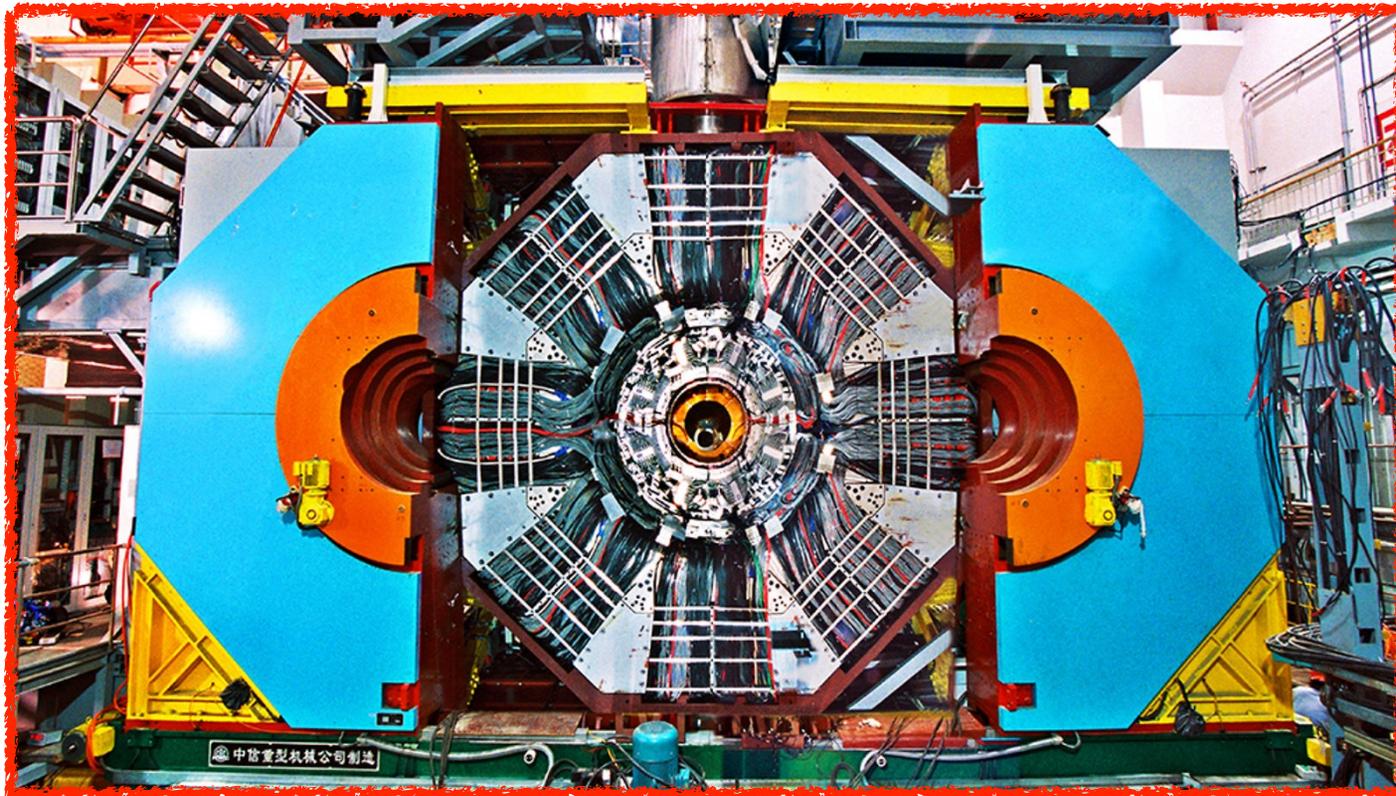


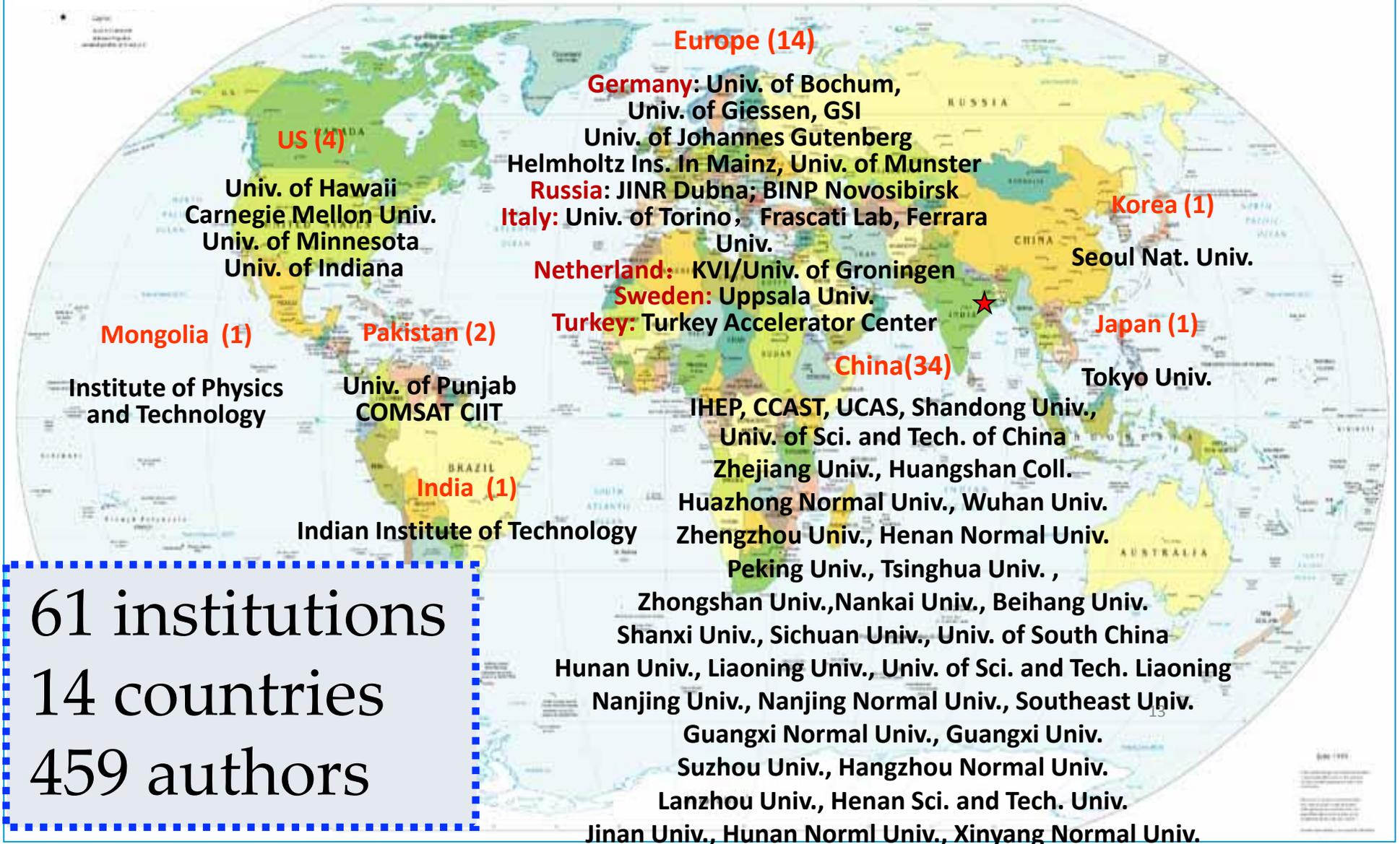
# Study of $D_s$ decays at **BESIII**



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**University of Minnesota**

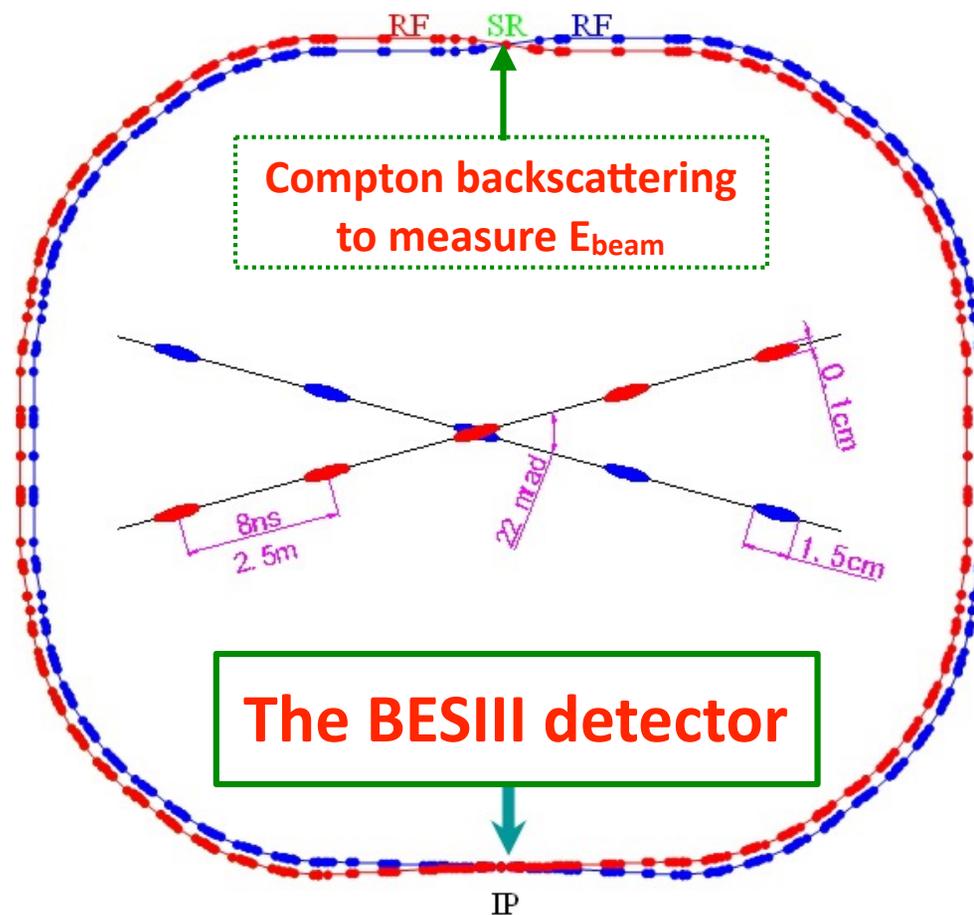
# Haji **The third generation of Beijing Spectrometer**

## BESIII Collaboration



# BEPC II (Beijing Electron-Positron Collider II)

- Double ring collider.
- Operating since 2008.
- $E_{\text{beam}} = 1\text{-}2.3\text{ GeV}$ .  
Optimal @ 1.89 GeV.



- Can fill up to 93 bunches in each ring w/ max current of 0.9A.
- Designed luminosity =  $1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$  was achieved in April 2016!

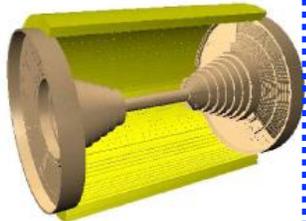
# BEPC II and BESIII



# BESIII detector

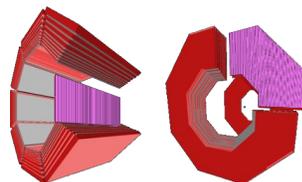
- A powerful general purpose detector.
- Excellent neutral/charged particle detection/identification with a large coverage.
  - ✓ Precision tracking
  - ✓ CsI calorimeter
  - ✓ PID via  $dE/dx$  & Time of Flight

MDC: small cell & Gas:  
He/C<sub>3</sub>H<sub>8</sub> (60/40), 43 layers  
 $\sigma_p/p=0.5\%$ @1GeV,  $\sigma_{dEdx}=6\%$

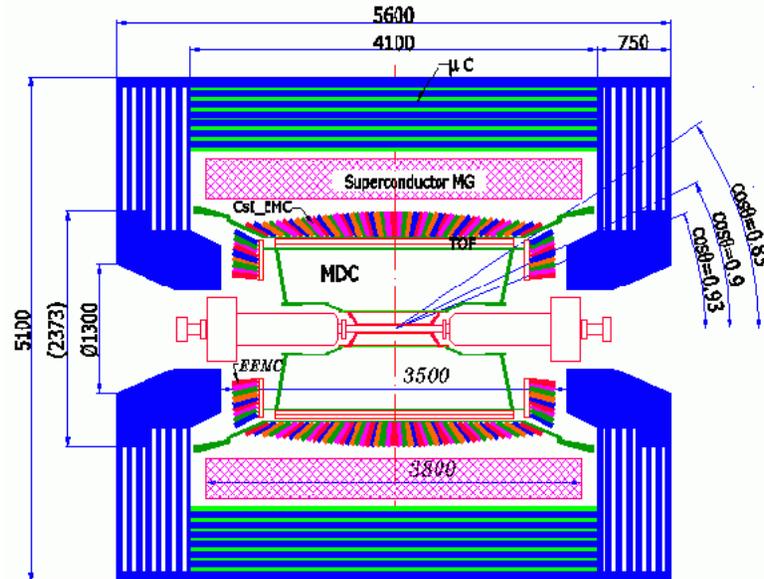


R inner: 63mm ;  
R outer: 810mm  
Length: 2582 mm  
Layers: 43

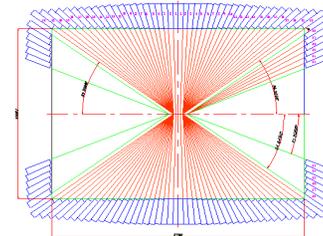
MUC: 9 layers RPC  
(8 layers in Endcap)  
 $\sigma_{R\Phi}=1.4\sim 1.7\text{cm}$



Magnet: 1T Super conducting



EMCAL: CsI(Tl) crystal  
 $\Delta E/E=2.5$  @1GeV



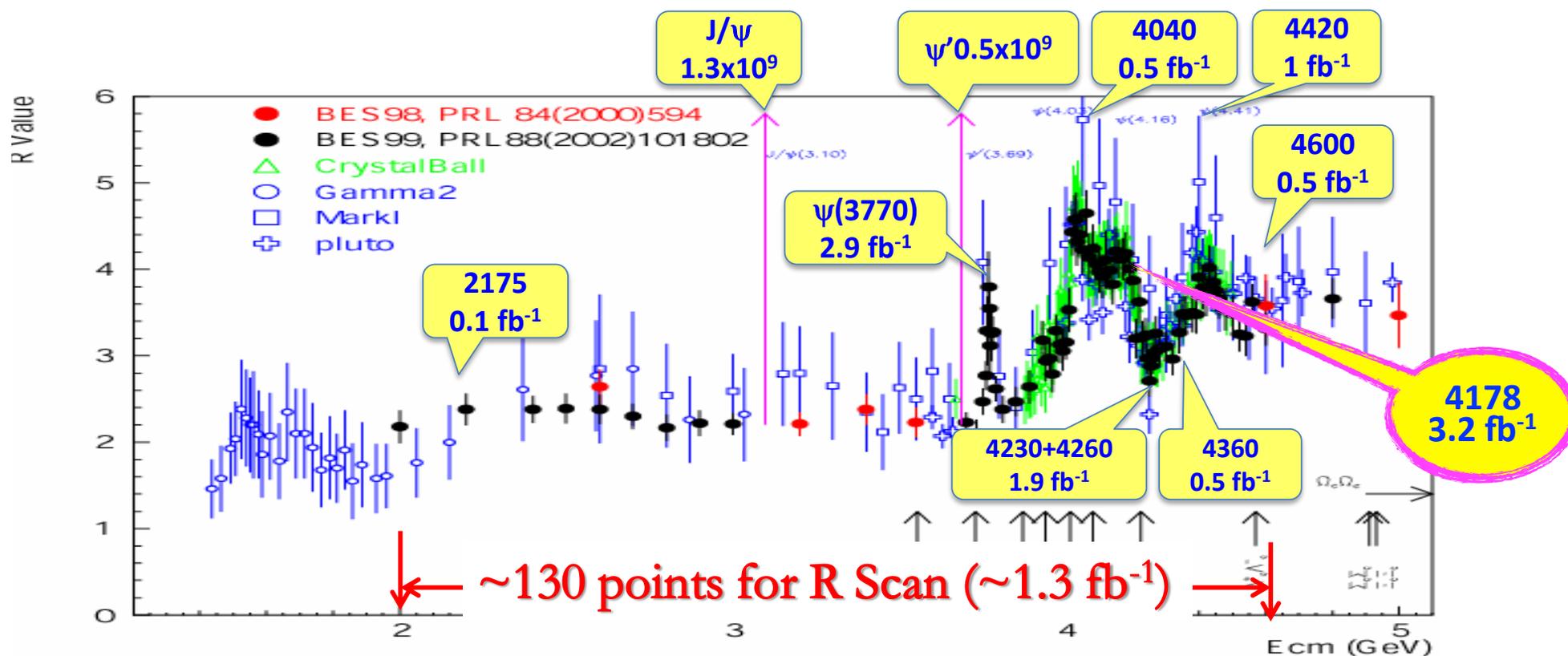
Crystals: 28 cm (15 X<sub>0</sub>)  
Barrel:  $|\cos\theta| < 0.83$   
Endcap:  
 $0.85 < |\cos\theta| < 0.93$

Time of Flight  
 $\sigma_T=100\text{ps}$  in Barrel  
 $110\text{ps}$  in Endcap

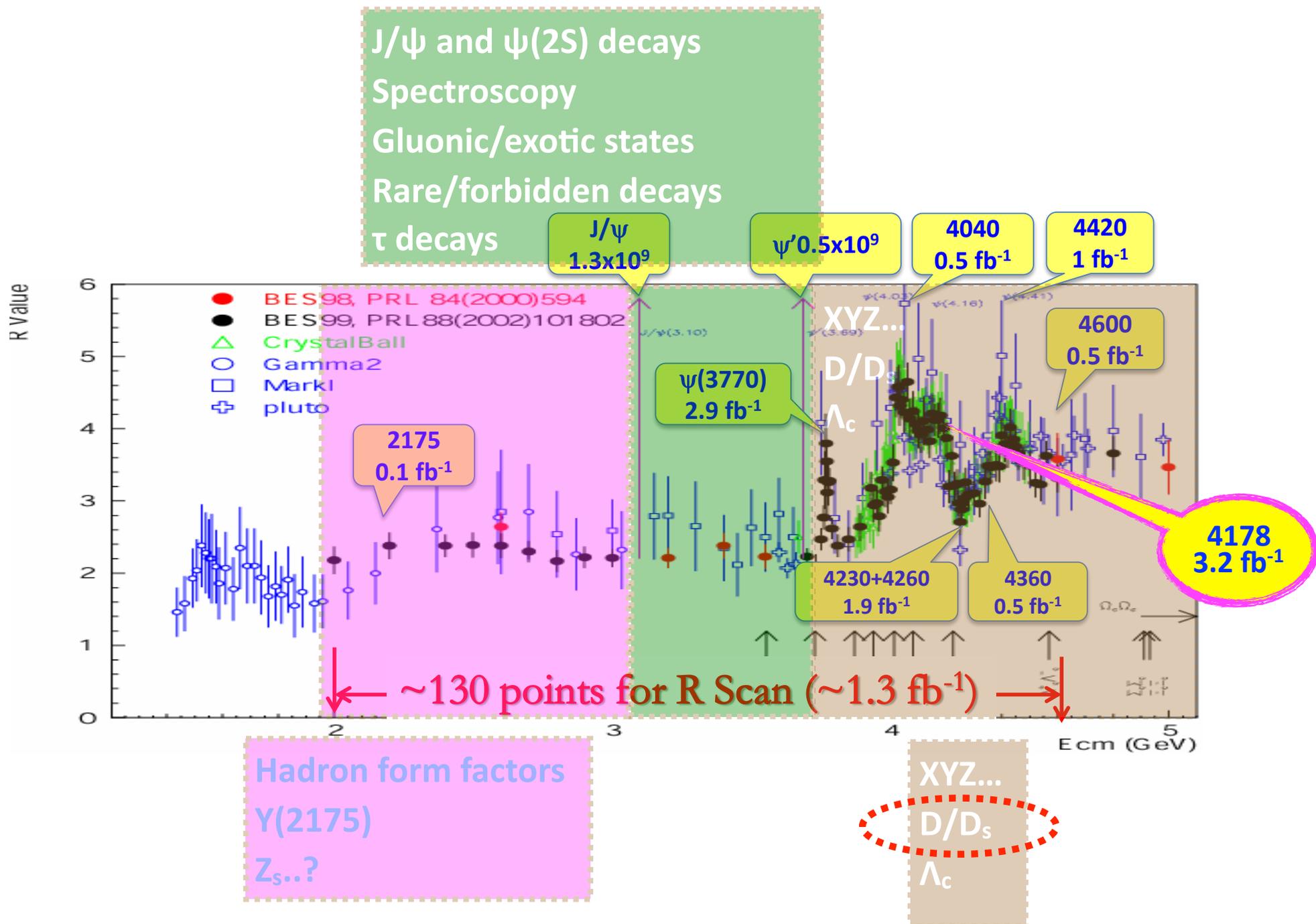
BTOF: two layers  
ETOF: 48 scintillators for each  
MRPC --- new ETOF



# $e^+e^-$ annihilation samples taken $E_{cm}$ from $\sim 2$ GeV up to $\sim 4.6$ GeV



World largest  $J/\psi$ ,  $\psi(2S)$ ,  $\psi(3770)$ ,  $\psi(4170)$ ,  
 $Y(4260)$ , ... produced directly from  $e^+e^-$  collision

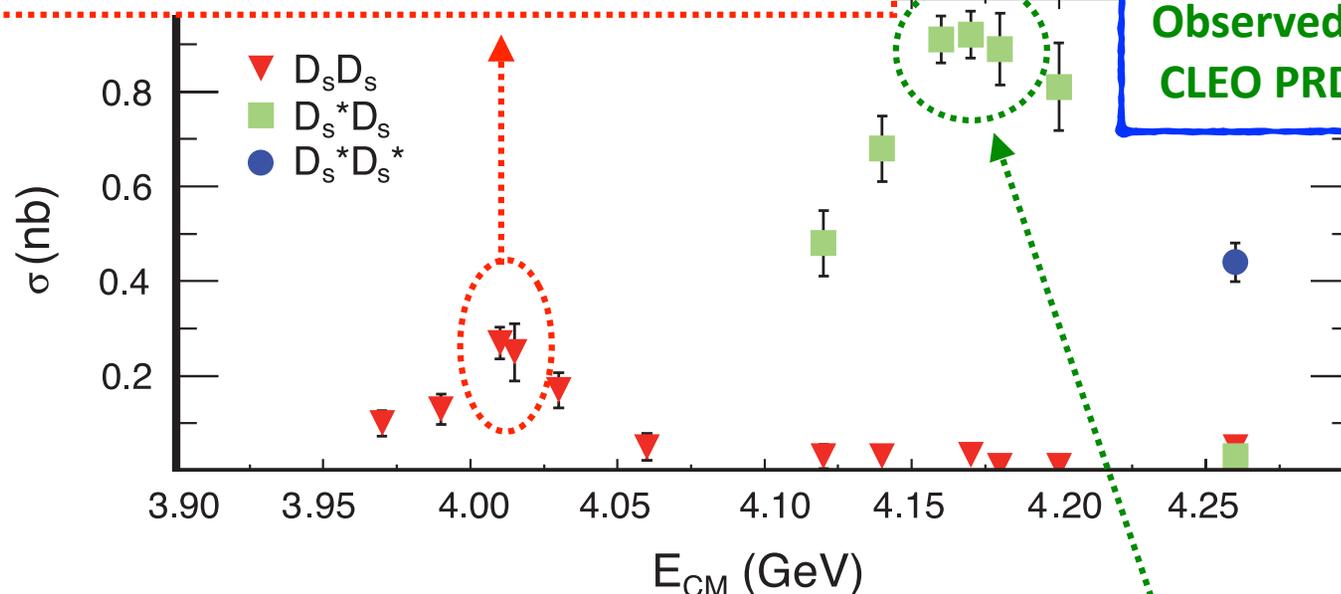


## Two main $D_s$ samples at BESIII

- $E_{\text{cm}} = 4009 \text{ MeV}$ :  $0.48 \text{ fb}^{-1}$  :  $\sim 0.3\text{M } D_s^\pm$  produced.
- $E_{\text{cm}} = 4178 \text{ MeV}$ :  $3.19 \text{ fb}^{-1}$  :  $\sim 6\text{M } D_s$  produced.

@ 4.009 GeV :  $e^+e^- \rightarrow D_s D_s$  produced, simple/clean.

But lower production rate.



Observed  $\sigma(e^+e^- \rightarrow D_s^{(*)} D_s^{(*)})$   
CLEO PRD80, 072001 (2009)

@ 4.178 GeV :  $e^+e^- \rightarrow D_s^* D_s$  produced w/  $\text{BF}(D_s^* \rightarrow \gamma D_s) \sim 94\%$ .  
But higher production rate.

## Typical analysis method to measure BF

- In our sample,  $D_s$  mesons are produced in pair:

@  $E_{\text{cm}} = 4009 \text{ MeV}$  :  $e^+e^- \rightarrow D_s^+D_s^-$

@  $E_{\text{cm}} = 4178 \text{ MeV}$  :  $e^+e^- \rightarrow D_s^{*+}D_s^-$ ,  $D_s^{*+} \rightarrow (\gamma/\pi^0)D_s^+$  (+ c.c.)

- Reconstruct one of the  $D_s$  (tag),

you know there must be the other  $D_s$  (signal),

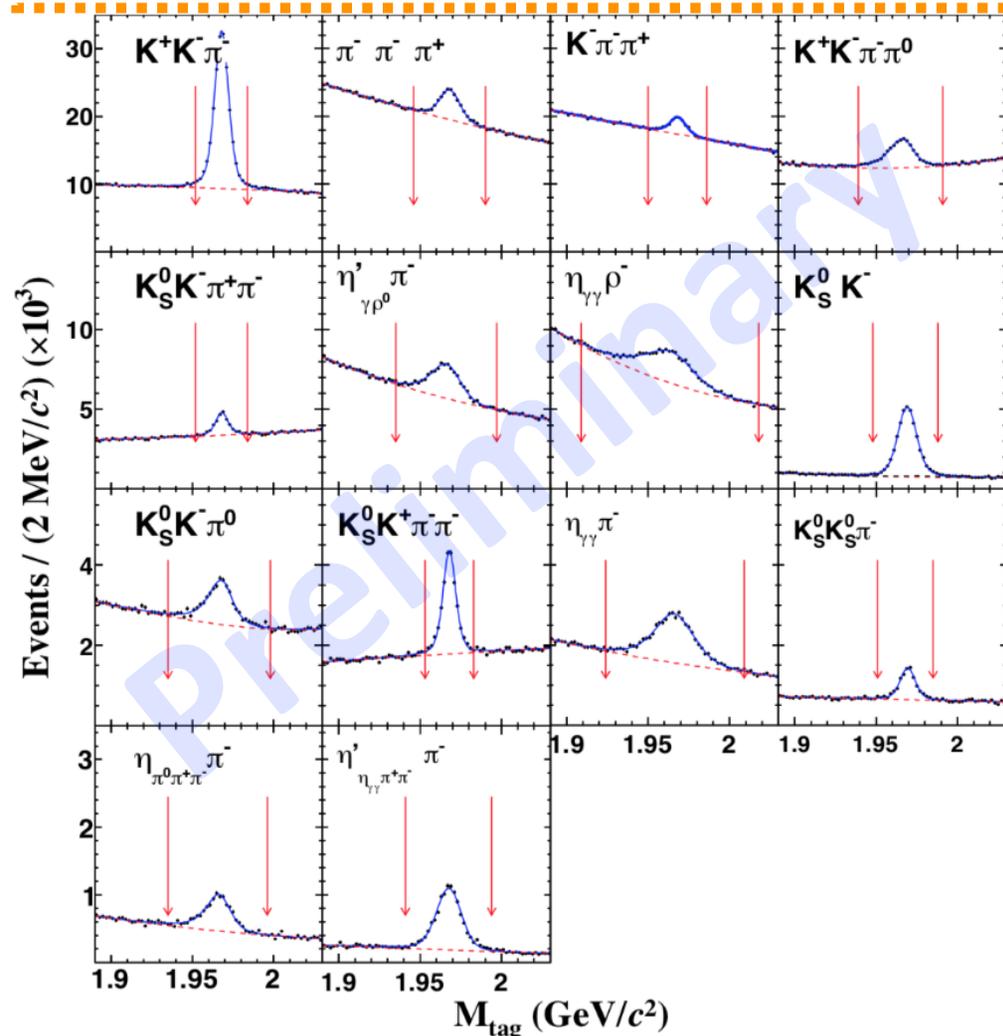
allowing measurements of absolute BFs.

$$\begin{aligned} \text{I.e., } \text{BF}(D_s \rightarrow \mu\nu) &= [\text{B}(D_s \rightarrow \text{tag}) \times \text{BF}(D_s \rightarrow \mu\nu)] / \text{BF}(D_s \rightarrow \text{tag}) \\ &= [\text{Double Tag yields}] / [\text{Single Tag yields}]. \end{aligned}$$

Systematics associated with the reconstruction of  $D_s \rightarrow \text{tag}$  also tend to be canceled in this ratio.

# Typical analysis method continued

Total  $D_s$  single-tag yield  $\sim 0.4M$  events



To obtain **Single Tag yields**, we fit to:

- $M_{bc} = \sqrt{(E_{beam})^2 - |\vec{p}_D|^2}$  in the 4009 sample
  - $M_{inv}(D_s)$  in the 4178 sample.
- Shown here as an example.

To obtain **Double Tag yields**, we fit to:

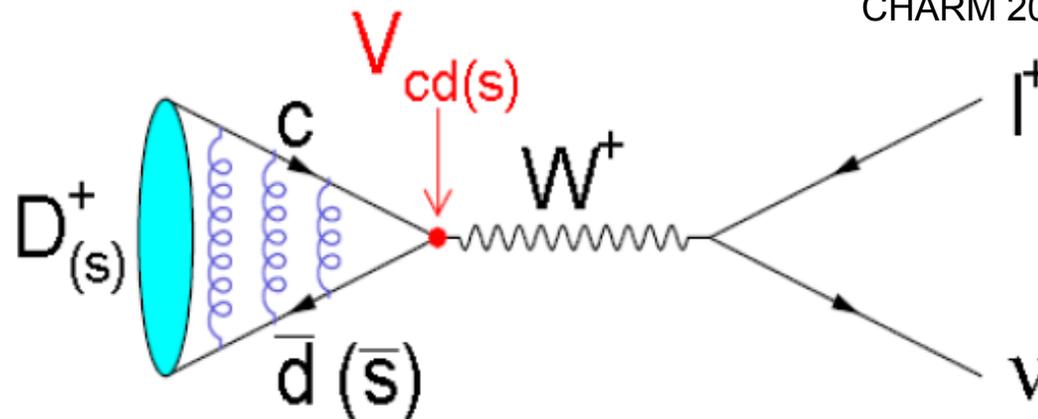
- Select signal region in  $M_{inv}(D_s)$  (red arrows in the left plot).
- Look at their recoil sides.

If a missing particle (e.g.,  $\nu$  or  $n$ ), use missing mass-squared;

$$\begin{aligned}
 MM^2 &= E_{miss}^2 - |\vec{p}_{miss}|^2 \\
 &= (E_{cm} - E_{tag} - E_l)^2 - |-\vec{p}_{tag} - \vec{p}_l|^2
 \end{aligned}$$

which peaks @ 0 if a  $\nu$  is missing.

# Pureleptonic decays



To the lowest order;

$$\Gamma(D_{(s)}^+ \rightarrow l^+ \nu) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_l^2 m_{D_{(s)}^+} \left(1 - \frac{m_l^2}{m_{D_{(s)}^+}^2}\right)^2$$

-The decay rate goes as  $f_{D(s)}^2 \times |V_{cd(s)}|^2$ .

The game is to measure the BF, and then

- ▶ use the CKM elements predicted by unitarity to obtain experimental values for  $f_{D(s)}$ .

This provides tests of lattice QCD methods under the assumption that new-physics contributions to leptonic decays can be neglected, or

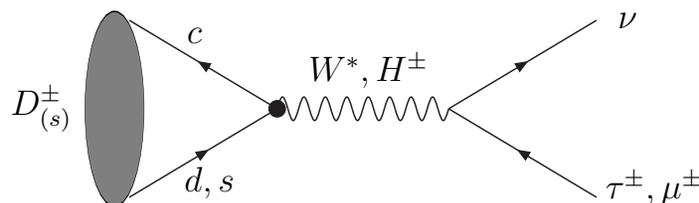
- ▶ or  $f_{D(s)}$  predicted by lattice QCD to determine elements of CKM elements.

Also, ratio of the decay rates between  $D_{(s)} \rightarrow \mu\nu$  and  $D_{(s)} \rightarrow \tau\nu$  are very interesting!  
For instance;

$$R \equiv \frac{\Gamma(D_s^+ \rightarrow \tau^+ \nu)}{\Gamma(D_s^+ \rightarrow \mu^+ \nu)} = \frac{m_{\tau^+}^2 \left(1 - \frac{m_{\tau^+}^2}{M_{D_s^+}^2}\right)^2}{m_{\mu^+}^2 \left(1 - \frac{m_{\mu^+}^2}{M_{D_s^+}^2}\right)^2}$$

- With the known masses,  $R_{D_{s^+}} = 9.74 \pm 0.01$ .  
Allows us to check lepton universality!
- Any deviation from the expected R could indicate non-SM effects.

## Speaking of R and lepton universality



- In certain models, such as the two-Higgs-doublet, the lepton universality still holds

I.e., A.G. Akeroyd et. al. (PRD75,075004(2007));

For the case of  $D_s$ , the SM rate is modified by a factor of

$$r_{D_s} \equiv \left[ 1 + \left( \frac{1}{m_c + m_s} \right) \left( \frac{M_{D_s}}{m_{H^\pm}} \right)^2 \left( m_c - \frac{m_s \tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right) \right]^2, \text{ where}$$

$\epsilon_0$  is a higher order correction (= 0 @ tree level).

- This only affects the absolute rates:

E.g., for  $D_s \rightarrow \mu\nu$ ,

$$\text{BF}_{\text{exp}} = \Gamma_{\text{SM}} \times \tau_{D_s} \times r_{D_s} = (5.28 \pm 0.05) \times 10^{-3} \times r_{D_s},$$

where  $f = 249.0 \pm 1.2$  MeV and  $|V_{cs}| = 0.973394$  are used.

The uncertainty is dominated by the  $D_s$  lifetime.

# Experimental status on $D_s^+$ pure leptonic decays and advantage of data taken @ mass threshold

▾  $\Gamma(D_s^+ \rightarrow \mu^+ \nu_\mu) / \Gamma_{\text{total}}$

CLEO/BESIII : statistically limited

Belle/BaBar :  $\Delta_{\text{stat.}} \sim \Delta_{\text{system.}}$  or Systematically limited

| VALUE ( $10^{-3}$ ) | EVTS               | DOCUMENT ID       | TECN       | COMMENT                    |
|---------------------|--------------------|-------------------|------------|----------------------------|
| <b>5.50 ± 0.23</b>  | <b>OUR AVERAGE</b> |                   |            |                            |
| 4.95 ± 0.67 ± 0.26  | 69                 | 1 ABLIKIM         | 2016O BES3 | $e^+e^-$ at 4.009 GeV      |
| 5.31 ± 0.28 ± 0.20  | 492 ± 26           | 2 ZUPANC          | 2013 BELL  | $e^+e^-$ at $Y(4S), Y(5S)$ |
| 6.02 ± 0.38 ± 0.34  | 275 ± 17           | 3 DEL-AMO-SANCH.. | 2010J BABR | $e^+e^-$ , 10.58 GeV       |
| 5.65 ± 0.45 ± 0.17  | 235 ± 14           | ALEXANDER         | 2009 CLEO  | $e^+e^-$ at 4170 MeV       |

CLEO :  $\mu\nu$  : Systematically most precise : Rel. syst. error = 3%  
Our MC study showed  $\sim 3 \text{ fb}^{-1}$  would give us  $\sim 3\%$  stat. error

▾  $\Gamma(D_s^+ \rightarrow \tau^+ \nu_\tau) / \Gamma_{\text{total}}$

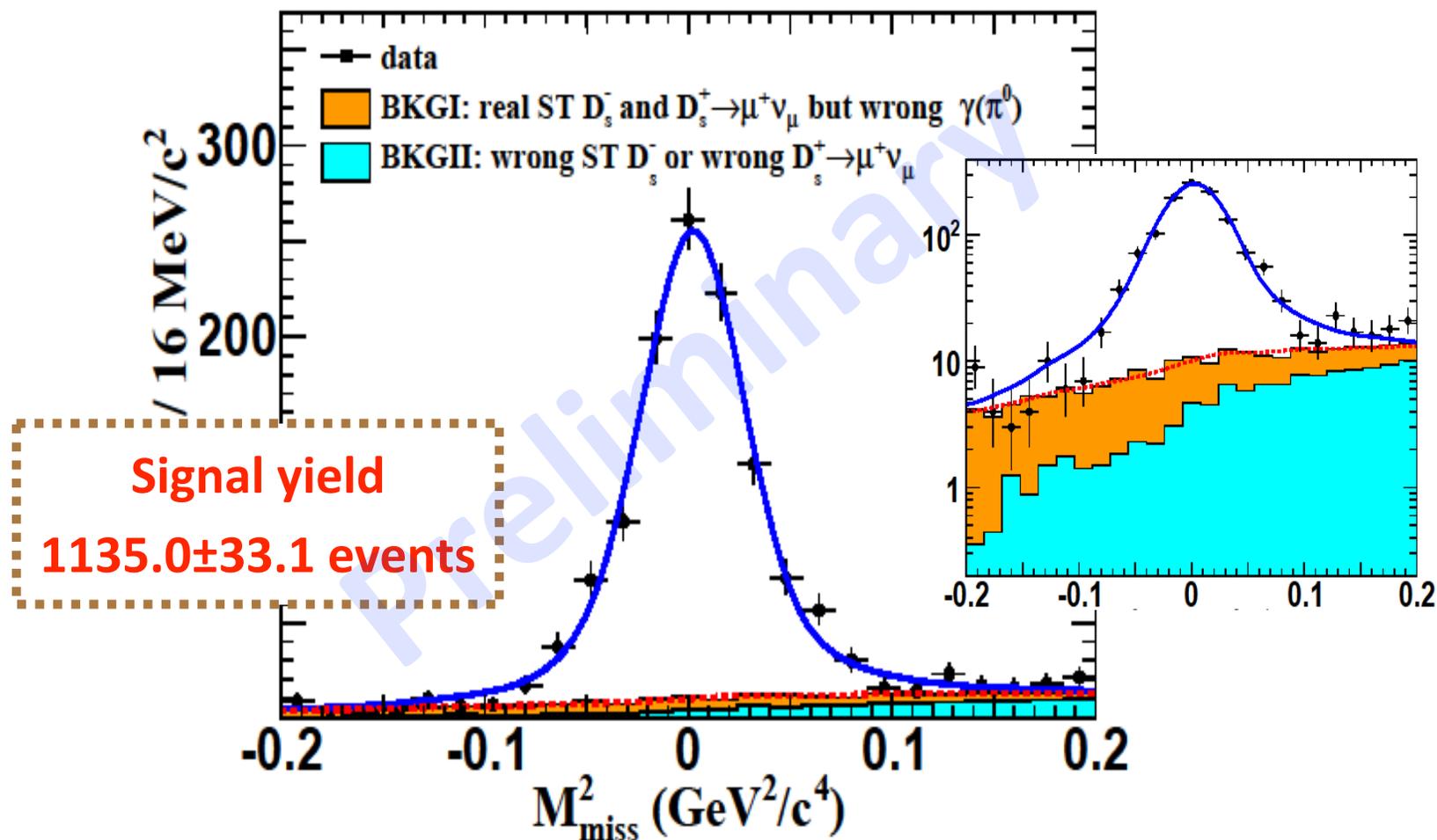
| VALUE ( $10^{-2}$ )            | EVTS               | DOCUMENT ID       | TECN       | COMMENT  |
|--------------------------------|--------------------|-------------------|------------|--|
| <b>5.48 ± 0.23</b>             | <b>OUR AVERAGE</b> |                   |            |  |
| 4.83 ± 0.65 ± 0.26             | 33                 | 1 ABLIKIM         | 2016O BES3 | $e^+e^-$ at 4.009 GeV                                    |
| 5.70 ± 0.21 $^{+0.31}_{-0.30}$ | 2.2k               | 2 ZUPANC          | 2013 BELL  | $e^+e^-$ at $Y(4S), Y(5S)$                               |
| 4.96 ± 0.37 ± 0.57             | 748 ± 53           | 3 DEL-AMO-SANCH.. | 2010J BABR | $e^- \bar{\nu}_e \nu_\tau, \mu^- \bar{\nu}_\mu \nu_\tau$ |
| 6.42 ± 0.81 ± 0.18             | 126 ± 16           | 4 ALEXANDER       | 2009 CLEO  | $\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau$                |
| 5.52 ± 0.57 ± 0.21             | 155 ± 17           | 4 NAIK            | 2009A CLEO | $\tau^+ \rightarrow \rho^+ \bar{\nu}_\tau$               |
| 5.30 ± 0.47 ± 0.22             | 181 ± 16           | 4 ONYISI          | 2009 CLEO  | $\tau^+ \rightarrow e^+ \nu_e \bar{\nu}_\tau$            |

$$D_s^+ \rightarrow \mu^+ \nu_\mu$$

based on the 4178 data

- Demanding the track penetrate deep in MUC

→ Suppress backgrounds effectively, including  $D_s^+ \rightarrow \tau^+(\rightarrow \pi^+ \bar{\nu}_\tau) \nu_\tau$ .



- Preliminary result:

$$\text{BF}(D_s \rightarrow \mu \nu_\mu) = (5.28 \pm 0.15_{\text{stat}} \pm 0.14_{\text{syst}}) \times 10^{-3}.$$

Consistent with other existing results.

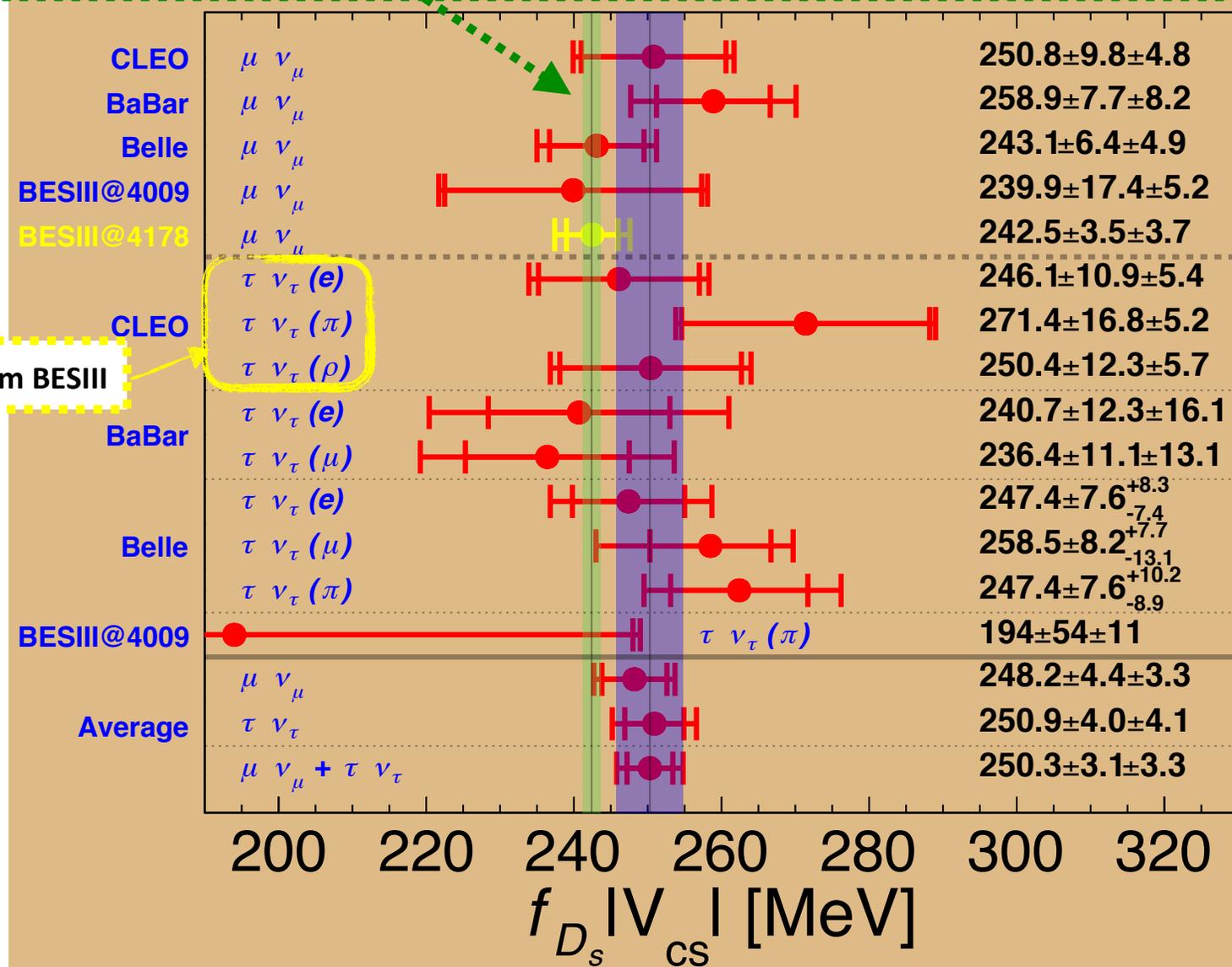
But most precise single measurement.

▼  $\Gamma(D_s^+ \rightarrow \mu^+ \nu_\mu) / \Gamma_{\text{total}}$

$\Gamma_{20}/\Gamma$

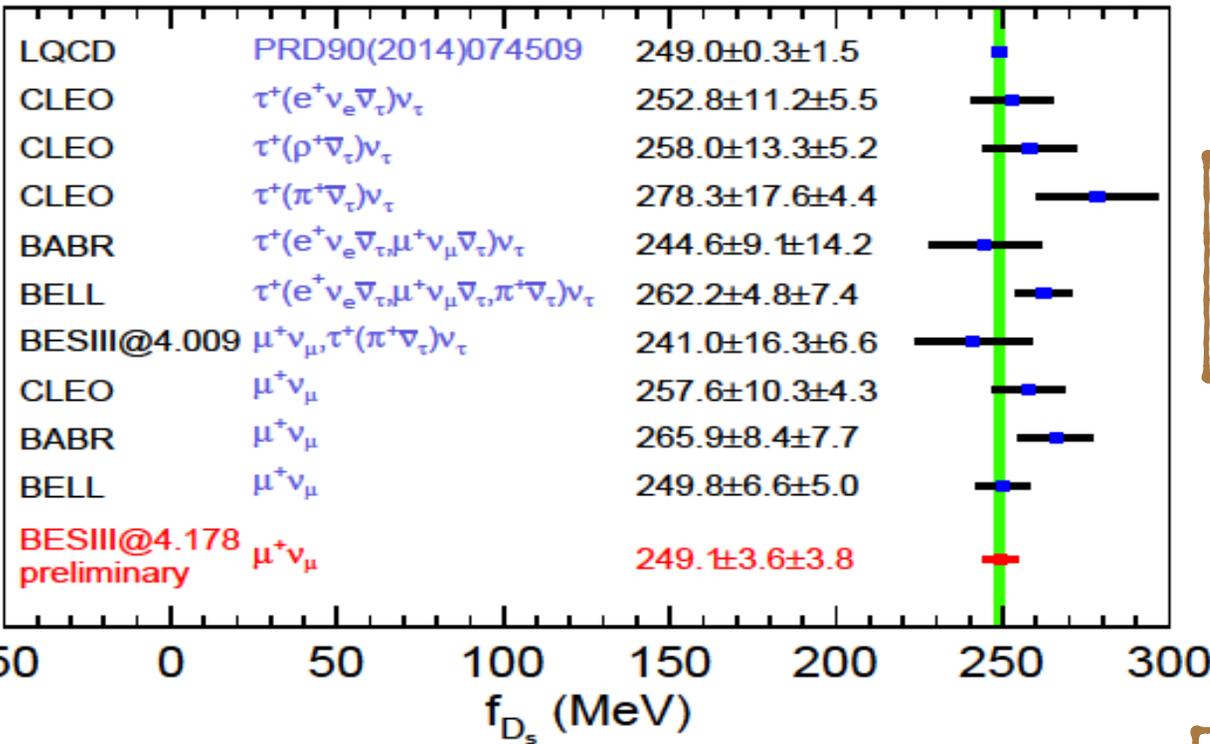
| VALUE ( $10^{-3}$ )   | EVTS               | DOCUMENT ID       | TECN  | COMMENT                               |
|---|--------------------|-------------------|-------|---------------------------------------|
| <b>5.50 ± 0.23</b>  | <b>OUR AVERAGE</b> |                   |       |                                       |
| 4.95 ± 0.67 ± 0.26  | 69                 | 1 ABLIKIM         | 2016O | BES3<br>$e^+e^-$ at 4.009 GeV         |
| 5.31 ± 0.28 ± 0.20  | 492 ± 26           | 2 ZUPANC          | 2013  | BELL<br>$e^+e^-$ at $Y(4S)$ , $Y(5S)$ |
| 6.02 ± 0.38 ± 0.34  | 275 ± 17           | 3 DEL-AMO-SANCH.. | 2010J | BABR<br>$e^+e^-$ , 10.58 GeV          |
| 5.65 ± 0.45 ± 0.17  | 235 ± 14           | ALEXANDER         | 2009  | CLEO<br>$e^+e^-$ at 4170 MeV          |
| ••• We do not use the following data for averages, fits, limits, etc. ••• |                    |                   |       |                                       |
| 6.44 ± 0.76 ± 0.57  | 169 ± 18           | 4 WIDHALM         | 2008  | BELL<br>See ZUPANC 2013               |
| 5.94 ± 0.66 ± 0.31  | 88                 | 5 PEDLAR          | 2007A | CLEO<br>See ALEXANDER 2009            |
| 6.8 ± 1.1 ± 1.8   | 553                | 6 HEISTER         | 2002I | ALEP<br>Z decays                      |

With  $f_{D_s} = 249.0 \pm 1.2$  MeV (From Rosner and Stone, PDG 2016 mini-review)  
 and  $|V_{cs}| = 0.973394^{+0.000074}_{-0.000096}$  from CKM-fitter (2015)

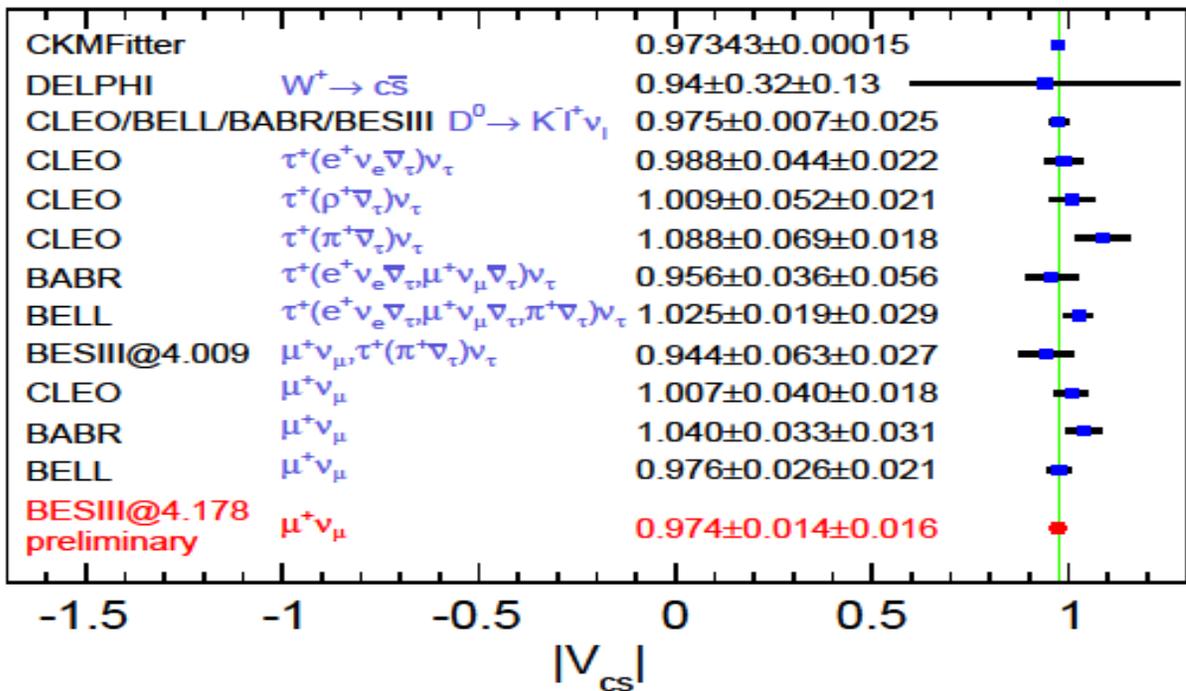


Consistent within  $1.7\sigma$  w/OUT the new BESIII measurement.

It will be interesting to revisit this once we have the “ $\tau\nu$ ” measurements from BESIII!!



- Taking  $|V_{cs}|^{CKMfitter}$  as an input, we have  
 $f_{D_s} = 249.1 \pm 3.6 \pm 3.8$  MeV.



- Taking  $f_{D_s}$  (LQCD;PRD90,074509) as an input, we have  
 $|V_{cs}| = 0.974 \pm 0.014 \pm 0.016$ .

- Our preliminary result on  $D^0 \rightarrow K^- \mu v$ , with a help of  $f_{D^K}(0)$  (LQCD;PRD82,114506), also gives a consistent result;  
 $|V_{cs}| = 0.9569 \pm 0.0051 \pm 0.0241$ .  
 Here, statistically superior, but suffered by the uncertainties from FFs as in all SL analyses.

## and the R

Taking the weighted average between our preliminary result of  $\text{BF}(D_s \rightarrow \mu \nu_\mu)$  and the current PDG average gives  $\text{BF}(D_s \rightarrow \mu \nu_\mu) = (5.38 \pm 0.15) \times 10^{-3}$ .

With the current PDG average of  $\text{BF}(D_s \rightarrow \tau \nu_\tau)$ , we have

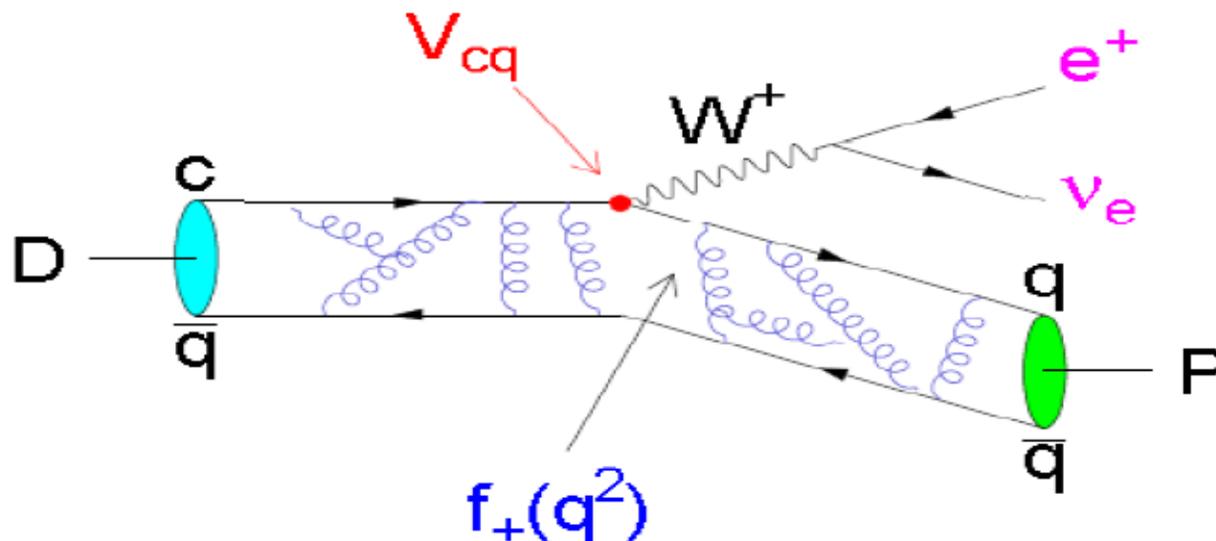
$$R \equiv \frac{\Gamma(D_s^+ \rightarrow \tau^+ \nu)}{\Gamma(D_s^+ \rightarrow \mu^+ \nu)} = \frac{m_{\tau^+}^2 \left(1 - \frac{m_{\tau^+}^2}{M_{D_s^+}^2}\right)^2}{m_{\mu^+}^2 \left(1 - \frac{m_{\mu^+}^2}{M_{D_s^+}^2}\right)^2}$$

**= 10.2 ± 0.5.**

Consistent with the expectation,  $9.74 \pm 0.01$  at  $0.9\sigma$ .

We should also improve  $\text{BF}(D_s \rightarrow \tau \nu_\tau)$  soon...

# Semileptonic decays



$$\frac{d\Gamma}{dq^2} = \frac{G_F^2 p^3}{24\pi^3} |f_+(q^2)|^2 |V_{cd(s)}|^2$$

- The differential decay rate goes as  $|f_+(q^2)|^2 \times |V_{cd(s)}|^2$ .
- Still, the game is to measure the BF, and then
  - ▶ use the CKM elements predicted by unitarity to obtain experimental values for  $f_+(q^2=0)$ .
  - ▶ or  $f_+(q^2=0)$  predicted by lattice QCD to determine elements of CKM elements.

# Some popular parametrization of form factors

## - Simple pole:

$$f_+(q^2) = \frac{f_+(0)}{1 - q^2/M_{\text{pole}}^2}$$

## - Modified pole:

$$f_+(q^2) = \frac{f_+(0)}{\left(1 - \frac{q^2}{M_{\text{pole}}^2}\right) \left(1 - \alpha \frac{q^2}{M_{\text{pole}}^2}\right)}$$

## - ISGW2:

$$f_+(q^2) = f_+(q_{\text{max}}^2) \left(1 + \frac{r^2}{12} (q_{\text{max}}^2 - q^2)\right)^{-2}$$

## - Series expansion:

$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

**$D_s \rightarrow \eta (\eta') e \nu$**   
**based on the 4178 data**

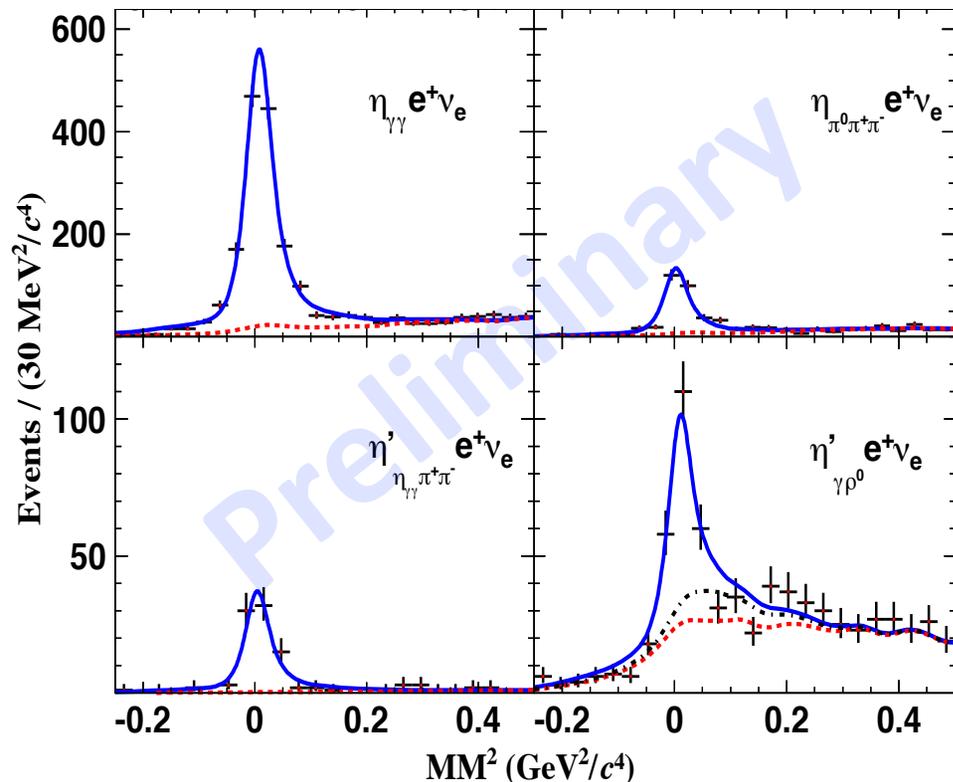
**Allows us to:**

- **extract  $f_+^{\eta(\prime)}(0)$  and compare to LQCD prediction ... for the 1st time!**
- **extract  $|V_{cs}|$ !**
- **extract the mixing angle between  $\eta$  and  $\eta'$  (C. Di Donato et al. PRD 85, 013016 (2012));**

$$\begin{pmatrix} |\eta\rangle \\ |\eta'\rangle \end{pmatrix} = \begin{pmatrix} \cos\phi_P & -\sin\phi_P \\ \sin\phi_P & \cos\phi_P \end{pmatrix} \begin{pmatrix} |\eta_q\rangle \\ |\eta_s\rangle \end{pmatrix}$$

$$\frac{\Gamma(D_s^+ \rightarrow \eta' e^+ \nu) / \Gamma(D_s^+ \rightarrow \eta e^+ \nu)}{\Gamma(D^+ \rightarrow \eta' e^+ \nu) / \Gamma(D^+ \rightarrow \eta e^+ \nu)} \simeq \cot^4 \phi_P,$$

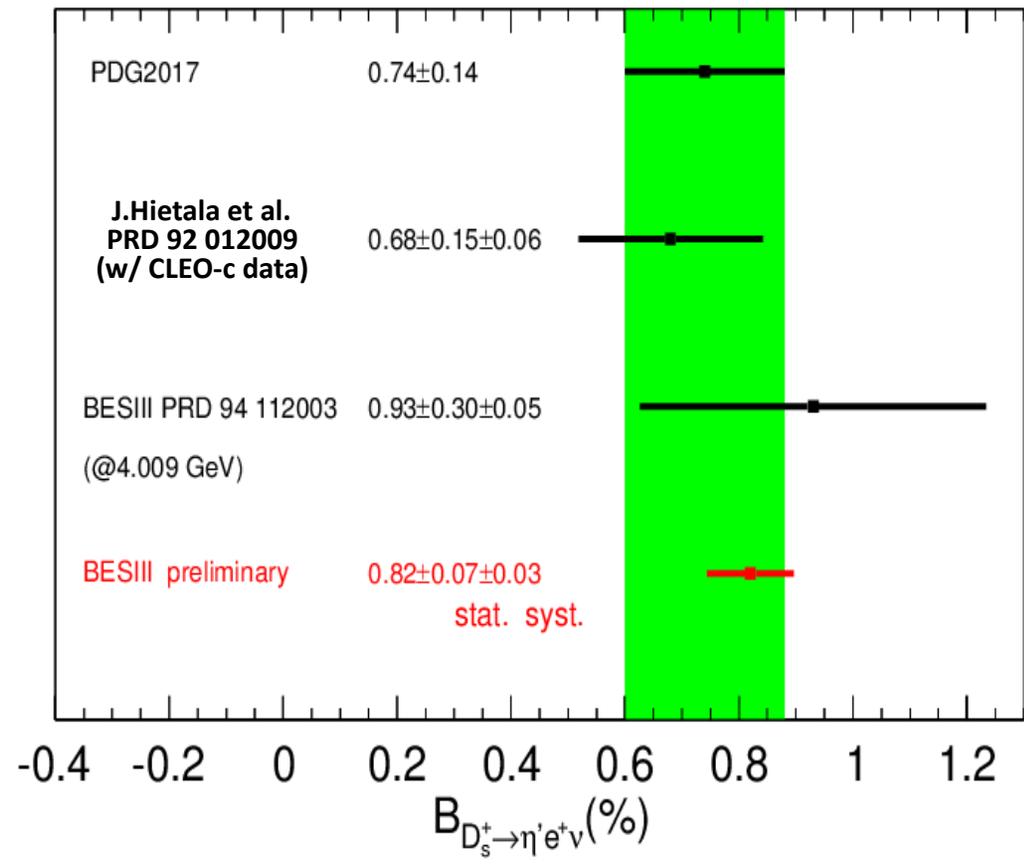
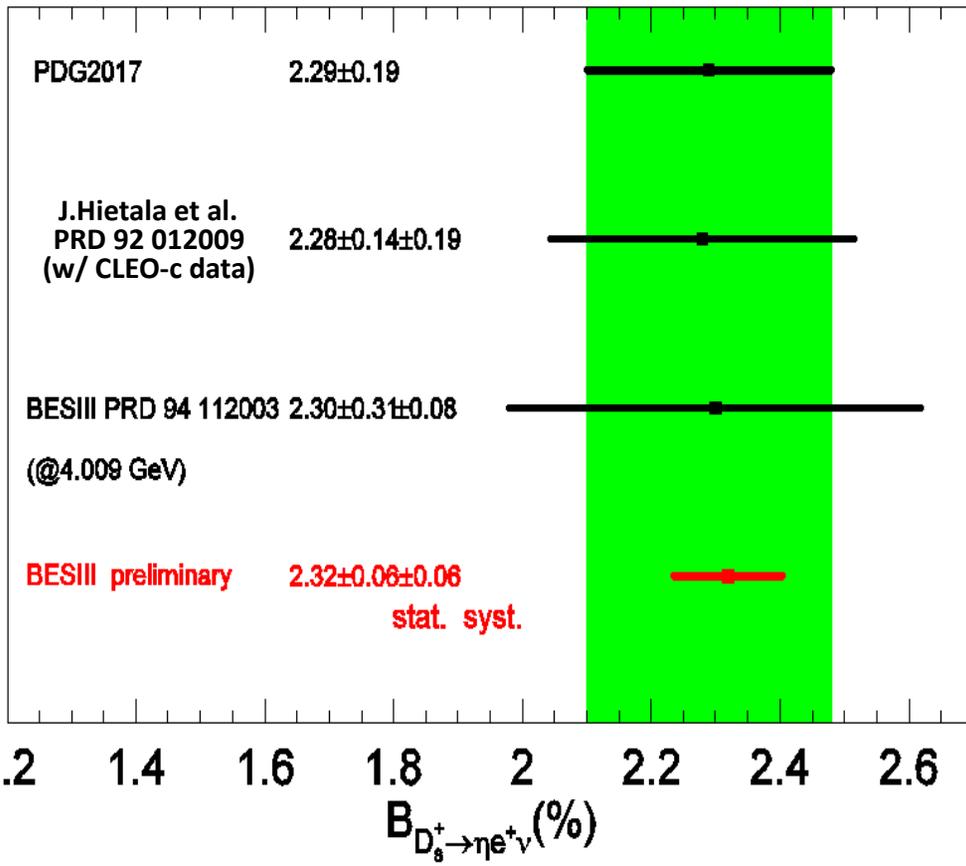
**assuming the phase space and form factors cancel in the ratios between D and  $D_s$ .**



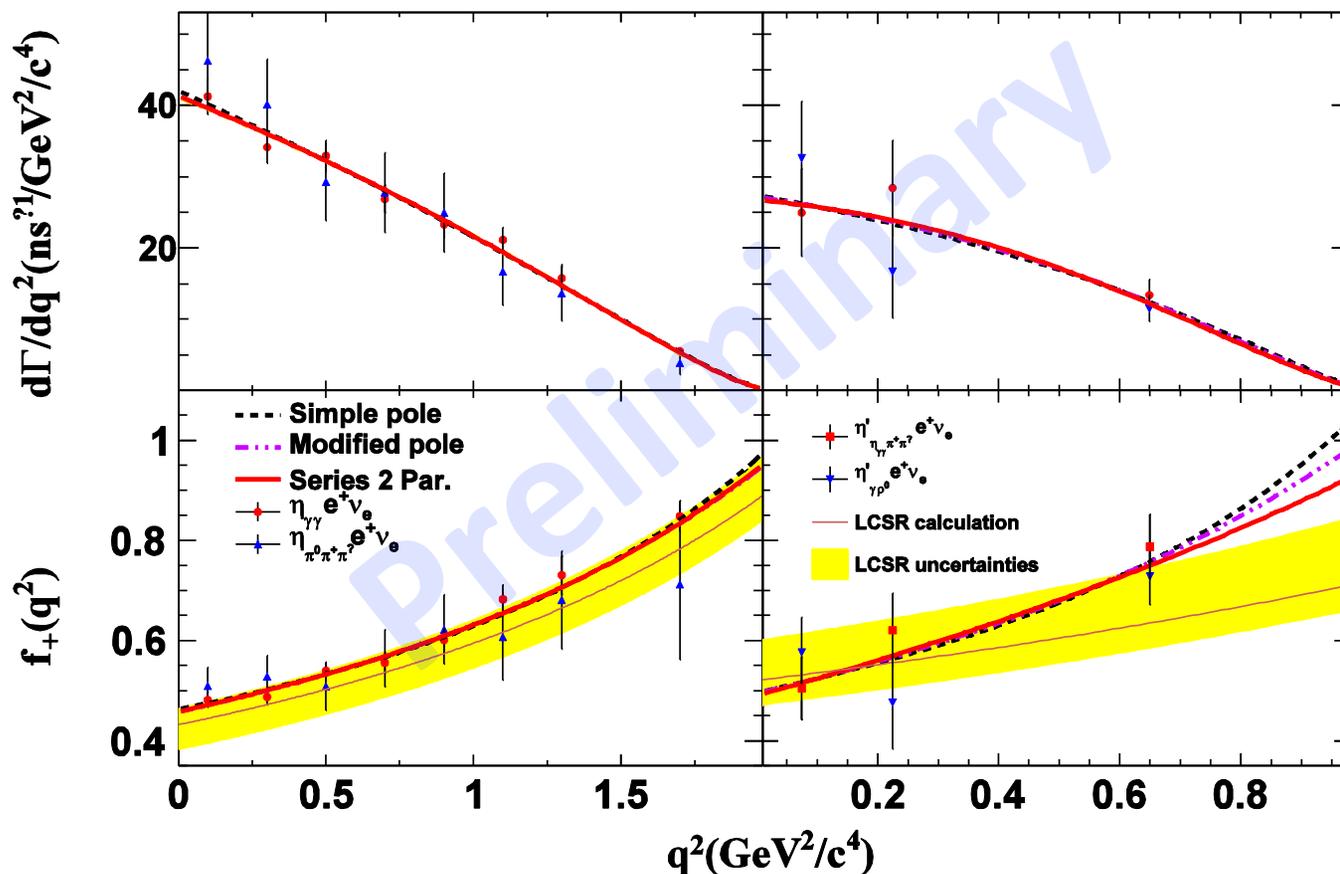
- **Detect:**
  - ▶ tag side (14 different decay modes).
  - ▶ the trans. photon from  $D_s^* \rightarrow \gamma D_s$ .
  - ▶  $\eta \rightarrow \gamma\gamma$  and  $\pi^+\pi^-\pi^0$ .
  - ▶  $\eta' \rightarrow \pi^+\pi^-\eta_{\gamma\gamma}$  and  $\gamma\rho$ .
- Yields are extracted from MM2.
- Fit to the two different final states simultaneously.

| Decay             | $\eta^{(\prime)}$ decay | $\epsilon_{\gamma(\pi^0)\text{SL}}$ (%) | $N_{\text{DT}}^{\text{tot}}$ | $\mathcal{B}_{\text{SL}}$ (%) |
|-------------------|-------------------------|---|------------------------------|-------------------------------|
| $\eta e^+ \nu_e$  | $\gamma\gamma$          | $41.11 \pm 0.27$                        | $1834 \pm 47$                | $2.32 \pm 0.06 \pm 0.06$      |
|                   | $\pi^0\pi^+\pi^-$       | $16.06 \pm 0.31$                        |                              |                               |
| $\eta' e^+ \nu_e$ | $\eta\pi^+\pi^-$        | $14.07 \pm 0.10$                        | $261 \pm 22$                 | $0.82 \pm 0.07 \pm 0.03$      |
|                   | $\gamma\rho^0$          | $18.98 \pm 0.10$                        |                              |                               |

**Consistent with previous measurements,  
but the most precise to date!**



# Fits to partial decay rates and projections onto form factors



- Again, fit to the two different final states simultaneously.

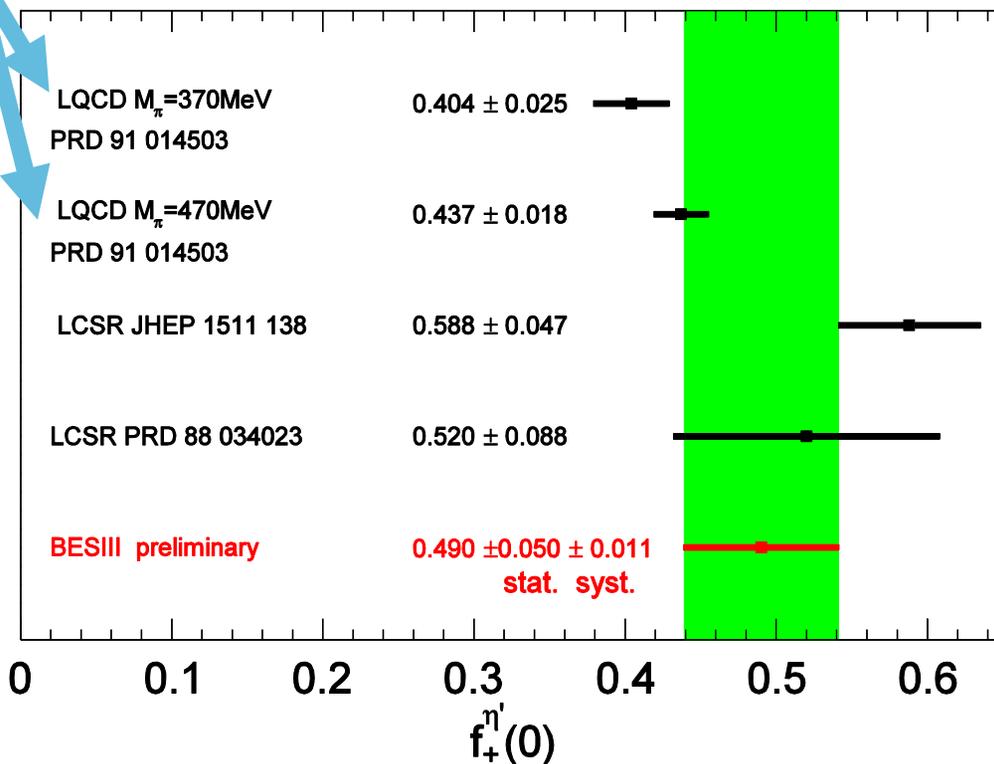
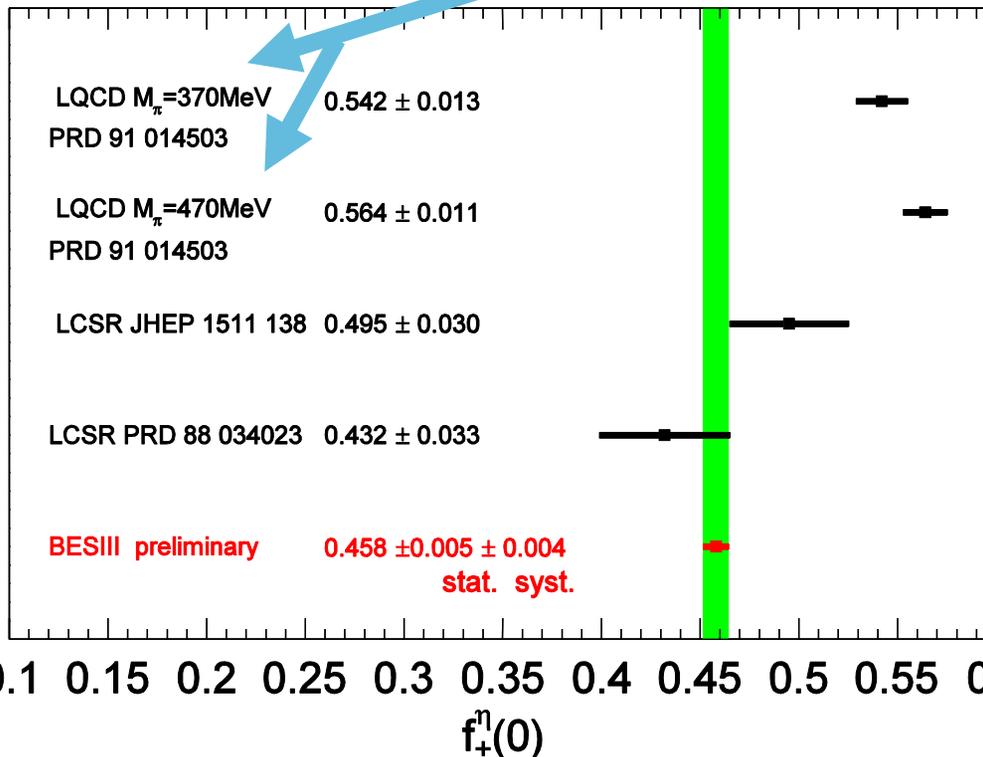
| Case              | Simple pole                        |                   |                      | Modified pole                      |              |                      | Series 2 Par.                      |               |                      |
|-------------------|------------------------------------|-------------------|----------------------|------------------------------------|--------------|----------------------|------------------------------------|---------------|----------------------|
|                   | $f_+^{\eta^{(\prime)}}(0) V_{cs} $ | $M_{\text{pole}}$ | $\chi^2/\text{NDOF}$ | $f_+^{\eta^{(\prime)}}(0) V_{cs} $ | $\alpha$     | $\chi^2/\text{NDOF}$ | $f_+^{\eta^{(\prime)}}(0) V_{cs} $ | $r_1$         | $\chi^2/\text{NDOF}$ |
| $\eta e^+ \nu_e$  | 0.450(5)(3)                        | 3.77(8)(5)        | 12.2/14              | 0.445(5)(3)                        | 0.30(4)(3)   | 11.4/14              | 0.446(5)(4)                        | -2.2(2)(1)    | 11.5/14              |
| $\eta' e^+ \nu_e$ | 0.494(45)(10)                      | 1.88(54)(5)       | 1.8/4                | 0.481(44)(10)                      | 1.62(91)(11) | 1.8/4                | 0.477(49)(11)                      | -13.1(76)(11) | 1.9/4                |

# First measurement of $f_+^{\eta(\prime)}$

Taking  $|V_{cs}|$  CKMfitter and  $f_+^{\eta(\prime)}(0) |V_{cs}|$  extracted with the series 2 Parameters as input, we obtain

$$f_+^{\eta}(0) = 0.458 \pm 0.005_{stat} \pm 0.004_{syst} \quad f_+^{\eta'}(0) = 0.490 \pm 0.050_{stat} \pm 0.011_{syst}$$

No systematic uncertainty is considered

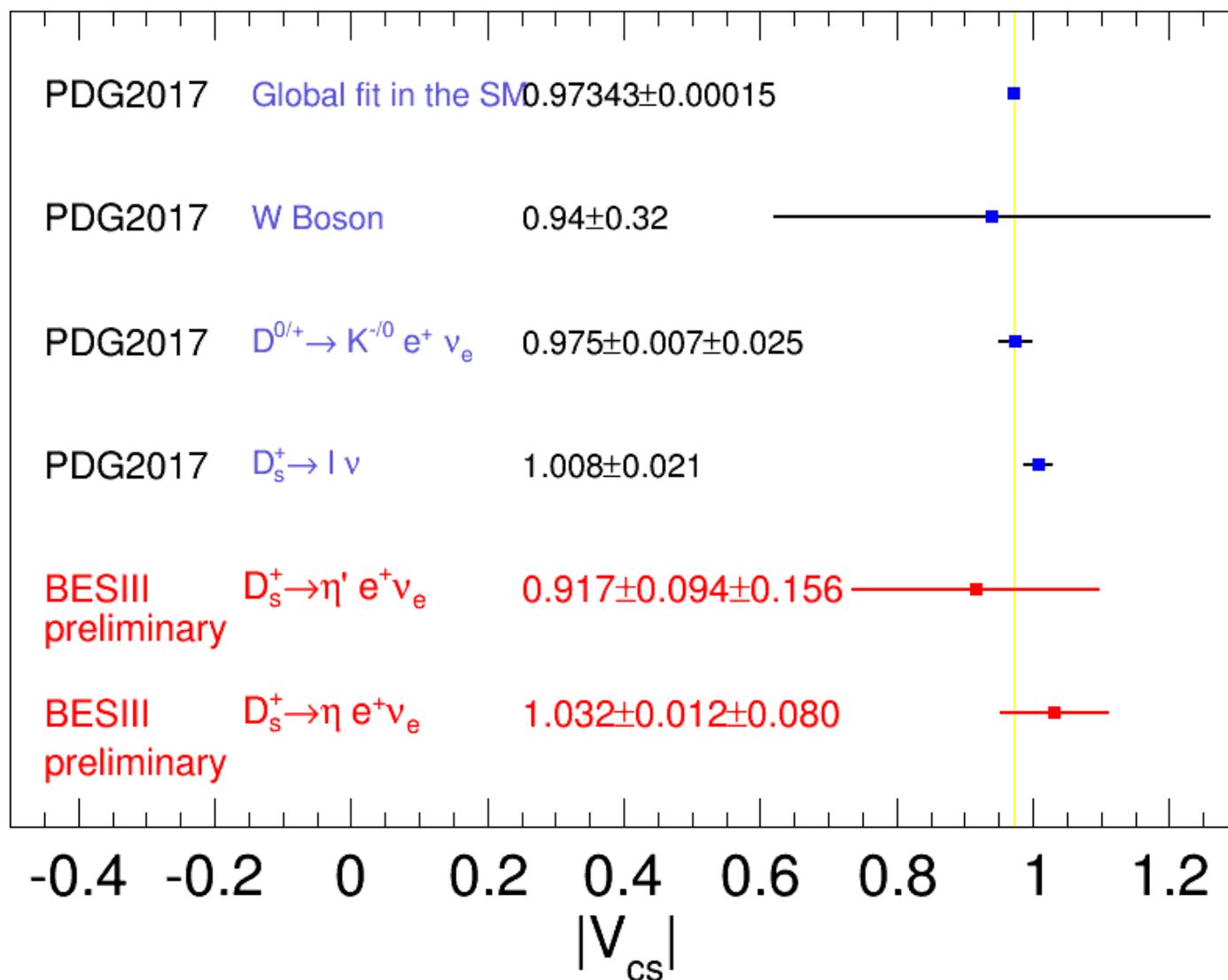


# Extracting $|V_{cs}|$

Only reported one uncertainty, but include both statistical and systematic

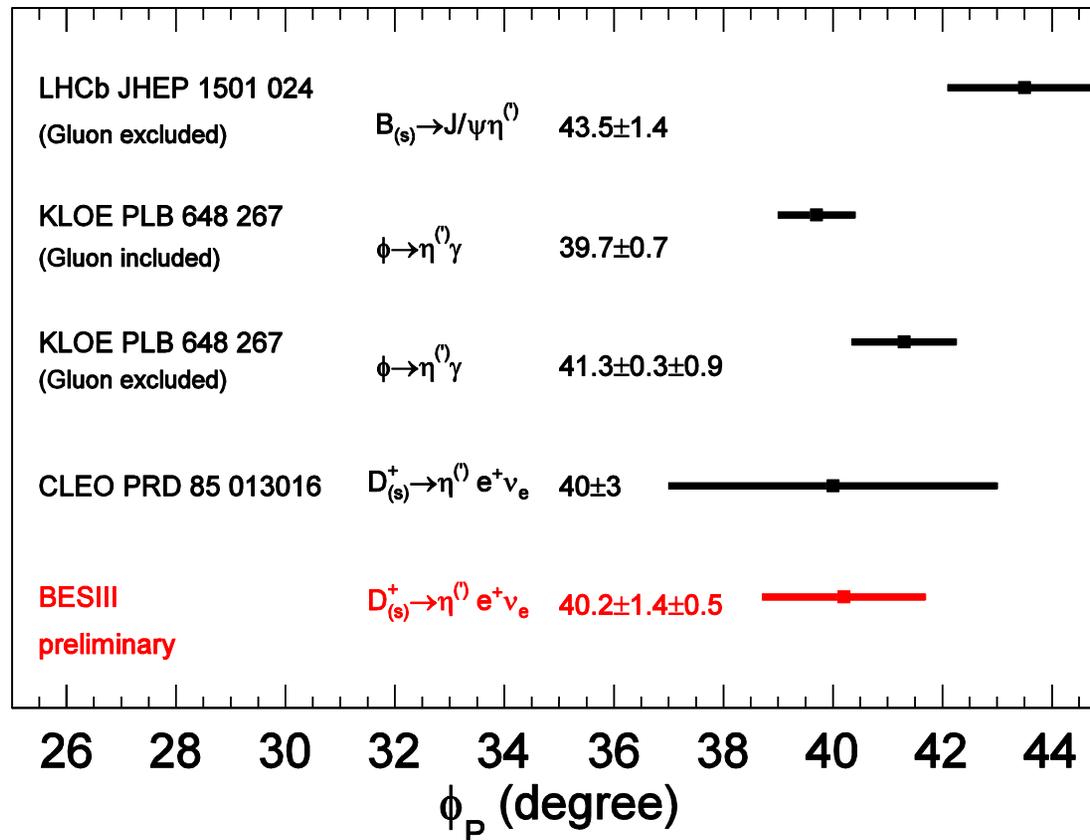
Taking  $f_+^{D_s \rightarrow \eta^{(\prime)}}(0)$

PRD88 034023 as input, we obtain



# $\eta/\eta'$ mixing angle

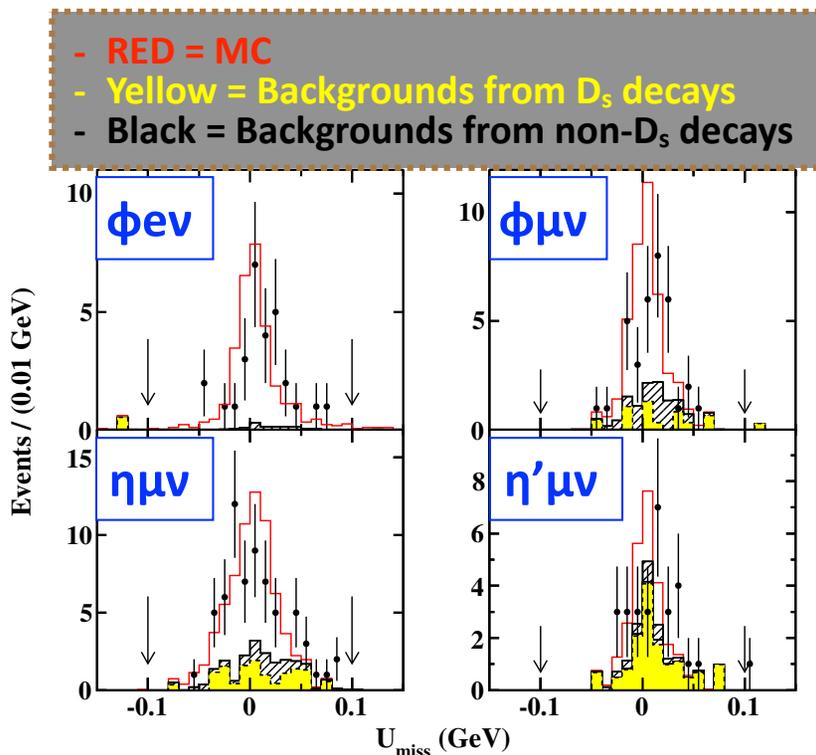
- Combined this work and  $B(D^+ \rightarrow \eta e \nu) = (10.74 \pm 0.81 \pm 0.51) \times 10^{-4}$  and  $B(D^+ \rightarrow \eta' e \nu) = (1.91 \pm 0.51 \pm 0.13) \times 10^{-4}$  (BESIII arXiv:1803.05570: Submitted to PRD)



- Good consistency with the existing measurements.

# $D_s \rightarrow (\eta/\eta') \mu \nu$ and $\phi (e/\mu) \nu$

## based on the 4009 data : PRD 97, 012006 (2018)

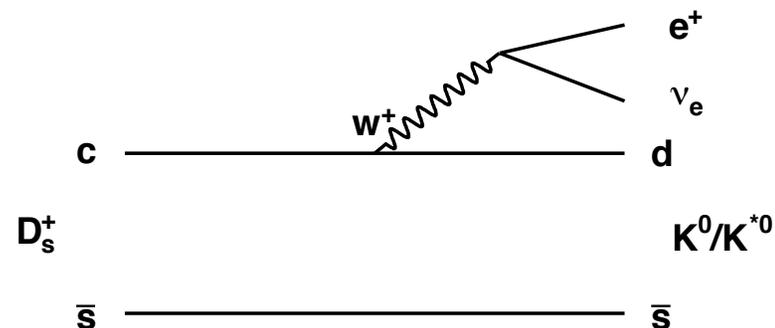


- Reconstruct:  $\phi \rightarrow KK/\eta \rightarrow \gamma\gamma/\eta' \rightarrow (\pi\pi\eta/\gamma\rho)$
  - First measurements of the muonic mode!
  - Combined this work and our own earlier work (based on the 4009 data; PRD 94, 112003 (2016)), we also have the following unities;
- $$\Gamma(D_s \rightarrow \phi \mu \nu) / \Gamma(D_s \rightarrow \phi e \nu) = 0.86 \pm 0.29$$
- $$\Gamma(D_s \rightarrow \eta \mu \nu) / \Gamma(D_s \rightarrow \eta e \nu) = 1.05 \pm 0.24$$
- $$\Gamma(D_s \rightarrow \eta' \mu \nu) / \Gamma(D_s \rightarrow \eta' e \nu) = 1.14 \pm 0.69.$$

| $\mu^+$ mode                            | $\mathcal{B}_{\text{BESIII}} (\%)$ | $\mathcal{B}_{\text{PDG}} (\%)$ | $e^+$ mode                          | $\mathcal{B}_{\text{BESIII}} (\%)$ | $\mathcal{B}_{\text{PDG}} (\%)$ |
|---|------------------------------------|---------------------------------|-------------------------------------|------------------------------------|---------------------------------|
| $D_s^+ \rightarrow \phi \mu^+ \nu_\mu$  | $1.94 \pm 0.53 \pm 0.09$           | ...                             | $D_s^+ \rightarrow \phi e^+ \nu_e$  | $2.26 \pm 0.45 \pm 0.09$           | $2.39 \pm 0.23$                 |
| $D_s^+ \rightarrow \eta \mu^+ \nu_\mu$  | $2.42 \pm 0.46 \pm 0.11$           | ...                             | $D_s^+ \rightarrow \eta e^+ \nu_e$  | $2.30 \pm 0.31 \pm 0.08$ [8]       | $2.28 \pm 0.24$                 |
| $D_s^+ \rightarrow \eta' \mu^+ \nu_\mu$ | $1.06 \pm 0.54 \pm 0.07$           | ...                             | $D_s^+ \rightarrow \eta' e^+ \nu_e$ | $0.93 \pm 0.30 \pm 0.05$ [8]       | $0.68 \pm 0.16$                 |

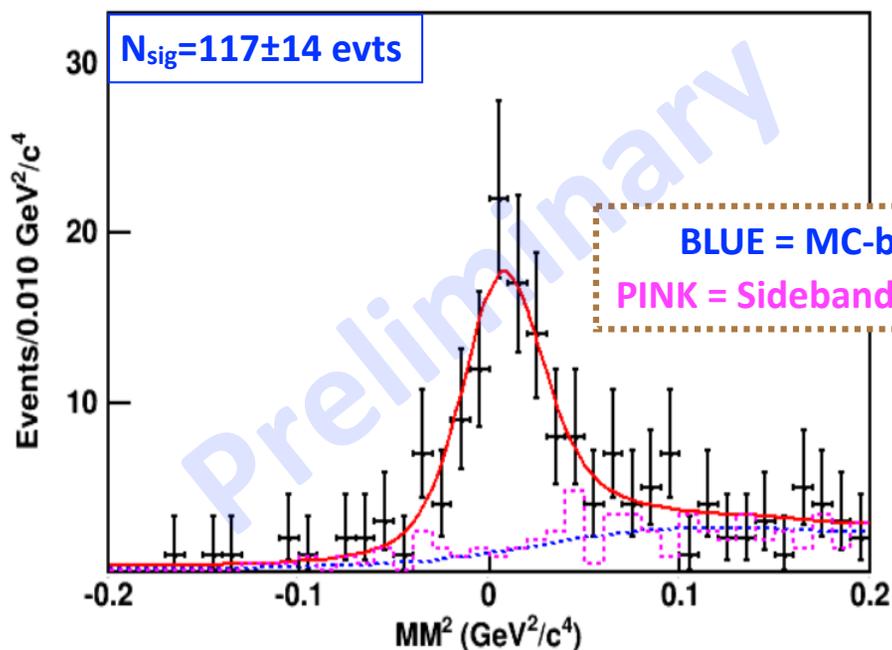
# $D_s \rightarrow (K^0/K^{*0}) e \nu$ based on the 4178 data

- The current experimental results on this CS decay is rather sparse.
- We should be able to improve the situation with our 4178 data!

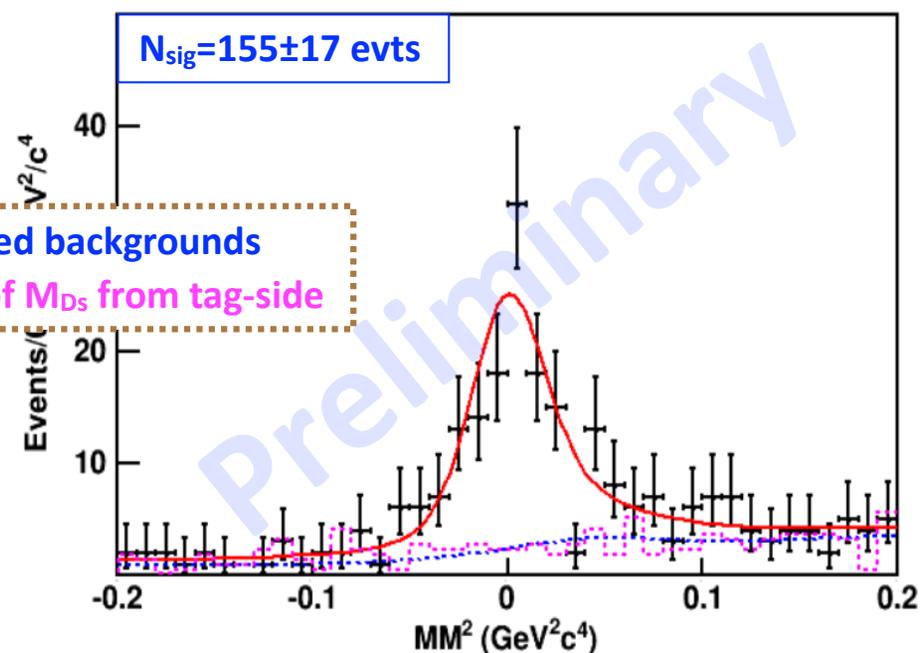


| $\Gamma(D_s^+ \rightarrow K^0 e^+ \nu_e) / \Gamma_{\text{total}}$ <span style="float: right;"><math>\Gamma_{28} / \Gamma</math></span>        |      |                         |                      |                |                                  |
|---|------|-------------------------|----------------------|----------------|----------------------------------|
| VALUE ( $10^{-2}$ )   | EVTS | DOCUMENT ID             | TECN                 | COMMENT        |                                  |
| $0.39 \pm 0.08 \pm 0.03$  | 42   | <a href="#">HIETALA</a> | <a href="#">2015</a> | Uses CLEO data |                                  |
| ••• We do not use the following data for averages, fits, limits, etc. •••   |      |                         |                      |                |                                  |
| $0.37 \pm 0.10 \pm 0.02$  | 14   | <a href="#">YELTON</a>  | <a href="#">2009</a> | CLEO           | See <a href="#">HIETALA 2015</a> |
| $\Gamma(D_s^+ \rightarrow K^*(892)^0 e^+ \nu_e) / \Gamma_{\text{total}}$ <span style="float: right;"><math>\Gamma_{29} / \Gamma</math></span> |      |                         |                      |                |                                  |
| Unseen decay modes of the $K^*(892)^0$ are included.  |      |                         |                      |                |                                  |
| VALUE ( $10^{-2}$ )   | EVTS | DOCUMENT ID             | TECN                 | COMMENT        |                                  |
| $0.18 \pm 0.04 \pm 0.01$  | 32   | <a href="#">HIETALA</a> | <a href="#">2015</a> | Uses CLEO data |                                  |
| ••• We do not use the following data for averages, fits, limits, etc. •••   |      |                         |                      |                |                                  |
| $0.18 \pm 0.07 \pm 0.01$  | 7.5  | <a href="#">YELTON</a>  | <a href="#">2009</a> | CLEO           | See <a href="#">HIETALA 2015</a> |

$K^0(=K_S \rightarrow \pi^+\pi^-)ev$



$K^{*0}(\rightarrow K^+\pi^-)ev$



BLUE = MC-based backgrounds

PINK = Sidebands of  $M_{D_s}$  from tag-side

### Preliminary results

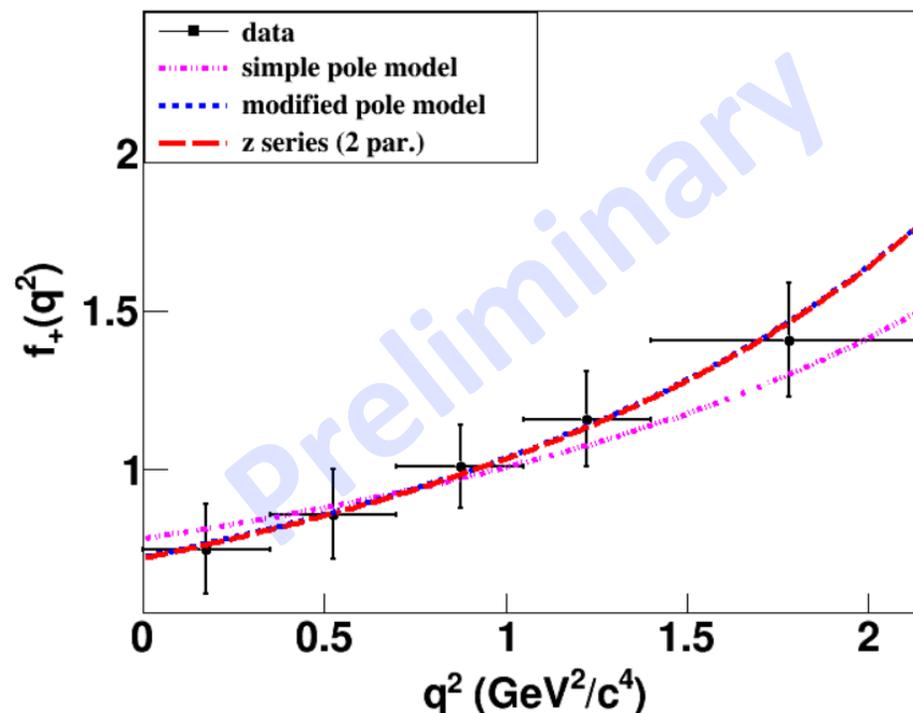
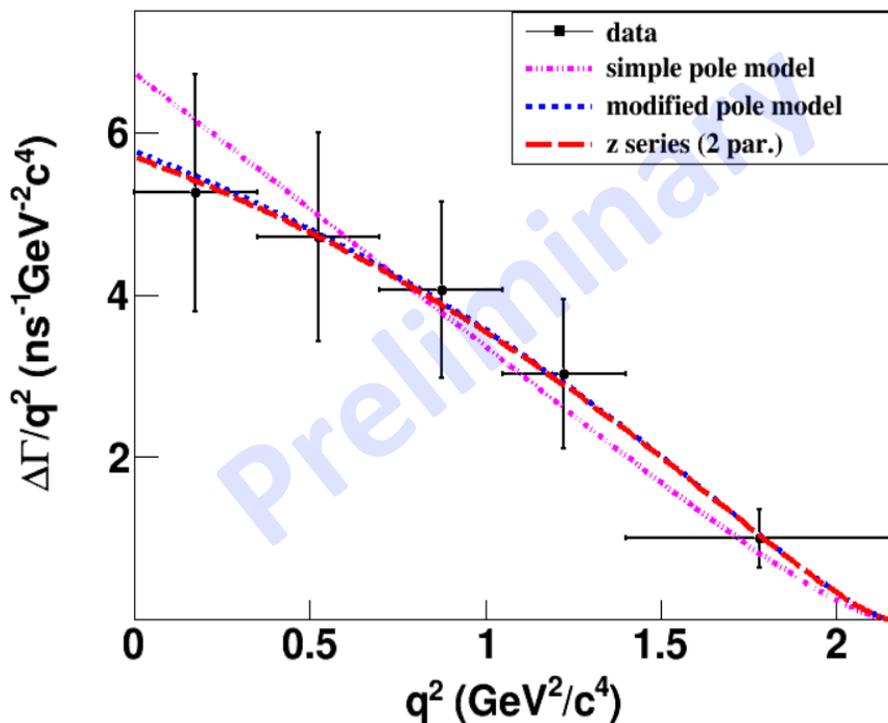
$$\text{BF}(D_s \rightarrow K^0 e \nu) = (3.25 \pm 0.38 \pm 0.14) \times 10^{-3} : (3.9 \pm 0.9) \times 10^{-3} \text{ [PDG2017]}$$

$$\text{BF}(D_s \rightarrow K^{*0} e \nu) = (2.38 \pm 0.26 \pm 0.12) \times 10^{-3} : (1.8 \pm 0.4) \times 10^{-3} \text{ [PDG2017]}$$

- Good agreement with the existing result, but more precise!
- Still, statistically limited.

# D<sub>s</sub> → K<sup>0</sup> e ν:

## Fits to partial decay rate and projection onto its form factor



**The FFs are extracted for the first time!**

| Model                 | Parameter        | Value                       | $f_+(0)$                    |
|-----------------------|------------------|-----------------------------|-----------------------------|
| Simple pole           | $f_+(0) V_{cd} $ | $0.175 \pm 0.010 \pm 0.001$ | $0.778 \pm 0.044 \pm 0.004$ |
| Modified pole model   | $f_+(0) V_{cd} $ | $0.163 \pm 0.017 \pm 0.003$ | $0.725 \pm 0.076 \pm 0.013$ |
| Series two parameters | $\alpha$         | $0.45 \pm 0.44 \pm 0.02$    | $0.720 \pm 0.084 \pm 0.013$ |
|                       | $f_+(0) V_{cd} $ | $0.162 \pm 0.019 \pm 0.003$ |                             |
|                       | $r_1$            | $-2.94 \pm 2.32 \pm 0.14$   |                             |

Inserting  $|V_{cd}| = 0.22492 \pm 0.00050$  obtained by CKMfitter, the  $f_+(0)$  can be obtained.

## Extracting FF for $D_s \rightarrow K^{*0} e \nu$

- The differential decay rate depends on 5 variables (PRL 110,131802) and can be expressed in terms of 3 helicity amplitudes:

$$\frac{d^5\Gamma}{dm_{K\pi} dq^2 d\cos\theta_K d\cos\theta_e d\chi} = \frac{3}{8(4\pi)^4} G_F^2 |V_{cd}|^2 \frac{p_{K\pi} q^2}{M_{D_s}^2} \mathcal{B}(K^{*0} \rightarrow K^+ \pi^-) |\mathcal{BW}(m_{K\pi})|^2$$

$$\times \left[ (1 + \cos\theta_e)^2 \sin^2\theta_K |H_+(q^2, m_{K\pi})|^2 \right. \\ + (1 - \cos\theta_e)^2 \sin^2\theta_K |H_-(q^2, m_{K\pi})|^2 \\ + 4\sin^2\theta_e \cos^2\theta_K |H_0(q^2, m_{K\pi})|^2 \\ + 4\sin\theta_e (1 + \cos\theta_e) \sin\theta_K \cos\theta_K \cos\chi H_+(q^2, m_{K\pi}) H_0(q^2, m_{K\pi}) \\ - 4\sin\theta_e (1 - \cos\theta_e) \sin\theta_K \cos\theta_K \cos\chi H_-(q^2, m_{K\pi}) H_0(q^2, m_{K\pi}) \\ \left. - 2\sin^2\theta_e \sin^2\theta_K \cos 2\chi H_+(q^2, m_{K\pi}) H_-(q^2, m_{K\pi}) \right].$$

The helicity amplitudes of  $H_+(q^2)$ ,  $H_-(q^2)$  and  $H_0(q^2)$  take the form of

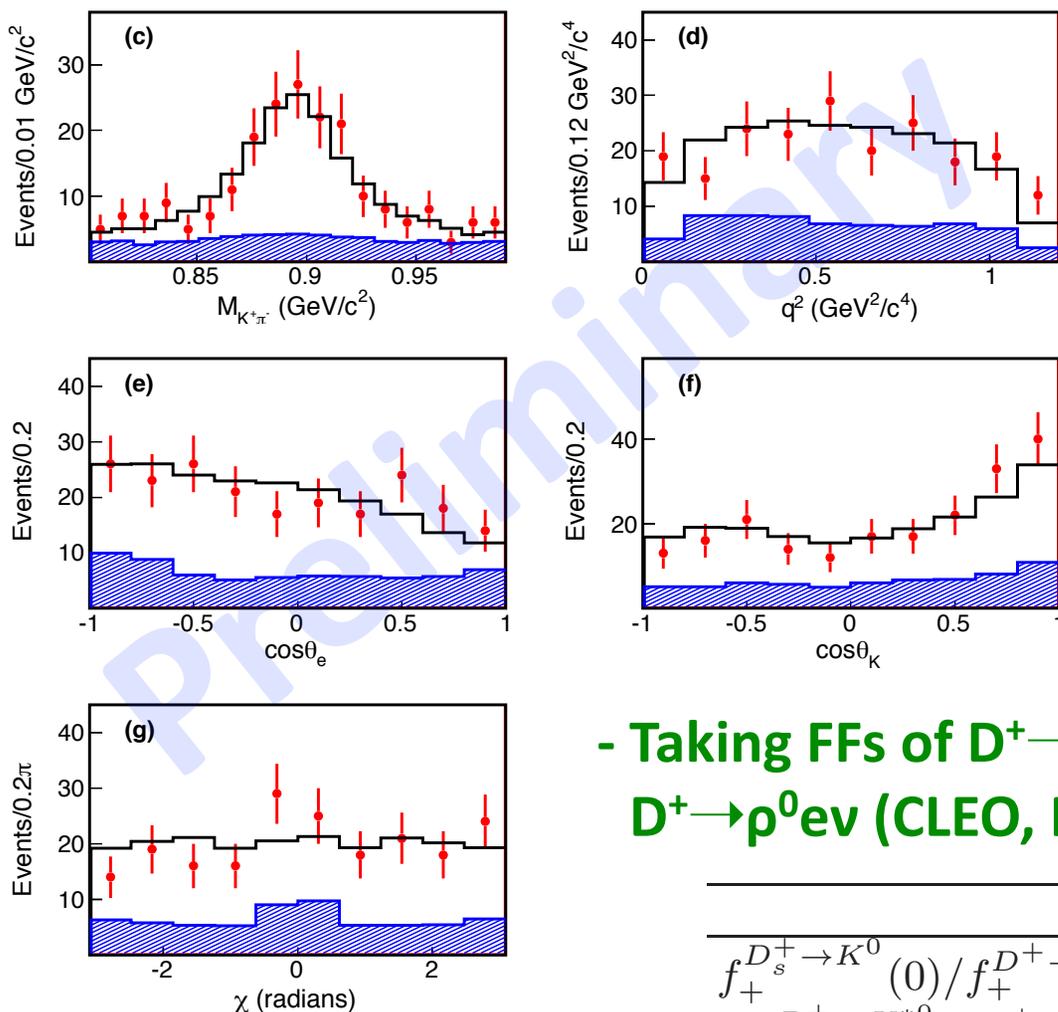
$$H_{\pm}(q^2) = (M_{D_s} + m_{K\pi}) A_{\pm}(q^2) \mp \frac{2M_{D_s} p_{K\pi}}{M_{D_s} + M_{K\pi}} V(q^2) \text{ and}$$

$$H_0(q^2) = \frac{1}{2m_{K\pi} q} \left[ (M_{D_s}^2 - m_{K\pi}^2 - q^2)(M_{D_s} + m_{K\pi}) A_1(q^2) - \frac{4M_{D_s}^2 p_{K\pi}^2}{M_{D_s} + M_{K\pi}} A_2(q^2) \right],$$

$$A_i(q^2) = \frac{A_i(0)}{1 - q^2/M_A^2} \text{ and } V(q^2) = \frac{V(0)}{1 - q^2/M_V^2}, \quad r_V = \frac{V(0)}{A_1(0)} \text{ and } r_2 = \frac{A_2(0)}{A_1(0)}.$$

- We perform 5 dimensional fit to extract the form factor ratios,  $r_V$  and  $r_2$ .

## Projections of the fit onto the 5 variables



- Preliminary: The ratio of FFs, extracted for the first time, are

$$r_V = 1.67 \pm 0.34 \pm 0.16$$

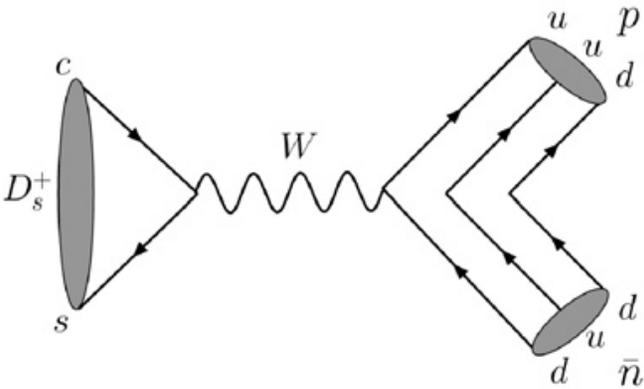
$$r_2 = 0.77 \pm 0.28 \pm 0.07$$

- Taking FFs of  $D^+ \rightarrow \pi^0 e \nu$  (BESIII, PRD96,012002) and  $D^+ \rightarrow \rho^0 e \nu$  (CLEO, PRL110,131802), we also obtained;

|   | Values   |
|---|--|
| $f_+^{D_s^+ \rightarrow K^0}(0) / f_+^{D^+ \rightarrow \pi^0}(0)$ | $1.16 \pm 0.14(\text{stat.}) \pm 0.02(\text{syst.})$ |
| $r_V^{D_s^+ \rightarrow K^{*0}} / r_V^{D^+ \rightarrow \rho^0}$   | $1.13 \pm 0.26(\text{stat.}) \pm 0.11(\text{syst.})$ |
| $r_2^{D_s^+ \rightarrow K^{*0}} / r_2^{D^+ \rightarrow \rho^0}$   | $0.93 \pm 0.36(\text{stat.}) \pm 0.10(\text{syst.})$ |

These provide a test of the LQCD predictions.

# Hadronic decays

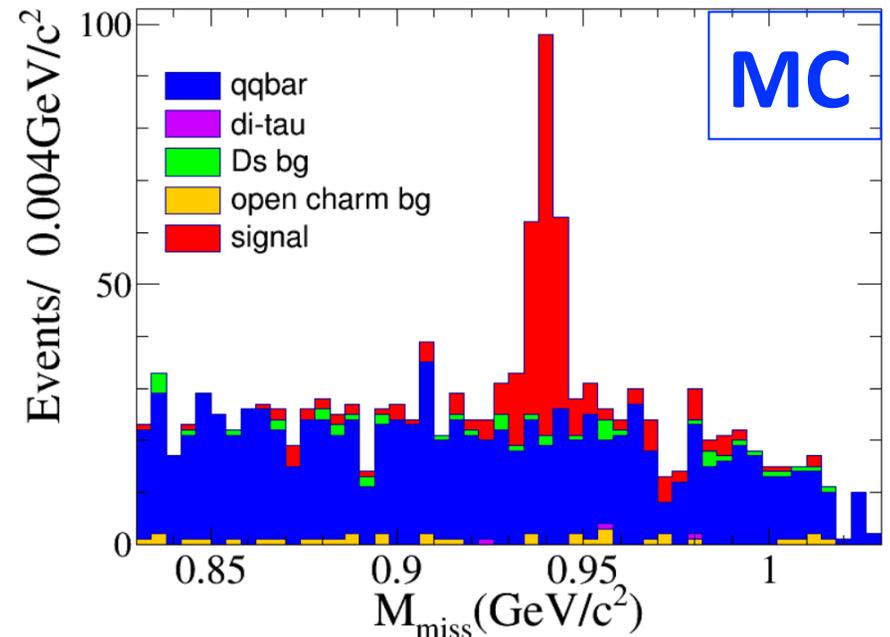


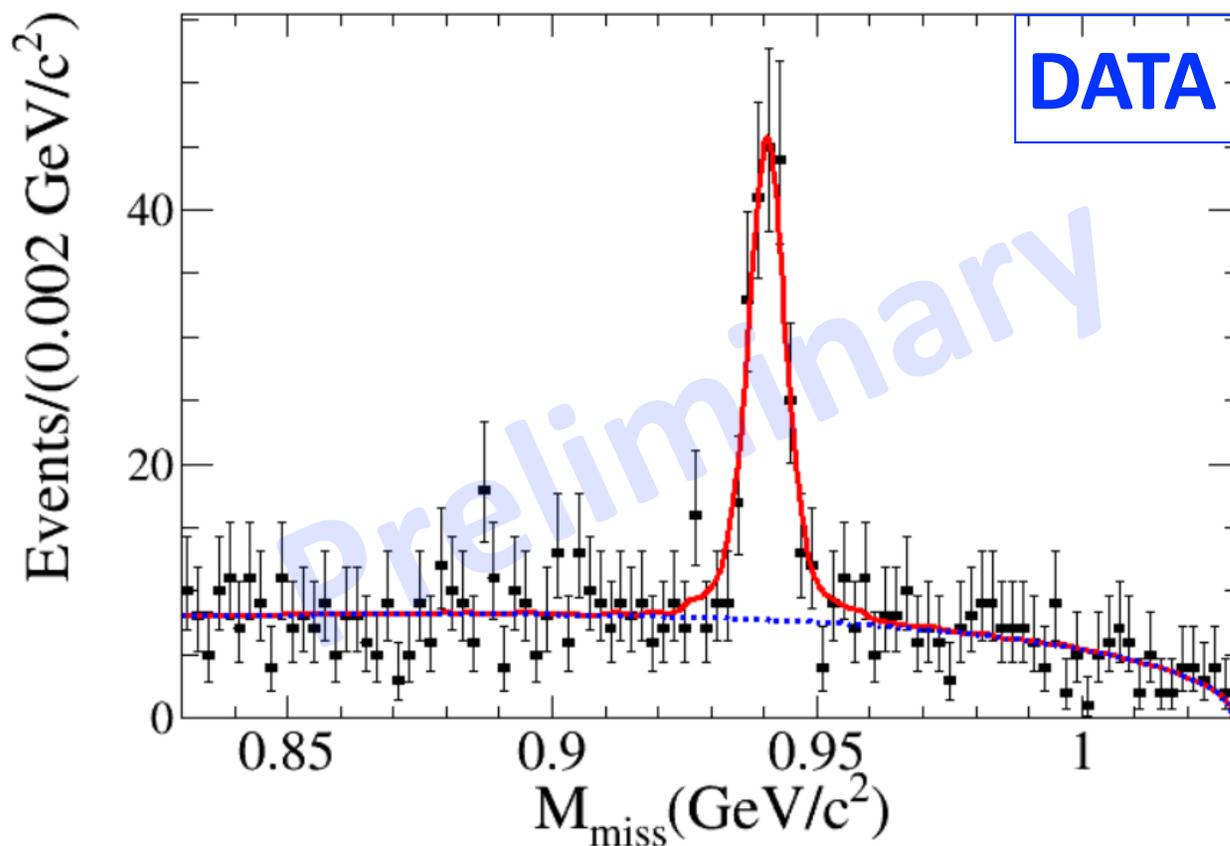
$$D_s \rightarrow p \bar{n}$$

based on the 4178 data

- The only kinematically allowed hadronic decay, involving baryons.
- Short-distance contribution is expected to be small :  $BF \sim 10^{-6}$ .  
But long-distance can enhance BF to  $\sim 10^{-3}$  (C.H. Chen, et al. PLB663, 326).
- First evidence was reported by CLEO with a signal of  $13.0 \pm 3.6$  events with  $BF = (1.30 \pm 0.36^{+0.12}_{-0.16}) \times 10^{-3}$  (PRL100, 181802).

- Reconstruct everything, but the neutron.
- Our MC (scaled to the data size) predicts a trivial background shape.





- Preliminary:

$\text{BF}(D_s \rightarrow p\bar{n}) = (1.22 \pm 0.10) \times 10^{-3}$ . Statistical uncertainty only.

- Likely statistically limited (Syst. would be dominated by PID).

- Confirmed the CLEO's result with an improved precision.

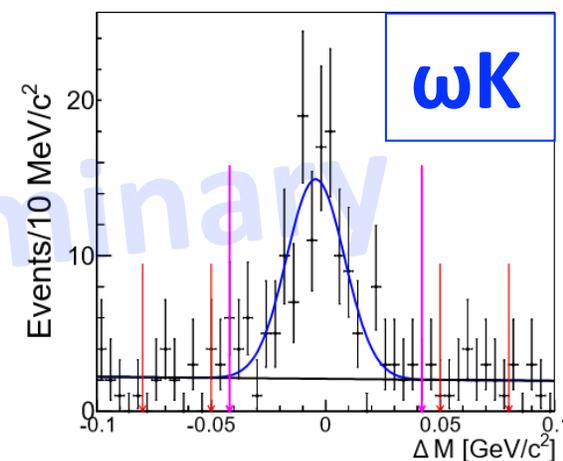
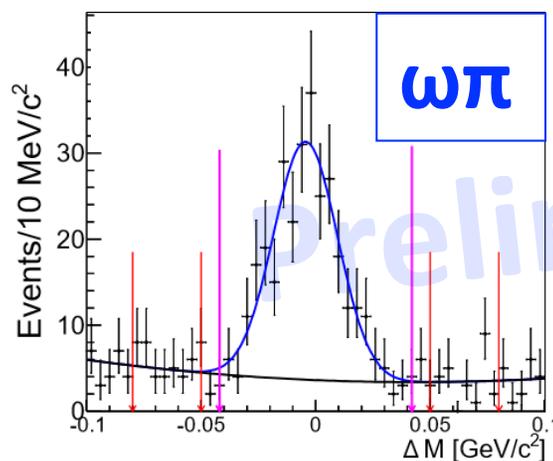
## $D_s \rightarrow \omega\pi$ and $\omega K$ based on the 4178 data

- $\omega\pi$  : CF : Has seen by CLEO (PRD80,051102) :  $BF = (2.1 \pm 0.9 \pm 0.1) \times 10^{-3}$ .
- $\omega K$ : SCS: CLEO (PRD80,051102) set an UL =  $2.4 \times 10^{-3}$  @ 90% C.L.
- Q. Qin et al. (PRD89, 054006) predicts (factorization)  
 $BF(\omega K) \sim 10^{-3}$  or it could become  $\sim 10^{-4}$  if  $\rho$ - $\omega$  mixing is considered.

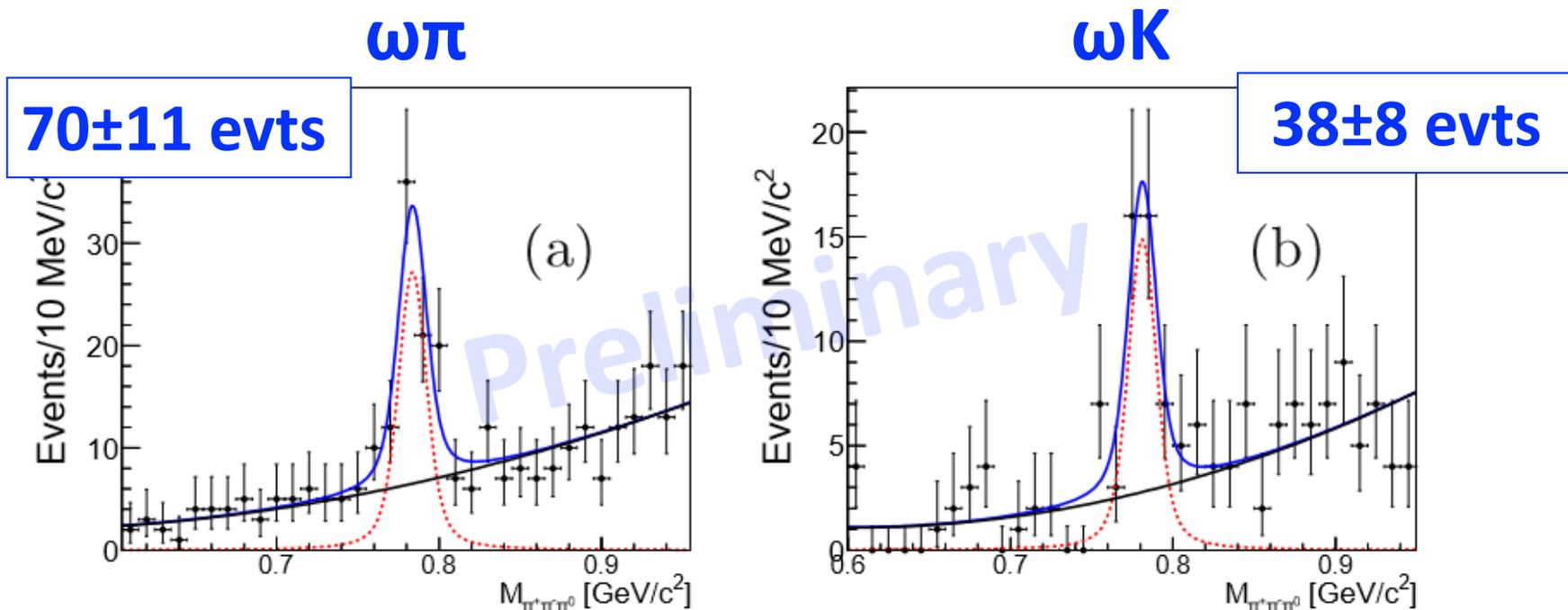
- Start with selecting  $D_s \rightarrow$  tag and  $D_s \rightarrow \omega$  ( $\pi/K$ ) candidates.

Here  $\Delta M = M_{\text{signal-side}} - M_{\text{tag-side}}$ .

- The sidebands in  $\Delta M$  from both data and MC show no peaking backgrounds in  $M_{\pi\pi\pi 0}$  of the  $M_\omega$  region.



# Projecting onto $M_{\pi^+\pi^-\pi^0}$ from the signal region of $\Delta M$



- Preliminary:  $\text{BF}(D_s \rightarrow \omega\pi) = (1.85 \pm 0.30 \pm 0.19) \times 10^{-3} : 7.7\sigma$  stat. sig.  
Consistent with CLEO's measurement, but more precise.
- Preliminary:  $\text{BF}(D_s \rightarrow \omega K) = (1.13 \pm 0.24 \pm 0.14) \times 10^{-3} : 6.2\sigma$  stat. sig.  
First observation!

## Summary

- Our results on (semi-)leptonic  $D_s$  decays improve the precisions on the decay constant, form factors, and  $|V_{cs}|$ .  
More results on (semi-)leptonic decays are coming, including  $D_s \rightarrow X e \nu$ .
- Our preliminary results on hadronic decays have confirmed and improved the precisions over the previous results from CLEO.  
(a lot) More measurements in  $D_s$  hadronic decays are coming.
- Not mentioned in detail in this report:
  - ▶  $D_s^+ \rightarrow \mu^+ \nu_\mu$  : PRD 94, 072004 (2016)
  - ▶  $D_s^+ \rightarrow \eta(\eta') e^+ \nu_e$  : PRD 94, 112003 (2016)
  - ▶  $D_s^+ \rightarrow \eta' \rho^+$  and  $\eta' X$  : PLB 750, 466 (2015)