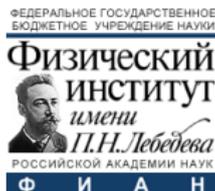


XYZ states as hadronic molecules

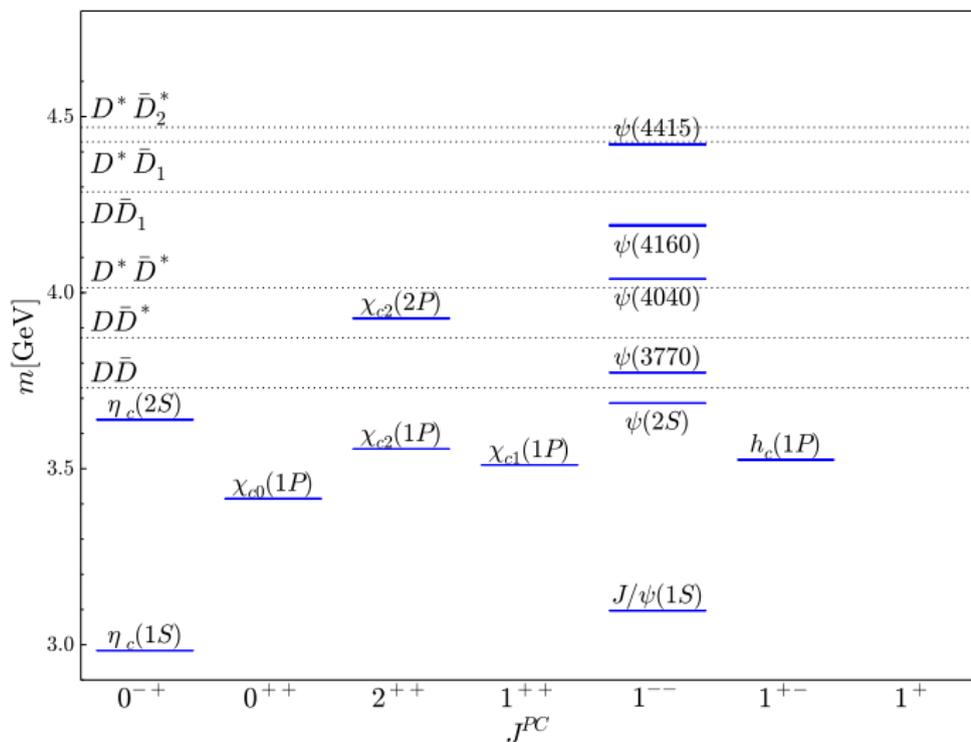
A.V. Nefediev

(LPI, Moscow)

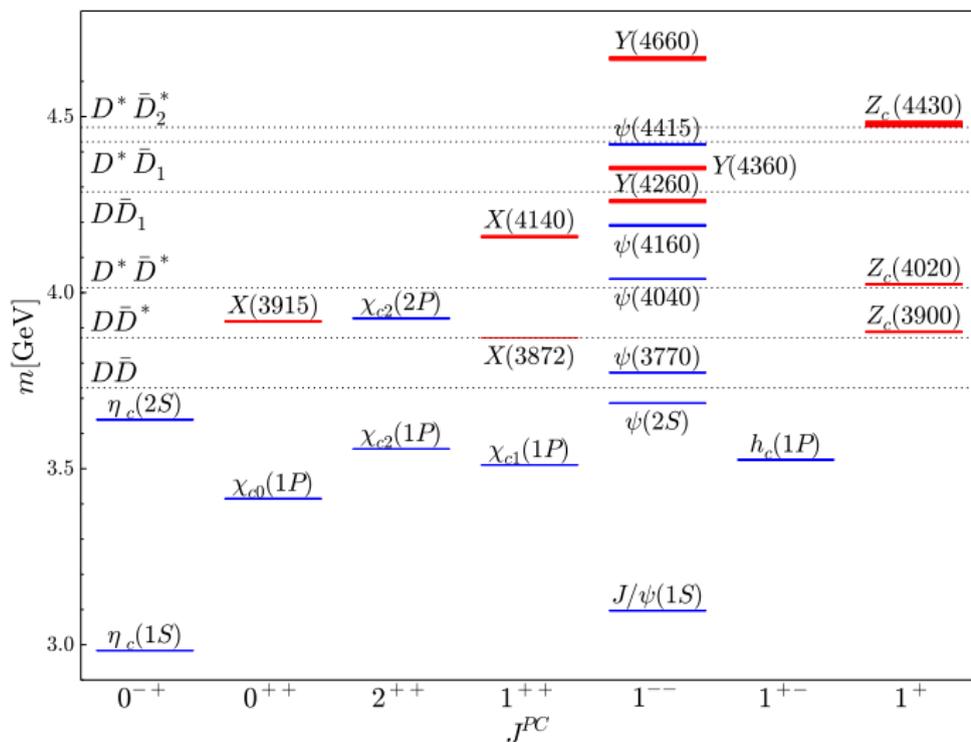


Charm 2018, Novosibirsk, Russia, 21-25 May 2018

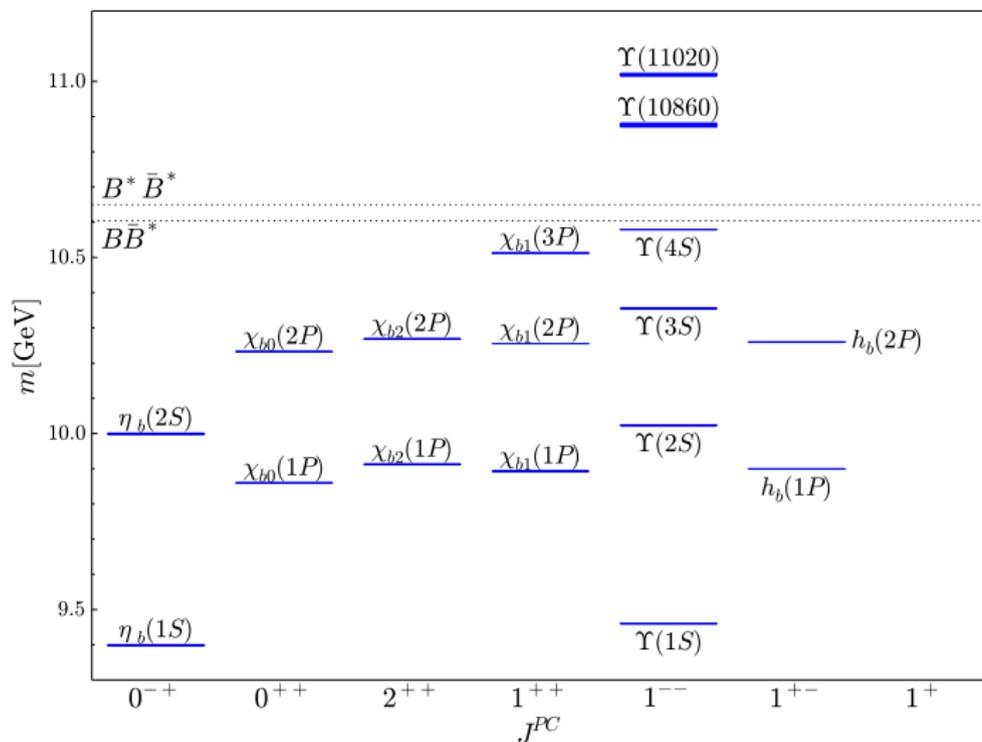
Spectrum of charmonium



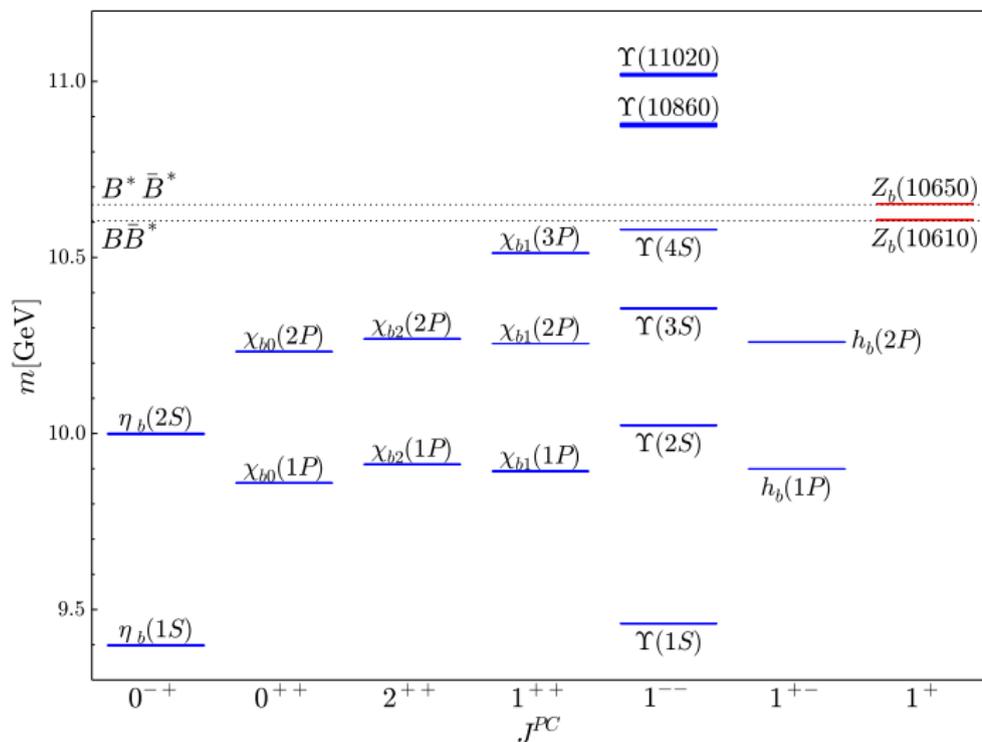
Spectrum of charmonium



Spectrum of bottomonium



Spectrum of bottomonium



Meet XYZ states

- X 's are new exotic states

$$X(3872) \quad X(3915) \quad X(4140) \quad \dots$$

- Y 's are exotic vector states (to tell from neat $\bar{c}c$ quarkonia ψ 's)

$$Y(4230) \quad Y(4260) \quad Y(4360) \quad Y(4660) \quad \dots$$

- Z 's are charged exotic states

$$Z_c(3900) \quad Z_c(4020) \quad Z_c(4430) \quad Z_b(10610) \quad Z_b(10650) \quad \dots$$

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Naming scheme for XYZ states under review by PDG

Quark model



$$H = 2m_Q + \frac{p^2}{m_Q} + \sigma r - \frac{4\alpha_s}{3r} + C + V_{\text{spin-dep}}$$

Successes:

- Good description of spectrum below open-flavour threshold
- Reasonable description of leptonic, radiative, hadronic widths

Failure:

- Breakdown for higher quarkonia

What is missing?

- Constituent gluons
- Effects of light-quarks: loops, thresholds, pions

If not $\bar{Q}Q$ then what? Proposals...

- Tetraquark



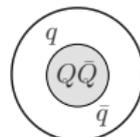
Compact object made of $(Qq)_{\bar{3}}$ and $(\bar{q}\bar{Q})_3$

- Hybrid



Compact object made of $(Q\bar{Q})_8 + \text{gluons}$

- Hadro-Quarkonium



$(Q\bar{Q})_1$ surrounded by light quarks

- Hadronic Molecule



Extended object made of $(\bar{Q}q)_1$ and $(\bar{q}Q)_1$

What is hadronic molecule?

Molecule = large probability to observe resonance in a given hadron-hadron channel

- Proximity of open-flavour thresholds \implies large admixture of meson-meson component in the w.f. of the resonance
- Nature of the resonance can be different:
bound *versus* virtual state \implies dynamical problem

Disclaimer: because of inelastic channels, poles in the complex E -plane are always on unphysical Riemann Sheets, away from the real axis \implies state = resonance

- Binding forces can be different:
 s - *versus* t -channel exchanges \implies different models

Have we met hadronic molecules so far?

Yes, we have! We know them for years in few nucleon systems

- 3S_1 NN system with $I = 0$:

$$a = 5.4 \text{ fm} \quad r_e = 1.7 \text{ fm}$$

Pole on **RS-I** with $E_B = 2.23 \text{ MeV} \implies$ **deuteron**

- 1S_0 NN system with $I = 1$:

$$a = -24 \text{ fm} \quad r_e = 2.7 \text{ fm}$$

Pole on **RS-II** with $E_B = 0.067 \text{ MeV} \implies$ **virtual state**

Composite or elementary?

$$F(k) = \frac{1}{-\frac{1}{a} + \frac{1}{2}k^2 r_e - ik}$$

Define probability to observe compact state $0 \leq Z \leq 1$:

$$a = \frac{2(1-Z)}{(2-Z)} \frac{1}{\sqrt{2\mu E_B}} \quad r_e = -\frac{Z}{(1-Z)} \frac{1}{\sqrt{2\mu E_B}} + O\left(\frac{1}{\beta}\right)$$

$\beta (\gg k)$ — (inverse) range of force

Deuteron: $Z \rightarrow 0 \implies$ **molecule** (Weinberg'60's)

Elementary (confined) state

- Effective range is large
- Scattering length is small
- **Two** near-threshold poles

Composite (molecular) state

- Effective range is small
- Scattering length is large
- **One** near-threshold pole

\implies **pole counting rules** (Morgan'1992)

What to expect from molecules?

- Predominantly S -wave **bound** or **virtual** state of $(\bar{Q}q)$ and $(\bar{q}Q)$ mesons
- Seen in elastic $((\bar{Q}q) + (\bar{q}Q))$ and inelastic (e.g. $(\bar{Q}Q) + (\bar{q}q)$) channels
- **Bound state molecule:**
 - below-threshold **peak** in inelastic channels
 - above-threshold hump in elastic channels
- **Virtual state molecule:**
 - threshold **cusp** in inelastic channels
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Impossible to distinguish

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Hard to distinguish

Impossible to distinguish

Combined analysis of all measured production and decay channels for a given resonance is necessary to reveal its nature

Heavy-quark spin symmetry

- Exotic XYZ states contain **heavy quarks** (HQ)
- In the limit $m_Q \rightarrow \infty$ ($m_Q \gg \Lambda_{\text{QCD}}$) spin of HQ **decouples**
 \implies **Heavy Quark Spin Symmetry** (HQSS)
- For realistic m_Q 's HQSS is **approximate** but rather **accurate** symmetry of QCD
- Predictions of HQSS **depend crucially** on the **nature** of states under study
(Cleven et al.'2015)
- **Quarkonium component** of the w.f. (if exists) may impact the predictions
(Cincioglu et al.'2016)
- HQSS is a **tool** to relate properties of states with different HQ spin orientation
 \implies **Spin partners**
(Guo et al.'2009, Bondar et al.'2011, Voloshin et al.'2010, Mehen et al.'2011, Nieves et al.'2012, Guo et al.'2013, Albaladejo et al.'2015, Baru et al.'2016)

The X family

$X(3872)$: Experimental status

- Quantum numbers: $J^{PC} = 1^{++}$, $I = 0$
- Mass and width:

$$M_X = 3871.68 \pm 0.17 \text{ MeV} \quad \Gamma_X < 1.2 \text{ MeV}$$

$$M_{D^0} + M_{\bar{D}^{*0}} - M_X = (0.00 \pm 0.18) \text{ MeV}$$

- Observation modes:

- $X \rightarrow \pi^+ \pi^- J/\psi$

(Belle 2003, CDF, $D\bar{0}$, BABAR 2004-2006, LHCb 2013)

- $X \rightarrow \pi^+ \pi^- \pi^0 J/\psi$

(Belle 2005, BABAR 2010)

- $X \rightarrow D\bar{D}^* \begin{cases} \nearrow D\bar{D}\pi \\ \searrow D\bar{D}\gamma \end{cases}$

(Belle 2006, BABAR 2007)

- $X \rightarrow \gamma J/\psi \quad X \rightarrow \gamma \psi'(3686)$

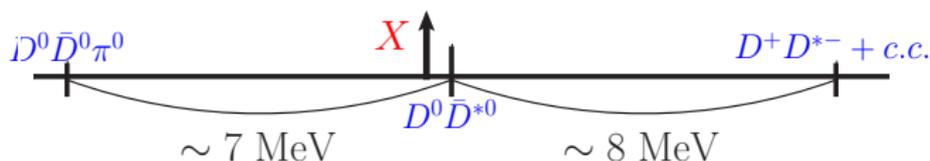
(BABAR 2008, Belle 2010/2011, LHCb 2014)

- $e^+e^- \rightarrow \gamma X(3872)$

(BESIII 2014)

Approach to $X(3872)$

- $X(3872)$ is a **shallow bound state** ($E_B \ll 1$ MeV) with a large admixture of the $D\bar{D}^*$ component in the w.f.
- The **short-range π component** of the w.f. is responsible for the $X(3872)$ **production at high energies**, for **radiative decays** and **decays to light hadrons**
- **Hadronic (long-range) component** is responsible for **open-charm decays**
- **Three-body ($D\bar{D}\pi$) dynamics** is important in $X(3872)$ because of a very specific ordering of thresholds



(Suzuki'2005, Fleming et al.'2007, Baru et al.'2011, Guo et al.'2014)

$X(3915)$

Experimental background (Belle & BaBar)

- **Seen** in $B \rightarrow KX \rightarrow K(\omega J/\psi)$ and $\gamma\gamma \rightarrow X \rightarrow \omega J/\psi$
- **Not seen** in $D\bar{D}$
- Belle: 0^{++} or 2^{++} ($\chi_{c0}(2P)$ or $\chi_{c2}(2P)$ charmonium?)
- BaBar: 2^{++} **ruled out** by angular analysis in $\omega J/\psi$ ($\chi_{c0}(2P)$?)
- **Good candidate** for $\chi_{c0}(2P)$ exists: $X^*(3860)$ (Belle'2017)

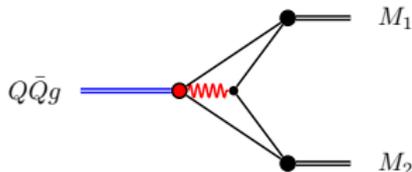
Theoretical insights

- $\chi_{c0}(2P)$ assignment for $X(3915)$ is **questionable**
(Guo&Meißner'2012,Olsen'2014,Zhou et al.'2015)
- 2^{++} ruled out for $\bar{c}c$ charmonium, not **for exotics**
(Liu et al.'2010)
- Current data **not compatible** with 2^{++} $D^*\bar{D}^*$ molecule
(Baru et al.'2017)
- 0^{++} $D_s\bar{D}_s$ molecule assignment is **plausible** \Leftarrow **To be verified**
(Li&Voloshin'2015)

The Y family

Y(4260)

- **Small** e^+e^- width, **dip** in R -ratio \implies **hybrid?**
 - Quantum numbers **OK** (vector hybrid)
 - Mass **OK** (compatible with lattice and models)
 - Decay modes **unclear yet**



Specific pattern of open-flavour decays **to be verified** in experiment

- Resides near S -wave $D_1\bar{D}$ threshold \implies **molecule?**
 - **Good description** of data in $J/\psi\pi\pi$, $h_c\pi\pi$ and $D\bar{D}^*\pi$ final states
 - **Natural explanation** of $Z_c(3900)$ appearance in $Y(4260)$ decays
 - **Confirmed prediction** of $e^+e^- \rightarrow \gamma X(3872)$ in energy region near $Y(4260)$

(Wang et al.'2013)

(Guo et al.'2013)

The Z family

$Z_c(3900)$

Experimental status:

- Quantum numbers: $J^{PC} = 1^{+-}$, $I = 1$
- Mass and width:

$$M = 3886.6 \pm 2.4 \text{ MeV} \quad \Gamma = 28.1 \pm 2.6 \text{ MeV}$$

- Observation modes: $J/\psi\pi$, $D\bar{D}^*$

Theoretical insights:

- **Cannot be $\bar{c}c$ state** — minimal quark contents **four-quark**
- Resides close to the **$D\bar{D}^*$ threshold** \implies **molecule?**
- Isovector **cousin** of $X(3872)$? (opposite C -parity)
- If confirmed to reside **above threshold**
 \implies Nontrivial **interplay** of different dynamics needed!

$Z_b(10610)$ & $Z_b(10650)$: Experimental status

- Quantum numbers: $J^{PC} = 1^{+-}$, $I = 1$
- Masses and widths:

$$M = 10607.2 \pm 2.0 \text{ MeV} \quad \Gamma = 18.4 \pm 2.4 \text{ MeV}$$

$$M = 10652.2 \pm 1.5 \text{ MeV} \quad \Gamma = 11.5 \pm 2.2 \text{ MeV}$$

- Production and decay modes:

$$\Upsilon(10860) \rightarrow \pi Z_b^{(\prime)} \rightarrow \pi B^{(*)} \bar{B}^*$$

$$\Upsilon(10860) \rightarrow \pi Z_b^{(\prime)} \rightarrow \pi\pi\Upsilon(nS) \quad n = 1, 2, 3$$

$$\Upsilon(10860) \rightarrow \pi Z_b^{(\prime)} \rightarrow \pi\pi h_b(mP) \quad m = 1, 2$$

- No suppression** from heavy quark spin flip

$$\text{BF}(\Upsilon(10860) \rightarrow h_b(mP)\pi\pi) \simeq \text{BF}(\Upsilon(10860) \rightarrow \Upsilon(nS)\pi\pi)$$

$Z_b(10610)$ & $Z_b(10650)$ as molecules

$m_b \gg \Lambda_{\text{QCD}} \implies$ Heavy Quark Spin Symmetry

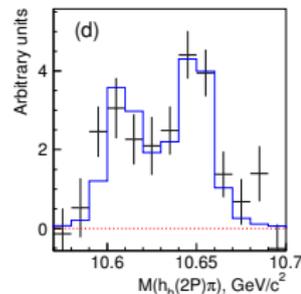
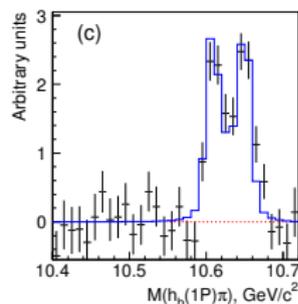
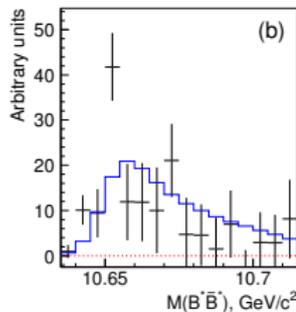
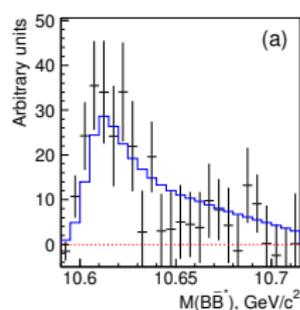
Molecule Z_b and Z'_b spin w.f.'s are ($B = 0_{\bar{b}q}^-$, $\bar{B} = 0_{\bar{q}b}^-$, $B^* = 1_{\bar{b}q}^-$, $\bar{B}^* = 1_{\bar{q}b}^-$)

$$|Z_b\rangle = \frac{1}{\sqrt{2}} \left[(1_{\bar{b}b}^- \otimes 0_{\bar{q}q}^-)_{S=1} + (0_{\bar{b}b}^- \otimes 1_{\bar{q}q}^-)_{S=1} \right]$$

$$|Z'_b\rangle = \frac{1}{\sqrt{2}} \left[(1_{\bar{b}b}^- \otimes 0_{\bar{q}q}^-)_{S=1} - (0_{\bar{b}b}^- \otimes 1_{\bar{q}q}^-)_{S=1} \right]$$

(Bondar et al.'2011)

Line shapes of the Z_b 's can be described well in the molecule picture



(Hanhart et al.'2015, Guo et al.'2016)

$Z_b(10610)$ & $Z_b(10650)$ as molecules

$m_b \gg \Lambda_{\text{QCD}} \implies$ Heavy Quark Spin Symmetry

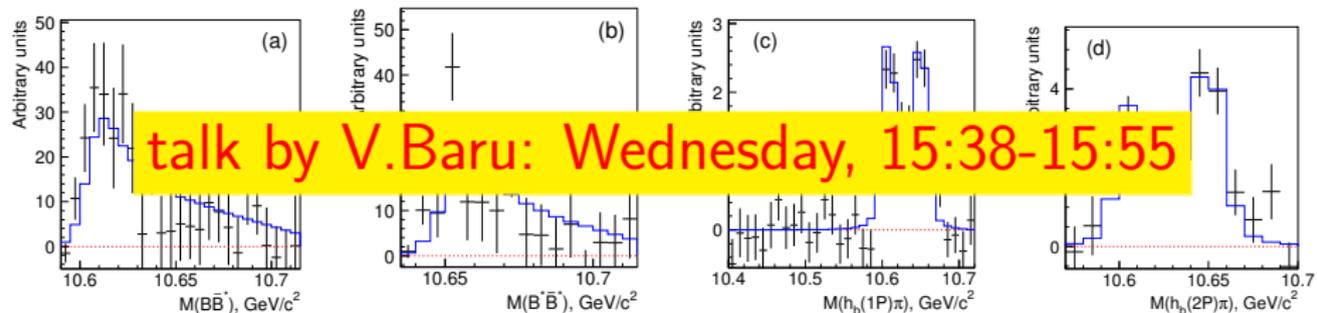
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(Hanhart et al.'2015, Guo et al.'2016)

Spin partners (c -sector)

$Y(4260) = D_1 \bar{D}$ molecule $\implies Y(4360) = D_1 \bar{D}^* / D_2 \bar{D}^*$ molecule

(Wang et al.'2013)

$Z_c(3900) = D \bar{D}^*$ molecule $\implies Z_c(4020) = D^* \bar{D}^*$ molecule

(Voloshin'2013)

$X(3872) = D \bar{D}^*$ molecule $\implies X_{c2} = D^* \bar{D}^*$ molecule

(Nieves&Valderrama'2012, Guo et al.'2013, Baru et al.'2016)

To be verified by...

- Investigating decay modes

$$Y(4260) \rightarrow D \bar{D}^* \pi, \pi \pi J/\psi$$

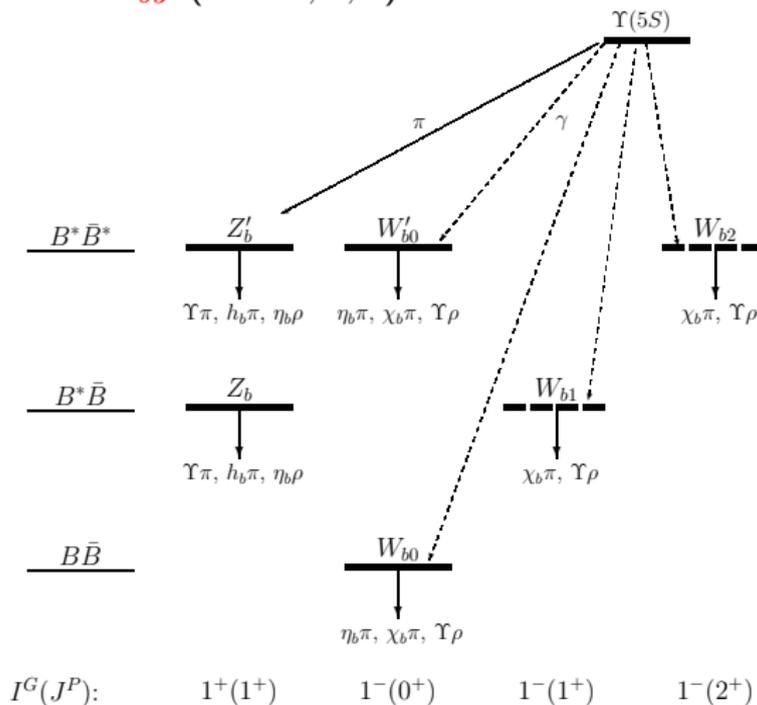
$$Y(4360) \rightarrow D^* \bar{D}^* \pi$$

$$Z_c(3900) \rightarrow D \bar{D}^*, \pi J/\psi, \pi \psi', \pi h_c, \rho \eta_c$$

- Building systematic theoretical approach to $D^{(*)} D_J$ molecules
- Investigating HQSS breaking effects in c -sector
- Investigating role of pions

Spin partners (b -sector)

Prediction of Heavy Quark Spin Symmetry: J^{++} spin partner
molecular states W_{bJ} ($J = 0, 1, 2$) should exist

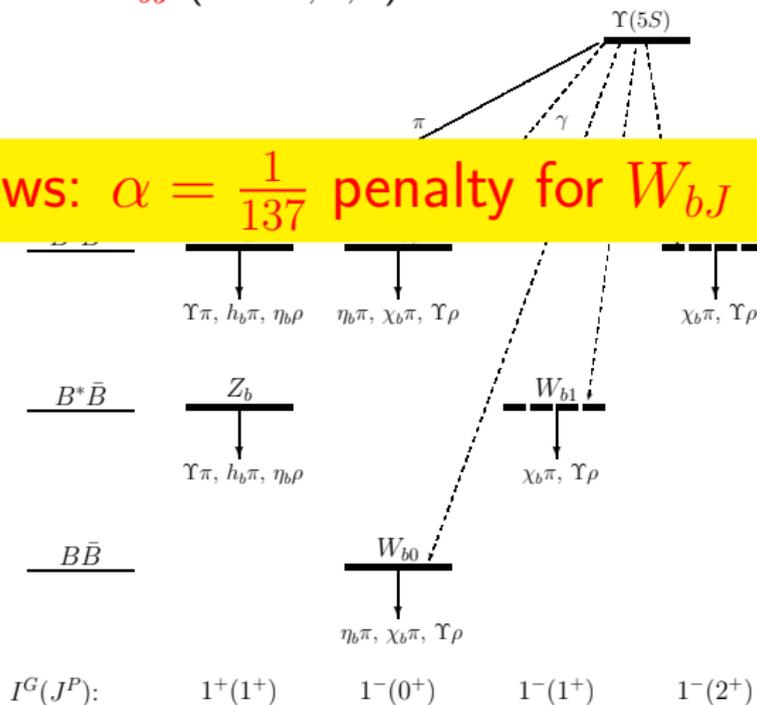


(Bondar et al.'2011, Voloshin'2011)

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Bad news: $\alpha = \frac{1}{137}$ penalty for W_{bJ} production



(Bondar et al.'2011, Voloshin'2011)

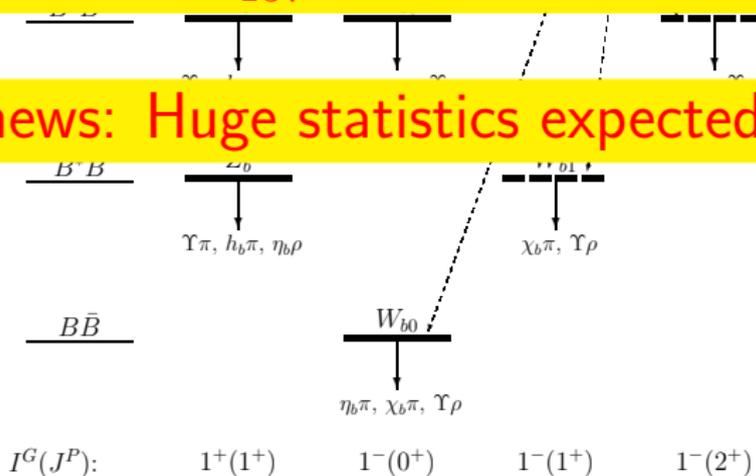
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molecular states W_{bJ} ($J = 0, 1, 2$) should exist



Bad news: $\alpha = \frac{1}{137}$ penalty for W_{bJ} production

Good news: Huge statistics expected at Belle-II



(Bondar et al.'2011, Voloshin'2011)

Conclusions

Molecule model is a **commonly accepted** and **phenomenologically successful** description of **exotic states**:

- Describes specific **line shapes**
- Predicts **spin partners**
- Explains **mass splittings**:

$$M_{Y(4260)} - M_{X(3872)} \approx M_{D_1(2420)} - M_{D^*}$$

$$M_{Z_b(10650)} - M_{Z_b(10610)} \approx M_{B^*} - M_B$$

Further developments:

- Relation between **different heavy-quark sectors**
- Proper inclusion of **pions** and **compact components**
- Generalisation to **$SU(3)$ flavour group** for light quarks
- Tests of **accuracy of HQSS**, especially in the **charm sector**