

# Rare charm decays

*A quest for New Physics?*



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# 1. Introduction: experimental data

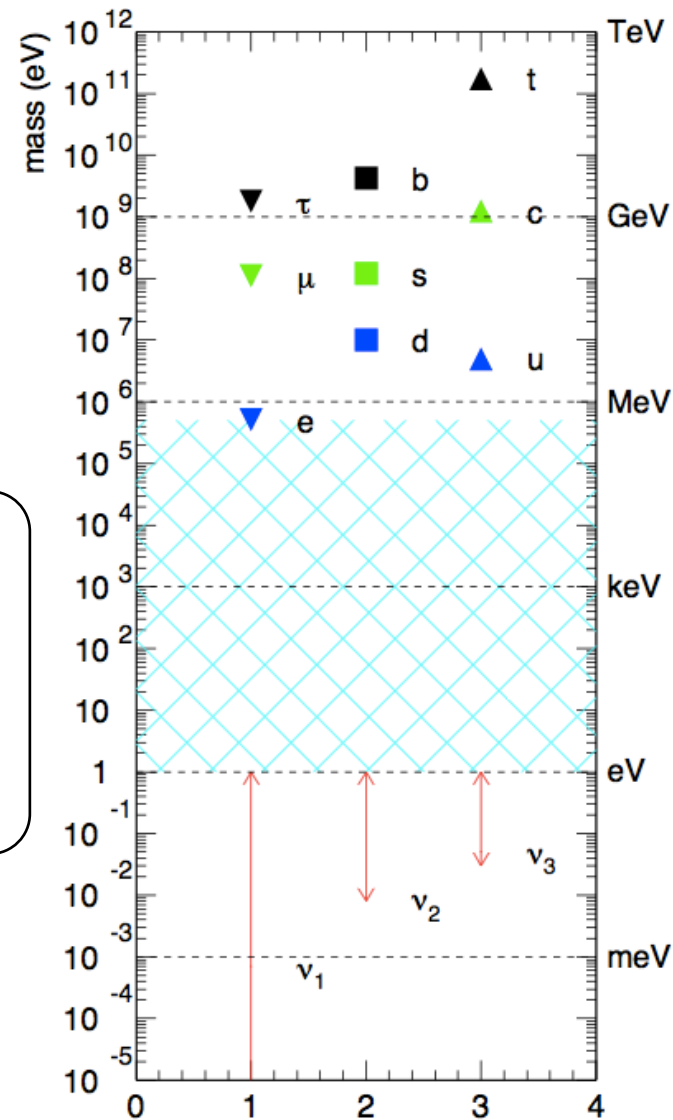
Gauge forces in SM do not distinguish between fermions of different generations:

- $e, \mu, \tau$  have same electrical charge
  - quarks have same color charge
- “Lepton universality”

- ★ Why generations? Why only 3? Are there only 3?
- ★ Why hierarchies of masses and mixings?
- ★ Can there be transitions between quarks/leptons of the same charge but different generations?

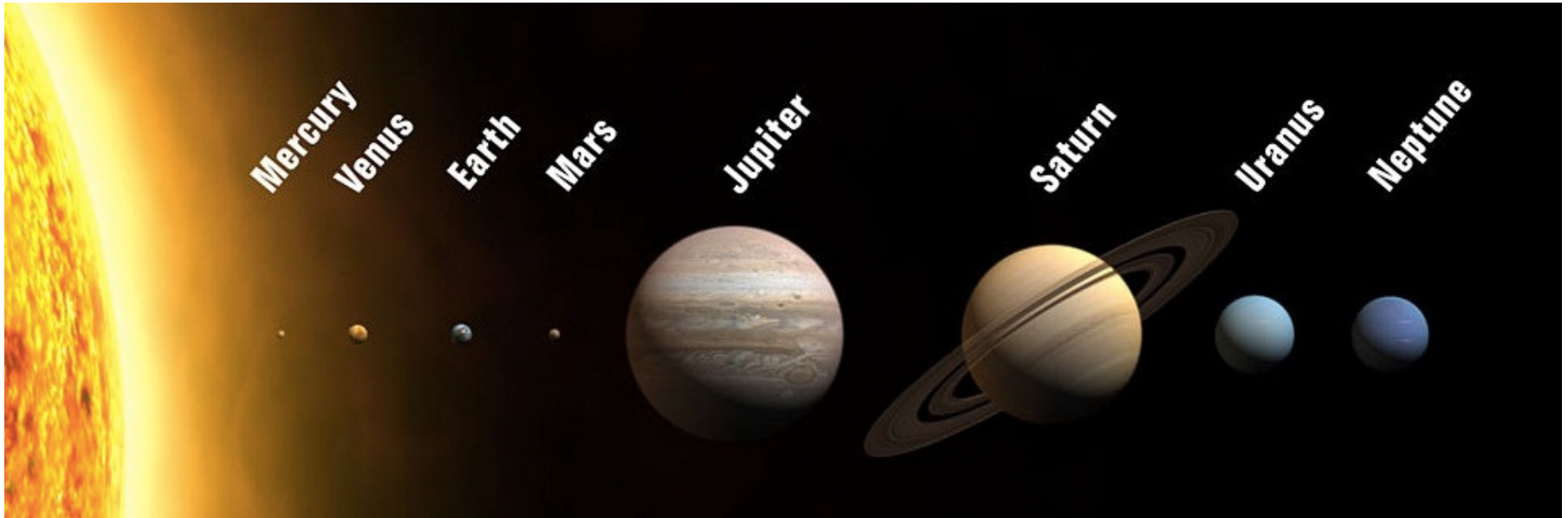
The flavor puzzle

Is there a guiding principle that explains this pattern?



Caution: fermion mass hierarchy might not have a single explanation...

Why is  $M_{\text{Jupiter}} \gg M_{\text{Mercury}}$ ?

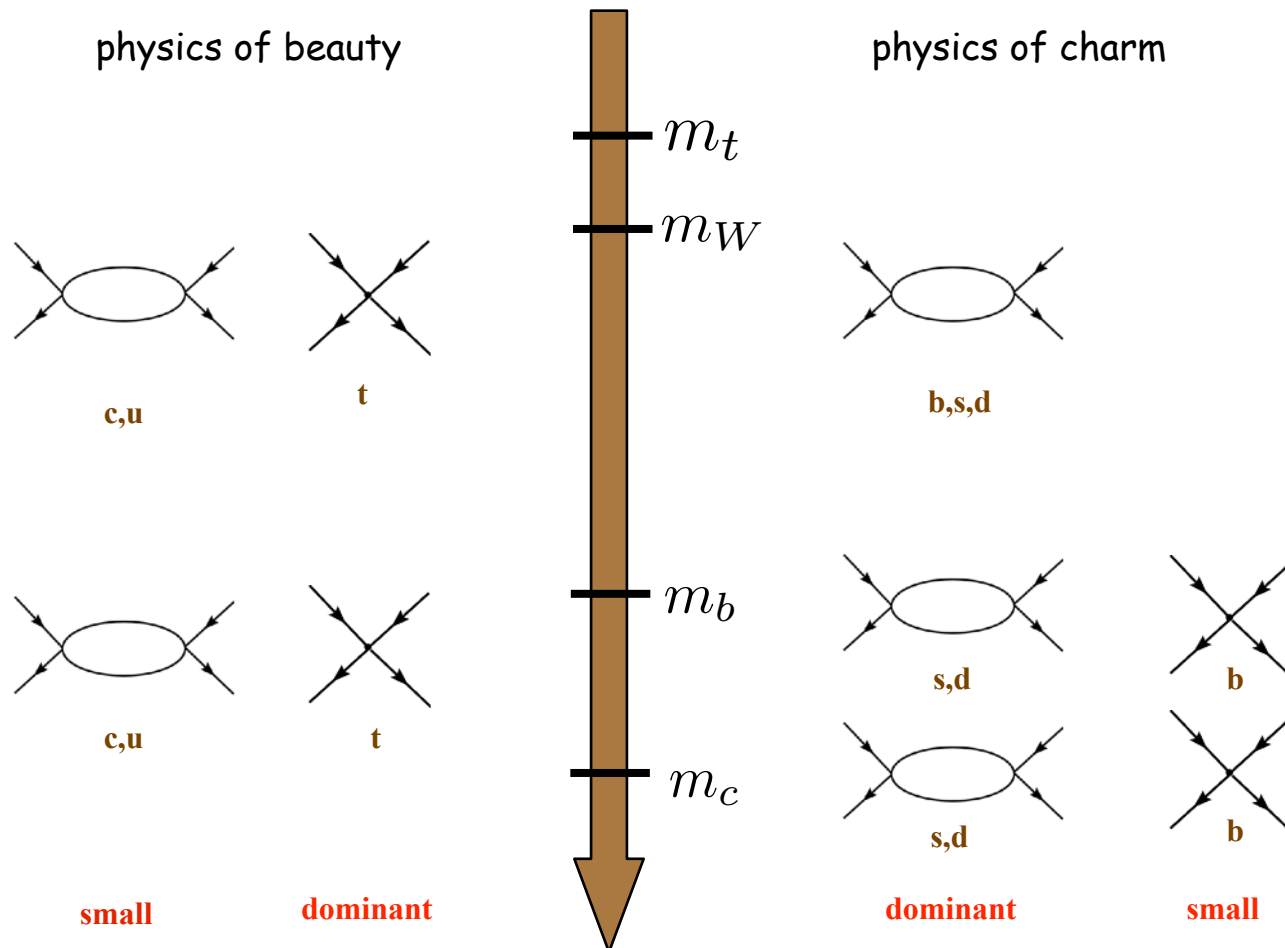


But what if it does?  
New Physics?

# Introduction: energy scales

★ Main goal of the exercise: understand physics at the most fundamental scale

★ It is important to understand relevant energy scales for the problem at hand



## 2a. Rare decays: short distance

★ Effective Lagrangian can be obtained by integrating out heavy modes

- Contrary to b-physics, two matching scales ( $M_W$  and  $m_b$ )
- GIM mechanism is effective for light quarks
- Only two operators at  $M_W$

$$H_{\text{eff}}(M_W > \mu > m_b) = \frac{4G_F}{\sqrt{2}} \sum_{q=d,s,b} V_{cq}^* V_{uq} [C_1(\mu) \mathcal{O}_1^q + C_2(\mu) \mathcal{O}_2^q]$$

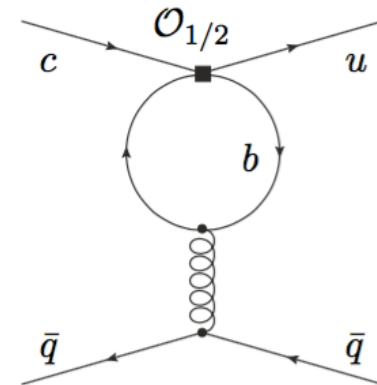
$$\mathcal{O}_1^q = (\bar{u}_L \gamma_\mu T^a q_L) (\bar{q}_L \gamma^\mu T^a c_L),$$

$$\mathcal{O}_2^q = (\bar{u}_L \gamma_\mu q_L) (\bar{q}_L \gamma^\mu c_L),$$

- Ten operators at  $m_b$
- Those that correspond to rare decays

$$\mathcal{O}_9 = \frac{\alpha_{\text{em}}}{4\pi} (\bar{u}_L \gamma_\mu c_L) (\bar{\ell} \gamma^\mu \ell),$$

$$\mathcal{O}_{10} = \frac{\alpha_{\text{em}}}{4\pi} (\bar{u}_L \gamma_\mu c_L) (\bar{\ell} \gamma^\mu \gamma_5 \ell).$$



# Short distance (cont.)

★ Effective Lagrangian can be obtained by integrating out heavy modes

- Most recent results: NNLL

De Boer, Muller, Seidel, 2016

	$\bar{C}_1$	$\bar{C}_2$	$\bar{C}_3$	$\bar{C}_4$	$\bar{C}_5$	$\bar{C}_6$
LL	-0.517	1.266	0.010	-0.025	0.007	-0.029
NLL	-0.356	1.157	0.014	-0.042	0.010	-0.045
NNLL	-0.317	1.140	0.013	-0.040	0.009	-0.045

- Short distance contribution for  $\mu < m_b$  for  $C_9(\mu)$  Wilson coefficient

$$C_9(\mu) = C_9(m_b) + W^{(n_f=4)}(\mu, m_b) R U^{(n_f=5)}(m_b, M_W) C(M_W),$$

$$W^{(n_f=4)}(\mu, m_b) = -\frac{1}{2} \int_{a_s(m_b)}^{a_s(\mu)} da_s \frac{\kappa(a_s)}{\beta(a_s)} U^{(n_f=4)}(\mu, m_b),$$

$$\frac{d}{d \ln \mu_1} U^{(n_f)}(\mu_1, \mu_2) = \gamma^T(n_f, \mu_1) U^{(n_f)}(\mu_1, \mu_2)$$

- The results are

	$C_7^{\text{eff}}$	$C_8^{\text{eff}}$	$C_9$	$C_{10}$	$C_9^{\text{NNLL}}$	$C_{10}^{\text{NNLL}}$
LL	0.078	-0.055	-0.098	0		
NLL	0.051	-0.062	-0.309	0	-0.488	0

An order of magnitude difference between leading log and NNLL results for  $C_9$ !

# Short distance/long distance

★ Effective Lagrangian can be obtained by integrating out heavy modes

- Take into account light quarks: "effective Wilson coefficient"  $C_9^{\text{eff}}(\mu)$

De Boer, Muller, Seidel, 2016

$$C_9^{\text{eff}}(\mu, s) = (V_{cd}^* V_{ud} + V_{cs}^* V_{us}) \left( C_9(\mu) + Y^{(ds)}(\mu, s) \right) \\ + V_{cd}^* V_{ud} Y^{(d)}(\mu, s) + V_{cs}^* V_{us} Y^{(s)}(\mu, s),$$

- ... where  $Y^{(s)}(\mu, s)$ ,  $Y^{(d)}(\mu, s)$  and  $Y^{(ds)}(\mu, s)$  are functions of  $C$  and  $\log(m_q^2/\mu^2)$

Burdman et al (02),

Fajfer et al (03), Paul et al (11)

★ Long distance effects: hadron resonances and others

- Since-particle resonances modify  $C_9^{\text{eff}}(\mu)$  as  $C_9^{\text{eff}} \rightarrow C_9^{\text{eff}} + \frac{3\pi}{\alpha^2} \sum_i \kappa_i \frac{m_{V_i} \Gamma_{V_i \rightarrow l^+ l^-}}{m_{V_i}^2 - s - im_{V_i} \Gamma_{V_i}}$ ,

$$C_9^{\text{R}} = a_\rho e^{i\delta_\rho} \left( \frac{1}{q^2 - m_\rho^2 + im_\rho \Gamma_\rho} - \frac{1}{3} \frac{1}{q^2 - m_\omega^2 + im_\omega \Gamma_\omega} \right) \\ + \frac{a_\phi e^{i\delta_\phi}}{q^2 - m_\phi^2 + im_\phi \Gamma_\phi},$$

- Similar modifications are present for other "effective Wilson coefficients"

- In principle, should also contain contributions from two-particle states, etc.

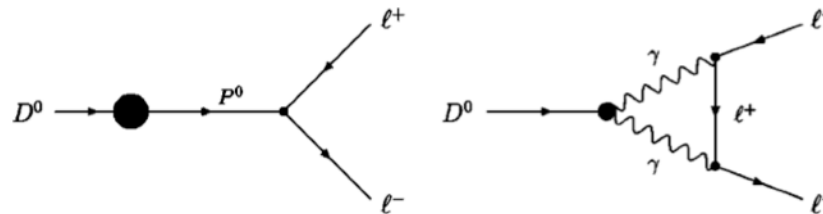
## 2b. Rare leptonic decays: phenomenology

★ Standard Model contribution to  $D \rightarrow \mu^+\mu^-$ .

$$B_{D^0\ell^+\ell^-}^{(\text{s.d.})} \simeq \frac{G_F^2 M_W^2 f_D m_\ell}{\pi^2} F, \quad F = \sum_{i=d,s,b} V_{ui} V_{ci}^* \left[ \frac{x_i}{2} + \frac{\alpha_s}{4\pi} x_i \cdot \left( \ln^2 x_i + \frac{4 + \pi^2}{3} \right) \right]$$

UKQCD, HPQCD; Jamin, Lange;  
Penin, Steinhauser; Khodjamirian

★ Long distance analysis



Burdman, Golowich, Hewett,  
Pakvasa; Fajfer, Prelovsek, Singer

Update soon: AAP

$$B_{D^0\ell^+\ell^-}^{(\text{mix})} = \sum_{P_n} \langle P_n | \mathcal{H}_{wk}^{(\text{p.c.})} | D^0 \rangle \frac{1}{M_D^2 - M_{P_n}^2} B_{P_n\ell^+\ell^-} \quad \left| \quad \text{Im } \mathcal{M}_{D^0 \rightarrow \ell^+\ell^-} = \frac{1}{2!} \sum_{\lambda_1, \lambda_2} \int \frac{d^3 q_1}{2\omega_1 (2\pi)^3} \frac{d^3 q_2}{2\omega_2 (2\pi)^3} \times \mathcal{M}_{D \rightarrow \gamma\gamma} \mathcal{M}_{\gamma\gamma \rightarrow \ell^+\ell^-}^* (2\pi)^4 \delta^{(4)}(p - q_1 - q_2) \right.$$

- LD effects amount to  $\text{Br} \sim 10^{-13}$

- BGHP (2002) paper probably overestimates LD contributions to  $D \rightarrow \mu^+\mu^-$ .



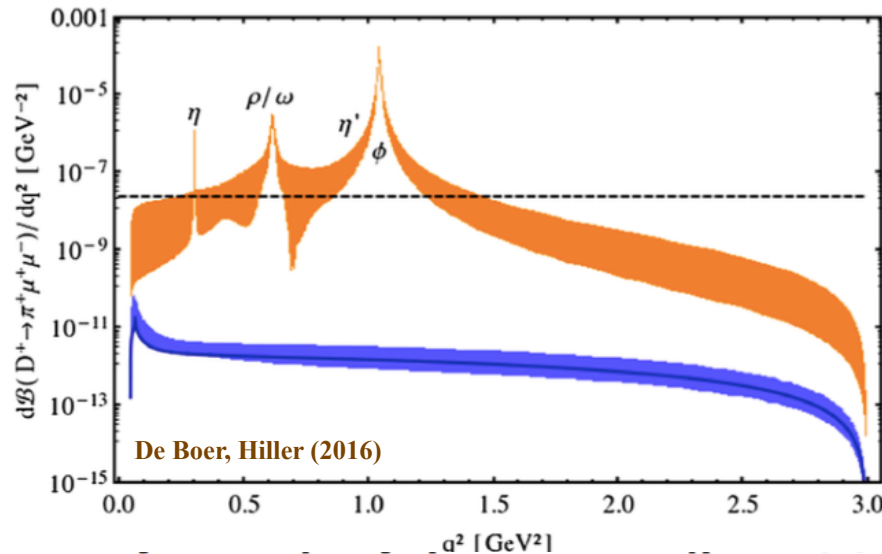
# Rare semileptonic decays: phenomenology

- These decays also proceed at one loop in the SM; GIM is very effective
  - SM rates are expected to be small

De Boer, Hiller (2016)

- ★ Rare decays  $D \rightarrow M e^+e^-/\mu^+\mu^-$  just like  $D \rightarrow e^+e^-/\mu^+\mu^-$  are mediated by  $c \rightarrow u$  II
  - SM contribution is dominated by LD effects, e.g.

Burdman, Golowich, Hewett, Pakvasa;  
Fajfer, Prelovsek, Singer



Carve out “resonance window” by comparing  $f_{\text{Resonance}}/f_{\text{Lead Resonance}}$  to experimental sensitivity?

$q^2$ bin	$\mathcal{B}(D^+ \rightarrow \pi^+ \mu^+ \mu^-)_{\text{nr}}^{\text{SM}}$	90% C.L. [27]
Full $q^2$ : $(2m_\mu)^2 \leq q^2 \leq (m_{D^+} - m_{\pi^+})^2$	$3.7 \times 10^{-12} (\pm 1, \pm 3, {}^{+16}_{-15}, \pm 1, {}^{+3}_{-1}, {}^{+158}_{-12})$	$7.3 \times 10^{-8}$
Low $q^2$ : $0.250^2 \text{ GeV}^2 \leq q^2 \leq 0.525^2 \text{ GeV}^2$	$7.4 \times 10^{-13} (\pm 1, \pm 4, {}^{+23}_{-21}, {}^{+10}_{-11}, {}^{+10}_{-1}, {}^{+238}_{-23}, {}^{+6}_{-5})$	$2.0 \times 10^{-8}$
High $q^2$ : $q^2 \geq 1.25^2 \text{ GeV}^2$	$7.4 \times 10^{-13} (\pm 1, \pm 6, {}^{+15}_{-14}, \pm 6, {}^{+0}_{-1}, {}^{+136}_{-45}, {}^{+27}_{-20})$	$2.6 \times 10^{-8}$

# Rare decays: new physics

## ★ Can New Physics be “hiding” in the up-type quark transitions?

- explicit models can be constructed where it can be done
- long-distance effects complicate interpretation
- must use exp and theo tricks to sort out

$$\mathcal{O}_7 = \frac{e}{8\pi^2} m_c F_{\mu\nu} \bar{u} \sigma^{\mu\nu} (1 + \gamma_5) c,$$

$$\mathcal{O}_9 = \frac{e^2}{16\pi^2} \bar{u}_L \gamma_\mu c_L \bar{\ell} \gamma^\mu \ell,$$

$$\mathcal{O}_{10} = \frac{e^2}{16\pi^2} \bar{u}_L \gamma_\mu c_L \bar{\ell} \gamma^\mu \gamma_5 \ell,$$

$$\mathcal{O}'_7 = \frac{e}{8\pi^2} m_c F_{\mu\nu} \bar{u} \sigma^{\mu\nu} (1 - \gamma_5) c,$$

$$\mathcal{O}'_9 = \frac{e^2}{16\pi^2} \bar{u}_R \gamma_\mu c_R \bar{\ell} \gamma^\mu \ell,$$

$$\mathcal{O}'_{10} = \frac{e^2}{16\pi^2} \bar{u}_R \gamma_\mu c_R \bar{\ell} \gamma^\mu \gamma_5 \ell,$$

Maybe correlations between different measurements can help sorting out NP in charm?

# Generic NP contribution to $D \rightarrow \mu^+\mu^-$

★ Most general effective Hamiltonian:

$$\langle f | \mathcal{H}_{NP} | i \rangle = G \sum_{i=1} \tilde{C}_i(\mu) \langle f | Q_i | i \rangle(\mu)$$

$$\begin{aligned} \tilde{Q}_1 &= (\bar{\ell}_L \gamma_\mu \ell_L) (\bar{u}_L \gamma^\mu c_L), & \tilde{Q}_4 &= (\bar{\ell}_R \ell_L) (\bar{u}_R c_L), \\ \tilde{Q}_2 &= (\bar{\ell}_L \gamma_\mu \ell_L) (\bar{u}_R \gamma^\mu c_R), & \tilde{Q}_5 &= (\bar{\ell}_R \sigma_{\mu\nu} \ell_L) (\bar{u}_R \sigma^{\mu\nu} c_L), \\ \tilde{Q}_3 &= (\bar{\ell}_L \ell_R) (\bar{u}_R c_L), & & \text{plus } L \leftrightarrow R \end{aligned}$$

★ ... thus, the amplitude for  $D \rightarrow e^+e^-/\mu^+\mu^-$  decay is

$$\mathcal{B}_{D^0 \rightarrow \ell^+\ell^-} = \frac{M_D}{8\pi\Gamma_D} \sqrt{1 - \frac{4m_\ell^2}{M_D^2}} \left[ \left(1 - \frac{4m_\ell^2}{M_D^2}\right) |A|^2 + |B|^2 \right]$$

$$|A| = G \frac{f_D M_D^2}{4m_c} [\tilde{C}_{3-8} + \tilde{C}_{4-9}],$$

$$|B| = G \frac{f_D}{4} \left[ 2m_\ell (\tilde{C}_{1-2} + \tilde{C}_{6-7}) + \frac{M_D^2}{m_c} (\tilde{C}_{4-3} + \tilde{C}_{9-8}) \right], \quad \tilde{C}_{i-k} \equiv \tilde{C}_i - \tilde{C}_k$$

**Many NP models give contributions to both D-mixing and  $D \rightarrow e^+e^-/\mu^+\mu^-$  decay: correlate!!!**

# Mixing vs rare decays: ruling out models

## ★ Relating mixing and rare decay

- consider an example: heavy vector-like quark (Q=+2/3)
- appears in little Higgs models, etc.

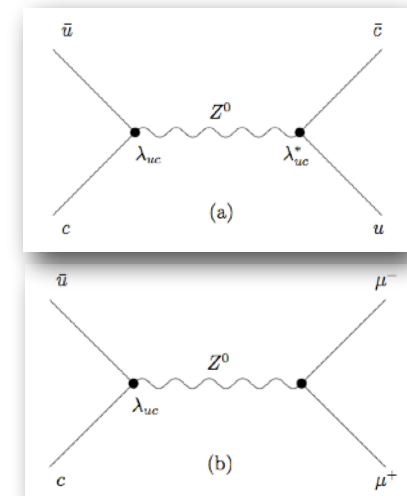
E. Golowich, J. Hewett, S. Pakvasa and A.A.P.  
PRD79, 114030 (2009)

Mixing: 
$$\mathcal{H}_{2/3} = \frac{g^2}{8 \cos^2 \theta_w M_Z^2} \lambda_{uc}^2 Q_1 = \frac{G_F \lambda_{uc}^2}{\sqrt{2}} Q_1$$

$$x_D^{(+2/3)} = \frac{2G_F \lambda_{uc}^2 f_D^2 M_D B_{Dr}(m_c, M_Z)}{3\sqrt{2}\Gamma_D}$$

Rare decay: 
$$A_{D^0 \rightarrow \ell^+ \ell^-} = 0 \quad B_{D^0 \rightarrow \ell^+ \ell^-} = \lambda_{uc} \frac{G_F f_D m_\mu}{2}$$

$$\mathcal{B}_{D^0 \rightarrow \mu^+ \mu^-} = \frac{3\sqrt{2}}{64\pi} \frac{G_F m_\mu^2 x_D}{B_{Dr}(m_c, M_Z)} \left[ 1 - \frac{4m_\mu^2}{M_D} \right]^{1/2} \simeq 4.3 \times 10^{-9} x_D \leq 4.3 \times 10^{-11} .$$



$$\lambda_{uc} \equiv -(V_{ud}^* V_{cd} + V_{us}^* V_{cs} + V_{ub}^* V_{cb})$$

Note: a NP parameter-free relation!



# Rare semileptonic decays: New Physics

➤ Rare semileptonic decays can be used to study New Physics

★ Example: R-parity-violating SUSY/leptoquarks

- operators with the same parameters contribute to D-mixing
- feed results into rare decays

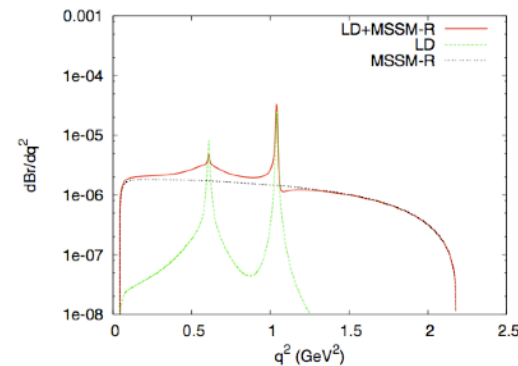
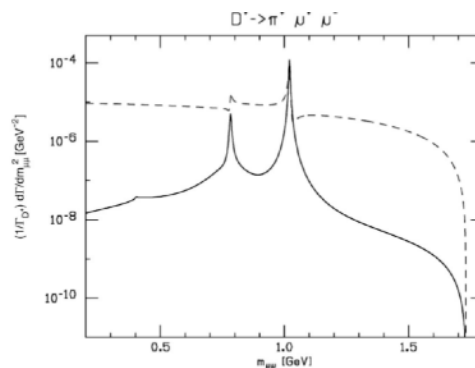
Burdman, Golowich, Hewett, Pakvasa;  
Fajfer, Prelovsek, Singer

Mode	LD	Extra heavy $q$	LD + extra heavy $q$
$D^+ \rightarrow \pi^+ e^+ e^-$	$2.0 \times 10^{-6}$	$1.3 \times 10^{-9}$	$2.0 \times 10^{-6}$
$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	$2.0 \times 10^{-6}$	$1.6 \times 10^{-9}$	$2.0 \times 10^{-6}$

Mode	MSSM $\tilde{R}$	LD + MSSM $\tilde{R}$
$D^+ \rightarrow \pi^+ e^+ e^-$	$2.1 \times 10^{-7}$	$2.3 \times 10^{-6}$
$D^+ \rightarrow \pi^+ \mu^+ \mu^-$	$6.5 \times 10^{-6}$	$8.8 \times 10^{-6}$

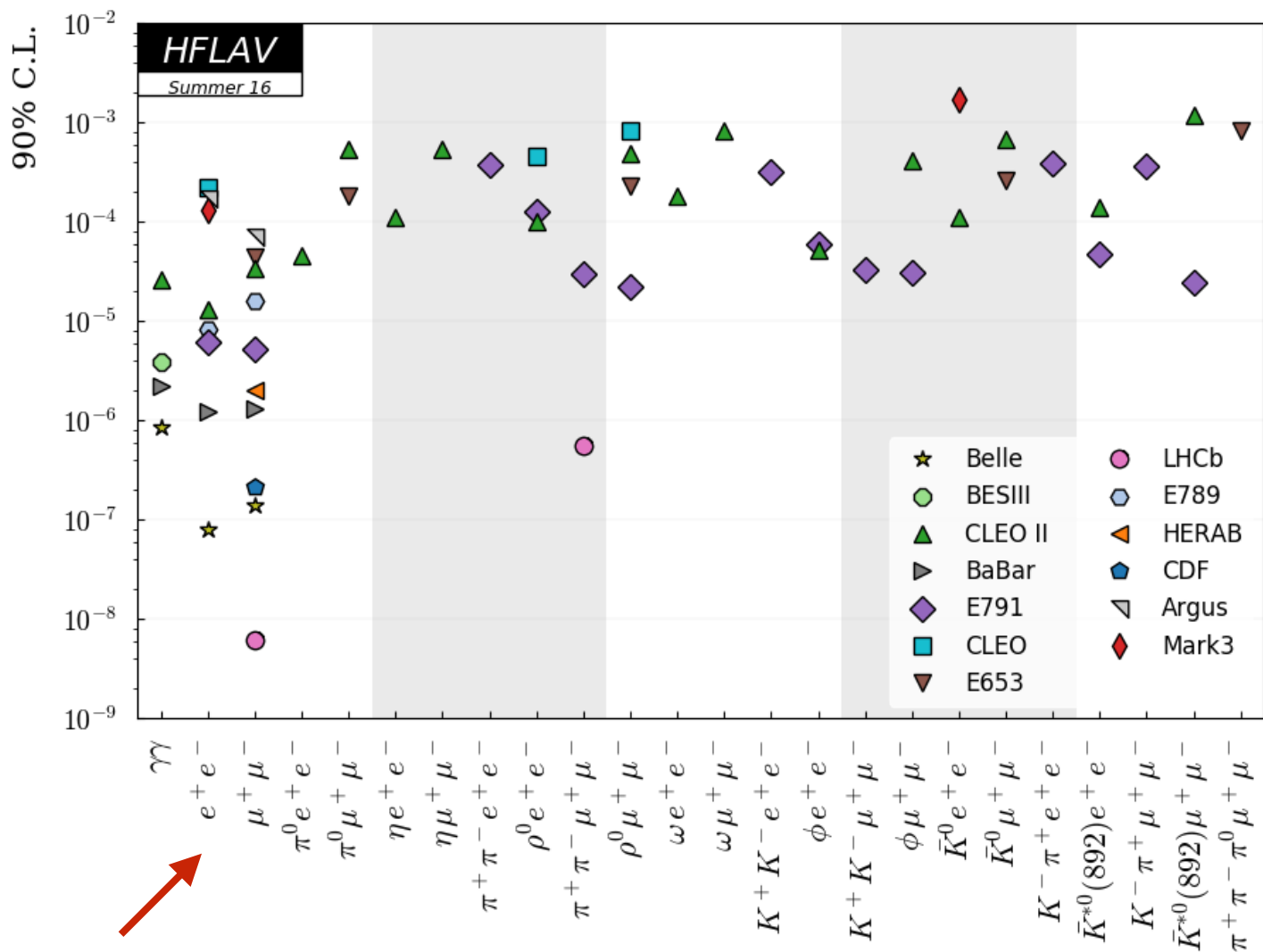
Fajfer, Kosnik, Prelovsek



★ Direct CP-violating asymmetries in  $D \rightarrow \pi\mu\mu$ ?

De Boer, Hiller (2016)

# Rare charm decays: experiment



# Any other ideas?

## ★ Two-body decays of B and D

- only one hadron to deal with: decay constant?
- **but**: probes limited number of operators, helicity suppression
  - e.g. not sensitive to vector-like New Physics (such as vector Z')
- soft photon effects preclude studies of **electron** decay modes:

$$\frac{\mathcal{B}(D^0 \rightarrow \gamma \ell^+ \ell^-)}{\mathcal{B}(D^0 \rightarrow \ell^+ \ell^-)} \propto \alpha \frac{m_D^2}{m_\ell^2}$$

## ★ Three-body decays of B and D

- probes several operators, many different observables
- **but**: two hadrons: four form-factors, hard to calculate non-perturbatively

- recent "issues" with lepton universality in B-decays  $R_K = \frac{\text{BR}(B \rightarrow K \mu^+ \mu^-)}{\text{BR}(B \rightarrow K e^+ e^-)}$   
 $= 0.745_{-0.074}^{+0.090}$  (stat)  $\pm 0.036$  (syst)

LHCb (2014)

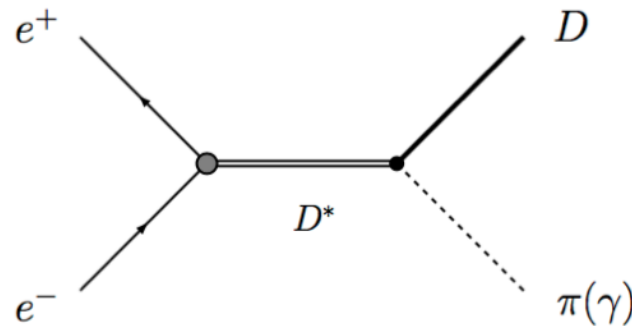
Can one remove helicity suppression AND enlarge the set of probed operators by studying electroweak decays of excited states of D or B (like D\* or B\*)?

**No, but...**

# Studies of $D^*(B^*) \rightarrow e^+e^-$ in resonance production

★ Instead of searching for a decay of  $D^*/B^*$ , let's produce it!

- resonant enhancement possible if  $e^+e^-$  energy is tuned to  $m_{D^*}(m_{B^*})$
- single heavy flavor + photon in the final state is a nice tag



Khodjamirian, Mannel, AAP  
JHEP 11 (2015) 142

- contrary to a usual way of studying FCNC, production cross section is small

★ This way, the FCNC branching ratio for  $D^*(2007) \rightarrow e^+e^-$  is probed

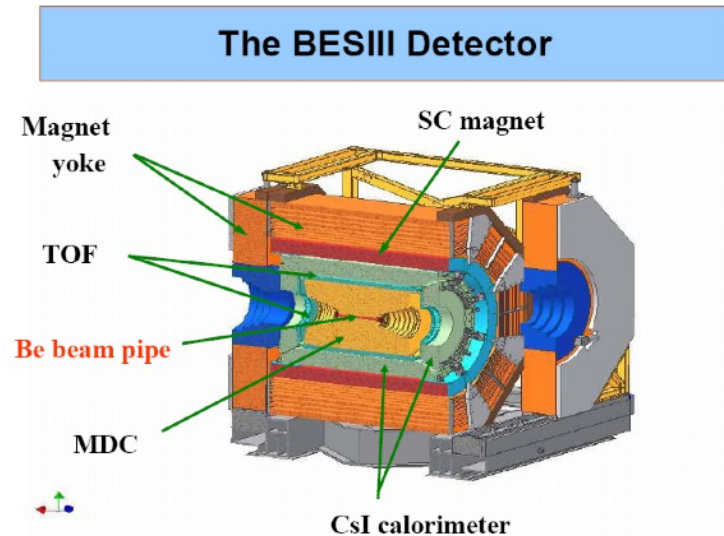
$$\sigma(e^+e^- \rightarrow D\pi)_{\sqrt{s} \simeq m_{D^*}} \equiv \sigma_{D^*}(s) = \frac{12\pi}{m_{D^*}^2} \mathcal{B}_{D^* \rightarrow e^+e^-} \mathcal{B}_{D^* \rightarrow D\pi} \frac{m_{D^*}^2 \Gamma_0^2}{(s - m_{D^*}^2)^2 + m_{D^*}^2 \Gamma_0^2},$$



# Studies of $D^*(B^*) \rightarrow e^+e^-$ in resonance production

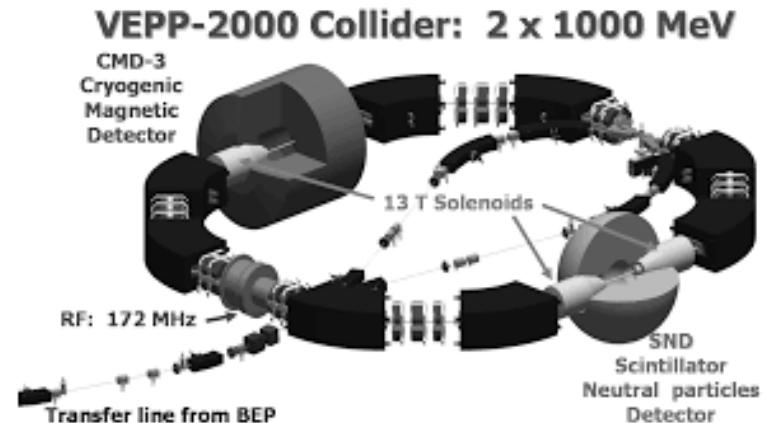
## ★ BEPCII machine with BESIII detector (China)

- optimized for  $\Psi(3770)$
- already made scans  $\sqrt{s} = 2.0 - 4.2$  GeV.
- luminosity is about  $5 \times 10^{31} \text{ cm}^{-2}\text{s}^{-1}$



## ★ VEPP-2000 machine (Novosibirsk, Russia)

- optimized for  $E_{CM} < 2000$  MeV
- possible upgrade to  $E_{CM} > 2000$  MeV
- luminosity is about  $1 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$



## ★ HIEPA: new tau-charm factory in Hefei (if approved)

- luminosity is about  $5 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$

# Studies of $D^*(B^*) \rightarrow e^+e^-$ in the Standard Model

★ Standard Model, short distance:

- local  $O_9$  and  $O_{10}$  operators

$$O_9 = \frac{e^2}{16\pi^2} (\tilde{Q}_1 + \tilde{Q}_7), \quad O_{10} = \frac{e^2}{16\pi^2} (\tilde{Q}_7 - \tilde{Q}_1)$$

- additional dipole contribution

$$H_{\text{eff}}^{(\gamma\gamma)} = \frac{4G_F}{\sqrt{2}} C_7^{\text{c,eff}} \left( \frac{e}{16\pi^2} m_c \bar{u}_L \sigma^{\mu\nu} c_R F_{\mu\nu} \right)$$

★ Decay amplitude depends on additional non-perturbative parameter

$$\langle 0 | \bar{u} \sigma^{\mu\nu} c | D^*(p) \rangle = i f_{D^*}^T (\epsilon^\mu p^\nu - p^\mu \epsilon^\nu)$$

Khodjamirian, Mannel, AAP  
JHEP 11 (2015) 142

★ Short-distance result is well-defined

$$\mathcal{B}_{D^* \rightarrow e^+e^-} = \frac{\alpha^2 G_F^2}{96\pi^3 \Gamma_0} m_{D^*}^3 f_{D^*}^2 \left( \left| C_9^{\text{c,eff}} + 2 \frac{m_c}{m_{D^*}} \frac{f_{D^*}^T}{f_{D^*}} C_7^{\text{c,eff}} \right|^2 + |C_{10}^{\text{c}}|^2 \right)$$

★ ... but the Br is small (the width is not though):  $\mathcal{B}_{D^* \rightarrow e^+e^-}^{SD} = \frac{\Gamma(D^* \rightarrow e^+e^-)}{\Gamma_0} \approx 2.0 \times 10^{-19}$

★ LD contributions are of the same order of magnitude or less!!!

No helicity suppression: no issues with testing lepton universality!

# D\*(B\*) → e+e-: example of NP contribution

- ★ A plethora of NP models that realize charm (beauty) FCNC interactions can be probed
  - consider a model with a Z' coupling to a left-handed FCNC quark currents

$$\begin{aligned} \mathcal{L}_{Z'} &= -g'_{Z'1} \bar{\ell}_L \gamma_\mu \ell_L Z'^\mu - g'_{Z'2} \bar{\ell}_R \gamma_\mu \ell_R Z'^\mu \\ &\quad - g_{Z'1}^{cu} \bar{u}_L \gamma_\mu c_L Z'^\mu - g_{Z'2}^{cu} \bar{u}_R \gamma_\mu c_R Z'^\mu. \end{aligned}$$

- ★ At low energies integrate out Z':

$$\mathcal{L}_{\text{eff}}^{Z'} = -\frac{1}{M_{Z'}^2} \left[ g'_{Z'1} g_{Z'1}^{cu} \tilde{Q}_1 + g'_{Z'1} g_{Z'2}^{cu} \tilde{Q}_2 + g'_{Z'2} g_{Z'2}^{cu} \tilde{Q}_6 + g'_{Z'2} g_{Z'1}^{cu} \tilde{Q}_7 \right]$$

- ★ ...which leads to a branching ratio (for  $g'_{Z'1} = \frac{g}{\cos \theta_W} \left( -\frac{1}{2} + \sin^2 \theta_W \right)$ ,  $g'_{Z'2} = \frac{g \sin^2 \theta_W}{\cos \theta_W}$ ),

$$\mathcal{B}_{D^* \rightarrow e^+ e^-}^{Z'} = \frac{\sqrt{2} G_F}{3\pi \Gamma_0} m_{D^*}^3 f_{D^*}^2 \frac{|g_{Z'1}^{cu}|^2}{M_{Z'}^2} \frac{M_Z^2}{M_{Z'}^2} \left( \frac{1}{4} - \sin^2 \theta_W + 2 \sin^4 \theta_W \right)$$

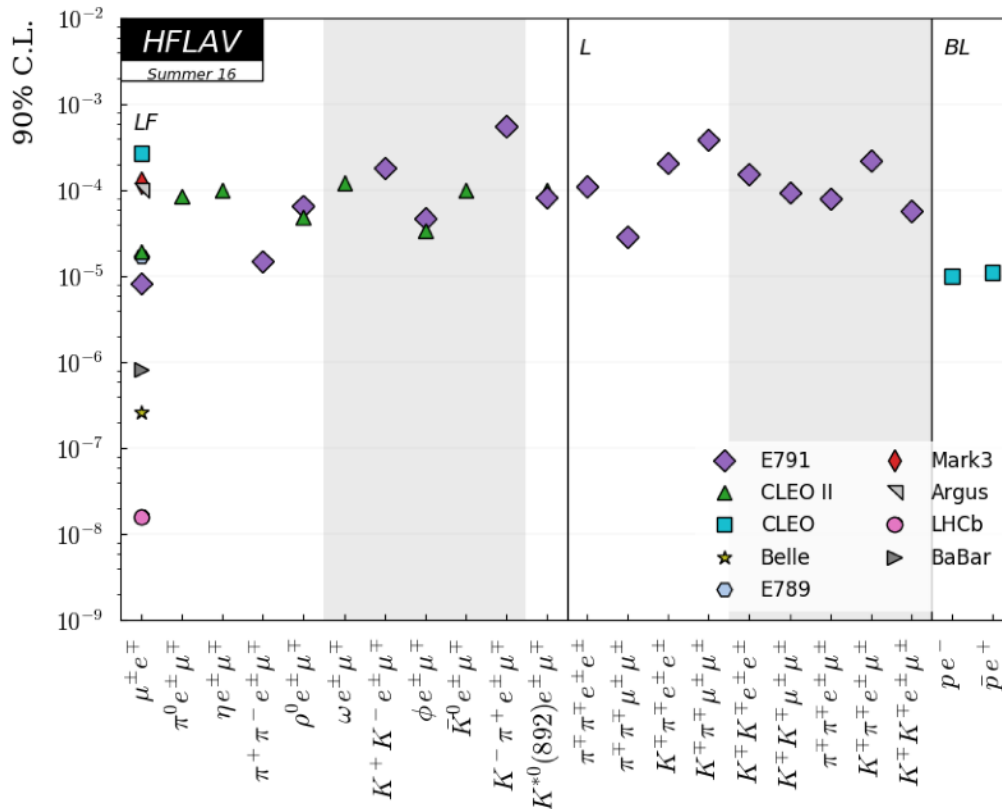
- ★ ... and current constraint of  $\mathcal{B}_{D^* \rightarrow e^+ e^-}^{Z'} < 2.5 \times 10^{-11}$

Plenty of room in the parameter space to constrain

# Studies of lepton flavor violation with charm

- To lift helicity suppression, add more particles to the final state:  $\gamma, \pi, \rho$ , e.g.

$$D^0 \rightarrow \gamma \mu^\pm e^\mp, D^0 \rightarrow \pi \mu^\pm e^\mp, D^0 \rightarrow \rho \mu^\pm e^\mp, \text{etc.}$$



D. Hazard and A.A.P., arXiv:1711.05314 [hep-ph]

- ... or consider other hadronic systems, e.g. LFV quarkonia decays  $M \rightarrow \ell_1 \bar{\ell}_2$  or  $M \rightarrow \gamma \ell_1 \bar{\ell}_2$

**Unfortunately, very scarce experimental data!**

D. Hazard and A.A.P., PRD94 (2016), 074023

# Studies of lepton flavor violation with charm

- ★ Multitude of NP operators: single operator dominance hypothesis (SODH)
  - but it is not often that only a single operator contributes, e.g. for quarkonia

$$\begin{aligned} \mathcal{L}_{lq} = & -\frac{1}{\Lambda^2} \sum_q \left[ \left( C_{VR}^q \bar{\ell}_1 \gamma^\mu P_R \ell_2 + C_{VL}^q \bar{\ell}_1 \gamma^\mu P_L \ell_2 \right) \bar{q} \gamma_\mu q \right. \\ & + \left( C_{AR}^q \bar{\ell}_1 \gamma^\mu P_R \ell_2 + C_{AL}^q \bar{\ell}_1 \gamma^\mu P_L \ell_2 \right) \bar{q} \gamma_\mu \gamma_5 q \\ & + m_2 m_q G_F \left( C_{SR}^q \bar{\ell}_1 P_R \ell_2 + C_{SL}^q \bar{\ell}_1 P_L \ell_2 \right) \bar{q} q \\ & \left. + m_2 m_q G_F \left( C_{PR}^q \bar{\ell}_1 P_R \ell_2 + C_{PL}^q \bar{\ell}_1 P_L \ell_2 \right) \bar{q} \gamma_5 q + h.c. \right] \end{aligned}$$

- Can (partially) do away with SODH if designer initial states are used

**Vector:** 
$$\mathcal{A}(V \rightarrow \ell_1 \bar{\ell}_2) = \bar{u}(p_1, s_1) \left[ A_V^{\ell_1 \ell_2} \gamma_\mu + B_V^{\ell_1 \ell_2} \gamma_\mu \gamma_5 + \frac{C_V^{\ell_1 \ell_2}}{m_V} (p_2 - p_1)_\mu + \frac{i D_V^{\ell_1 \ell_2}}{m_V} (p_2 - p_1)_\mu \gamma_5 \right] v(p_2, s_2) \epsilon^\mu(p).$$

**Scalar:** 
$$\mathcal{A}(S \rightarrow \ell_1 \bar{\ell}_2) = \bar{u}(p_1, s_1) [E_S^{\ell_1 \ell_2} + i F_S^{\ell_1 \ell_2} \gamma_5] v(p_2, s_2).$$

- No data (other than J/psi) exist!!!

$$\psi(2S) \rightarrow \gamma \chi_{c0}$$

D. Hazard and A.A.P., PRD94 (2016), 074023

# LFV pseudoscalar/scalar quarkonia decays

## ★ Constraints on Wilson coefficients of low energy operators

D. Hazard and A.A.P.,  
PRD94 (2016), 074023

Wilson coefficient	Leptons	Initial state					
	$\ell_1\ell_2$	$\eta_b$	$\eta_c$	$\eta(u/d)$	$\eta(s)$	$\eta'(u/d)$	$\eta'(s)$
$ C_{AL}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	...	...	FPS	FPS	FPS	FPS
	$e\tau$	...	...	FPS	FPS	FPS	FPS
	$e\mu$	...	...	$3 \times 10^{-3}$	$2 \times 10^{-3}$	$2.1 \times 10^{-1}$	$1.9 \times 10^{-1}$
$ C_{AR}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	...	...	FPS	FPS	FPS	FPS
	$e\tau$	...	...	FPS	FPS	FPS	FPS
	$e\mu$	...	...	$3 \times 10^{-3}$	$2 \times 10^{-3}$	$2.1 \times 10^{-1}$	$1.9 \times 10^{-1}$
$ C_{PL}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	...	...	FPS	FPS	FPS	FPS
	$e\tau$	...	...	FPS	FPS	FPS	FPS
	$e\mu$	...	...	$2 \times 10^3$	$1 \times 10^3$	$3.9 \times 10^4$	$3.6 \times 10^4$
$ C_{PR}^{q\ell_1\ell_2}/\Lambda^2 $	$\mu\tau$	...	...	FPS	FPS	FPS	FPS
	$e\tau$	...	...	FPS	FPS	FPS	FPS
	$e\mu$	...	...	$2 \times 10^3$	$1 \times 10^3$	$3.9 \times 10^4$	$3.6 \times 10^4$

★ More data is needed: use radiative decays:  $\mathcal{B}(V \rightarrow \gamma \ell_1 \bar{\ell}_2) = \mathcal{B}(V \rightarrow \gamma M) \mathcal{B}(M \rightarrow \ell_1 \bar{\ell}_2)$

$$\mathcal{B}(\psi(2S) \rightarrow \gamma \chi_{c0}(1P)) = 9.99 \pm 0.27\%,$$

$$\mathcal{B}(\psi(3770) \rightarrow \gamma \chi_{c0}(1P)) = 0.73 \pm 0.09\%.$$

$$\mathcal{B}(J/\psi \rightarrow \gamma \eta_c) = 1.7 \pm 0.4\%,$$

$$\mathcal{B}(\psi(2S) \rightarrow \gamma \eta_c) = 0.34 \pm 0.05\%.$$

$$\mathcal{B}(\Upsilon(2S) \rightarrow \gamma \chi_{b0}(1P)) = 3.8 \pm 0.4\%,$$

$$\mathcal{B}(\Upsilon(3S) \rightarrow \gamma \chi_{b0}(1P)) = 0.27 \pm 0.04\%,$$

$$\mathcal{B}(\Upsilon(3S) \rightarrow \gamma \chi_{b0}(2P)) = 5.9 \pm 0.6\%.$$

# LFV pseudoscalar/scalar decays

★ Very scarce LFV experimental data available P/S → μe, τe, etc.

- no data for pseudoscalar heavy-flavored meson decays
- no data for any scalar meson decays
- maybe use B-decays?

$\ell_1 \ell_2$	$e\mu$
$\mathcal{B}(\eta \rightarrow \ell_1 \ell_2)$	$6 \times 10^{-6}$
$\mathcal{B}(\eta' \rightarrow \ell_1 \ell_2)$	$4.7 \times 10^{-4}$
$\mathcal{B}(\pi^0 \rightarrow \ell_1 \ell_2)$	$3.6 \times 10^{-10}$

$$P = \eta_b, \eta_c, \eta^{(\prime)}, \dots$$

$$S = \chi_{b0}, \chi_{c0}, \dots$$

★ Constraints are available for quark off-diagonal currents from B/D → μe, τe, etc.

$\ell_1 \ell_2$	$\mu\tau$	$e\tau$	$e\mu$
$\mathcal{B}(B_d^0 \rightarrow \ell_1 \ell_2)$	$2.2 \times 10^{-5}$	$2.8 \times 10^{-5}$	$1.0 \times 10^{-9}$
$\mathcal{B}(B_s^0 \rightarrow \ell_1 \ell_2)$	...	...	$5.4 \times 10^{-9}$
$\mathcal{B}(\bar{D}^0 \rightarrow \ell_1 \ell_2)$	FPS	...	$1.3 \times 10^{-8}$
$\mathcal{B}(K_L^0 \rightarrow \ell_1 \ell_2)$	FPS	FPS	$4.7 \times 10^{-12}$

D. Hazard and A.A.P., PRD94 (2016), 074023  
D. Hazard and A.A.P., arXiv:1711.05314

# 3. Rare D(B)-decays with missing energy

➤ D-decays with missing energy can probe both heavy and light (DM) NP

★ SM process:  $D \rightarrow \nu\bar{\nu}$  and  $D \rightarrow \nu\bar{\nu}\gamma$ :

- for B-decays  $J_{Qq}^\mu = \bar{q}_L \gamma^\mu b_L$
- for D-decays  $J_{Qq}^\mu = \bar{u}_L \gamma^\mu c_L$

$$\mathcal{B}(D^0 \rightarrow \text{inv}) < 9.4 \times 10^{-5} \quad \text{Belle (2017)}$$

★ For  $B(D) \rightarrow \nu\bar{\nu}$  decays SM branching ratios are tiny

- SM decay is helicity suppressed, e.g.

$$\mathcal{B}(D^0 \rightarrow \nu\bar{\nu}) = \frac{G_F^2 \alpha^2 f_D^2 m_D^3}{16\pi^3 \sin^4 \theta_W \Gamma_{D^0}} |V_{bc} V_{ub}^*|^2 X(x_b)^2 x_\nu^2$$

- NP: other ways of flipping helicity?
- add a third particle to the final state?

What would happen if a photon is added to the final state?

★ For  $B(D) \rightarrow \nu\bar{\nu}\gamma$  decays SM branching ratios are still tiny

- need form-factors to describe the transition
- helicity suppression is lifted

★ BUT: missing energy does not always mean neutrinos

- nice constraints on light Dark Matter properties!!!

Decay	Branching ratio
$B_s \rightarrow \nu\bar{\nu}$	$3.07 \times 10^{-24}$
$B_d \rightarrow \nu\bar{\nu}$	$1.24 \times 10^{-25}$
$D^0 \rightarrow \nu\bar{\nu}$	$1.1 \times 10^{-30}$

Decay	Branching ratio
$B_s \rightarrow \nu\bar{\nu}\gamma$	$3.68 \times 10^{-8}$
$B_d \rightarrow \nu\bar{\nu}\gamma$	$1.96 \times 10^{-9}$
$D^0 \rightarrow \nu\bar{\nu}\gamma$	$3.96 \times 10^{-14}$

A. Badin, AAP (2010)

B. Bhattacharya, C. Grant, AAP (2018)



# Rare D(B)-decays: scalar DM

➤ Let us discuss B and D-decays simultaneously: physics is similar

Badin, AAP (2010)

★ **Generic interaction Lagrangian:**  $\mathcal{H}_{eff} = \sum_i \frac{2C_i^{(s)}}{\Lambda^2} O_i$

- respective neutral currents for B-and D-decays

$$O_1 = m_Q (J_{Qq})_{RL} (\chi_0^* \chi_0)$$

$$O_2 = m_Q (J_{Qq})_{LR} (\chi_0^* \chi_0)$$

$$O_3 = (J_{Qq}^\mu)_{LL} (\chi_0^* \overleftrightarrow{\partial}_\mu \chi_0)$$

$$O_4 = (J_{Qq}^\mu)_{RR} (\chi_0^* \overleftrightarrow{\partial}_\mu \chi_0)$$

★ **Scalar DM does not exhibit helicity suppression**

- B(D) → E<sub>mis</sub> is more powerful than B(D) → E<sub>mis</sub> γ

$$\mathcal{B}(D^0 \rightarrow \chi_0 \chi_0) = \frac{(C_1^{(s)} - C_2^{(s)})^2}{4\pi M_D \Gamma_D} \left( \frac{f_D M_D^2 m_c}{\Lambda^2 (m_c + m_u)} \right)^2 \sqrt{1 - 4x_\chi^2}$$

$$\frac{(C_1^{(s)} - C_2^{(s)})}{\Lambda^2} \leq 8 \times 10^{-8}$$

$$\begin{aligned} \mathcal{B}(D^0 \rightarrow \chi_0^* \chi_0 \gamma) &= \frac{f_D^2 \alpha C_3^{(s)} C_4^{(s)} M_D^5}{6\Lambda^4 \Gamma_D} \left( \frac{F_D}{4\pi} \right)^2 \\ &\times \left( \frac{1}{6} \sqrt{1 - 4x_\chi^2} (1 - 16x_\chi^2 - 12x_\chi^4) - 12x_\chi^4 \log \frac{2x_\chi}{1 + \sqrt{1 - 4x_\chi^2}} \right) \end{aligned}$$

$$\frac{C_3^{(s)}}{\Lambda^2} \frac{C_4^{(s)}}{\Lambda^2} \leq 1.55 \times 10^{-12} \text{ GeV}^{-4} \quad \text{for } m = 0,$$

$$\frac{C_3^{(s)}}{\Lambda^2} \frac{C_4^{(s)}}{\Lambda^2} \leq 7.44 \times 10^{-11} \text{ GeV}^{-4} \quad \text{for } m = 0.4 \times M_{B_d}$$

These general bounds translate into constraints onto constraints for particular models

# Example of a particular model of scalar DM

★ Several different models of light scalar DM

- simplest: singlet scalar DM
- more sophisticated - less restrictive

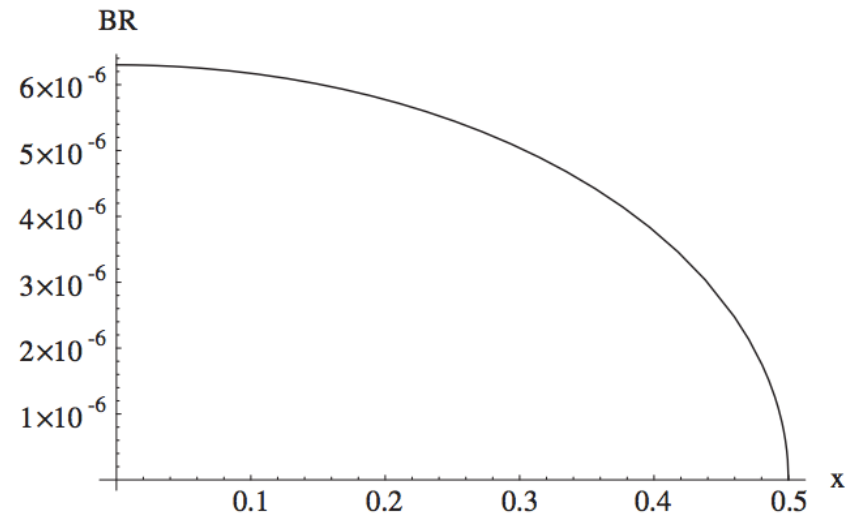
$$\begin{aligned}
 - \mathcal{L}_S &= \frac{\lambda_S}{4} S^4 + \frac{m_0^2}{2} S^2 + \lambda S^2 H^\dagger H \\
 &= \frac{\lambda_S}{4} S^4 + \frac{1}{2} (m_0^2 + \lambda v_{EW}^2) S^2 + \lambda v_{EW} S^2 h \\
 &\quad + \frac{\lambda}{2} S^2 h^2,
 \end{aligned}$$

★ B(D) decays rate in this model

$$\begin{aligned}
 \mathcal{B}(B_q \rightarrow SS) &= \left[ \frac{3g_w^2 V_{ib} V_{iq}^* x_t m_b}{128\pi^2} \right]^2 \frac{\sqrt{1 - 4x_S^2}}{16\pi M_B \Gamma_{B_q}} \left( \frac{\lambda^2}{M_H^4} \right) \\
 &\quad \times \left( \frac{f_{B_q} M_{B_q}^2}{m_b + m_q} \right)^2,
 \end{aligned}$$

- fix  $\lambda$  from relic density

$$\sigma_{\text{ann}} v_{\text{rel}} = \frac{8v_{EW}^2 \lambda^2}{M_H^2} \times \lim_{m_{h^*} \rightarrow 2m_S} \frac{\Gamma_{h^* X}}{m_{h^*}}$$



These results are complimentary to constraints from quarkonium decays with missing energy

# Rare D(B)-decays: fermionic DM

- ★ **Generic interaction Lagrangian:**  $\mathcal{H}_{eff} = \sum_i \frac{4C_i}{\Lambda^2} O_i$
- respective neutral currents for B-and D-decays
- $$O_1 = \left( J_{Qq}^\mu \right)_{LL} (\bar{\chi}_{1/2L} \gamma_\mu \chi_{1/2L})$$
- $$O_2 = \left( J_{Qq}^\mu \right)_{LL} (\bar{\chi}_{1/2R} \gamma_\mu \chi_{1/2R})$$
- $$O_3 = O_{1(L \leftrightarrow R)}, \quad O_4 = O_{2(L \leftrightarrow R)}$$
- $$O_5 = (J_{Qq})_{LR} (\bar{\chi}_{1/2L} \chi_{1/2R})$$
- $$O_6 = (J_{Qq})_{LR} (\bar{\chi}_{1/2R} \chi_{1/2L})$$
- $$O_7 = O_{5(L \leftrightarrow R)}, \quad O_8 = O_{6(L \leftrightarrow R)}$$
- + tensor operators

★ **Scalar DM does exhibit helicity suppression**

- B(D)  $\rightarrow$  E<sub>mis</sub> maybe less powerful than B(D)  $\rightarrow$  E<sub>mis</sub>  $\gamma$
- ... but it really depends on the DM mass!

Badin, AAP

$$\mathcal{B}(B_q \rightarrow \bar{\chi}_{1/2} \chi_{1/2}) = \frac{f_{B_q}^2 M_{B_q}^3}{16\pi \Gamma_{B_q} \Lambda^2} \sqrt{1 - 4x_\chi^2}$$

$$\times \left[ C_{57} C_{68} \frac{4M_{B_q}^2 x_\chi^2}{(m_b + m_q)^2} - (C_{57}^2 + C_{68}^2) \right]$$

$$\times \frac{M_{B_q}^2 (2x_\chi^2 - 1)}{(m_b + m_q)^2} - 2\tilde{C}_{1-8} \frac{x_\chi M_{B_q}}{m_b + m_q}$$

$$+ 2(C_{13} + C_{24})^2 x_\chi^2 \Big],$$

Lots of operators — less so in particular models

# Rare D(B)-decays: fermionic DM

★ Constraints from B decays are the best at the moment

TABLE I. Constraints (upper limits) on the Wilson coefficients of operators of Eq. (43) from the  $B_q \rightarrow \chi_{1/2} \bar{\chi}_{1/2}$  transition. Note that operators  $Q_9$ – $Q_{12}$  give no contribution to this decay.

$x_\chi$	$C_1/\Lambda^2, \text{ GeV}^{-2}$	$C_2/\Lambda^2, \text{ GeV}^{-2}$	$C_3/\Lambda^2, \text{ GeV}^{-2}$	$C_4/\Lambda^2, \text{ GeV}^{-2}$	$C_5/\Lambda^2, \text{ GeV}^{-2}$	$C_6/\Lambda^2, \text{ GeV}^{-2}$	$C_7/\Lambda^2, \text{ GeV}^{-2}$	$C_8/\Lambda^2, \text{ GeV}^{-2}$
0	...	...	...	...	$2.3 \times 10^{-8}$	$2.3 \times 10^{-8}$	$2.3 \times 10^{-8}$	$2.3 \times 10^{-8}$
0.1	$1.9 \times 10^{-7}$	$1.9 \times 10^{-7}$	$1.9 \times 10^{-7}$	$1.9 \times 10^{-7}$	$2.3 \times 10^{-8}$	$2.3 \times 10^{-8}$	$2.3 \times 10^{-8}$	$2.3 \times 10^{-8}$
0.2	$9.7 \times 10^{-8}$	$9.7 \times 10^{-8}$	$9.7 \times 10^{-8}$	$9.7 \times 10^{-8}$	$2.5 \times 10^{-8}$	$2.5 \times 10^{-8}$	$2.5 \times 10^{-8}$	$2.5 \times 10^{-8}$
0.3	$6.9 \times 10^{-8}$	$6.9 \times 10^{-8}$	$6.9 \times 10^{-8}$	$6.9 \times 10^{-8}$	$2.8 \times 10^{-8}$	$2.8 \times 10^{-8}$	$2.8 \times 10^{-8}$	$2.8 \times 10^{-8}$
0.4	$6.0 \times 10^{-8}$	$6.0 \times 10^{-8}$	$6.0 \times 10^{-8}$	$6.0 \times 10^{-8}$	$3.6 \times 10^{-8}$	$3.6 \times 10^{-8}$	$3.6 \times 10^{-8}$	$3.6 \times 10^{-8}$

★ ... the same is true for the radiative decays with missing energy

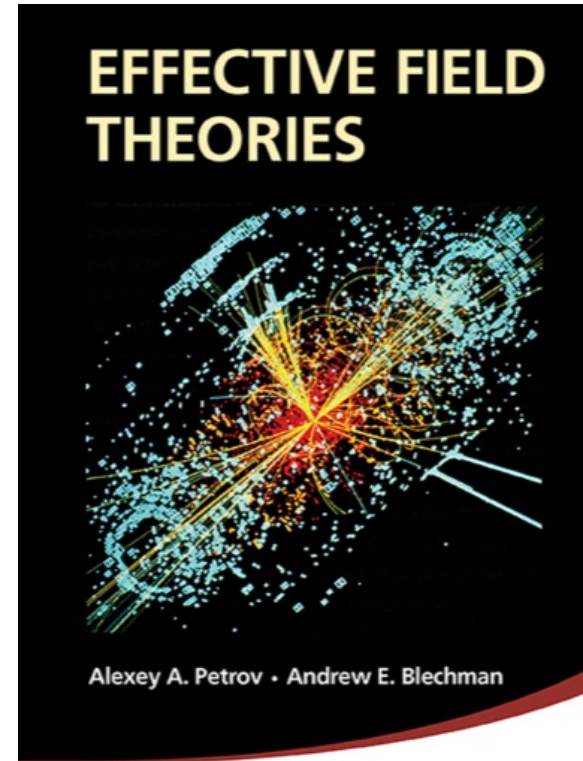
TABLE II. Constraints (upper limits) on the Wilson coefficients of operators of Eq. (43) from the  $B_q \rightarrow \chi_{1/2} \bar{\chi}_{1/2} \gamma$  transition. Note that operators  $Q_5$ – $Q_8$  give no contribution to this decay.

$x_\chi$	$C_1/\Lambda^2, \text{ GeV}^{-2}$	$C_2/\Lambda^2, \text{ GeV}^{-2}$	$C_3/\Lambda^2, \text{ GeV}^{-2}$	$C_4/\Lambda^2, \text{ GeV}^{-2}$
0	$6.3 \times 10^{-7}$	$6.3 \times 10^{-7}$	$6.3 \times 10^{-7}$	$6.3 \times 10^{-7}$
0.1	$7.0 \times 10^{-7}$	$7.0 \times 10^{-7}$	$7.0 \times 10^{-7}$	$7.0 \times 10^{-7}$
0.2	$9.2 \times 10^{-7}$	$9.2 \times 10^{-7}$	$9.2 \times 10^{-7}$	$9.2 \times 10^{-7}$
0.3	$1.5 \times 10^{-6}$	$1.5 \times 10^{-6}$	$1.5 \times 10^{-6}$	$1.5 \times 10^{-6}$
0.4	$3.4 \times 10^{-6}$	$3.4 \times 10^{-6}$	$3.4 \times 10^{-6}$	$3.4 \times 10^{-6}$

These general bounds translate into constraints onto constraints for particular models

## 4. Things to take home

- Indirect probes for new physics compete well with direct searches
  - for some observables sensitive to scales way above LHC
- Computational techniques for heavy flavors are well-established
  - but don't always work well: "heavy-quark-expansion" techniques for charm often miss threshold effects
  - "hadronic" techniques that sum over large number of intermediate states can be used, BUT one cannot use current experimental data on D-decays
- Calculations of New Physics contributions to mixing are in better shape
- Can correlate mixing and rare decays with New Physics models
  - signals in B/D-mixing vs B/D rare decays help differentiate among models
- New reach:  $D^*(B^*) \rightarrow e^+e^-$  can be studied with resonance production
  - plenty of parameter space for New Physics reach
  - probes models that  $D(B) \rightarrow e^+e^-/\mu^+\mu^-$  are not sensitive to
- Rare decays with missing energy provide excellent opportunities to constrain parameters of models with light Dark Matter
  - both scalar and fermionic DM models can be constrained



 World Scientific

# Rare radiative decays of charm I

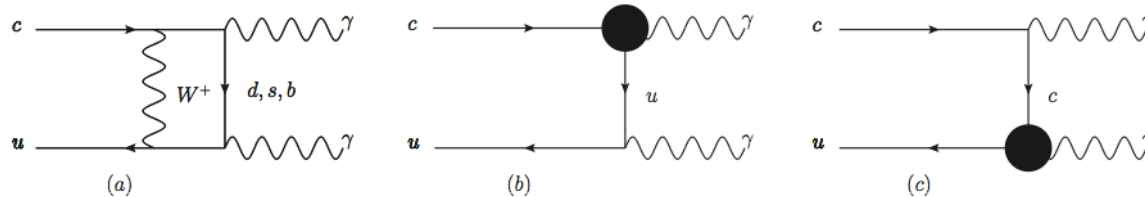
## ★ Standard Model contribution to $D \rightarrow \gamma\gamma$

$$A(D \rightarrow \gamma\gamma) = \epsilon_{1\mu}\epsilon_{2\nu} \left[ A_{PC}\epsilon^{\mu\nu\alpha\beta}k_{1\alpha}k_{2\beta} + iA_{PV} \left( g^{\mu\nu} - \frac{k_2^\mu k_1^\nu}{k_1 \cdot k_2} \right) \right]$$

$$\Gamma(D \rightarrow \gamma\gamma) = \frac{m_D^3}{64\pi} \left[ |A_{PC}|^2 + \frac{4}{m_D^4} |A_{PV}|^2 \right]$$

## ★ Short distance analysis

$$\mathcal{L} = -\frac{G_f}{\sqrt{2}}V_{us}V_{cs}^*C_{7\gamma}^{eff}\frac{e}{4\pi^2}F_{\mu\nu}m_c(\bar{u}\sigma^{\mu\nu}\frac{1}{2}(1+\gamma_5)c)$$



- only one operator contributes

- including QCD corrections, SD effects amount to  $\text{Br} = (3.6-8.1)\times 10^{-12}$

Paul, Bigi, Recksiegel (2011)

## ★ Long distance analysis

- long distance effects amount to  $\text{Br} = (1-3)\times 10^{-8}$

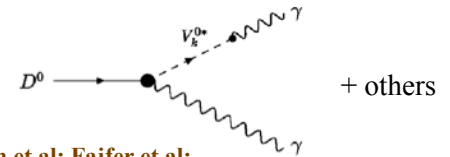
Burdman, Golowich, Hewett, Pakvasa (02);  
Fajfer, Singer, Zupan (01)

# Rare radiative decays of charm II

- Hope to isolate penguin-like contribution: BUT SM GIM is very effective
  - SM penguin contributions are expected to be small

★ Radiative decays  $D \rightarrow \gamma X$ ,  $\gamma\gamma$ : FCNC transition  $c \rightarrow u \gamma$

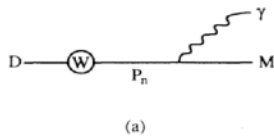
$$Q_7 = \frac{e}{8\pi^2} m_c F_{\mu\nu} \bar{u} \sigma^{\mu\nu} (1 + \gamma_5) c,$$



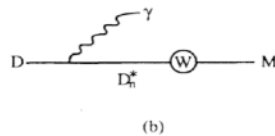
Burdman et al; Fajfer et al;  
Greub, Hurth, Misiak, Wyler

- SM contribution is dominated by LD effects
- dominated by SM anyway: useless for NP studies?

★ Examples of long-distance contributions

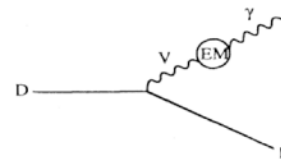


(a)



(b)

pole amplitudes (WA/WS)



VMD amplitudes



# Rare radiative decays of charm II

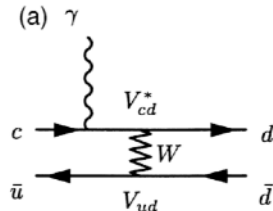
★ Theoretical predictions and experimental bounds ( $\times 10^5$ )

$D \rightarrow V\gamma$	Burdman et al	Fajfer et al	Khodjamirian et al
$D_s^+ \rightarrow \rho^+\gamma$	6–38	20–80	4.4
$D^0 \rightarrow \bar{K}^{*0}\gamma$	7–12	6–36	0.18
$D^0 \rightarrow \rho^0\gamma$	0.1–0.5	0.1–1	0.38
$D^0 \rightarrow \omega^0\gamma$	$\simeq 0.2$	0.1–0.9	—
$D^0 \rightarrow \phi^0\gamma$	0.1–3.4	0.4–0.9	—
$D^+ \rightarrow \rho^+\gamma$	2–6	0.4–6.3	0.43
$D_s^+ \rightarrow K^{*+}\gamma$	0.8–3	1.2–5.1	—

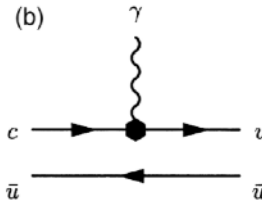
# Rare radiative decays of charm II

★ Try to find combinations of decays where LD contributions cancel

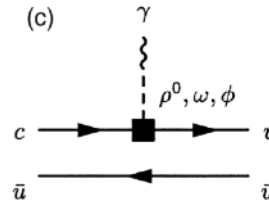
★ Consider exclusive decays  $D \rightarrow \gamma Q, \gamma \omega$ :  $\omega^{(I=0)} = \frac{1}{\sqrt{2}}(\bar{u}u + \bar{d}d)$ ,  $\rho^{(I=1)} = \frac{1}{\sqrt{2}}(\bar{u}u - \bar{d}d)$



$$V_{cd}^* V_{ud} \sim \lambda$$



$$V_{cb}^* V_{ub} \sim \lambda^5$$



+ QCD penguins and diagrams with photon emission from spectators

- Extract  $c \rightarrow uu \gamma$ : LD contribution cancels in  $R_{uu\gamma} = \frac{\Gamma(D^0 \rightarrow \omega\gamma) - \Gamma(D^0 \rightarrow \rho\gamma)}{\Gamma(D^0 \rightarrow \omega\gamma)}$

- Consider **isospin** asymmetries  $R_I = \frac{2\Gamma(D^0 \rightarrow \rho^0\gamma) - \Gamma(D^+ \rightarrow \rho^+\gamma)}{2\Gamma(D^0 \rightarrow \rho^0\gamma) + \Gamma(D^+ \rightarrow \rho^+\gamma)}$  (same with omega)

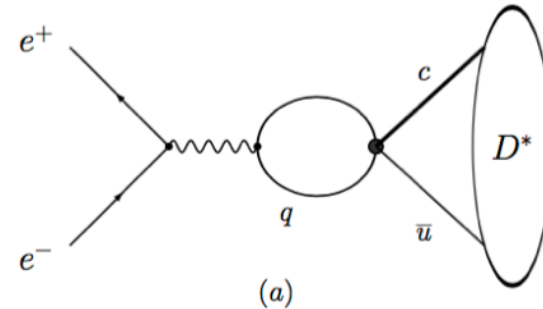
- isospin asymmetries are sensitive to 4-fermion operators with photon emissions from "spectators"

# Studies of $D^*(B^*) \rightarrow e^+e^-$ in the Standard Model

★ Standard Model, long distance:

- local  $O_1$  and  $O_2$  operators
- additional penguin-like contribution

★ Decay amplitude:



$$\langle e^+ e^- | \mathcal{H}_w | D^*(p) \rangle = -e^2 \bar{u}(p_-, s_-) \gamma^\mu v(p_+, s_+) \left( \frac{\Sigma_\mu(p^2)}{p^2} \right) \Big|_{p^2=m_{D^*}^2}$$

$$\text{with } \Sigma_\mu(p^2) = i \int d^4x e^{ip \cdot x} \langle 0 | T \{ j_\mu^{em}(x) \mathcal{H}_w(0) \} | D^*(p) \rangle$$

$$\Sigma_\mu^{(a)}(p^2) = \frac{G_F}{\sqrt{2}} \sum_{q=d,s} Q_q \left( C_1^{c(q)} + \frac{C_2^{c(q)}}{N_c} \right) \left\{ i \int d^4x e^{ip \cdot x} \langle 0 | T \{ \bar{q} \gamma_\mu q(x) \bar{q} \gamma_\nu q(0) \} | 0 \rangle \right\} \\ \times \langle 0 | \bar{u} \gamma^\nu c | D^*(p) \rangle,$$

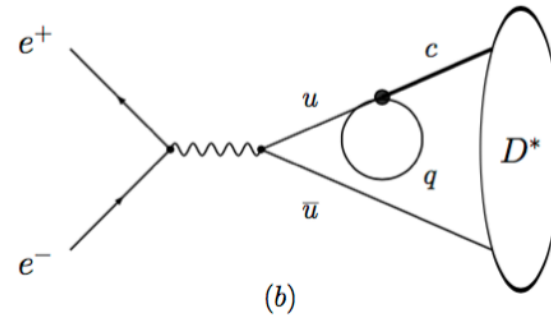
$$\Pi_{\mu\nu}^{(q)}(p) = (-g_{\mu\nu} p^2 + p_\mu p_\nu) \Pi^{(q)}(p^2)$$

$$\Pi^{(q)}(p^2) = \frac{p^2}{12\pi^2 Q_q^2} \int_0^\infty ds \frac{R^{(q)}(s)}{s(s-p^2-i\epsilon)} \quad \text{with} \quad R(s) \equiv \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)} = \sum_{q=u,d,s} R^{(q)}(s)$$

# Studies of $D^*(B^*) \rightarrow e^+e^-$ in the Standard Model

★ Standard Model, long distance:

- local  $O_1$  and  $O_2$  operators
- additional penguin-like contribution



★ As a result:

$$\mathcal{B}_{D^* \rightarrow e^+e^-}^{LD,A} \simeq \begin{cases} 4.7 \times 10^{-20} & \text{(NLO)} \\ 5.7 \times 10^{-18} & \text{(LO)} \end{cases} \quad \mathcal{B}_{D^* \rightarrow e^+e^-}^{(LD,b)} \geq (0.1 - 5.0) \times 10^{-19}$$

... and recall that the short distance  $\mathcal{B}_{D^* \rightarrow e^+e^-}^{SD} \approx 2.0 \times 10^{-19}$

★ Overall, the Standard Model contribution to  $D^* \rightarrow e^+e^-$  is rather small, but

- it is four orders of magnitude higher than the  $\text{Br}(D \rightarrow e^+e^-)$ !
- the long-distance contribution is moderate
- there is a large window to probe New Physics, as e.g. with BES-III

$$\mathcal{B}_{D^* \rightarrow e^+e^-} > 4 \times 10^{-13}$$

Khodjamirian, Mannel, AAP (2015)

Any interesting New Physics scenarios?