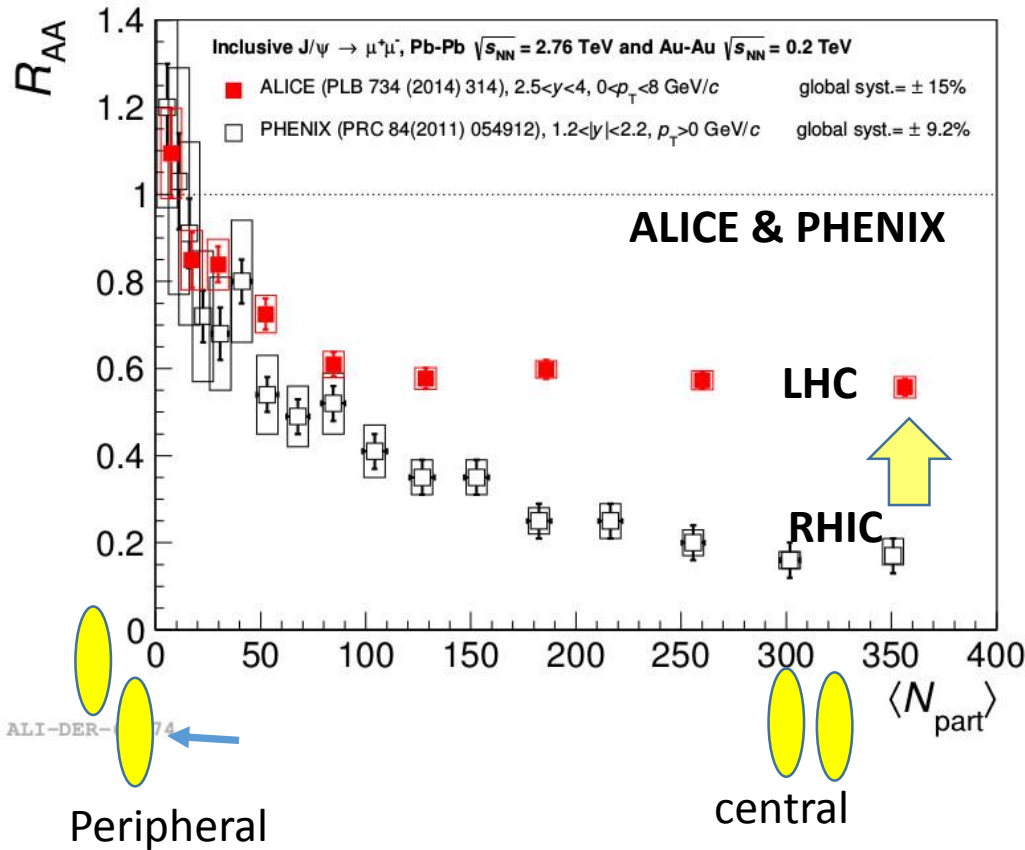
- [More science jobs](#)
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Regeneration + suppression

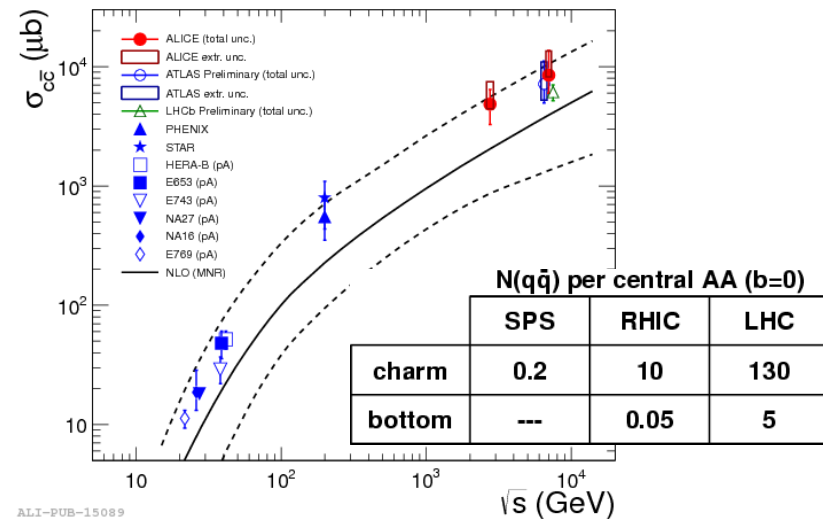
- J/ψ yield enhanced by **regeneration** in experiments at LHC



Throws, Schroedter, Rafelski,
Andronic, Braun-Munzinger,
Rapp, Zhao, Du (TAMU)
Zhuang, Liu, Zhou, BC (Tsinghua)



$$R_{AA} = \frac{N_{AA}^{initial} + N_{AA}^{rege}}{N_{pp*ncoll}^{J/\psi}}$$

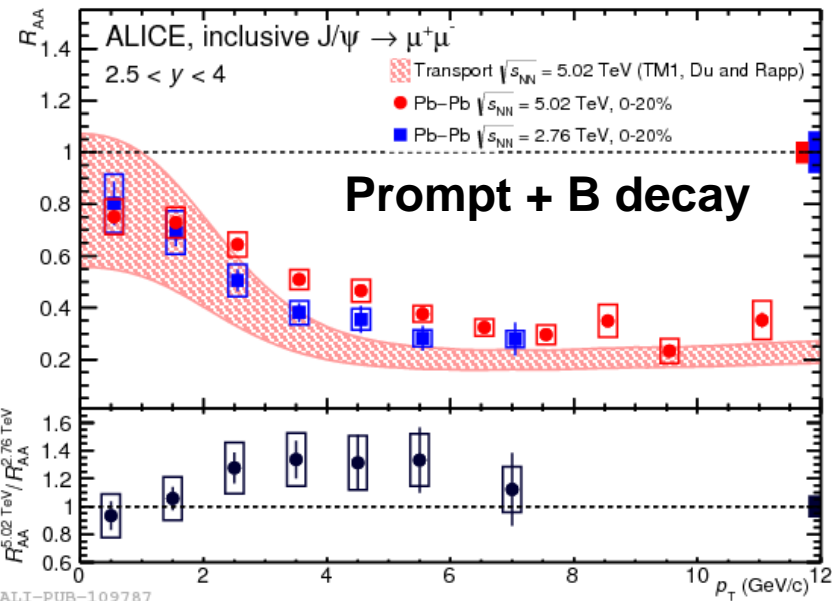


- **Large number of charm pairs enhance the regeneration**

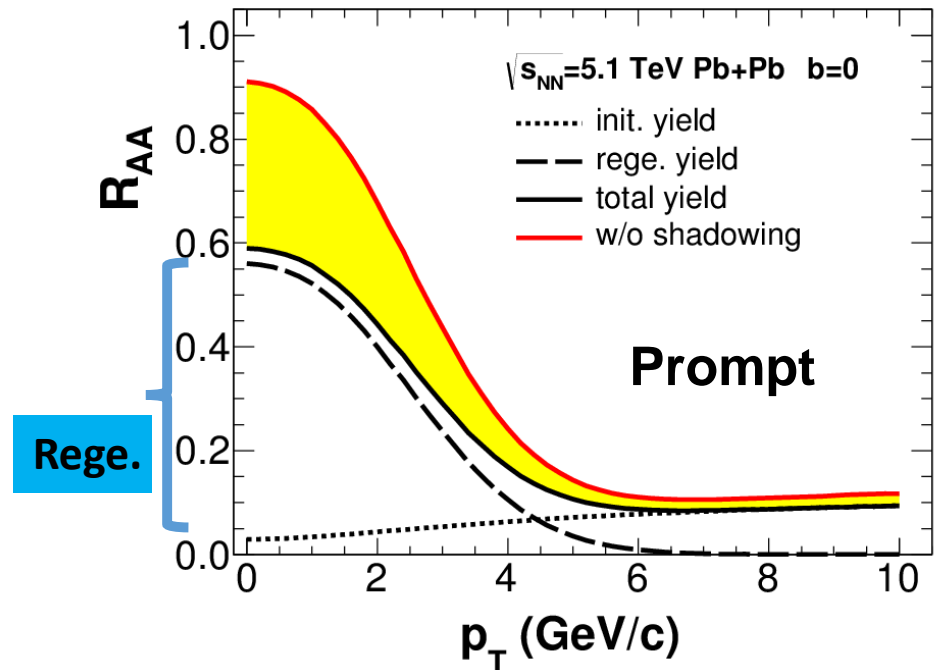
p_T dependence

p_T -
dependence

Primordial production V.S. regeneration



Rapp, Du, TAMU Transport



Zhuang, BC, Tsinghua Transport

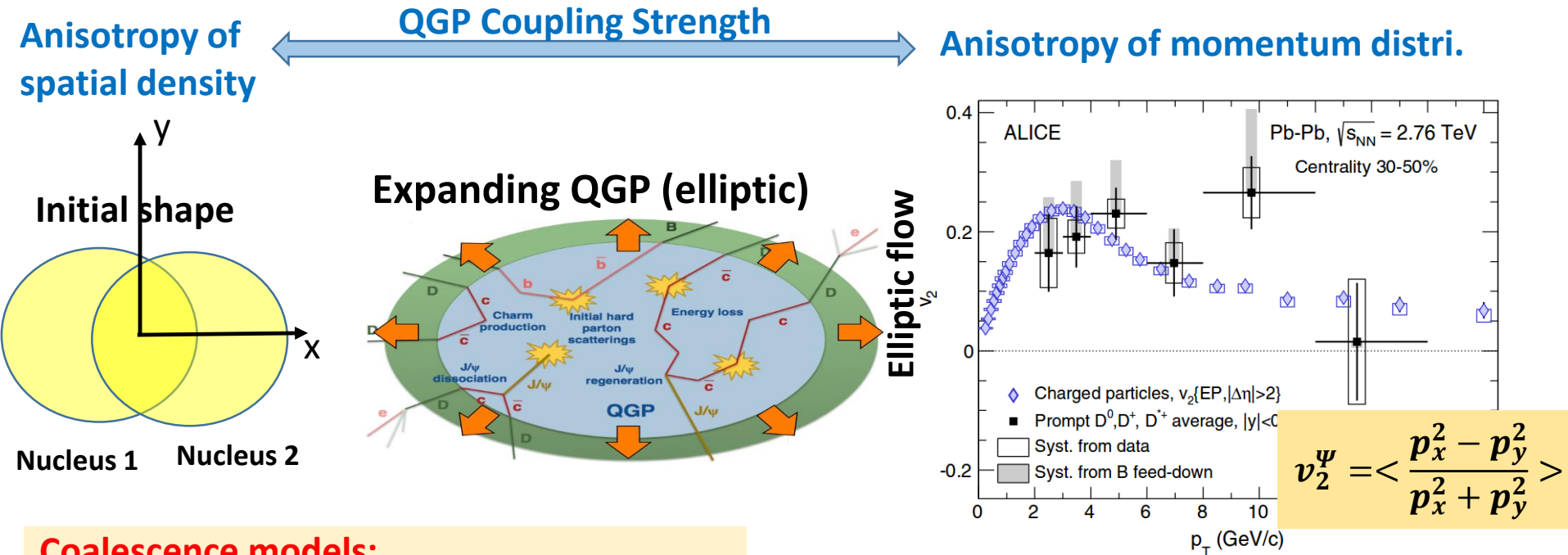
$$p_T^{charm} \sim 2T_{QGP} \sim 0.5 \text{ GeV}/c$$

Regenerated J/ψ from uncorrelated c and \bar{c} :
 charm suffer energy loss in QGP $\rightarrow J/\psi$ in LOW p_T

QGP expansion \rightarrow charm \rightarrow rege. Ψ

- At LHC energies of Pb-Pb, more than 90% of total J/ψ are from $c + \bar{c} \leftrightarrow J/\psi + g$

Hidden charm ($J/\psi, \psi(2S)$) open charm (D mesons)
are closely connected with



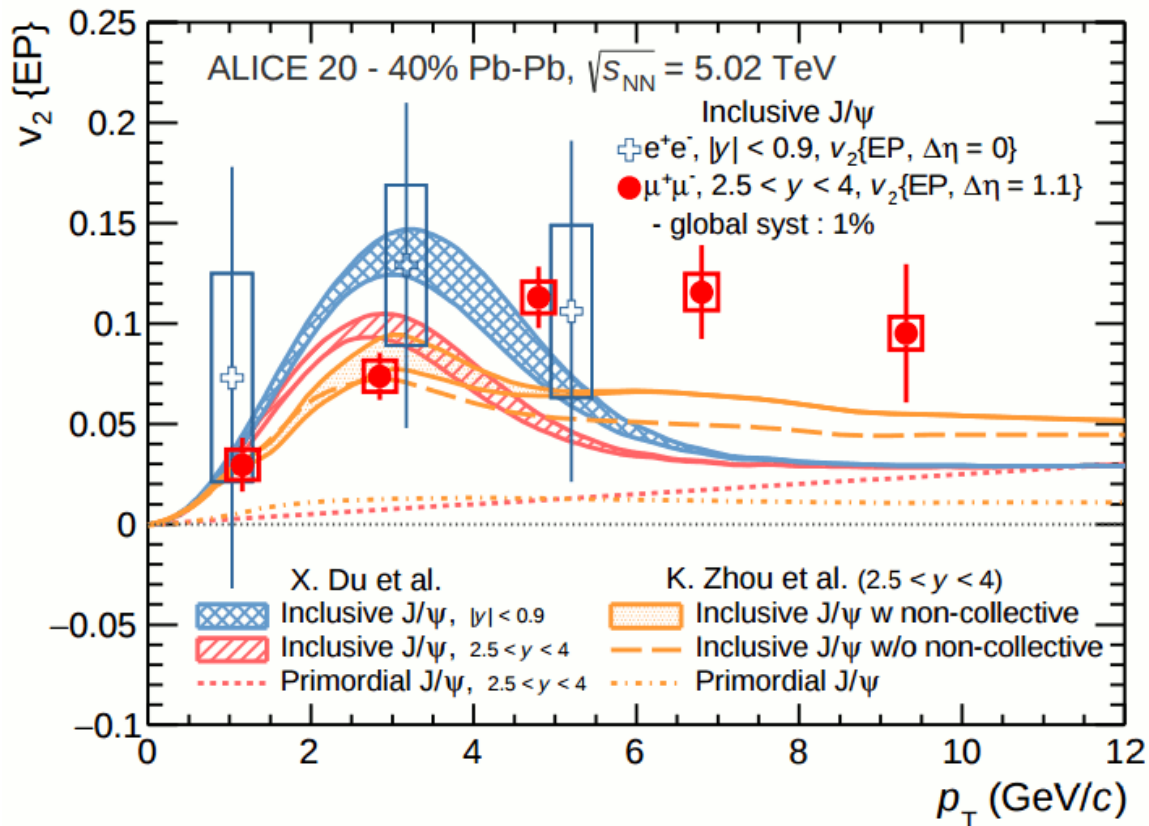
Coalescence models:

Che-ming Ko, Rapp, R.J. Fries, V. Greco, P. Sorensen, Thews, Schroedter, Rafelski, Andronic, Braun-Munzinger, et al

D meson elliptic flow, charm momentum thermalized ?
PRL, 111, 102301(2013)

QGP expansion \rightarrow charm \rightarrow rege. Ψ

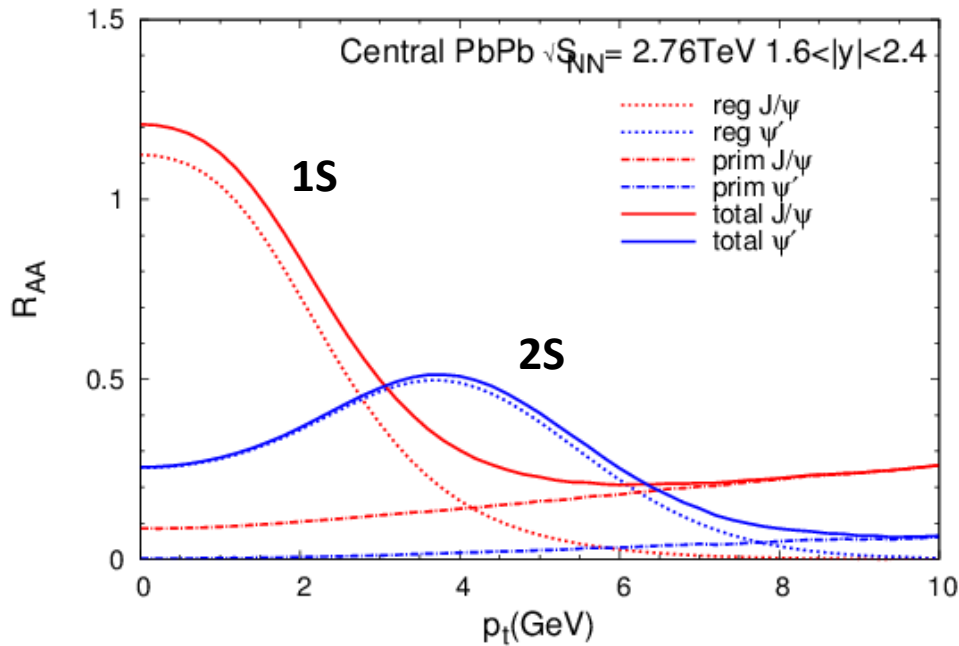
- ✓ Charm diffusion (thermalization) results in **large v_2^Ψ**



arXiv: 1711.03369

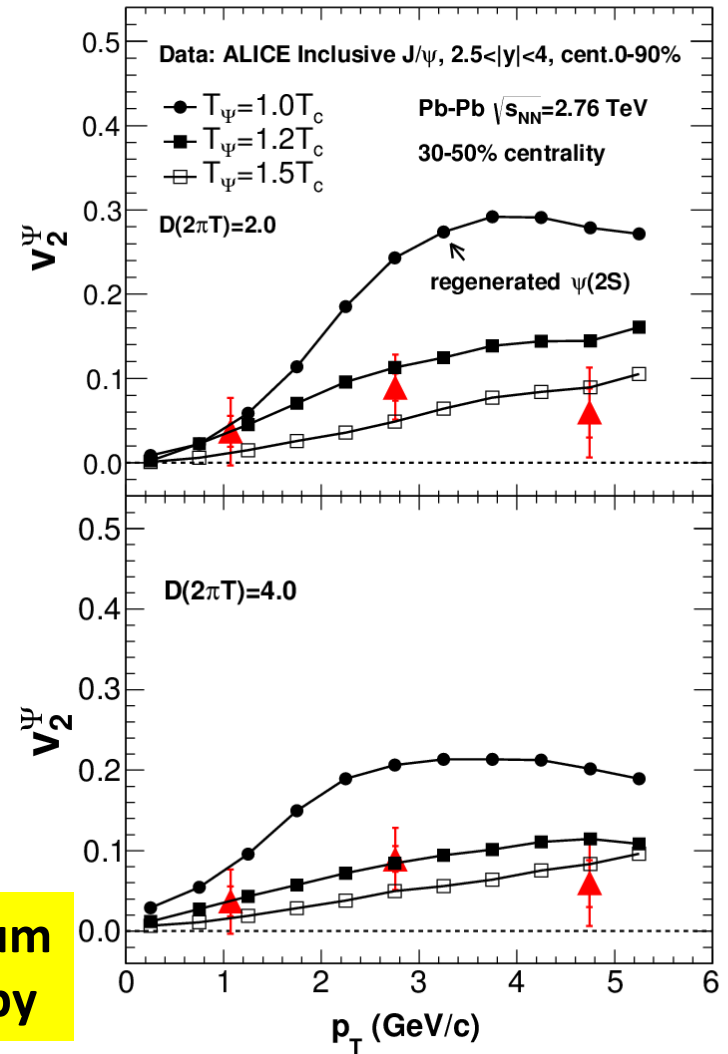
QGP expansion \rightarrow charm \rightarrow rege. Ψ

- ✓ Charm diffusion (thermalization) results in **large v_2^Ψ**
- ✓ Charm diffusions affect 1S and 2S



Du, Rapp, NPA 2015

Momentum anisotropy
 v_2 of 1S and 2S



BC, PRC 2017

$\psi(2S)$ physics

expected to be more interesting than J/ψ

$\psi(2S)$ with B meson decay

In AA collisions:

Ψ inclusive yield = initial + regenerated + B-meson decay

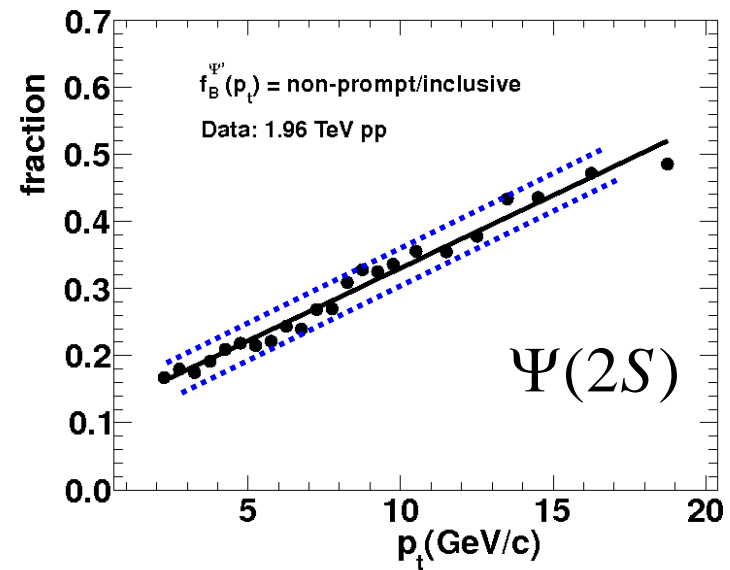
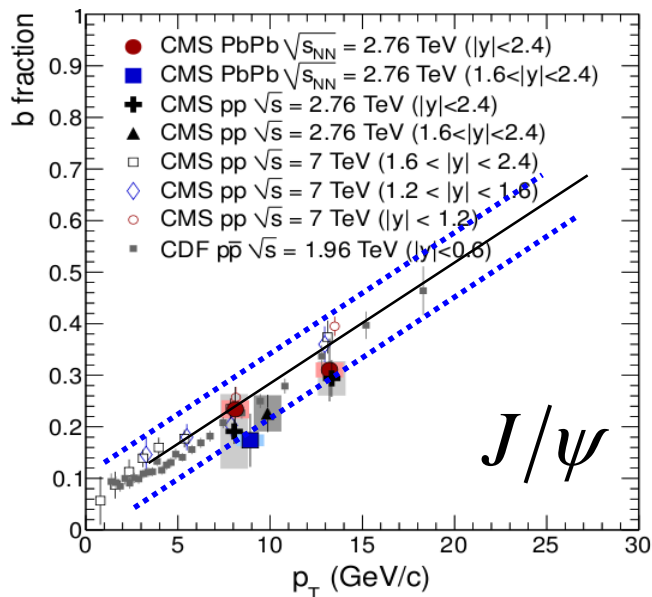
bottom quark energy loss

In pp collisions:

~ 10% of inclusive 1S are from B-decay

~ 15% of inclusive 2S are from B-decay

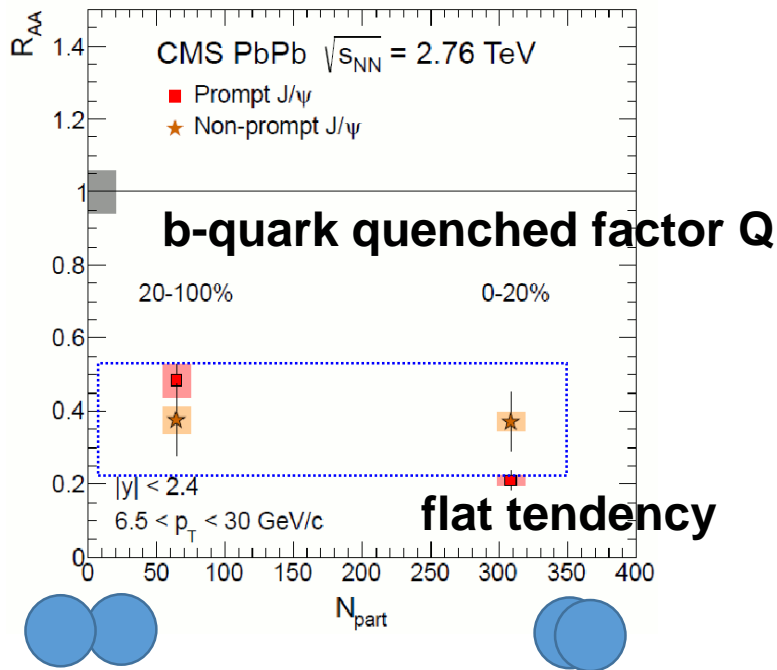
Very different from AA collisions (with QGP production).



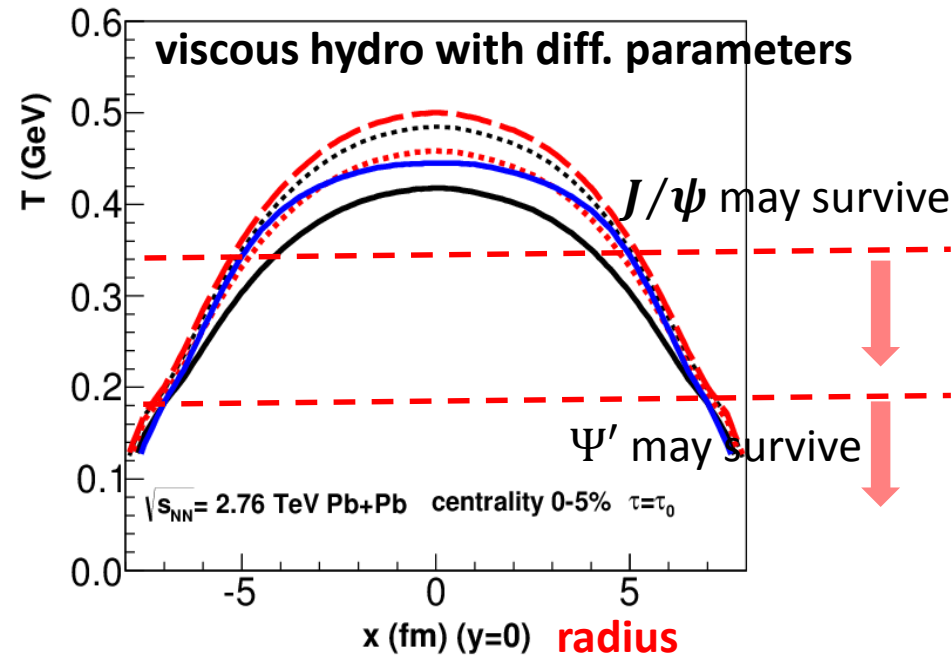
non-prompt fraction in pp collisions

$\psi(2S)$ with B meson decay

B-decay part



Prompt part

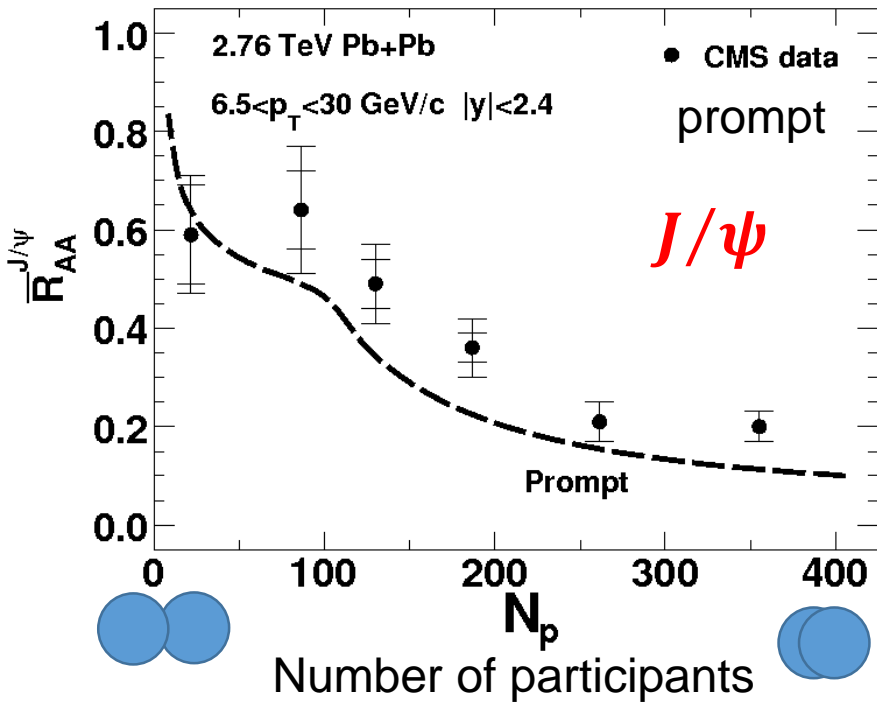


Bottom quark energy loss
Show weak N_p -dependence

Dissociation temperature	State	J/ ψ (1S)	χ_c (1P)	ψ' (2S)
T_d/T_c		2.10	1.16	1.12

● Based on sequential suppression,
Our calculated **ratio is around**
 ~ 0.2 for prompt 2S/1S

$\psi(2S)$ with B meson decay



With B-decay contribution, double ratio increase with centrality.

$$\frac{R_{AA}^{\psi'}}{R_{AA}^{J/\psi}} = \frac{R_{AA}^{\psi'}(N_p) + R_{AA}^{B \rightarrow \psi'} \text{ Const.}}{R_{AA}^{J/\psi}(N_p) + R_{AA}^{B \rightarrow J/\psi}}$$

inclusive
decrease

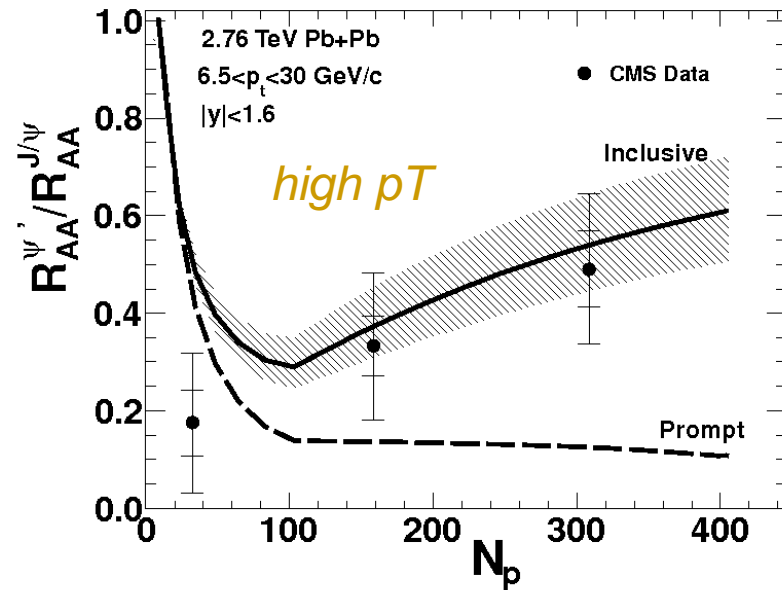
For high p_T , no regeneration

With $V=U$
(satz. et al)

$$\frac{T_d^{J/\psi}}{T_c} \approx 2.1$$

$$\frac{T_d^{\psi'}}{T_c} \approx 1.1$$

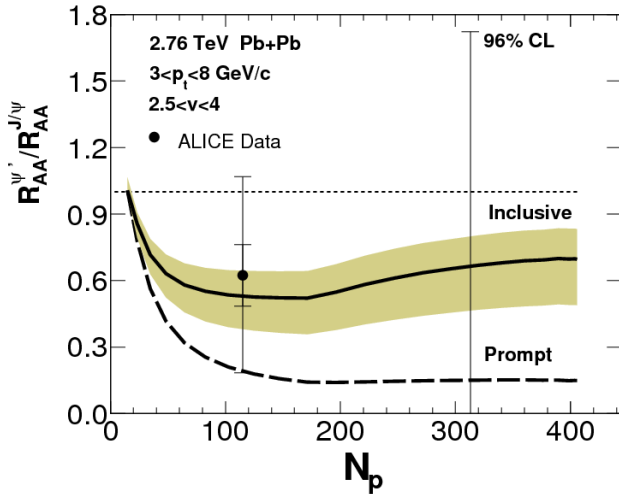
- For inclusive J/psi, ~30% from B decay
- For inclusive Psi(2s), ~90% from B decay



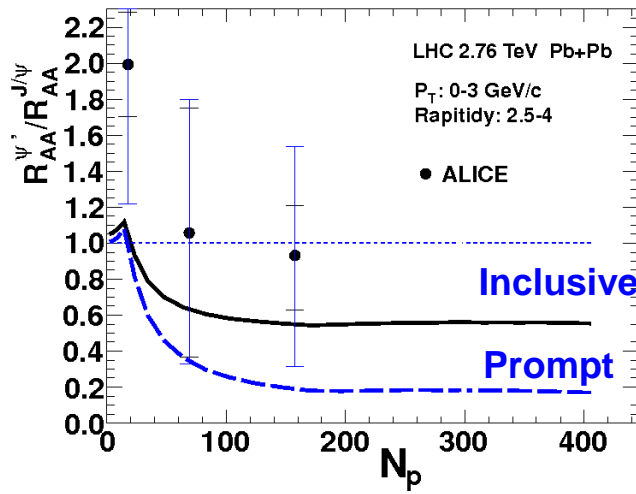
BC, Zhuang, et al, PLB 2013

$\psi(2S)$ with B meson decay

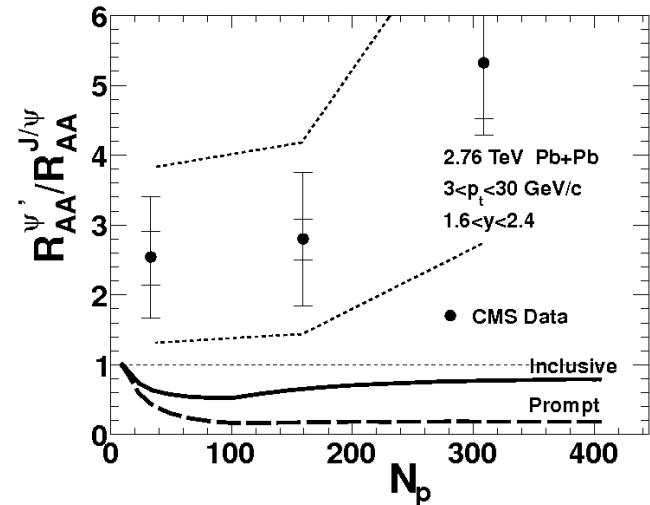
middle pT



Low pT



Inclusive yield



We still can not explain $2S > 1S$,

[*BC, Zhuang, et al, PLB726, 725-728 2013*](#)

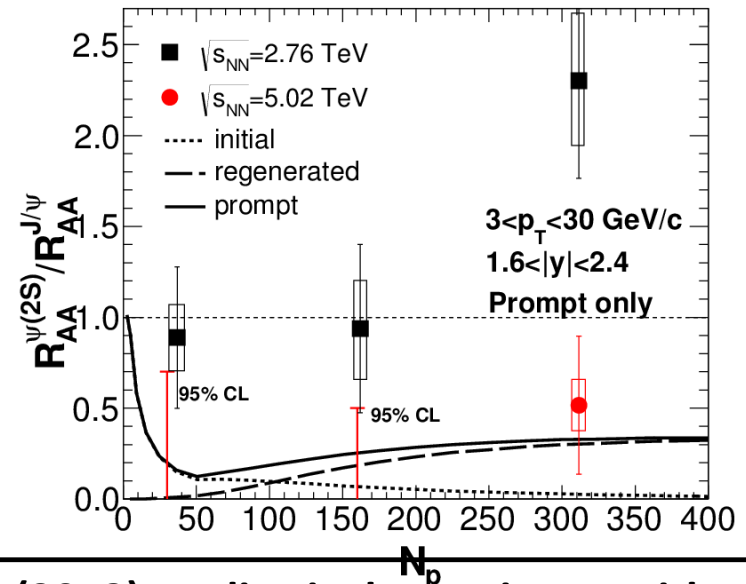
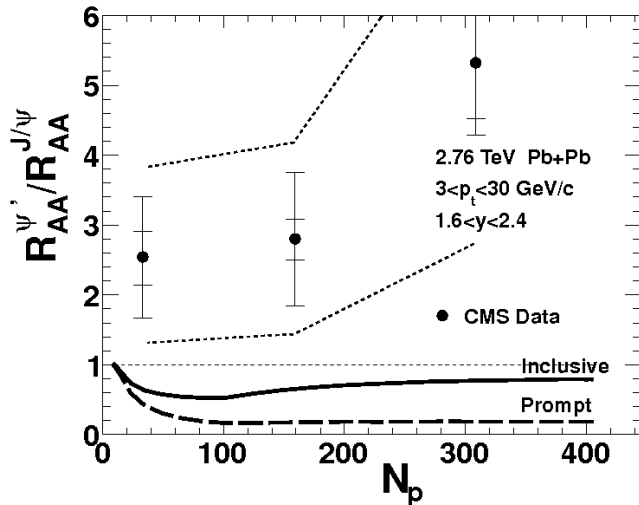
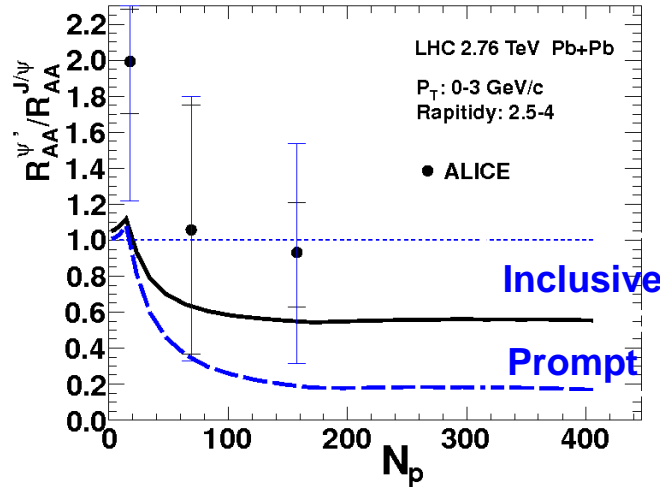
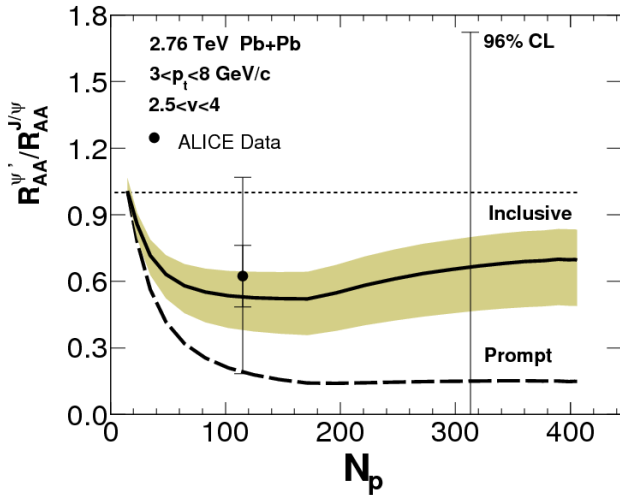
$\psi(2S)$ with B meson decay

middle pT

Low pT

Inclusive yield

Prompt:
2.76 TeV PRL (2014)
5.02 TeV PRL (2017)



We still can not explain $2S > 1S$,

[BC, Zhuang, et al, PLB726, 725-728 2013](#)

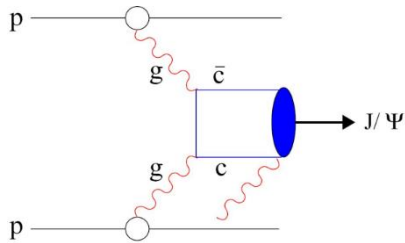
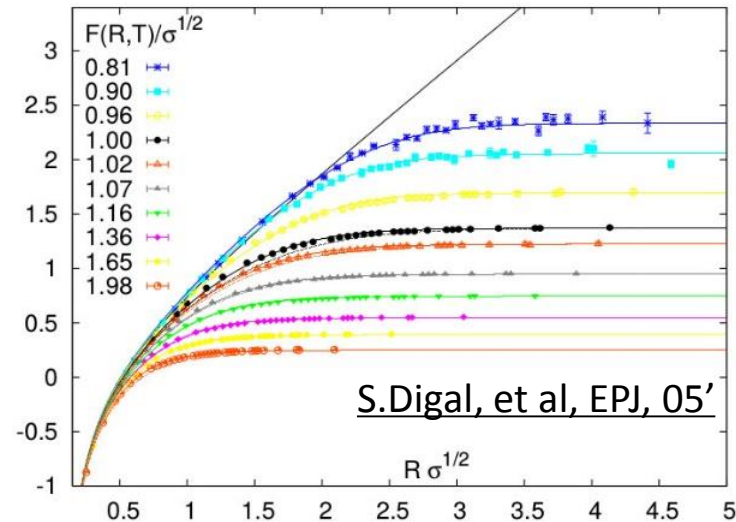
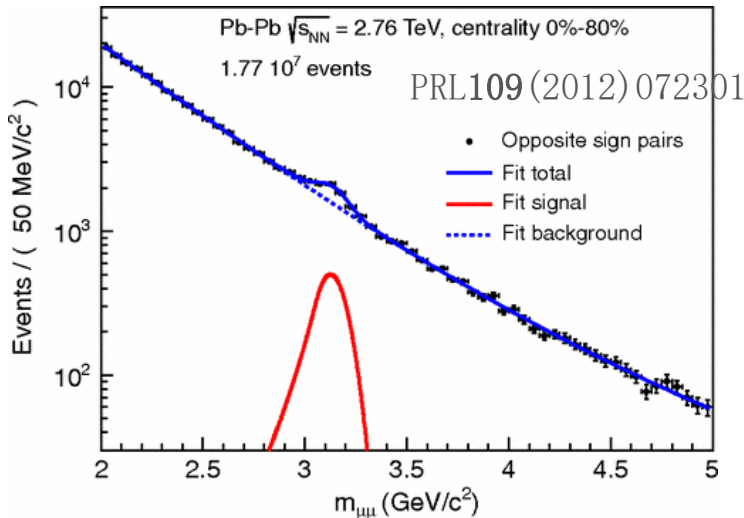
Our results(2013) qualitatively consistent with 5.02 TeV

$\psi(2S)$ in hot medium

How is **loosely bound $\psi(2S)$** produced in the QGP ?

Quarkonium as open quantum system

What is Experimentally Measured J/ψ and $\psi(2S)$?



(Cornell potential)

J/ψ

QGP evolution

time

(transitions)

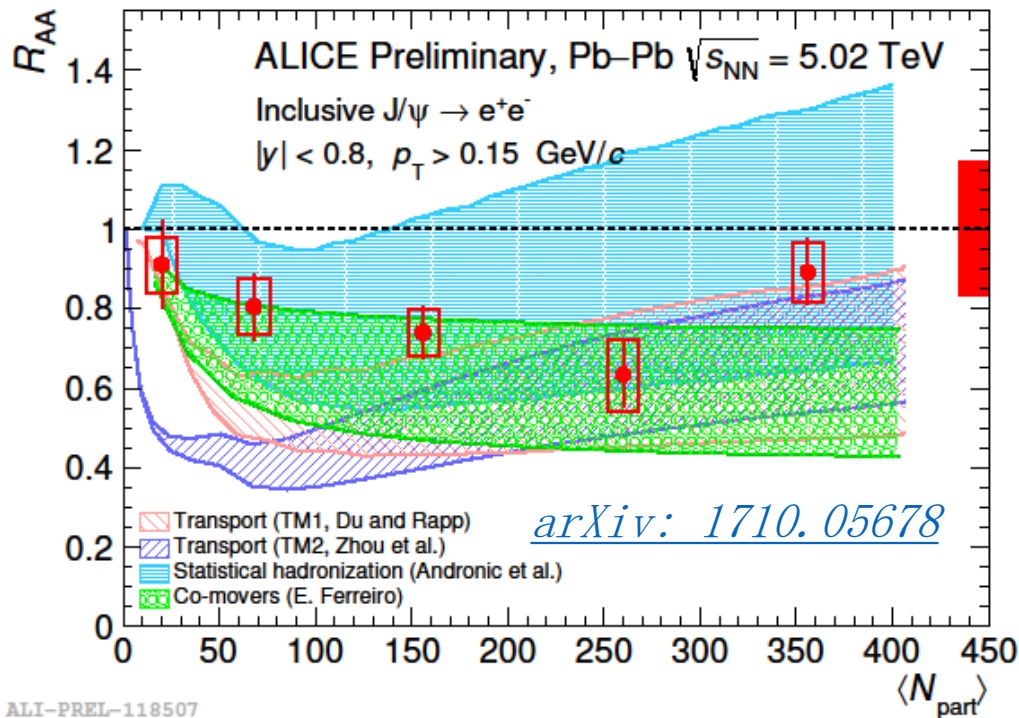
$$|c\bar{c}\rangle = c_{1S}(t)|J/\psi\rangle + c_{2S}(t)|\psi(2S)\rangle + \dots$$

Exp. measure the eigenstates of Cornell potential (in vacuum);
by dilepton decay.

$c\bar{c}$ dipole potential in QGP is COLOR SCREENED. **transitions**

Transitions between charmonia

Why we didn't focus on transitions of ψ before?



Large uncertainties of theoretical calculations and experimental data

Transitions between charmonia

Quantum evolutions about quarkonium:

BC, Du, Rapp, arXiv: 1612.02089
 Gossiaux, Katz, ZPC, 93', 16'
 Kopeliovich, et al, PRC, 15'
 Taesoo Song, et al, PRC, 15'
 Akamatsu, et al, arXiv: 1805.00167
 Blaizot, arXiv: 1711.10812

$$i\hbar \frac{\partial}{\partial t} \psi(r, t) = \left[-\frac{\hbar^2}{2m_\mu} \nabla^2 + V(r, t) \right] \psi(r, t)$$

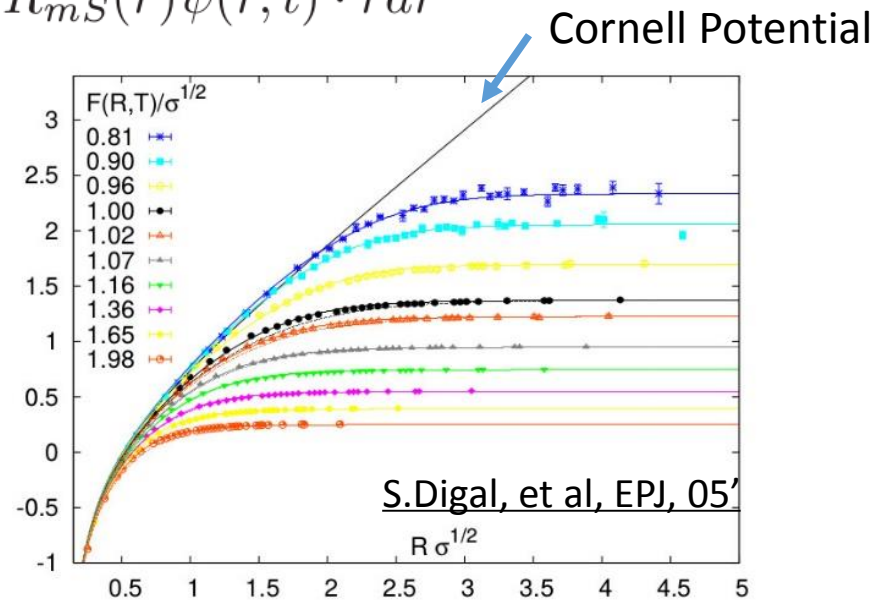
- mS eigenstate components in one dipole:

$$c_{mS}(t) = \langle R_{mS}(r) | \frac{\psi(r, t)}{r} \rangle = \int R_{mS}(r) \psi(r, t) \cdot r dr$$

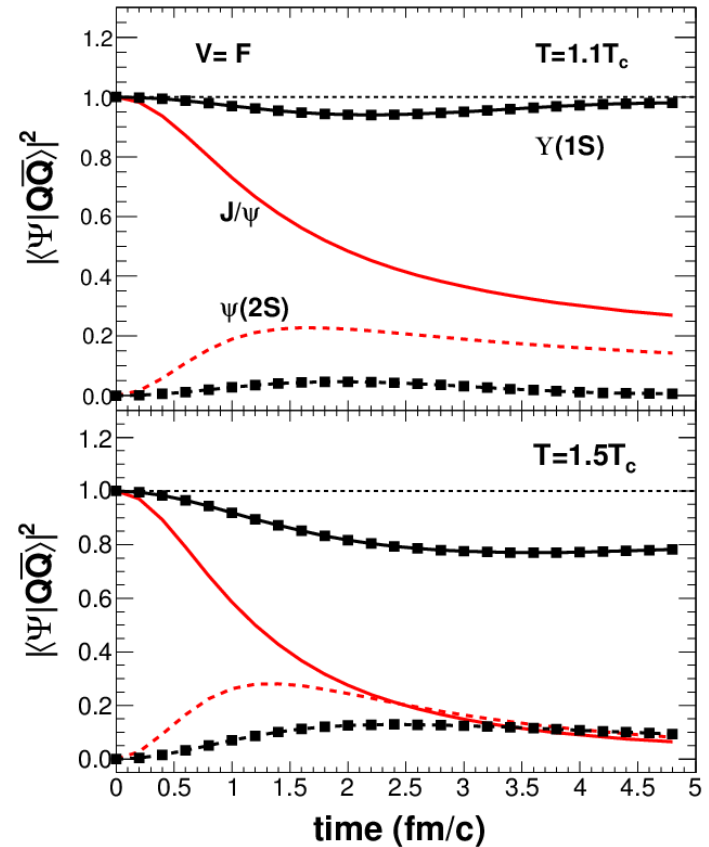
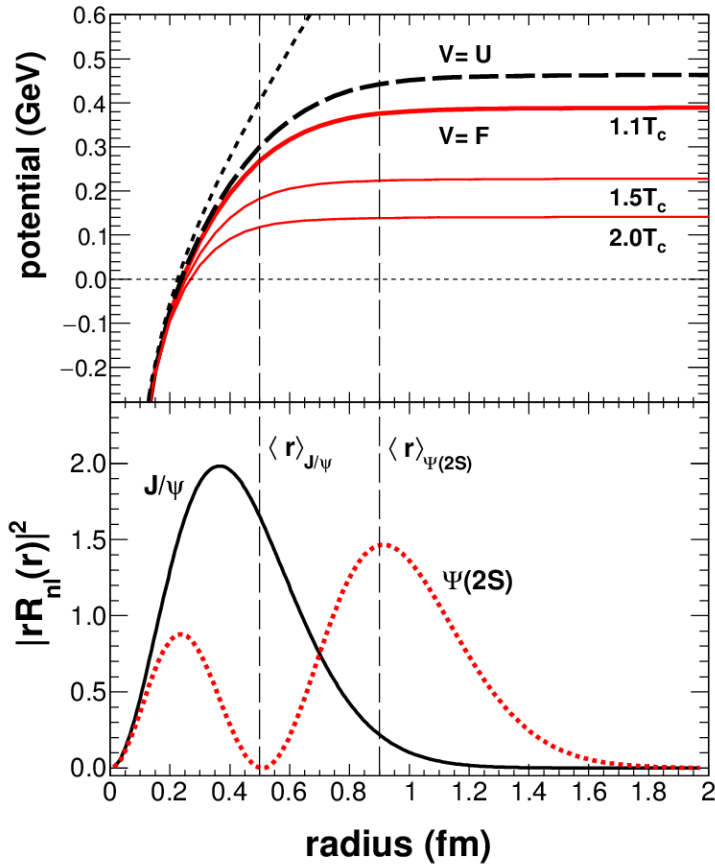
- Heavy quark potential
From Lattice QCD calculations.

- Static color screening
- Parton inelastic scattering

M. Laine, et al, JHEP, 07'
M. Strickland, PRC, 15'



Transitions between charmonia



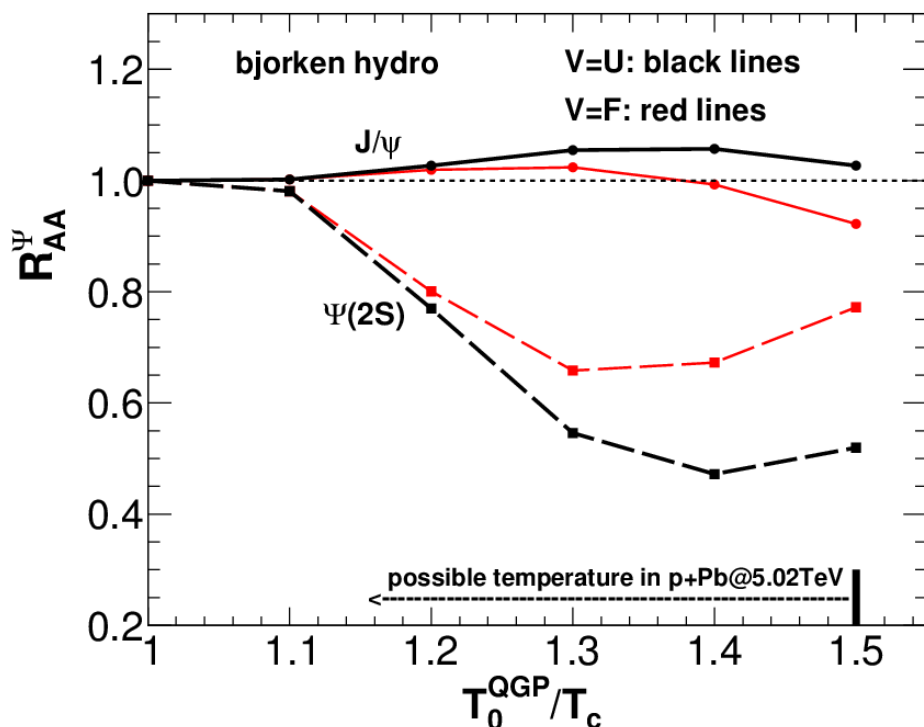
- Weak attractive force inside $c\bar{c}$ at high temperature.
- Potential restored for ground state at low temperature

$$|c\bar{c}\rangle = c_{1S}(t)|J/\psi\rangle + c_{2S}(t)|\Psi(2S)\rangle + \dots$$

Put one ground state in static hot medium

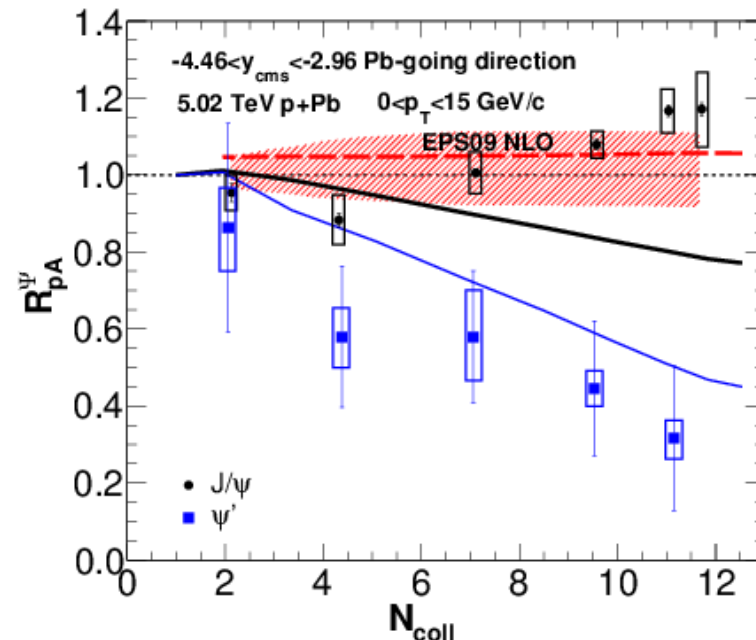
There are transitions.

Transitions between charmonia



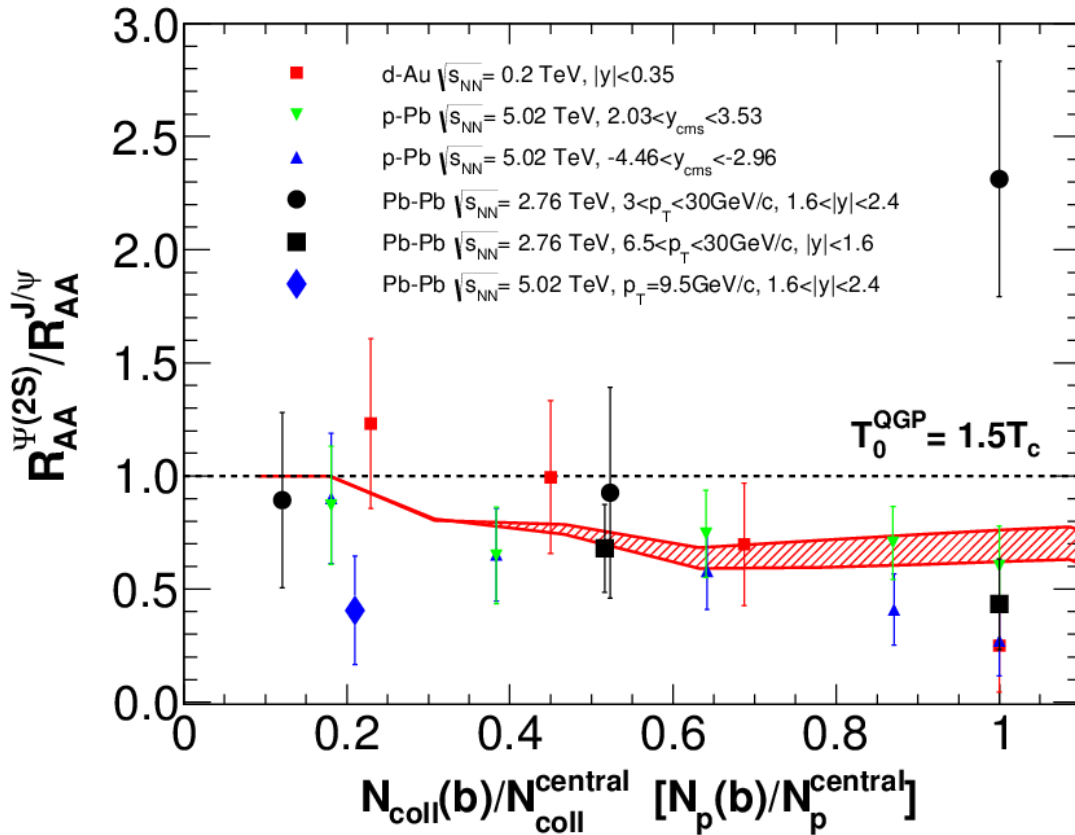
BC, Du, Rapp, in preparation

**$c\bar{c}$ evolutions in Bjorken hydro,
With only transition mechanism.**



Transport model
With dissociations
No transitions.
BC, Zhuang, PLB 2017

Transitions between charmonia

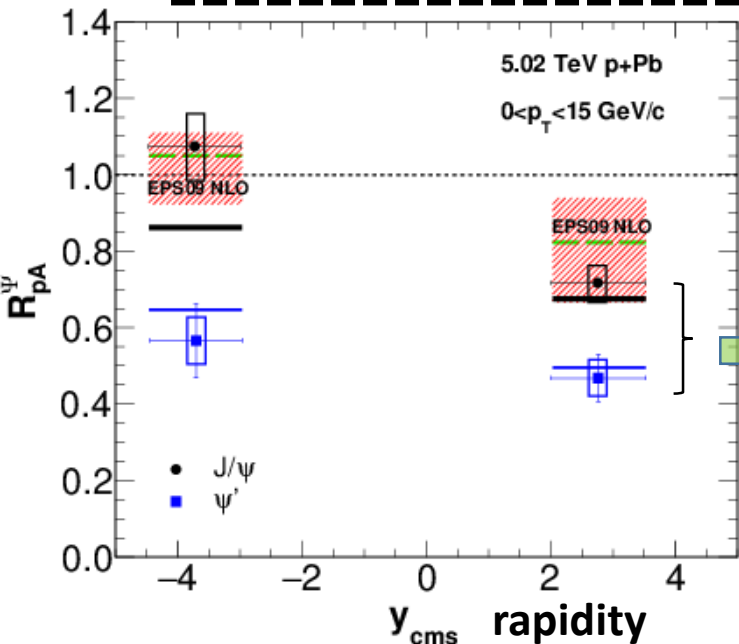


BC, Du, Rapp, in preparation

Very preliminary (pre-mature) comparison between **calculations with transitions** and **experimental data**.

Small QGP in p-Pb @5.02 TeV

charmonium production

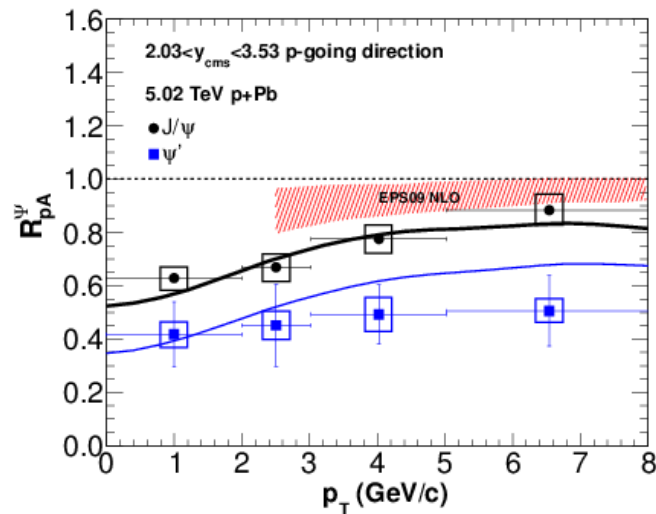
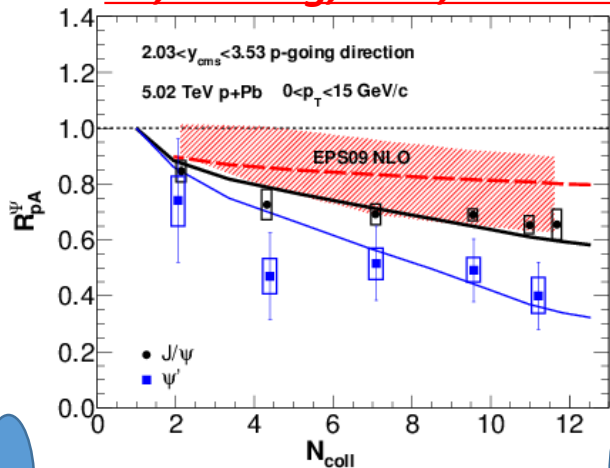


Final prompt J/psi :
 ~ 60% from direct,
 ~(30%, 10%) from (1P, 2S) decay

➤ Difference of J/ψ and ψ' R_{pA} indicates the final state interaction
 Hadron gas ? QGP ?

$$T_d^{\psi'} < T_{QGP}^{\text{max}}(pA) \approx 1.2 T_c < T_d^{J/\psi}$$

BC, Zhuang, et al, PLB 2017

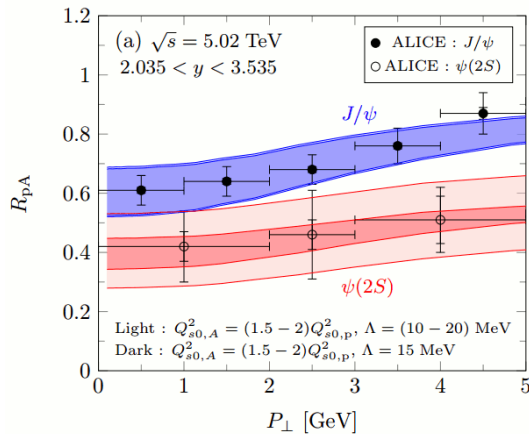


Transverse momentum

Flash comparisons

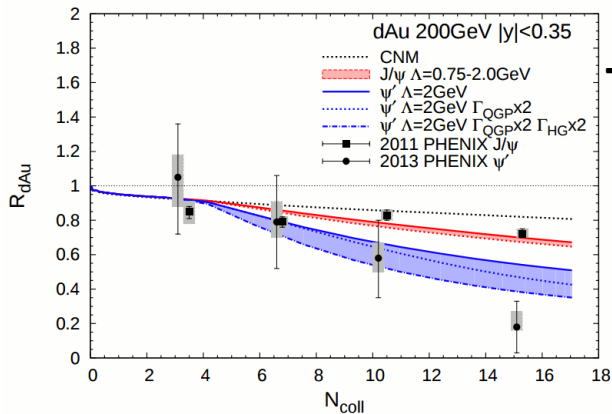
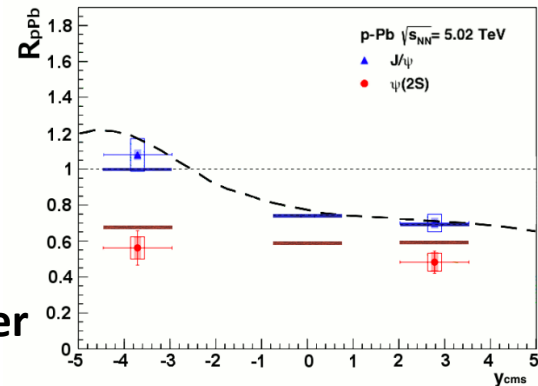
Models:

- Y. Q. Ma, et al, **CGC+ICEM**, **PRC 2018**
- Ferreiro, **Co-mover interactions**, **PLB 2015**
- Transport model (Du, Rapp), **QGP+HG**, **NPA 2015**
- Transport model (BC, Zhuang), **QGP**, **PLB 2017**



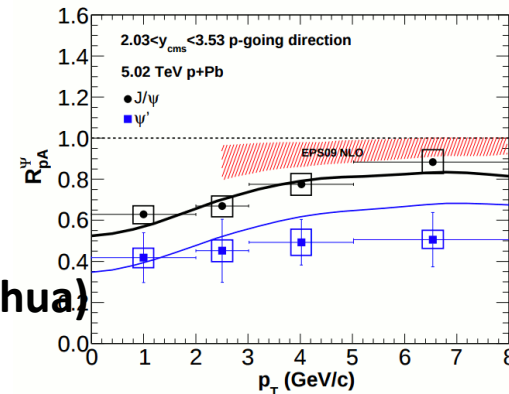
CGC+ICEM

Co-mover



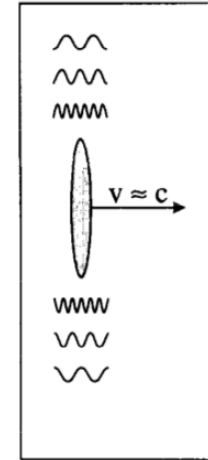
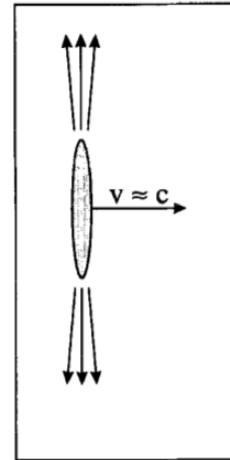
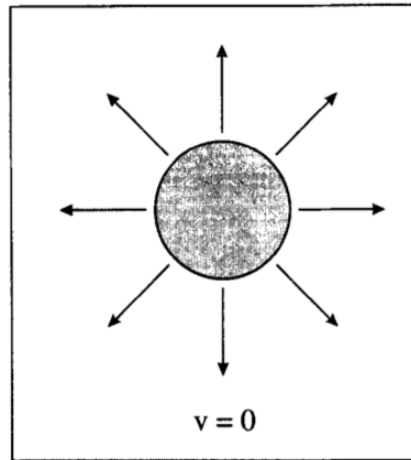
Transport (TAMU)

Transport (Tsinghua)



Equivalent Photon Approximation

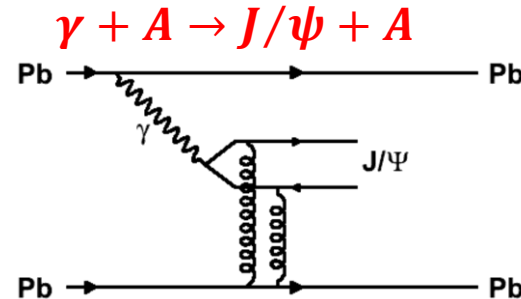
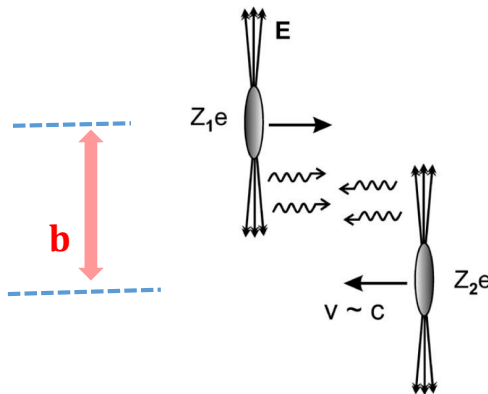
Prog.Part.Nucl.Phys. 39,503-564, 1997



$$eB \sim m_\pi^2 \sim 10^{18} G$$

charges moves at nearly speed of light → produce E-B fields

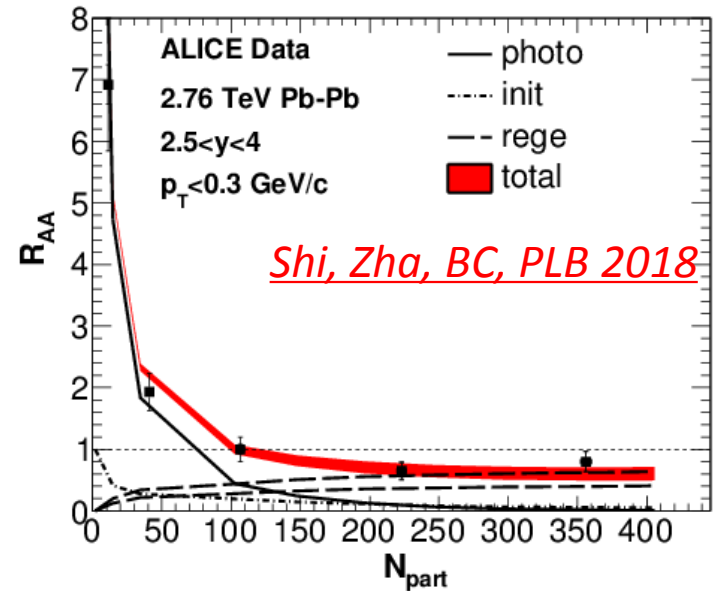
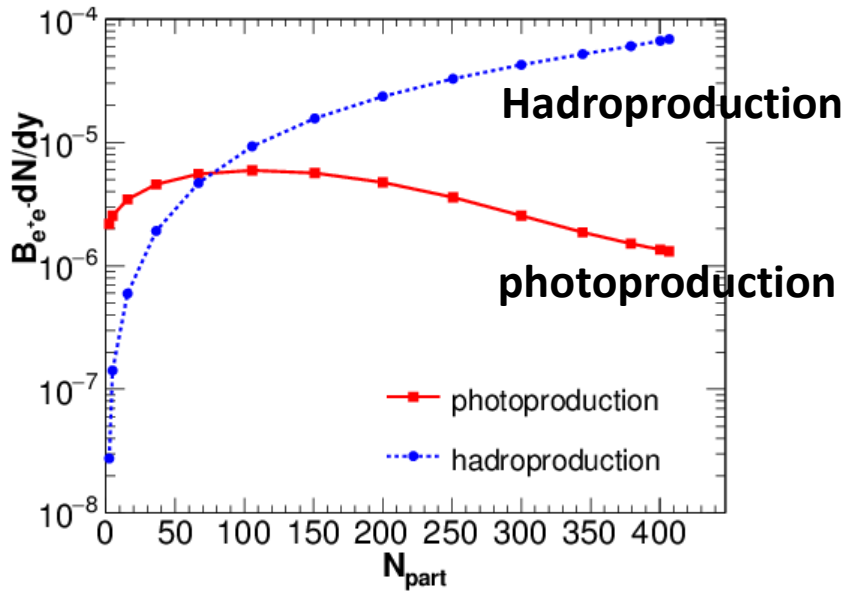
Equivalent-Photon-Approximation
Fermi, 1924'



$$|\gamma\rangle = C_{\text{pure}}|\gamma_{\text{pure}}\rangle + C_{\rho^0}|\rho^0\rangle + C_\omega|\omega\rangle + C_\phi|\phi\rangle + C_{J/\psi}|J/\psi\rangle + \dots + C_{q\bar{q}}|q\bar{q}\rangle$$

J/ψ from EM field + QGP

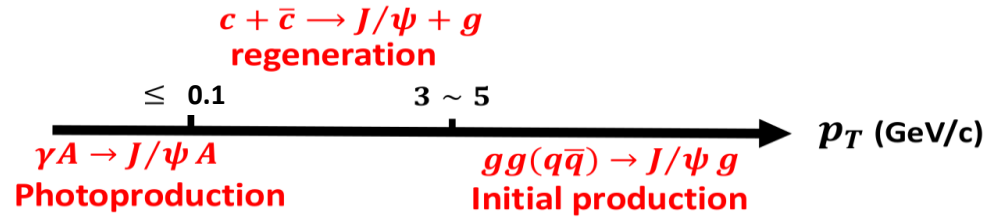
$$N_{\psi}^{\gamma A} \propto \int dw \frac{dN_{\gamma}}{dw} \sigma_{\gamma A \rightarrow J/\psi A} \Gamma_{QGP}^{decay}$$



$$R_{AA} = \frac{N^{\gamma A} + N_{AA}^{initial} + N_{AA}^{rege}}{N_{pp*ncoll}^{J/\psi}}$$

- Significant enhancement at $N_p \approx 80$, where $T_0^{QGP} = 2T_c$
- When $N_{part} \rightarrow 0$ ($b > 2R_A$),
hadroproduction $\rightarrow 0$, photoproduction \rightarrow non-zero, $R_{AA} \rightarrow$ infinity

Summary



- **Charm quark evolutions** affect the behavior of **regenerated** charmonia.
- $\psi(2S)$ may come from **transitions in the correlated charm pair**, or **recombination of un-correlated charm pairs**.
B hadron decay is important for inclusive $\psi(2S)$ yield.
- **Photoproduction** from strong EM fields are still important in extremely low p_T and semi-central collisions.

Some reference related to the talk:

BC, Zhuang, et al,	PLB 765, 323-327(2017)	p-Pb
BC,	PRC 95, 034908 (2017)	2S elliptic flows
Zhao, BC,	PLB 776, 17-21, (2018)	Charm diffusions
BC, Rapp, et al,	in preparation, (and 1612.02089)	Charmonium transitions in QGP
BC, Zhuang, et al,	1801.01677	EM fields and QGP on 2S/1S
Shi, Zha, BC	PLB 777, 399-405, (2018)	$\gamma A \rightarrow J/\psi A$
BC,	PRC 93, 054905 (2016)	Rapidity dependence

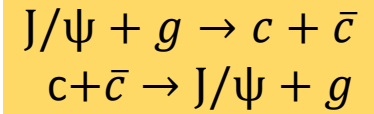


More slides

Transport equation

Transport model

$$\frac{\partial f_\psi}{\partial t} + \frac{\vec{p}_\psi}{E} \cdot \vec{\nabla}_x f_\psi = -\alpha_\psi f_\psi + \beta_\psi$$



$$\alpha_\psi(\vec{p}_t, \vec{x}_t, \tau, \vec{b}) = \frac{1}{2E_t} \int \frac{d^3\vec{k}}{(2\pi)^3 2E_g} \sigma_{g\psi}(\vec{p}, \vec{k}, T) 4F_{g\psi}(\vec{p}, \vec{k}) f_g(\vec{k}, T)$$

$$\partial_\mu(\rho_c u_{QGP}^\mu) = 0$$

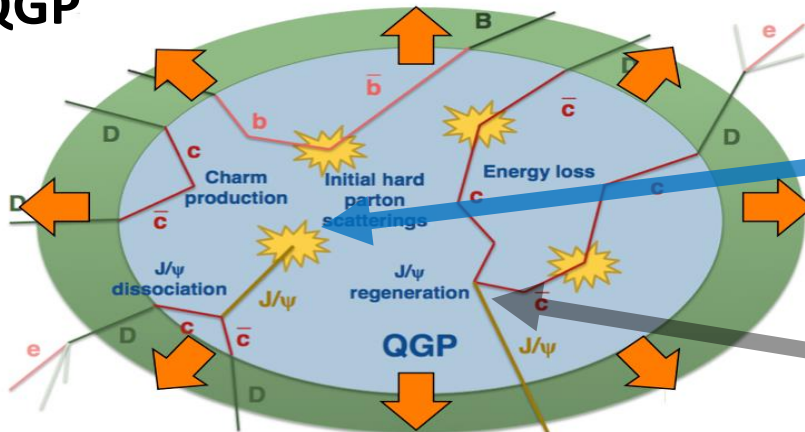
$$\beta_\psi(\vec{p}_t, \vec{x}_t, \tau, \vec{b}) = \frac{1}{2^4 (2\pi)^9 E_t} \int \frac{d^3\vec{k}}{E_g} \frac{d^3\vec{q}_c}{E_c} \frac{d^3\vec{q}_{\bar{c}}}{E_{\bar{c}}} W_{c\bar{c}}^{\psi g}(\vec{q}_c, \vec{q}_{\bar{c}}) f_c(\vec{q}_c, T) f_{\bar{c}}(\vec{q}_{\bar{c}}, T)$$

Dynamical evolution

$$\times (2\pi)^4 \delta^{(4)}(p + k - q_c - q_{\bar{c}})$$

$$N^{c\bar{c} \rightarrow J/\psi} \sim (N^{c\bar{c}})^2$$

Expanding QGP



Two components:

Initial hard scattering before QGP formation

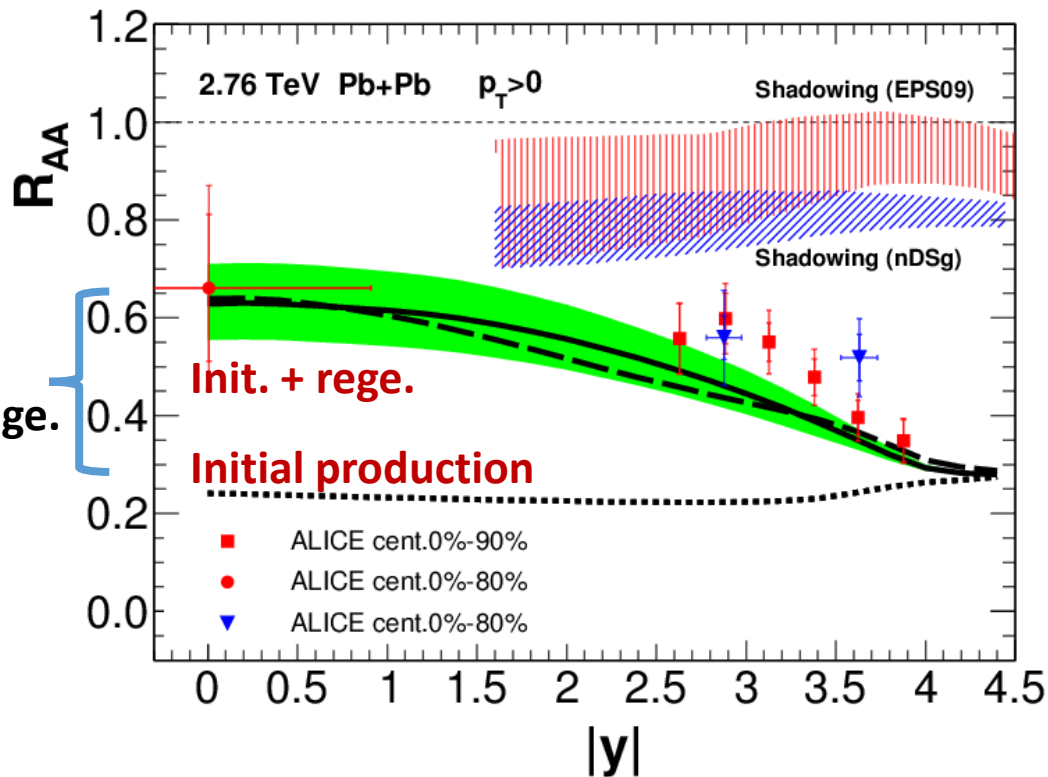
Regeneration:



Rapidity dependence

Rapidity - dependence

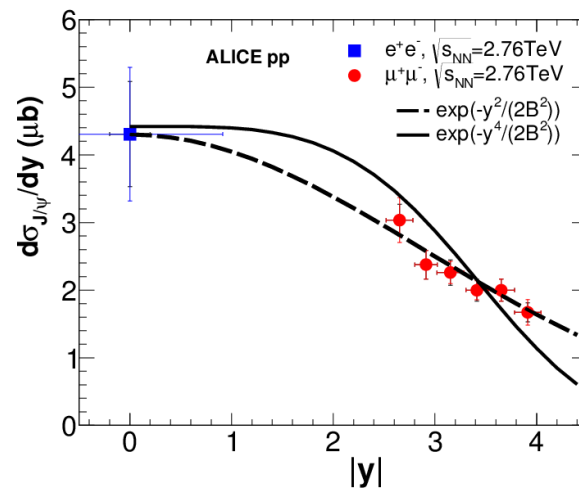
● $R_{AA}(y)$ nuclear modification factor with rapidity



[BC, PRC 93 \(2016\) 054905](#)

$$N_{J/\psi}^{rege} \sim \int dV \rho_c \rho_{\bar{c}} W_{combine}$$

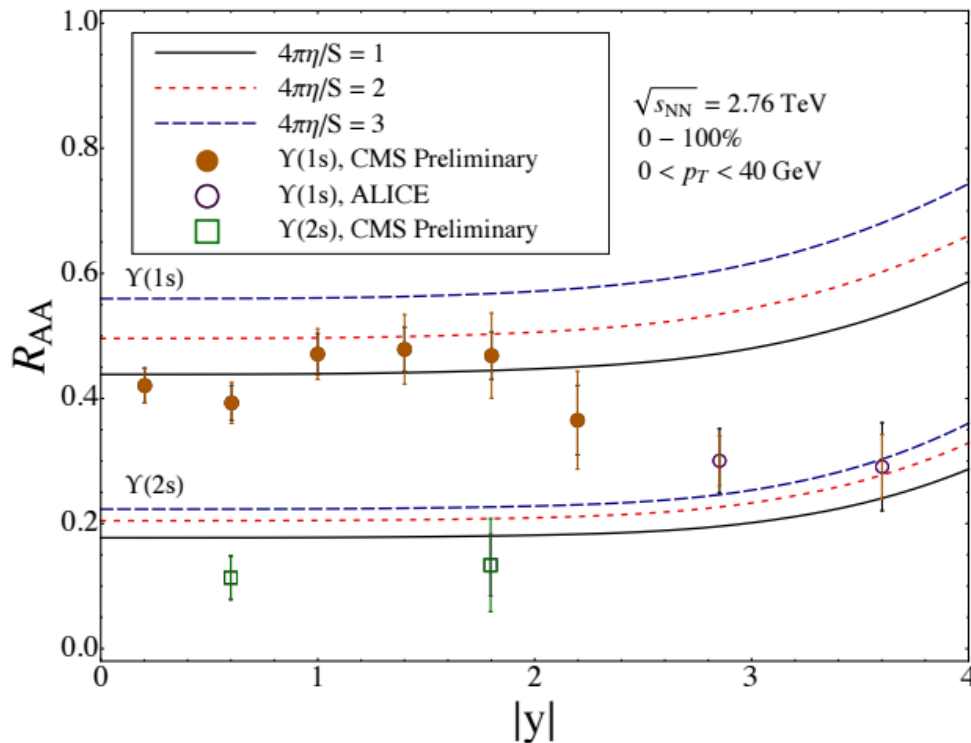
Regeneration dominates in central rapidity



$c\bar{c}$ production cross-section

Situation without recombination

- If no regeneration, $R_{AA}(y)$? (such as bottomonium)



weak/no regeneration for Y ,
due to
less bottom pairs

More reference:

Du, Rapp, He:

PRC 96, (2017) ,054901

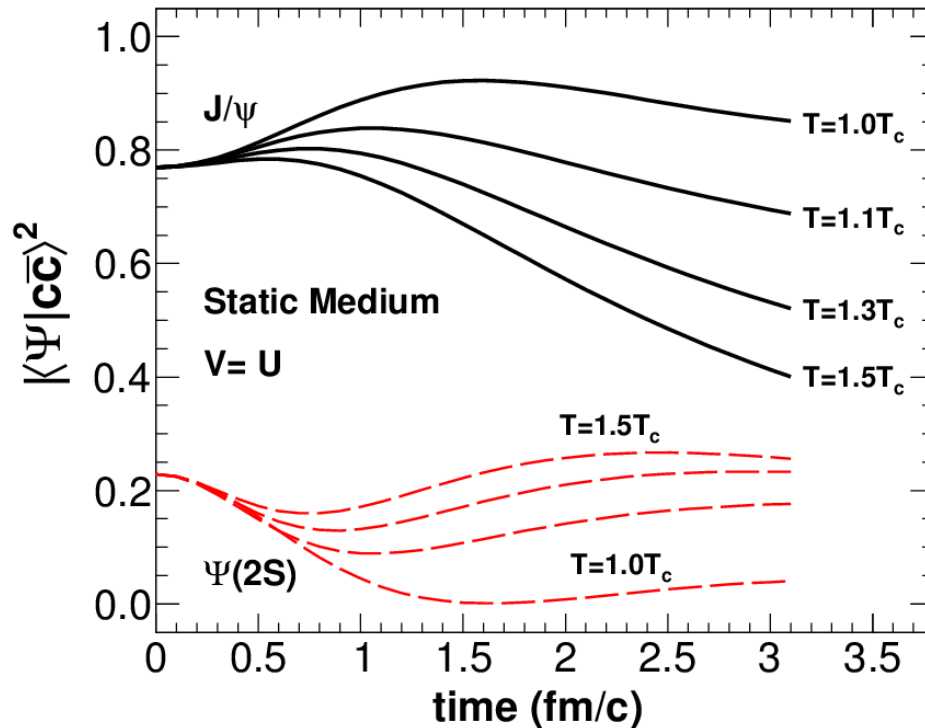
Blaizot, Escobedo: 1803.07996

BC, Zhao:

PLB 772 (2017) 819-824

M. Strickland, et al, Potential model
PRC 92 (2015) 061901,

Transitions between charmonia



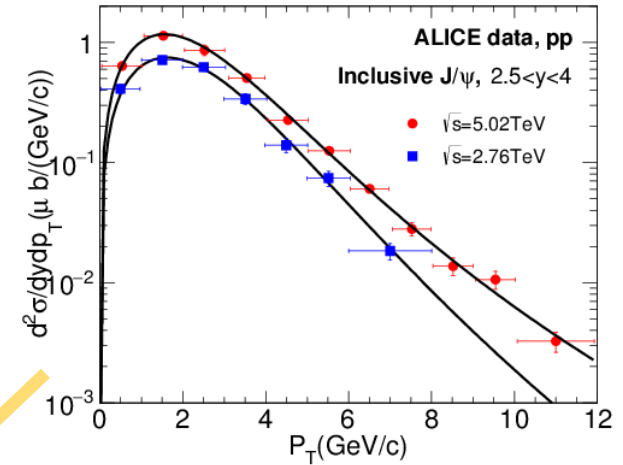
The evolutions also need $c\bar{c}$ initial wave function

- Initialize $c\bar{c}$ dipole with more realistic wave function, Containing components of both 1S and 2S
- **Different transitions happen at different T.**
(the normalization of $c\bar{c}$ wave function is conserved.)

p_T dependence

hadronic production in different p_T region

p_T range (GeV/c)	$\sigma_{p_{T1}-p_{T2}}/\sigma_{total}$
0 – 0.01	1.9×10^{-5}
0 – 0.05	4.8×10^{-4}
0 – 0.1	0.19%
0 – 0.5	4.5%
0 – 1	15%



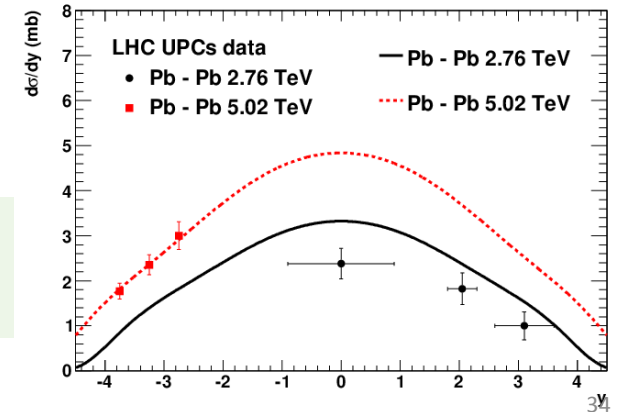
Zhao, BC, PLB 2017

Hadronic cross section

Mean p_T in hadroproduction $\langle p_T \rangle \sim 3 \text{ GeV/c}$

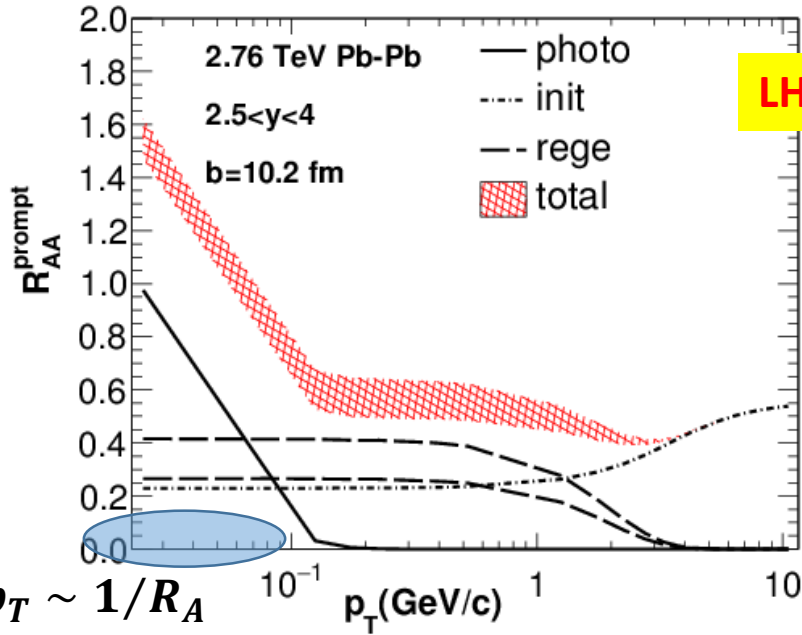
$\gamma + A \rightarrow J/\psi + X \quad p_T \sim 1/R_A \sim 0.03 \text{ GeV/c}$

Exp. $\langle p_T \rangle = 0.055 \text{ GeV/c}$ PRL 116, 222301 (2016)

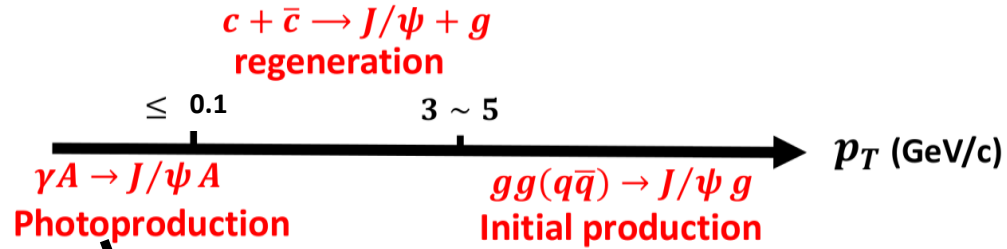


Shi, Zha, BC, PLB 2018

Total J/ψ from EB field + QGP

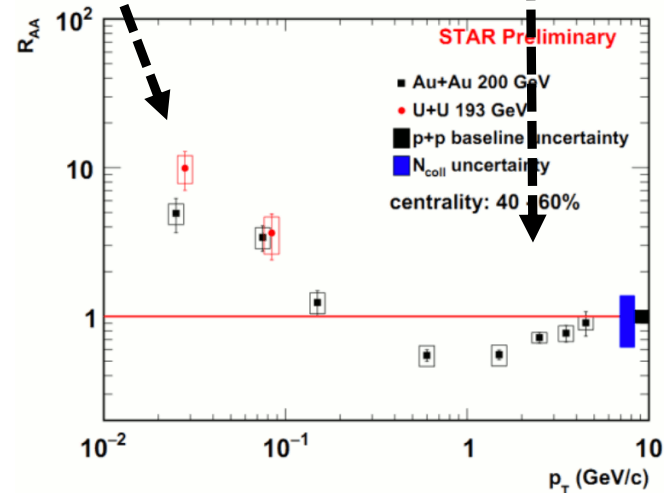
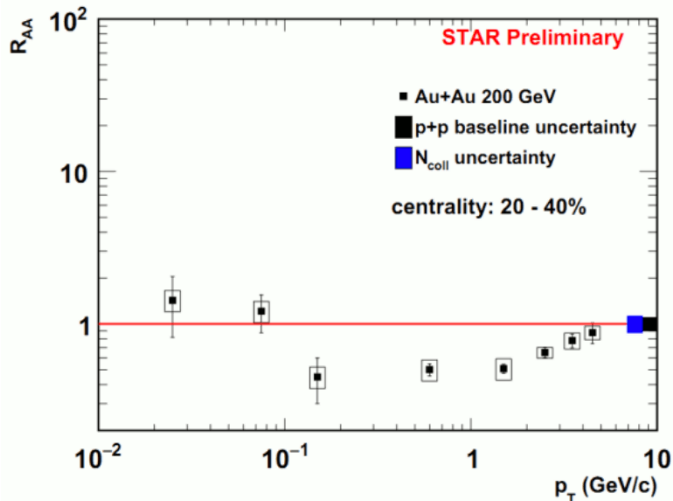


$$R_{AA} = \frac{N^{\gamma A} + N_{AA}^{initial} + N_{AA}^{rege}}{N_{pp*ncoll}^{J/\psi}}$$



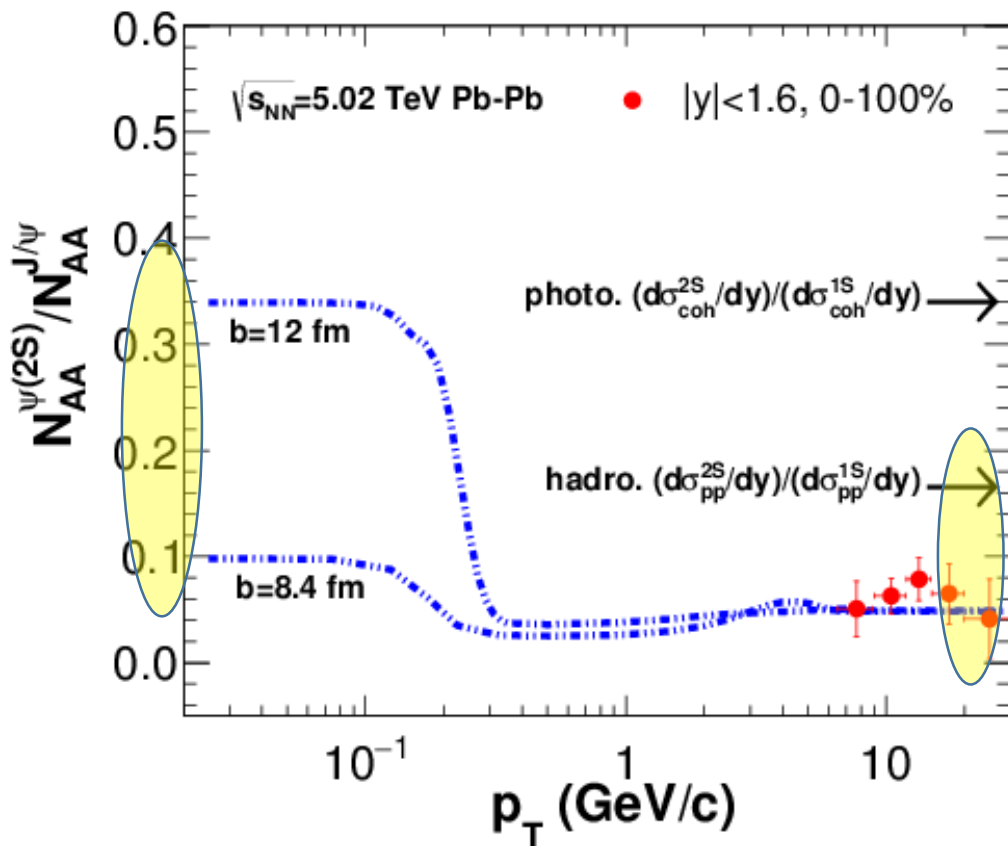
R_{AA} decreases, then increases with p_T

Shi, Zha, BC, PLB 2018



Photoproduced 2S/1S

BC, Zhuang, Carsten, et, arXiv: 1801.01677



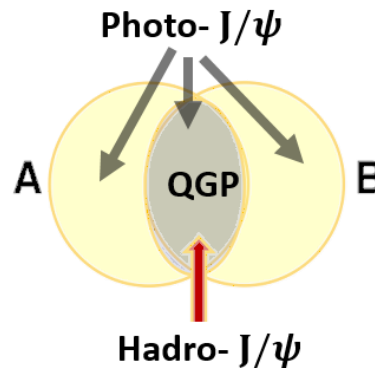
Our prediction in low p_T

➤ **Enhancement:**
 additional photoproduction
 + diff. spatial distribution

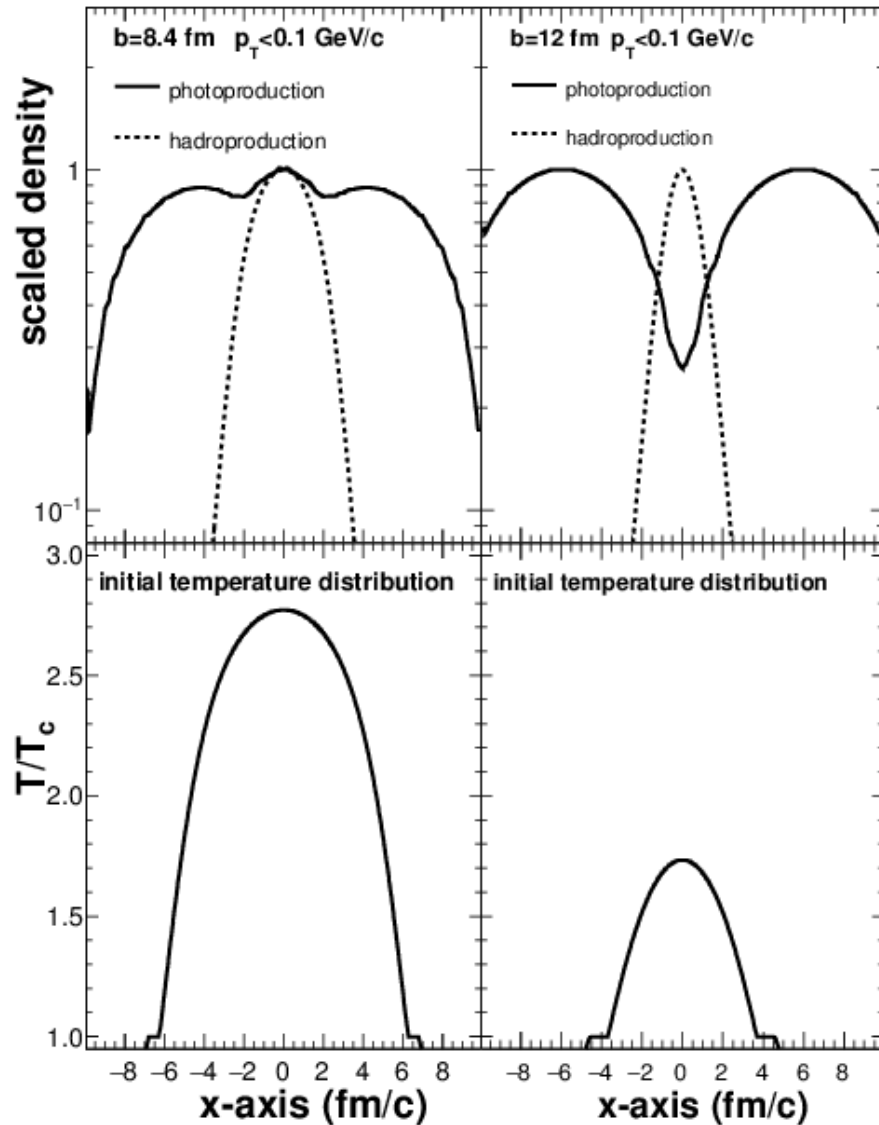
➤ **Suppression:** QGP effect.

➤ **Hadroproduction:**
 in the overlap area of two nuclei

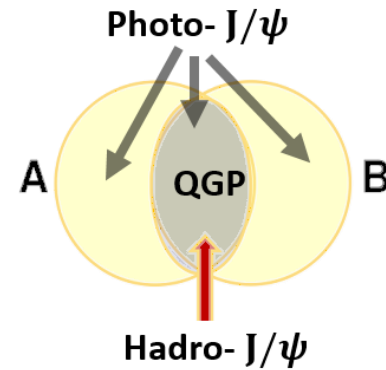
➤ **Photoproduction:**
 over the entire nuclear surface



Photoproduced 2S/1S



Spatial distributions of two productions



- **Hadroproduction:**
in the overlap area of two nuclei
- **Photoproduction:**
over the entire nuclear surface

Spatial distribution of medium Temperature

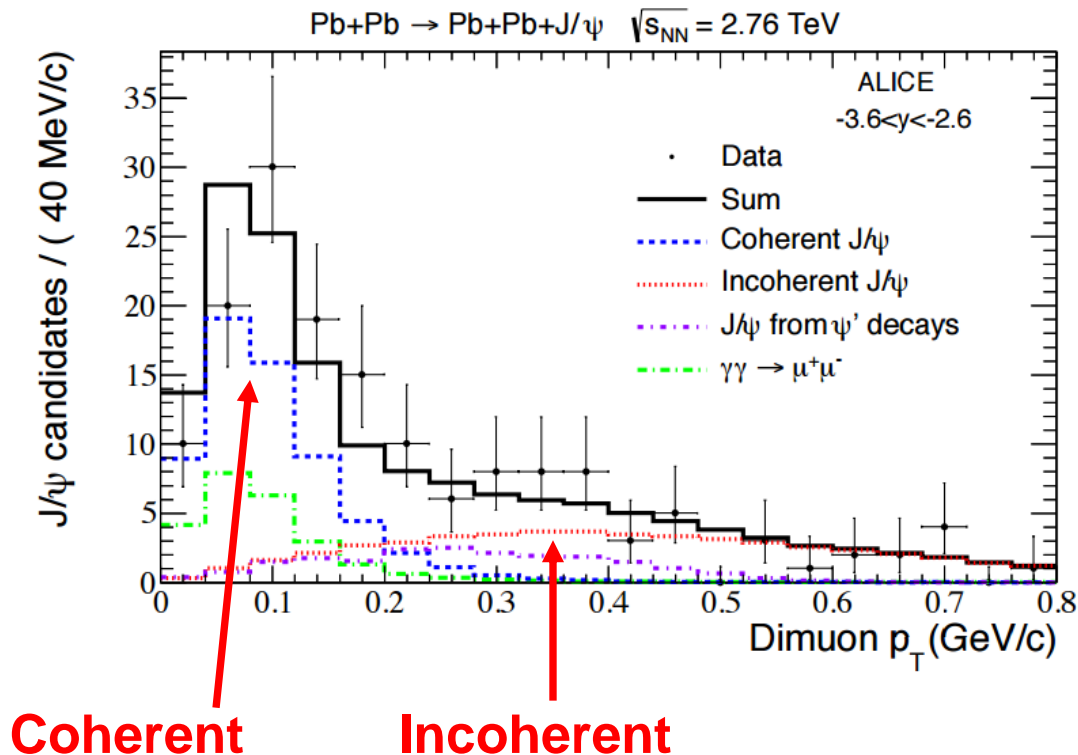
J/ψ coherent photoproduction

Vector meson dominant model

$$|\gamma\rangle = C_{\text{pure}}|\gamma_{\text{pure}}\rangle + C_{\rho^0}|\rho^0\rangle + C_{\omega}|\omega\rangle + C_{\phi}|\phi\rangle + C_{J/\psi}|J/\psi\rangle + \dots + C_{q\bar{q}}|q\bar{q}\rangle$$

Coherent: $\gamma + A \rightarrow J/\psi + X$

Incoherent: $\gamma + N \rightarrow J/\psi + X$



- In $p_T < 0.1$ GeV/c, coherent production dominates.

J/ψ from electromagnetic field

Mainly three ingredients:

$$N_{\psi}^{\gamma A} \propto \int d\omega \frac{dN_{\gamma}}{d\omega} \sigma_{\gamma A \rightarrow J/\psi A} \Gamma_{QGP}^{decay}$$

Given latter

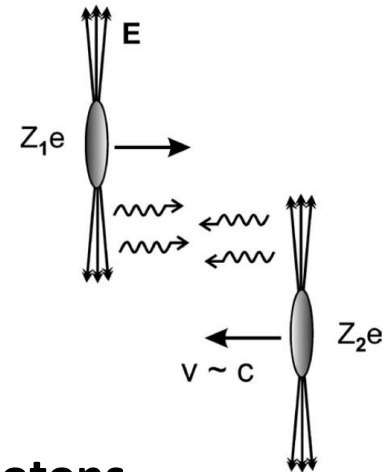
● Photon density $\frac{dN_{\gamma}}{d\omega}$ emitted by one nucleus

Poynting vector $\vec{S}(\vec{r}, t) = \vec{E}(\vec{r}, t) \times \vec{B}(\vec{r}, t) \xrightarrow{v \rightarrow c} |\vec{E}(\vec{r}, t)|^2 \vec{v}$

$$\int_{-\infty}^{\infty} dt \int d\vec{x}_{\perp} \cdot \vec{S}(\vec{r}, t) \stackrel{!}{=} \int_0^{\infty} d\omega \int d\vec{x}_{\perp} \omega n(\omega, \vec{x}_{\perp})$$

Energy flux of the fields

Energy flux of equivalent photons



$$\frac{dN_{\gamma}}{d\omega} = n(\omega) = \frac{1}{\pi\omega} \int d\vec{x}_T |\vec{E}_T(\vec{r}, \omega)|^2$$

$$= \frac{(Ze)^2}{\pi\omega} \int_0^{\infty} \frac{d^2\vec{k}_T}{(2\pi)^2} \left[\frac{F\left(\left(\frac{\omega}{v\gamma}\right)^2 + k_T^2\right)}{\left(\frac{\omega}{v\gamma}\right)^2 + k_T^2} \right]^2 \frac{k_T^2}{v^2}$$

Nuclear charge form factor is the **Fourier transform** of Woods-Saxon distribution.
For point particle, it's 1

Photon density