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Experimental Status of Conventional Charmonium Spectroscopy

Xiongfei Wang(王雄飞), Xinchou Lou

IHEP, CAS

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BESIII



KEDR



Outline

■ Introduction

- Conventional charmonium spectroscopy (CCS)
- Experimental apparatus

■ Recent CCS results

- J/ψ and $\psi(2S)$ resonance parameters
- $\chi_{cJ}(1P)$ resonance parameters
- $\eta_c(1S)$ resonance parameters
- Observations of $X(3823)$ and $X^*(3860)$

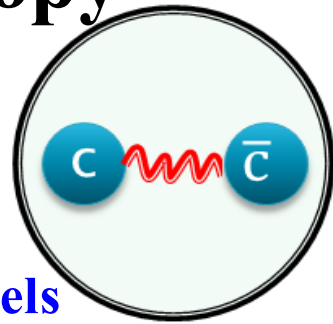
■ Summary

Conventional Charmonium Spectroscopy

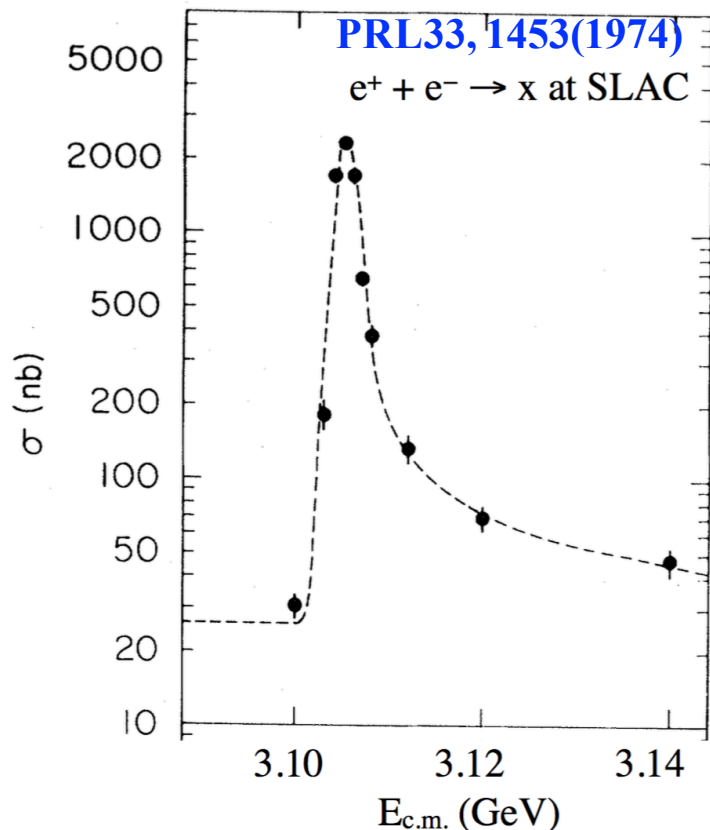
■ Nonrelativistic $c\bar{c}$ bound states

- J/ψ (1^3S_1) is the first member with $J^{PC} = 1^{--}$, other shown in right plots like $\psi(2S)$, $\psi(1D)$, *etc.*.

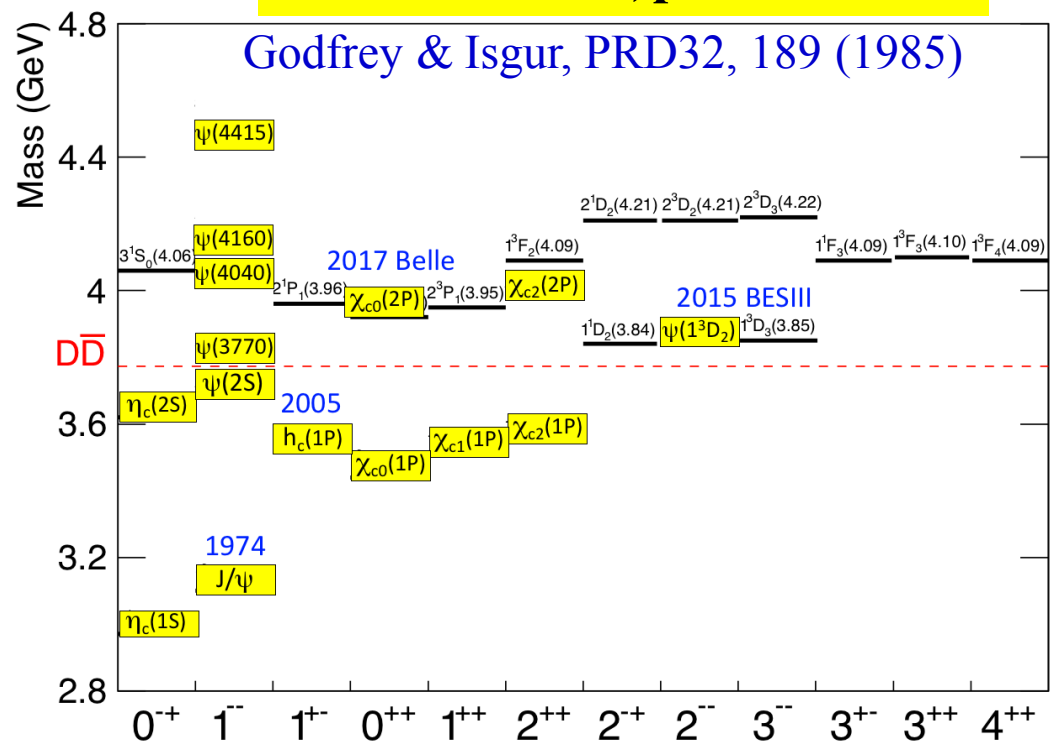
- Observations are consistent with predictions from potential models and L-QCD in describing spectra & onium properties!



November (1974) Revolution

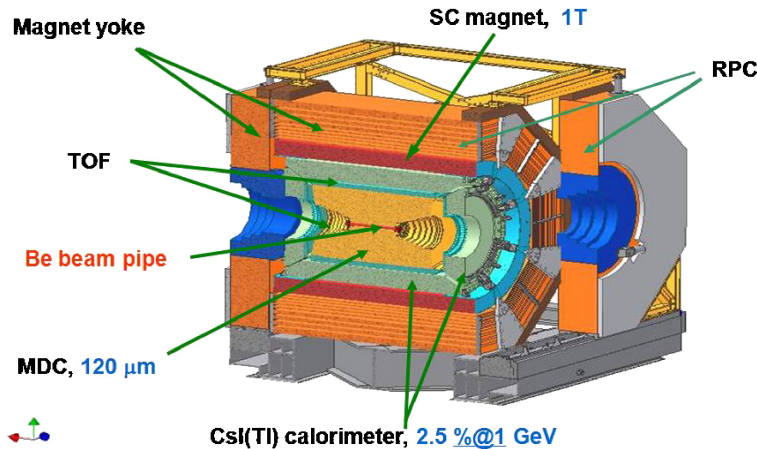


Discovered, predicted

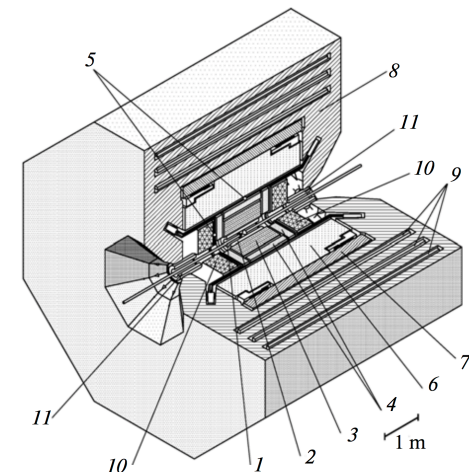


Experimental apparatus

BESIII experiment designed for studying in tau-c physics region (NIMA614 (2010) 345-399)

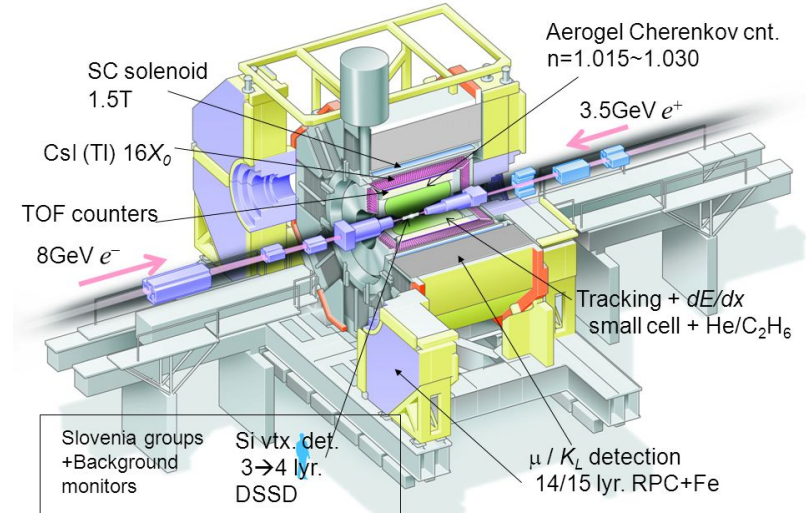


KEDR experiment designed for studying the c , b quarks and two photon physics (PPN, 2013, Vol. 44, No. 4, pp. 657–702)

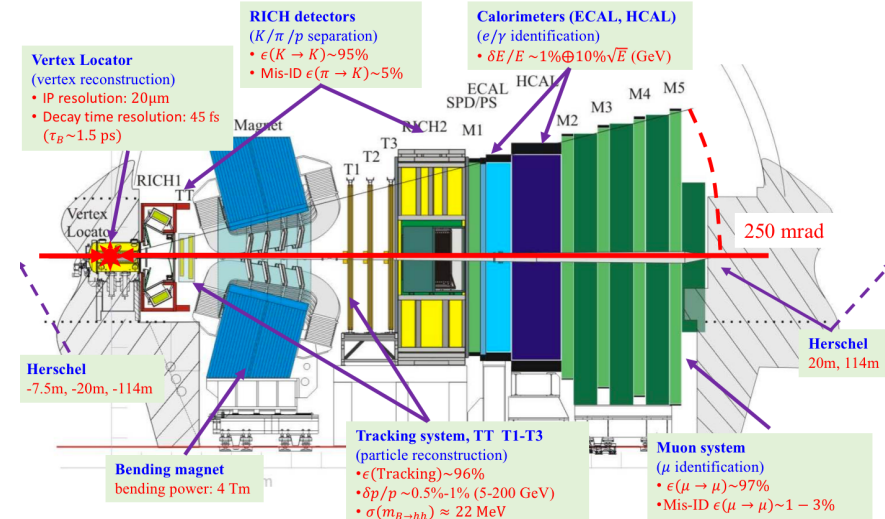


The central part of the KEDR detector: vacuum chamber of the collider (1); vertex detector (2); drift chamber (3); aerogel threshold Cherenkov counters (4); time of flight counters (5); liquid krypton barrel calorimeter (6); superconductive solenoid (7); magnet yoke (8); muon chambers (9); endcap CsI calorimeter (10); compensating coil (11).

Belle experiment designed for studying rare B-meson decay at $\Upsilon(4S)$ resonance (NIMA479(2002) 117-232)



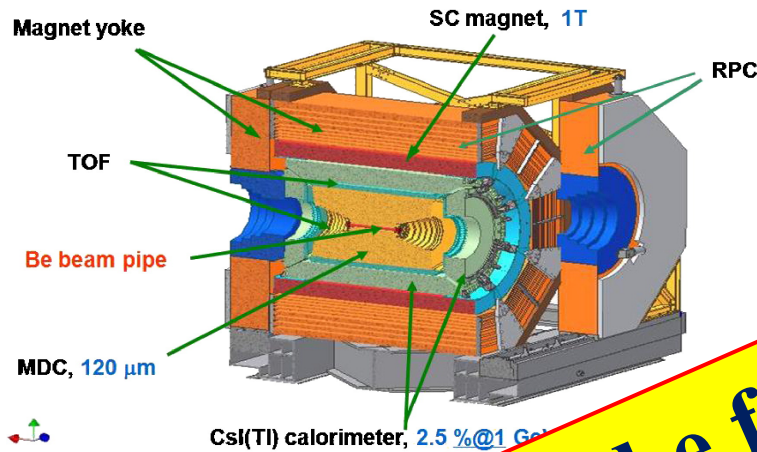
LHCb experiment aiming for precision measurements in b , c sectors. (JINT3(2008)S08005)



Experimental apparatus

BESIII experiment designed for studying in tau-c physics region (NIMA614 (2010) 345-399)

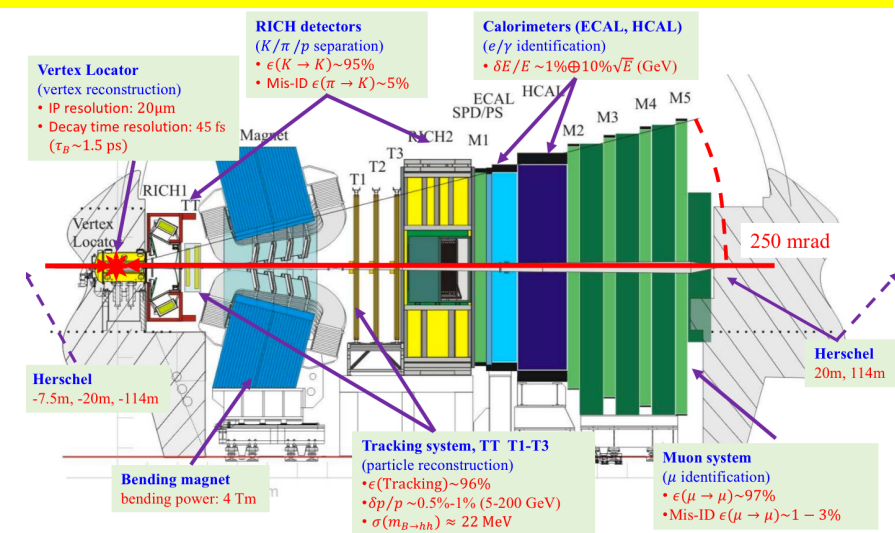
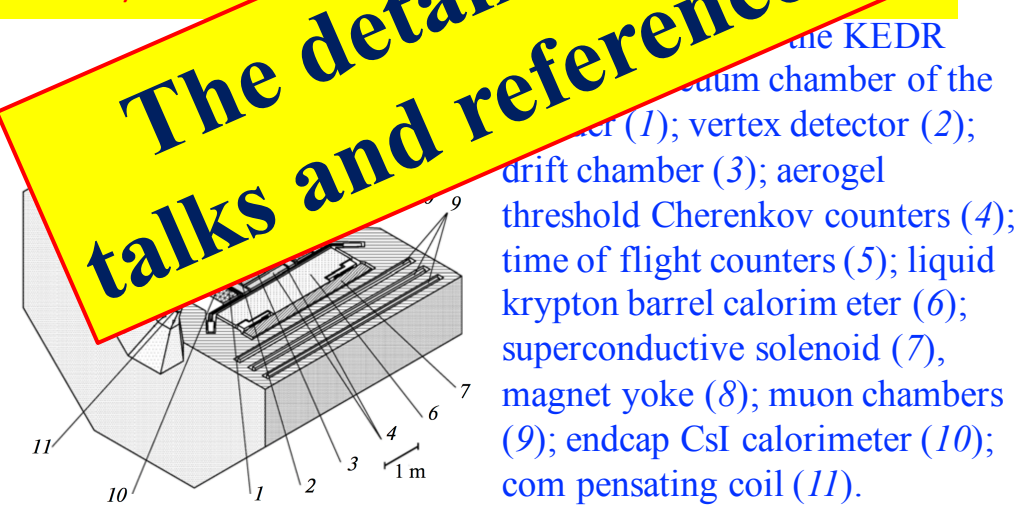
Belle experiment designed for studying rare B-meson decay at $\Upsilon(4S)$ resonance (NIMA479(2002) 117-232)



KEDR experiment designed for studying quarks and two photon (JINT3(2008)S08005)

Belle experiment aiming for precision measurements in *b, c* sectors. (JINT3(2008)S08005)

The details can be found in other special talks and references!



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■ Summary

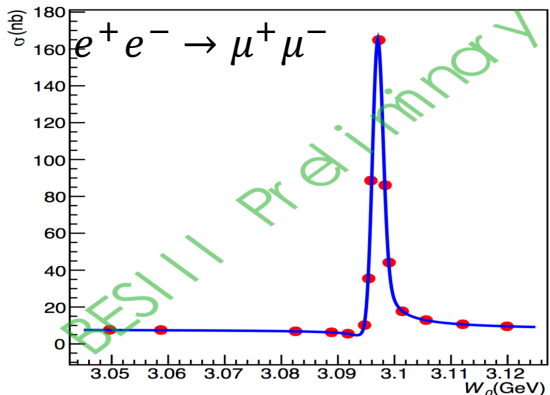
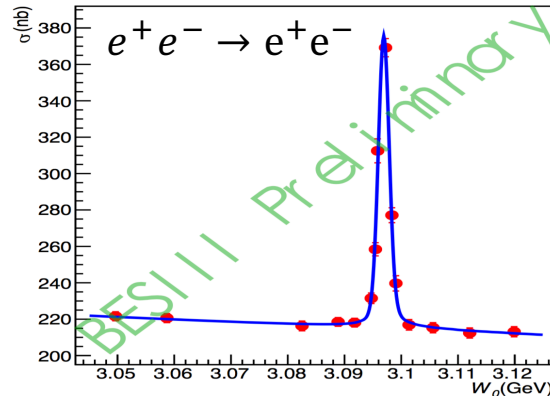
J/ψ and $\psi(2S)$ resonance parameters

BESIII *KEDR*

BESIII Precise measurement of J/ψ decay width

- Precise measurements of J/ψ decay widths provide a better understanding of the underlying physics.
- Updated with processes $e^+e^- \rightarrow e^+e^-$ and $e^+e^- \rightarrow \mu^+\mu^-$ at 15 c.m. energy points in the vicinity of the J/ψ resonance.

Simultaneous fit



Numerical Results

Parameters and their covariance matrix from fitting

Symbol	Value (keV)	V_{i1} (keV ²)	V_{i2} (keV ²)
$\Gamma_{ee}\Gamma_{ee}/\Gamma_{tot}$	0.348	0.0000684	0.0000373
$\Gamma_{ee}\Gamma_{\mu\mu}/\Gamma_{tot}$	0.339	0.0000373	0.0000300

↓

PRD88 (2013) 032007

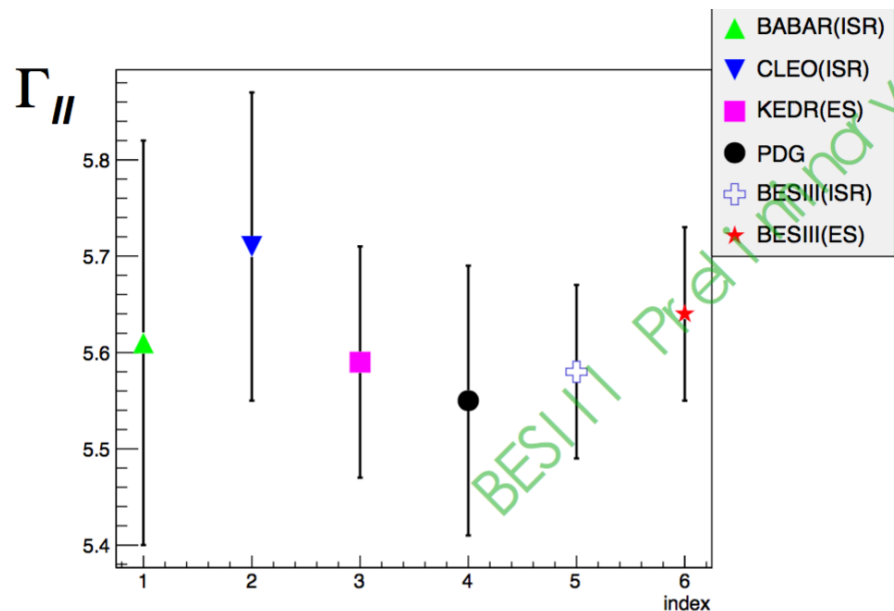
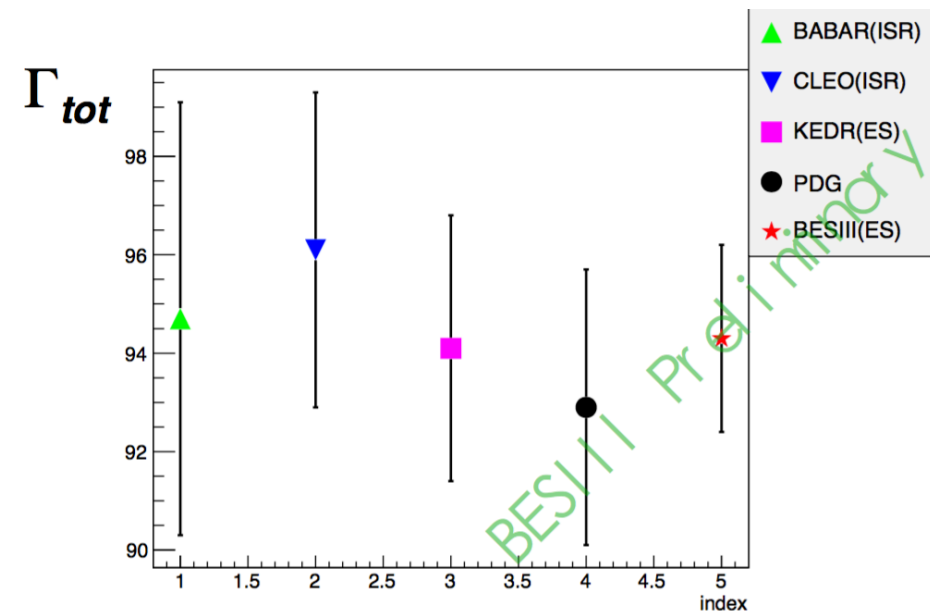
Combined with $B(J/\psi \rightarrow l^+l^-) = \Gamma_{ll}/\Gamma_{tot} = (5.978 \pm 0.040)\%$

↓

Symbol	Result
$\Gamma_{ee}/\Gamma_{\mu\mu}$	1.025 ± 0.014
Γ_{tot}	$(94.3 \pm 1.9) \text{ keV}$
Γ_{ll}	$(5.64 \pm 0.09) \text{ keV}$

- A global χ^2 function for decay width extraction: $\chi^2 = \Delta\sigma^T \cdot V^{-1} \cdot \Delta\sigma$
(See the details for backup page)

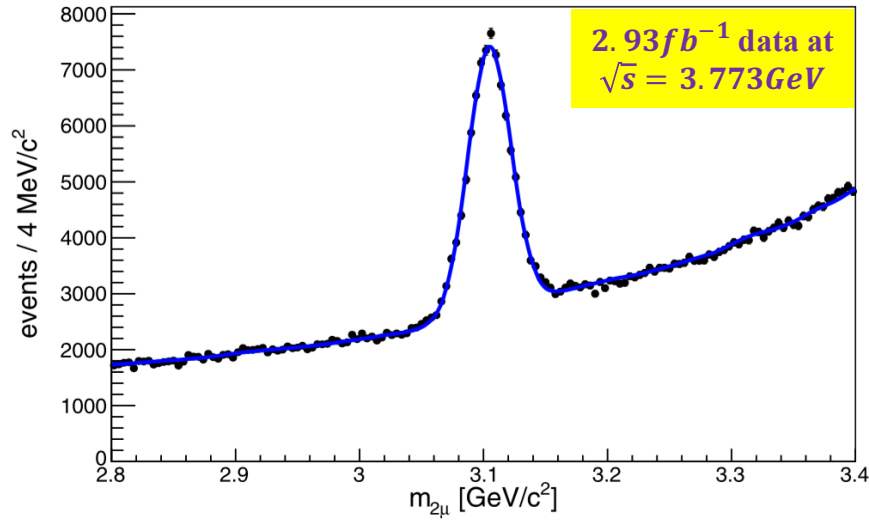
Comparison with results from others



- BESIII result is consistent with those from others.
- Together with BESIII result using ISR, this result achieves the best accuracy in the world by far.

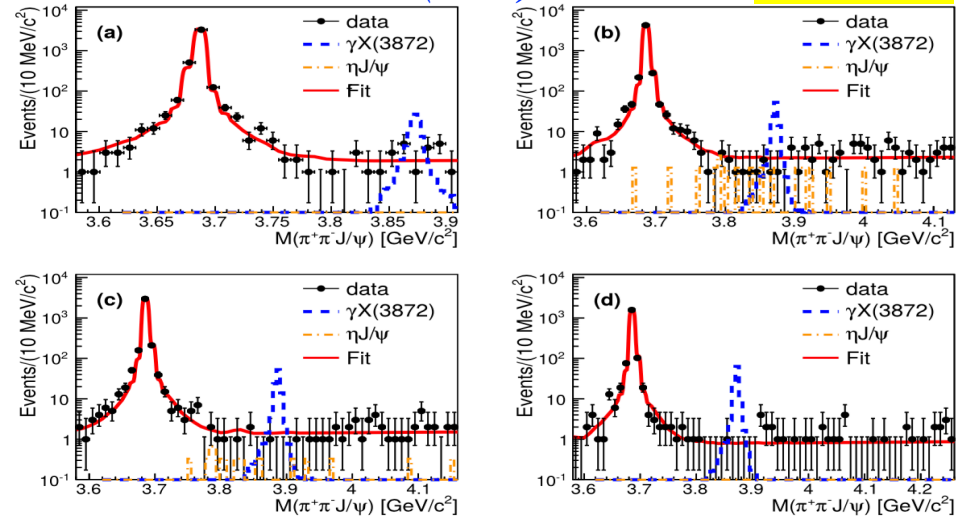
BESIII Measurement of J/ψ , $\psi(3686)$ electronic width

PLB 761(2016) 98-103



PLB 749(2015) 414-420

Data above
4.0GeV



■ The process $e^+ e^- \rightarrow J/\psi \gamma \rightarrow \mu^+ \mu^- \gamma$ applied for J/ψ electronic width

Measurement	$\Gamma_{ee} \cdot \mathcal{B}_{\mu\mu}$ [eV]	Used $\mathcal{B}_{\mu\mu}$ value [%]	Γ_{ee} [keV]
BaBar	$330.1 \pm 7.7_{\text{stat}} \pm 7.3_{\text{sys}}$	5.88 ± 0.10 [20]	5.61 ± 0.20
CLEO-c	$338.4 \pm 5.8_{\text{stat}} \pm 7.1_{\text{sys}}$	$5.953 \pm 0.056_{\text{stat}} \pm 0.042_{\text{sys}}$ [21]	$5.68 \pm 0.11_{\text{stat}} \pm 0.13_{\text{sys}}$
KEDR	$331.8 \pm 5.2_{\text{stat}} \pm 6.3_{\text{sys}}$	5.94 ± 0.06 [22]	5.59 ± 0.12
This work	$333.4 \pm 2.5_{\text{stat}} \pm 4.4_{\text{sys}}$	$5.973 \pm 0.007_{\text{stat}} \pm 0.037_{\text{sys}}$ [4]	$5.58 \pm 0.05_{\text{stat}} \pm 0.08_{\text{sys}}$

■ The process $e^+ e^- \rightarrow \gamma_{\text{ISR}} \pi^+ \pi^- J/\psi$ for $\psi(3686)$ electronic width with ISR method

$$\Gamma_{ee}^{\psi(3686)} = (2213 \pm 18_{\text{stat}} \pm 99_{\text{sys}}) \text{ eV}$$

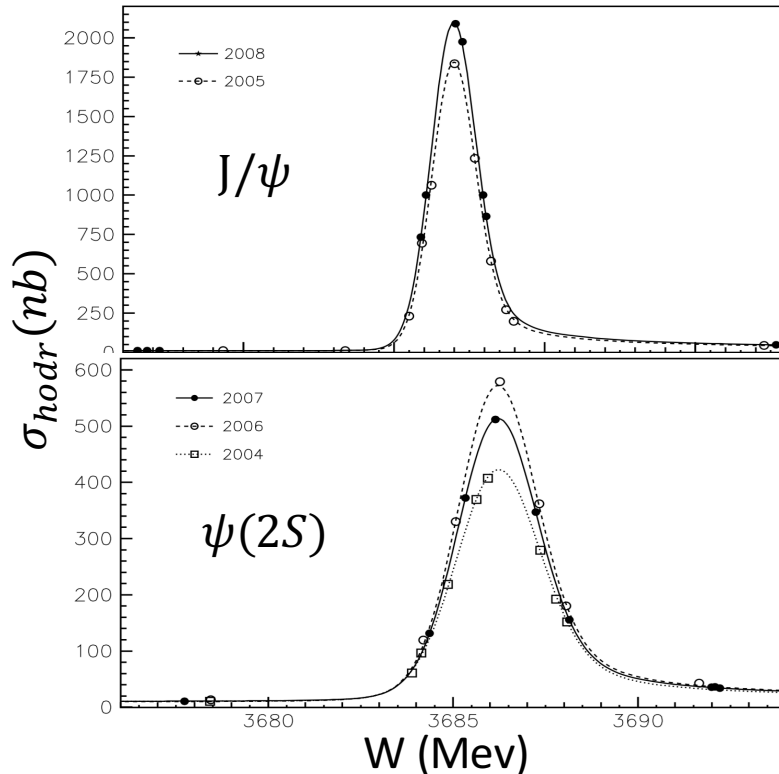
$$\Gamma_{ee}^{X(3872)} \mathcal{B}(X(3872) \rightarrow \pi^+ \pi^- J/\psi) < 0.13 \text{ eV} \quad @ 90\% \text{ C.L.}$$

■ Measurements are consistent with the PDG values

Measurement of J/ψ and $\psi(2S)$ masses

- Based on **six** high precision scans of the J/ψ region and **seven** high precision scans of $\psi(2S)$ in **KEDR detector**.
- Determined by fitting the inclusive hadronic cross sections.
- Beam energy was determined using the resonance depolarization method.

PLB 749(2015) 50-56



■ Weighting of results on masses

$$\langle M \rangle = \sum w_i \cdot M_i,$$

$$\sigma_{\text{stat}}^2 = \sum w_i^2 \cdot \sigma_{\text{stat},i}^2,$$

$$\sigma_{\text{syst}}^2 = \sum w_i^2 \cdot (\sigma_{\text{syst},i}^2 - \sigma_{\text{syst},0}^2) + \sigma_{\text{syst},0}^2,$$

$$w_i = 1/(\sigma_{\text{stat},i}^2 + \sigma_{\text{syst},i}^2 - \sigma_{\text{syst},0}^2),$$

Here $\sigma_{\text{syst},0}^2$ denotes a common part of systematic uncertainty

Resonance parameters on masses

$$M_{J/\psi} = 3096.900 \pm 0.002 \pm 0.006 \text{ MeV}$$

$$M_{\psi(2S)} = 3686.099 \pm 0.004 \pm 0.009 \text{ MeV}$$

■ Consistent with PDG values within 1σ

$\chi_{cJ}(1P)$ resonance parameters

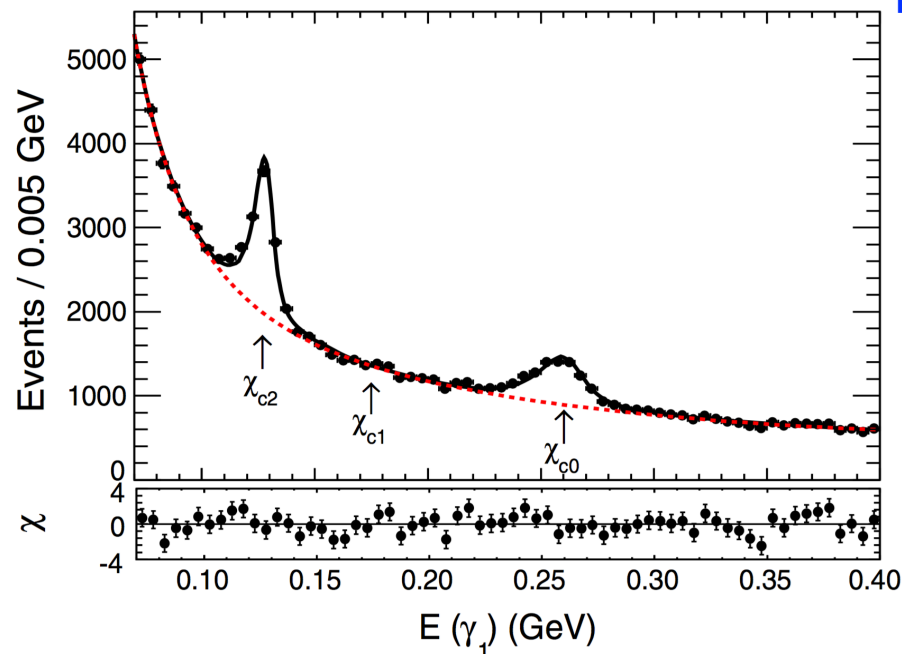
BESIII



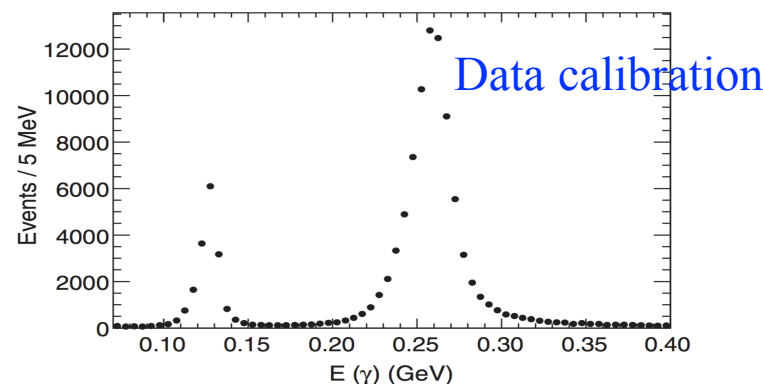
Improvement measurement of $\Gamma_{\gamma\gamma}(\chi_{c0,2})$

- Updated with the process $\chi_{c0,2} \rightarrow \gamma\gamma$ based on $\psi(2S)$ radiative decay.

PRD96, 092007(2017)



- The $\chi_{c0,2}$ shape modeled and fixed in the fit by the control sample $\psi(3686) \rightarrow \gamma\chi_{c0,2}, \chi_{c0,2} \rightarrow K^+K^-$



$$\mathcal{B}_1 = \mathcal{B}(\psi(3686) \rightarrow \gamma\chi_{c0,2}) \cdot \mathcal{B}_2 = \mathcal{B}(\chi_{c0,2} \rightarrow \gamma\gamma)$$

$$\Gamma_{\gamma\gamma}(\chi_{c0,2} \rightarrow \gamma\gamma) = \mathcal{B}(\chi_{c0,2} \rightarrow \gamma\gamma) \times \Gamma(\chi_{c0,2}),$$

$$\mathcal{R} = \frac{\Gamma_{\gamma\gamma}(\chi_{c2} \rightarrow \gamma\gamma)}{\Gamma_{\gamma\gamma}(\chi_{c0} \rightarrow \gamma\gamma)}$$

Quantity	PDG average values ^a	CLEO-c ^b	BESIII ^b	This measurement ^b
$\mathcal{B}_1 \times \mathcal{B}_2(10^{-5})(\chi_{c0})^c$	2.23 ± 0.14	$2.17 \pm 0.32 \pm 0.10$	$2.17 \pm 0.17 \pm 0.12$	$1.93 \pm 0.08 \pm 0.05$
$\mathcal{B}_1 \times \mathcal{B}_2(10^{-5})(\chi_{c2})^c$	2.50 ± 0.15	$2.68 \pm 0.28 \pm 0.15$	$2.81 \pm 0.17 \pm 0.15$	$2.83 \pm 0.08 \pm 0.06$
$\mathcal{B}_2(10^{-4})(\chi_{c0})^c$	2.23 ± 0.13	$2.31 \pm 0.34 \pm 0.15$	$2.24 \pm 0.19 \pm 0.15$	$1.93 \pm 0.08 \pm 0.07$
$\mathcal{B}_2(10^{-4})(\chi_{c2})^c$	2.74 ± 0.14	$3.23 \pm 0.34 \pm 0.24$	$3.21 \pm 0.18 \pm 0.22$	$3.10 \pm 0.09 \pm 0.13$
$\Gamma_{\gamma\gamma}(\chi_{c0})$ keV	2.24 ± 0.19	$2.36 \pm 0.35 \pm 0.22$	$2.33 \pm 0.20 \pm 0.22$	$2.03 \pm 0.08 \pm 0.14$
$\Gamma_{\gamma\gamma}(\chi_{c2})$ keV	0.53 ± 0.03	$0.66 \pm 0.07 \pm 0.06$	$0.63 \pm 0.04 \pm 0.06$	$0.60 \pm 0.02 \pm 0.04$
\mathcal{R}	0.236 ± 0.024	$0.278 \pm 0.050 \pm 0.036$	$0.271 \pm 0.029 \pm 0.030$	$0.295 \pm 0.014 \pm 0.028$

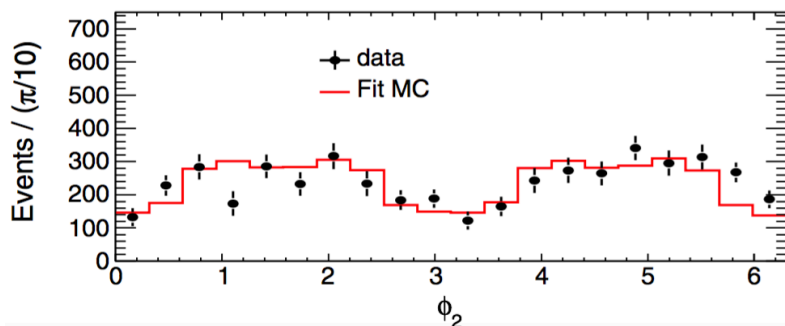
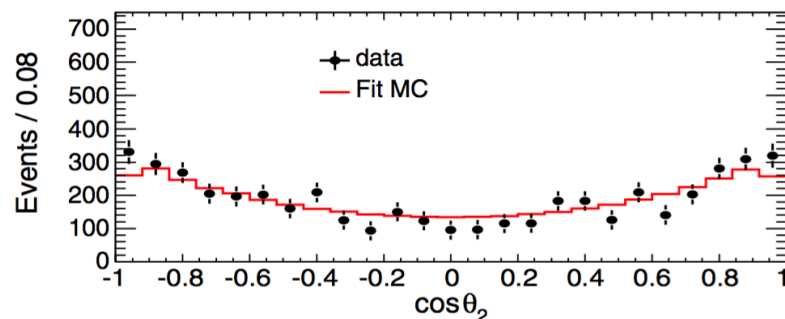
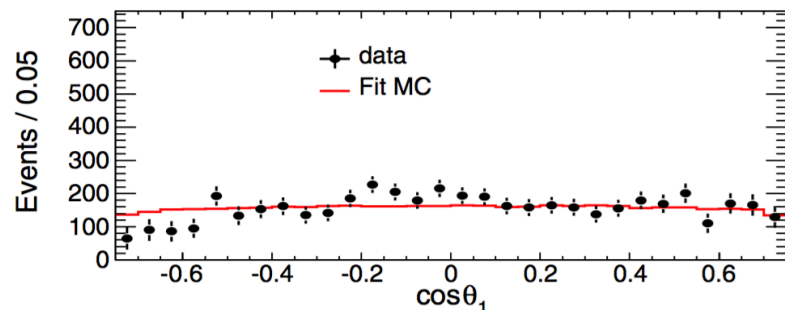
Upper limits for χ_{c1} :
 $\Gamma_{\gamma\gamma}(\chi_{c1}) < 5.3 \text{ eV}@90\%\text{C.L.}$
 $\mathcal{B}(\chi_{c1} \rightarrow \gamma\gamma) < 6.3 \times 10^{-6}$

- More precise measurement, consistent with the previous experimental results!
- Precisely measured \mathcal{R} calibrates the different theoretical potential models.

Improvement measurement of $\Gamma_{\gamma\gamma}(\chi_{c0,2})$

- A helicity amplitude analysis is performed for superposition of helicity-zero ($\lambda = 0$) and helicity-two ($\lambda = 2$) components for $\chi_{c2} \rightarrow \gamma\gamma$ decay.

PRD96, 092007(2017)



Variables definition:

- ✓ θ_1 : polar angle of radiative photon, with respect to the direction of positron beam;
- ✓ θ_2/ϕ_2 : polar/azimuthal angle of one of photons in $\chi_{c2} \rightarrow \gamma\gamma$ process at χ_{c2} rest frame, with respect to the direction of radiative photon direction;

Two photon width ratio for $\chi_{c2} \rightarrow \gamma\gamma$

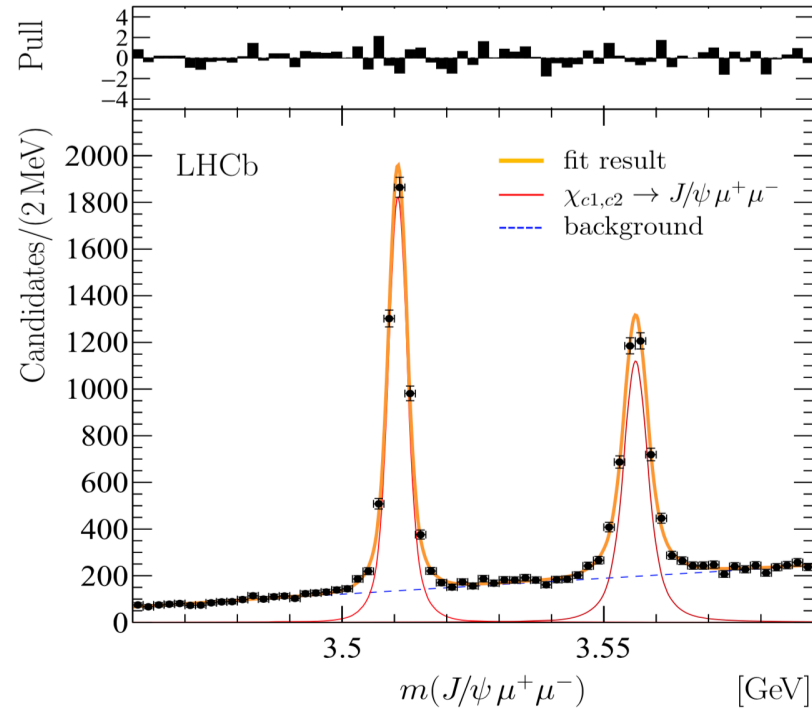
$$f_{0/2} = \frac{\Gamma_{\gamma\gamma}^{\lambda=0}(\chi_{c2})}{\Gamma_{\gamma\gamma}^{\lambda=2}(\chi_{c2})} = (0.0 \pm 0.6 \pm 1.2) \times 10^{-2}$$

- More precise measurement, consistent with the previous experimental results.
- Confirmed **helicity-zero component** highly suppressed.

Measurement of $\chi_{c1,2}$ resonance parameters

- Performed based on observation of $\chi_{c1,2} \rightarrow J/\psi \mu^+ \mu^-$.

PRL 117,221801(2017)



- An extended unbinned maximum likelihood fit

- ✓ The $\chi_{c1,2}$ signals are modeled by **relativistic Breit-Wigner functions with Blatt-Weisskopf form factors** with a meson radius parameter of 3 GeV^{-1} .
- ✓ The orbital angular momentum between the J/ψ meson and the $\mu^+ \mu^-$ pair is assumed to be 0 (1) for the χ_{c1} (χ_{c2}) cases.

- Numerical results for resonance parameters:

Quantity [MeV]	LHCb measurement	Best previous measurement	World average
$m(\chi_{c1})$	3510.71 ± 0.10	3510.72 ± 0.05	3510.66 ± 0.07
$m(\chi_{c2})$	3556.10 ± 0.13	3556.16 ± 0.12	3556.20 ± 0.09
$\Gamma(\chi_{c2})$	2.10 ± 0.20	1.92 ± 0.19	1.93 ± 0.11

$$m(\chi_{c2}) - m(\chi_{c0}) = 45.39 \pm 0.07 \pm 0.03 \text{ MeV}$$

- Observations presented here open up a new avenue for hadron spectroscopy at the LHC.

- ✓ To measure production of $\chi_{c1,2}$ states
- ✓ To extend measurements to low $p_t(\chi_{c1,2})$
- ✓ ...

$\eta_c(1S)$ resonance parameters

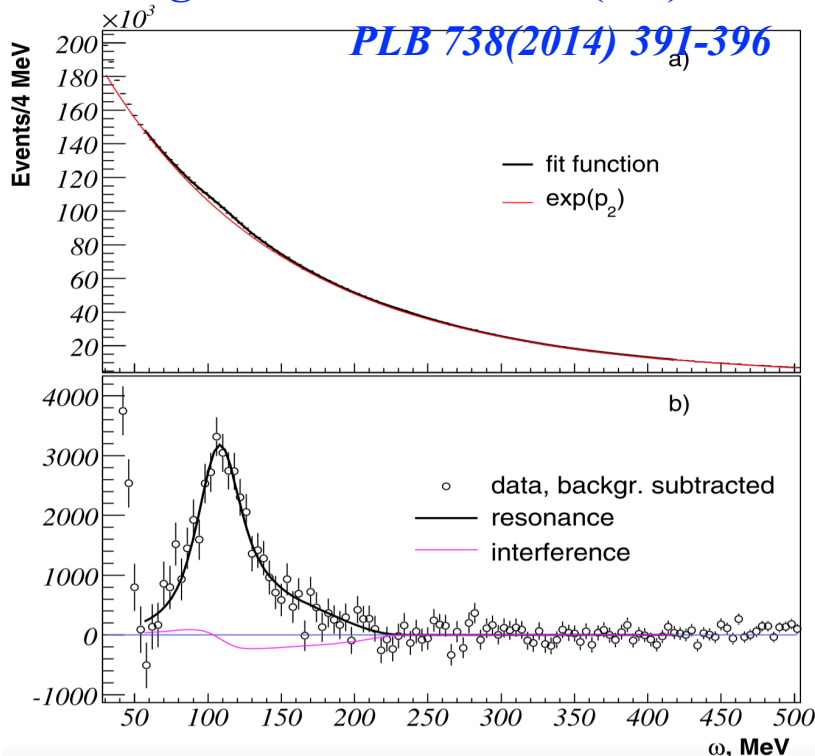
KEDR



Measurement of $\eta_c(1S)$ resonance parameters

■ Measured using inclusive photon spectrum in process $J/\psi \rightarrow \gamma\eta_c$ in **KEDR detector**.

■ Inclusive photon spectrum before/after background subtraction (a/b)



$$M_{\eta_c} = 2983.5 \pm 1.4^{+1.6}_{-3.6} \text{ MeV}$$

$$\Gamma_{\eta_c} = 27.2 \pm 3.1^{+5.4}_{-2.6} \text{ MeV}$$

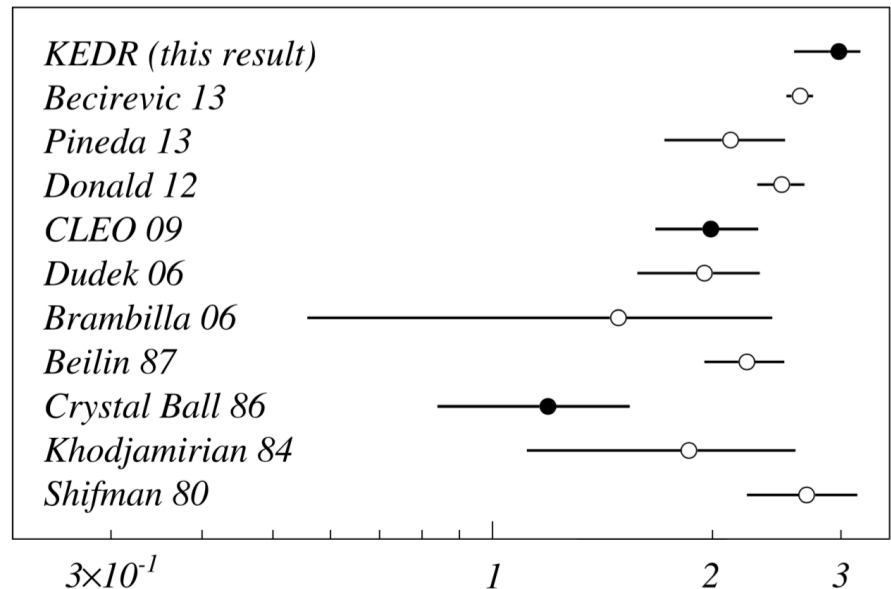
■ Consistent with PDG values within 1σ

■ Taking into account an asymmetric photon lineshape.

Decay Rate

$$\Gamma_{\gamma\eta_c}^0 = \frac{\mathcal{B}(J/\psi \rightarrow \gamma\eta_c)\Gamma_{J/\psi}}{f_{\text{cor}}} = 2.98 \pm 0.18^{+0.15}_{-0.33} \text{ keV}$$

f_{cor} correction factor

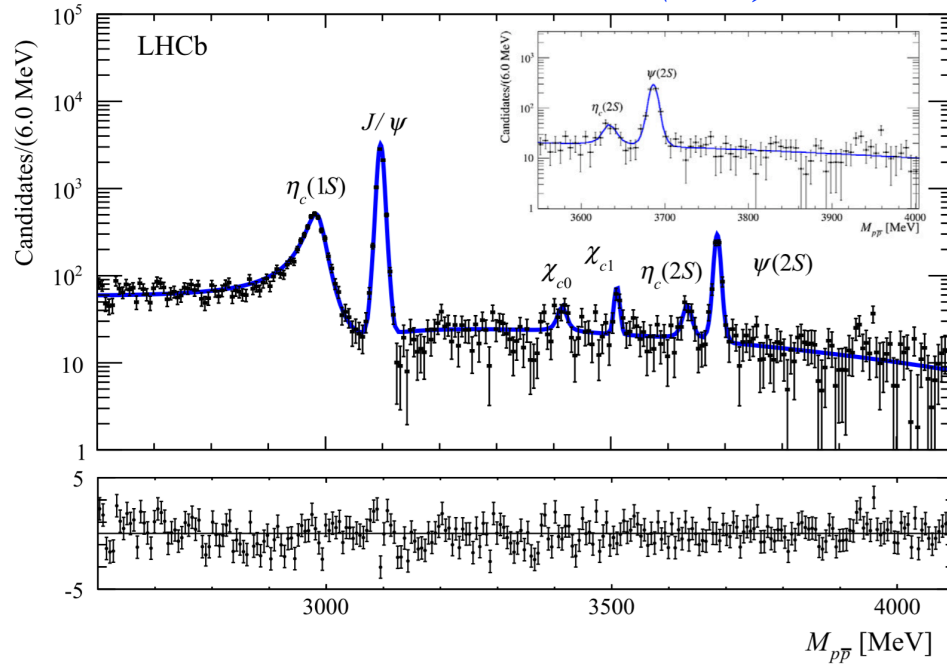


■ Consistent with other measurements (close circles) and theoretical predictions (open circles) within the errors.

Measurement of $\eta_c(1S)$ width parameter

- Performed with process $B^+ \rightarrow p\bar{p}K^+$ using 3.0 fb^{-1} $p\bar{p}$ collision data

PLB 769(2017) 305-313



Numerical results on masses

$$\begin{aligned} M_{J/\psi} - M_{\eta_c(1S)} &= 110.2 \pm 0.5 \pm 0.9 \text{ MeV}, \\ M_{\psi(2S)} - M_{\eta_c(2S)} &= 52.5 \pm 1.7 \pm 0.6 \text{ MeV}, \\ \Gamma_{\eta_c(1S)} &= 34.0 \pm 1.9 \pm 1.3 \text{ MeV}. \end{aligned}$$

- Consistent with PDG value

$$\Gamma_{\eta_c(1S)}^{\text{PDG}} = 31.8 \pm 0.8 \text{ MeV}.$$

- Compared with radiative decays, these mass and width determinations do not depend on the knowledge of the line shapes of the magnetic dipole transition.

- Observation of $\eta_c(2S) \rightarrow p\bar{p}$ (6.0σ) and search for $\psi(3770), X(3872) \rightarrow p\bar{p}$

Relative branching fractions:

$$\begin{aligned} R_{\eta_c(2S)} &= (1.58 \pm 0.33 \pm 0.09) \times 10^{-2}, \\ R_{\psi(3770)} &< 9(10) \times 10^{-2} \text{ @ } 90(95)\% \text{ C.L.}, \\ R_{X(3872)} &< 0.20(0.25) \times 10^{-2} \text{ @ } 90(95)\% \text{ C.L.} \end{aligned}$$

Observations of $X(3823)$ and $X^*(3860)$



Observation of $X(3823)$ or $\psi(3823)$

Status:

$c\bar{c}$ MESONS

$\psi(3823)$ was $X(3823)$ $I^G(J^{PC}) = ?^?(2^{--})$

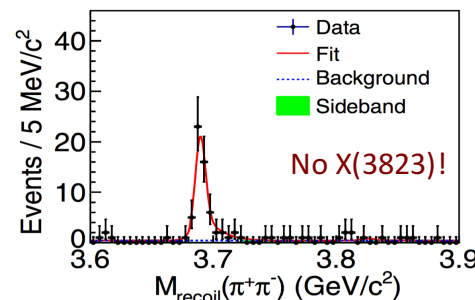
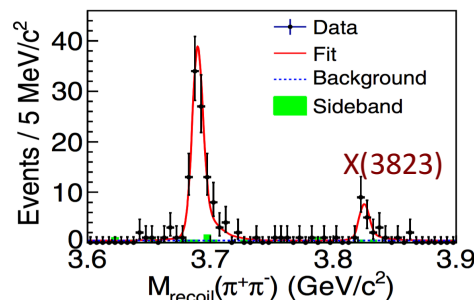
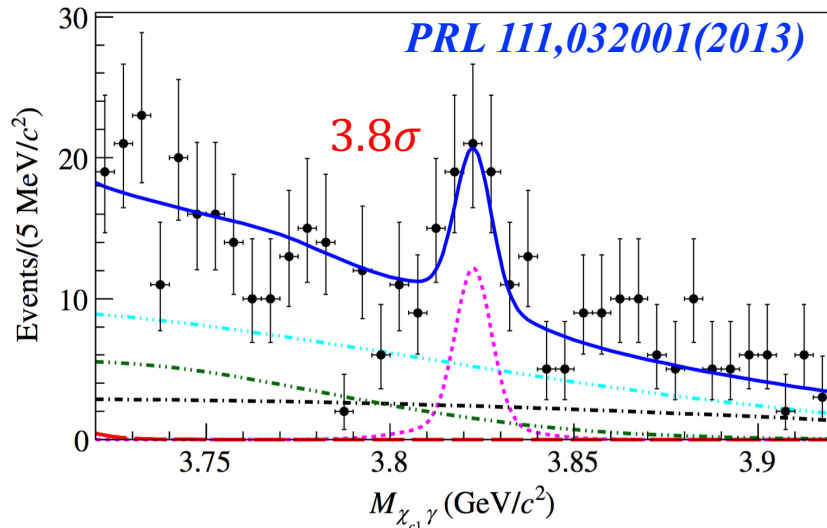
$\psi(3823)$ MASS 3822.2 ± 1.2 MeV

$\psi(3823)$ WIDTH < 16 MeV CL=90.0%

■ An evidence by **Belle** for the first time in process $B \rightarrow \gamma \chi_{c1} K$, but not observed in $\gamma \chi_{c2}$ final state.

■ Observed by **BESIII** in process $e^+e^- \rightarrow \pi^+\pi^-\gamma\chi_{c1}$ with 6.2σ statistical significance.

PRL 115,011803(2015)



- ✓ Simultaneous fit to data at 4.23, 4.26, 4.36, 4.42, 4.60 GeV
- ✓ $\psi(2S)$ signal for calibration

$M_{X(3823)}^{\text{Belle}} = 3823.1 \pm 1.8 \pm 0.7$ MeV
 $\Gamma_{X(3823)}^{\text{Belle}} < 24$ MeV @ 90% C.L.

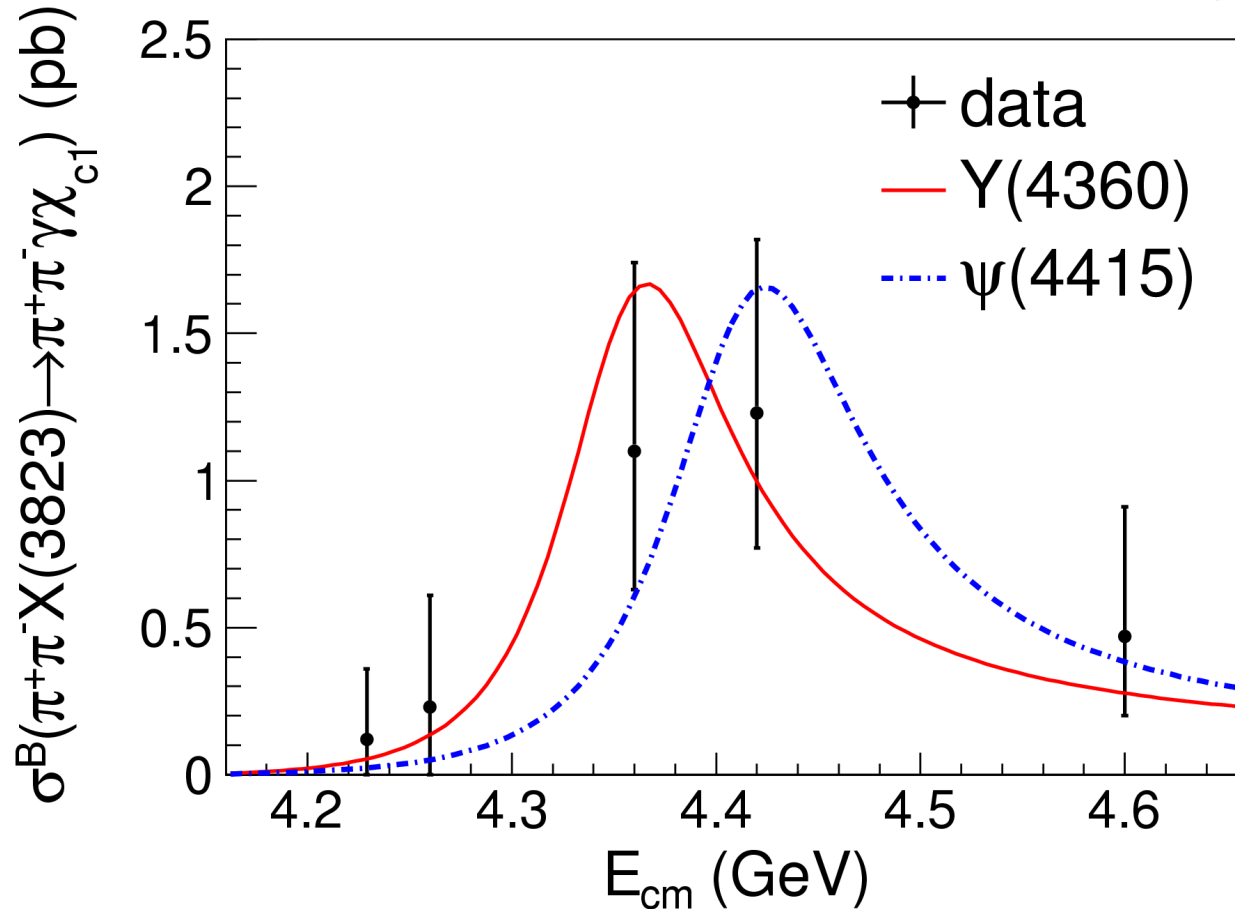
$M_{X(3823)}^{\text{BESIII}} = 3821.7 \pm 1.3 \pm 0.7$ MeV
 $\Gamma_{X(3823)}^{\text{BESIII}} < 16$ MeV @ 90% C.L.

- Good candidate for $\psi(1^3D_2 c\bar{c})$ charmonium state suggested.
- Production of $X(3823)$'s C-odd partner.

- These measurements are in good agreement with the assignment of the $X(3823)$ state as the $\psi(1^3D_2)$ charmonium state.

BESIII Production cross section

PRL 115,011803(2015)



1. Energy dependent cross section of $e^+e^- \rightarrow \pi^+\pi^-\chi(3823)$.
2. Both Y(4360) and Y(4415) line shape give reasonable description.

Observation of $X^*(3860)$ or $\chi_{c0}(2P)$

$c\bar{c}$ MESONS

$X(3915)$ was $\chi_{c0}(3915)$ $I^G(J^{PC}) = 0^+(0 \text{ or } 2^{++})$

The experimental analysis prefers $J^{PC} = 0^{++}$. However, a reanalysis presented in [ZHO 2015C](#) shows that if helicity-2 dominance assumption is abandoned and a sizable helicity-0 component is allowed, a $J^{PC} = 2^{++}$ assignment is possible.

No $\chi_{c0}(2P)$ candidate now!

$X(3915)$ MASS	3918.4 ± 1.9 MeV
$X(3915)$ WIDTH	20 ± 5 MeV (S = 1.1)

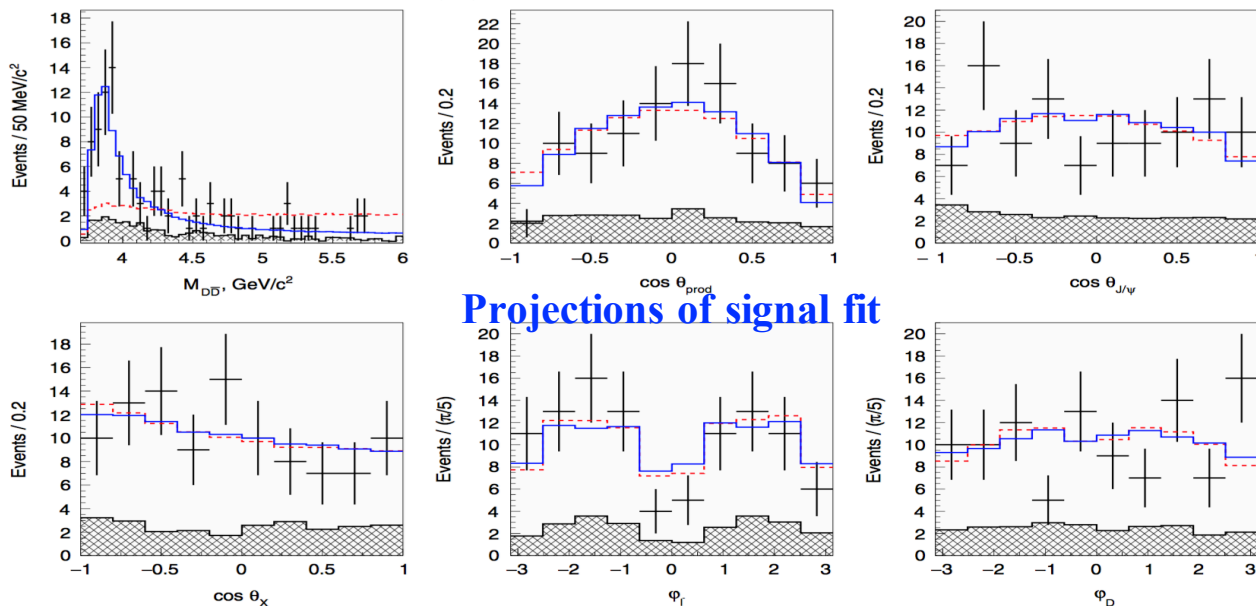
- A full amplitude analysis performed to the $e^+e^- \rightarrow J/\psi D\bar{D}$ process ($D \in D^0, D^+$) in a six-dimensional parameters space:

$$\Phi = (M_{D\bar{D}}, \theta_{\text{prod}}, \theta_{J/\psi}, \theta_{X^*}, \varphi_{J/\psi}, \varphi_D)$$

where, θ_{prod} production angle; $\theta_{J/\psi}, \theta_{X^*}$ helicity angles; $\varphi_{J/\psi}, \varphi_D$ azimuthal angles.

- Observation of a new charmonium-like state $X^*(3860)$ with 6.5σ statistical significance.

PRD 95,112003(2017)



Projections of signal fit

Resonance parameters
 $M_{X^*(3860)} = 3862_{-32}^{+26+40}$ MeV
 $\Gamma_{X^*(3860)} = 201_{-67}^{+154+88}$ MeV

- The $J^{PC} = 0^{++}$ hypothesis is favored over the $J^{PC} = 2^{++}$ hypothesis at the level of 2.5σ .

Observation of $X^*(3860)$ or $\chi_{c0}(2P)$

PRD 95,112003(2017)

■ Comparison of the $X^*(3860)$ and known charmonium-like states

State	J^{PC}	Nonresonant amplitude		
		Constant	NRQCD	$M_{D\bar{D}}^{-4}$
$X(3915)$	0^{++}	5.2σ	4.3σ	3.3σ
$X(3915)$	2^{++}	6.1σ	6.1σ	4.9σ
$\chi_{c2}(2P)$	2^{++}	6.8σ	7.0σ	6.2σ
$X(3940)$	2^{++}	6.0σ	5.6σ	5.2σ
$X(4160)$	0^{++}	6.8σ	6.3σ	5.8σ
$X(4160)$	2^{++}	10.7σ	11.0σ	13.5σ
$\chi_{c0}(2P)$ (lattice)	0^{++}	4.3σ	3.6σ	2.7σ

✓ $\sim 2.7\sigma$ level difference from predicted $\chi_{c0}(2P)$.

■ The $X^*(3860)$ global significance for alternative models

Model	Significance
Default (constant nonresonant)	8.5σ
NRQCD nonresonant	7.6σ
$M_{D\bar{D}}^{-4}$ nonresonant	6.5σ
Background mass calculation	8.4σ
Optimization ($a = 4$)	8.1σ
Optimization ($a = 6$)	8.1σ

✓ Disagree with the NRQCD prediction.

■ A new conventional charmonium state

- ✓ A better candidate for $\chi_{c0}(2P)$ charmonium state than $X(3915)$, well matched to expectation of $\chi_{c0}(2P)$ from potential model.
- ✓ Agree with $\chi_{c0}(2P)$ parameters determined from an alternative fit to Belle and BABAR:

$$M = 3837.6 \pm 11.5 \text{ MeV}$$

$$\Gamma = 221 \pm 19 \text{ MeV}$$

✓ A conventional charmonium state above $D\bar{D}$ threshold, coincide with $\chi_{c0}(2P)$.

■ Born cross section measurement

Data set	Energy, GeV	$\sigma_{e^+e^- \rightarrow J/\psi X^*(3860) (\rightarrow D\bar{D})}^{(\text{Born})}$, fb
$\Upsilon(1S)$	9.46	$77_{-66}^{+66} {}_{-7}^{+9}$
$\Upsilon(2S)$	10.02	$6.9_{-12.6}^{+12.6} {}_{-0.7}^{+0.9}$
$\Upsilon(3S)$	10.36	$77_{-85}^{+85} {}_{-8}^{+11}$
Continuum	10.52	$5.5_{-5.7}^{+5.7} {}_{-0.5}^{+0.7}$
$\Upsilon(4S)$	10.58	$21.7_{-4.3}^{+3.9} {}_{-2.1}^{+2.9}$
$\Upsilon(5S)$	10.87	$17.9_{-7.3}^{+7.2} {}_{-1.8}^{+2.4}$

Summary of recent experimental status for CCS

CCS	Collab.	M(MeV)	$\Gamma_{\text{tot}}(\text{keV})$	$\Gamma_{ll}(\text{keV})$	$\Gamma_{ee}(\text{keV})$	COMMENT
J/ψ	BESIII	---	94.3 ± 1.9	5.64 ± 0.09	5.58 ± 0.09	$e^+e^- \rightarrow e^+e^-, \mu^+\mu^-$ $e^+e^- \rightarrow J/\psi\gamma \rightarrow \mu^+\mu^-\gamma$
	KEDR	3096.900 ± 0.006	---	---	---	Inclusive hadronic mode
	PDG	3096.900 ± 0.006	92.9 ± 2.8	---	---	PDG AVERAGE
$\psi(2S)$	BESIII	---	---	---	2.213 ± 0.100	$e^+e^- \rightarrow \gamma_{\text{ISR}}\pi^+\pi^-J/\psi$
	KEDR	3686.009 ± 0.098	---	---	---	Inclusive hadronic mode
	PDG	3686.009 ± 0.098	296 ± 8	---	---	PDG AVERAGE

	CCS	Collab.	M(MeV)	Γ (MeV)	$\Gamma_{\gamma\gamma}$ (keV)	COMMENT
C	χ_{c0}	BESIII	---	---	2.03 ± 0.16	$\psi(3686) \rightarrow \gamma\chi_{c0}, \chi_{c0} \rightarrow \gamma\gamma$
		LHCb	---	---	---	---
		PDG	3414.75 ± 0.31	10.5 ± 0.6	---	PDG AVERAGE
η_c	χ_{c1}	BESIII	---	---	$<5.3 \times 10^{-3}$	$\psi(3686) \rightarrow \gamma\chi_{c0}, \chi_{c0} \rightarrow \gamma\gamma$
		LHCb	3510.71 ± 0.14	---		$\chi_{c1,2} \rightarrow J/\psi\mu^+\mu^-$
		PDG	3510.66 ± 0.07	0.84 ± 0.04	---	PDG AVERAGE
X(3) Or ψ'	χ_{c2}	BESIII	---	---	2.03 ± 0.16	$\psi(3686) \rightarrow \gamma\chi_{c0}, \chi_{c0} \rightarrow \gamma\gamma$
		LHCb	3556.10 ± 0.13	2.10 ± 0.20	---	$\chi_{c1,2} \rightarrow J/\psi\mu^+\mu^-$
		PDG	3556.20 ± 0.09	1.93 ± 0.11	---	PDG AVERAGE
$X^*(3860)$ Or $\chi_{c0}(2P)$	Belle	3862^{+26+40}_{-32-23}	$201^{+154+88}_{-67-82}$	---	$e^+e^- \rightarrow J/\psi D\bar{D}$	
	PDG	---	---	---	PDG AVERAGE	

■ Tables summarize more precise measurement, consistent with PDG average! 24

Summary of recent experimental status for CCS

CCS	Collab.	M(MeV)	$\Gamma_{\text{tot}}(\text{keV})$	$\Gamma_{ll}(\text{keV})$	$\Gamma_{ee}(\text{keV})$	COMMENT
J/ψ	BESIII	---	94.3 ± 1.9	5.64 ± 0.09	5.58 ± 0.09	$e^+e^- \rightarrow e^+e^-, \mu^+\mu^-$ $e^+e^- \rightarrow J/\psi\gamma \rightarrow \mu^+\mu^-\gamma$
	KEDR	3096.900 ± 0.006	---	---	---	Inclusive hadronic mode
	PDG	3096.900 ± 0.006	92.9 ± 2.8	---	---	PDG AVERAGE
$\psi(2S)$	BESIII	---	---	---	2.213 ± 0.100	$e^+e^- \rightarrow \gamma_{\text{ISR}}\pi^+\pi^-J/\psi$
	KEDR	3686.009 ± 0.098	---	---	---	Inclusive hadronic mode
	PDG	3686.009 ± 0.098	296 ± 8	---	---	PDG AVERAGE

CCS	Collab.	M(MeV)	$\Gamma(\text{MeV})$	$\Gamma_{\gamma\gamma}(\text{keV})$	COMMENT
χ_{c0}	BESIII	---	---	2.03 ± 0.16	$\psi(3686) \rightarrow \gamma\chi_{c0}, \chi_{c0} \rightarrow \gamma\gamma$
	LHCb	---	---	---	---
	---	---	---	---	---

CCS	Collab.	M(MeV)	$\Gamma(\text{MeV})$	$\Gamma_{\gamma\eta_c}^0(\text{keV})$	COMMENT
$\eta_c(1S)$	KEDR	$2983.5 \pm 1.4^{+1.6}_{-3.6}$	$27.2 \pm 3.1^{+5.4}_{-2.6}$	$2.98 \pm 0.18^{+0.15}_{-0.33}$	$J/\psi \rightarrow \gamma\eta_c$
	LHCb	---	$34.0 \pm 1.9 \pm 1.3$	---	$B^+ \rightarrow p\bar{p}K^+$
	PDG	2983.4 ± 0.5	31.8 ± 0.8	---	PDG AVERAGE
$X(3823)$ Or $\psi(3823)$	Belle	$3823.1 \pm 1.8 \pm 0.7$	< 24	---	$B \rightarrow \gamma\chi_{c1}K$
	BESIII	$3821.7 \pm 1.3 \pm 0.7$	< 16	---	$e^+e^- \rightarrow \pi^+\pi^-\gamma\chi_{c1}$
	PDG	3822.2 ± 1.2	< 16	---	PDG AVERAGE
$X^*(3860)$ Or $\chi_{c0}(2P)$	Belle	3862^{+26+40}_{-32-23}	$201^{+154+88}_{-67-82}$	---	$e^+e^- \rightarrow J/\psi D\bar{D}$
	PDG	---	---	---	PDG AVERAGE

■ Tables summarize more precise measurement, consistent with PDG average! 25

Summary

- Lots of progress in the study of conventional charmonium states at BESIII, Belle, KEDR and LHCb, recently.
 - Precise/improved measurements:
 - ✓ J/ψ and $\psi(2S)$ resonance parameters
 - ✓ $\chi_{cJ}(1P)$ resonance parameters
 - ✓ $\eta_c(1S)$ resonance parameters
 - Observations of $\psi(1^3D_2)=X(3823)$ and $\chi_{c2}(2P)=X^*(3860)$
- BESIII/Belle/KEDR/LHCb will continue the study, Belle II at KEK will start data taking very soon.

Thanks for your attention!

Backup

Decay width extraction — Global χ^2

To consider:

- Correlations between measured cross sections of the same channel at different energy points;
- Correlations between measured cross sections of different channels at the same energy point,

a global χ^2 function is constructed:

$$\chi^2 = \Delta\sigma^T \cdot V^{-1} \cdot \Delta\sigma$$

where

$$\Delta\sigma(i) = \begin{cases} \sigma_{ee}^{exp}(i) - \sigma_{ee}^{the}(i) & i = 1 - 15 \\ \sigma_{\mu\mu}^{exp}(i - 15) - \sigma_{\mu\mu}^{the}(i - 15) & i = 16 - 30 \end{cases}$$

and

$$V(i, j) = \begin{cases} V_{ee}(i, j) + \delta(i - j) \left(\frac{d\sigma_{ee}^{the}}{dW_0}(i) \Delta W_0(i) \right)^2 & i = 1 - 15, j = 1 - 15 \\ \frac{\sigma_{ee}^{exp}(i) \sigma_{\mu\mu}^{exp}(j - 15)}{L(i) L(j - 15)} V_L(i, j - 15) + \delta(i + 15 - j) \frac{d\sigma_{ee}^{the}}{dW_0}(i) \frac{d\sigma_{\mu\mu}^{the}}{dW_0}(j) (\Delta W_0(i))^2 & i = 1 - 15, j = 16 - 30 \\ \frac{\sigma_{ee}^{exp}(j) \sigma_{\mu\mu}^{exp}(i - 15)}{L(i - 15) L(j)} V_L(i - 15, j) + \delta(i - j - 15) \frac{d\sigma_{ee}^{the}}{dW_0}(j) \frac{d\sigma_{\mu\mu}^{the}}{dW_0}(i) (\Delta W_0(j))^2 & i = 16 - 30, j = 1 - 15 \\ V_{\mu\mu}(i - 15, j - 15) + \delta(i - j) \left(\frac{d\sigma_{\mu\mu}^{the}}{dW_0}(i - 15) \Delta W_0(i - 15) \right)^2 & i = 16 - 30, j = 16 - 30 \end{cases}$$

Decay width extraction — Formulas and parameters

- Analytical formulas for resonance terms and interference terms of cross sections of $e^+e^- \rightarrow e^+e^-$ and $e^+e^- \rightarrow \mu^+\mu^-$ with ISR considered are carefully derived ¹ with structure function method ²

$$\sigma(s, \cos \theta) = \int \bar{\sigma}(s(1-x), \cos \theta) F(s, x) dx$$

- The energy spread effect is described by gauss distribution

$$\sigma'(W_0) = \int \sigma(W) \left(\frac{1}{\sqrt{2\pi}\sigma_W} \exp -\frac{(W-W_0)^2}{2\sigma_W^2} \right) dW$$

- The FSR factor $R^{FSR}(W_0)$ are obtained via numerical method with the Babayaga generator as the ratio of the calculated cross sections with the FSR switch therein turned on and off. With it

$$\sigma^{the}(W_0) = \sigma'(W_0) \cdot R^{FSR}(W_0)$$

- The final function form of the theoretical cross section formula:

$$\sigma_{ll}^{the} = \sigma_{ll}^{the}(W_0, M, \Gamma_{tot}, \Gamma_{ee}\Gamma_{ll}/\Gamma_{tot}, \sqrt{\Gamma_{ee}\Gamma_{ll}}, \sigma_W) \text{ with } ll = ee \text{ or } \mu\mu$$

- $\Gamma_{ee}\Gamma_{ee}/\Gamma_{tot}$ and $\Gamma_{ee}\Gamma_{\mu\mu}/\Gamma_{tot}$ can be obtained by measuring these cross sections and then fitting them.
- Combined $B(J/\psi \rightarrow l^+l^-) = \Gamma_{ll}/\Gamma_{tot}$ measured by our BESIII collaboration in 2013 ³, Γ_{tot} and Γ_{ll} can be obtained from $\Gamma_{ee}\Gamma_{ee}/\Gamma_{tot}$ and $\Gamma_{ee}\Gamma_{\mu\mu}/\Gamma_{tot}$ by parameter transformation.

¹X.Y. Zhou, Y.D. Wang, L.G. Xia, Analytical Forms of Cross Sections of Di-lepton Production from e^+e^- Collision around the J/ψ Resonance, arXiv:1701.00218.

²E.A. Kuraev, V.S. Fadin, Sov. J. Nucl. Phys., 41 (1985) 466.

³M. Ablikim, et al., BESIII Collaboration, Phys. Rev. D 88 (2013) 032007.

Improvement measurement of $\chi_{c0,2}$ two-photon width

Validate reliability of background function.

$$f_{bg} = p_0 + p_1 E + p_2 E^2 + p_3 E^a$$

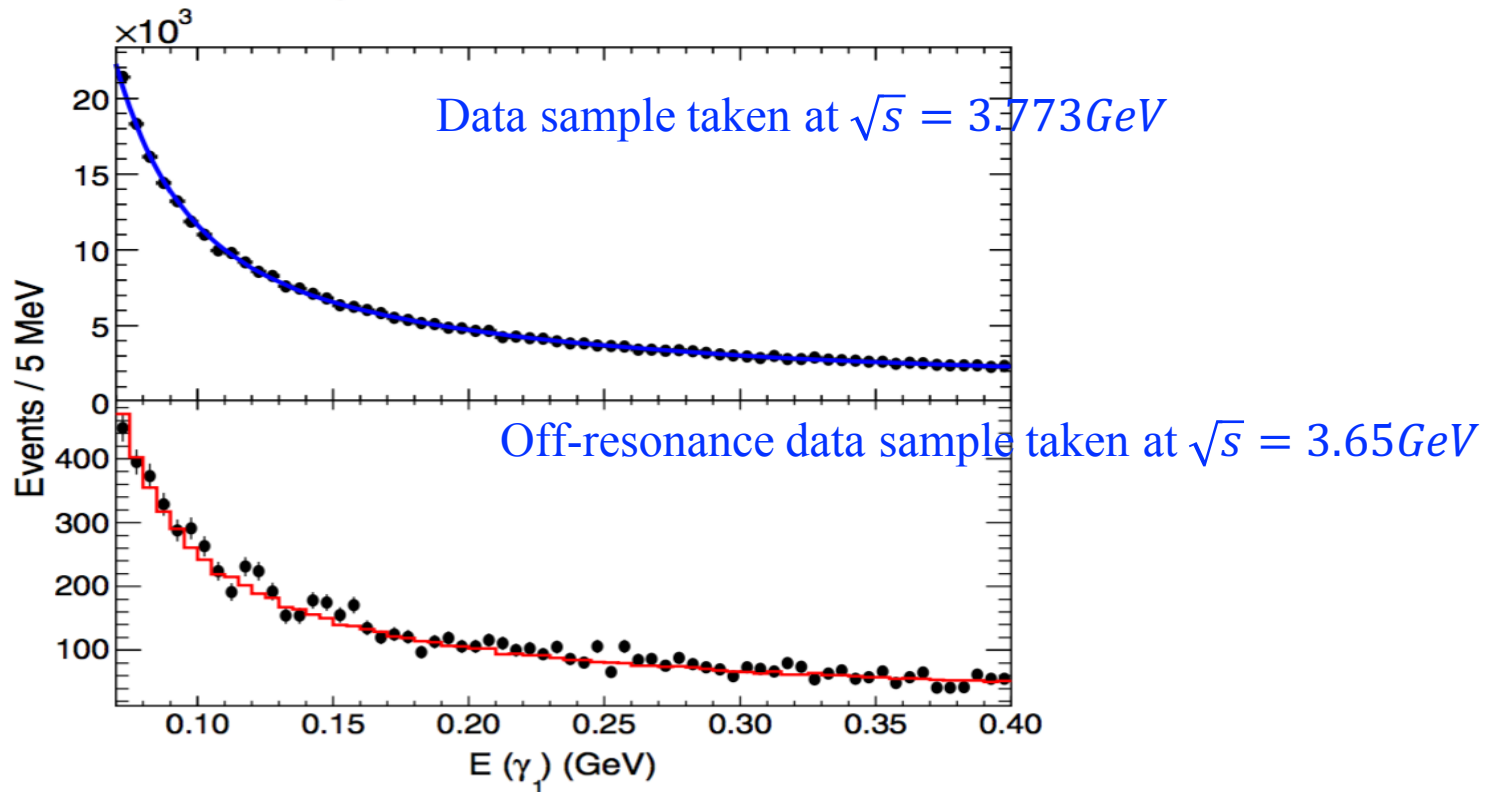


FIG. 2. Background $E(\gamma_1)$ spectrum. Upper plot: The best fit result (blue solid line) to $\psi(3770)$ data (dots with error bar) using Eq. (2). Lower plot: The comparison of $E(\gamma_1)$ spectrum between off- $\psi(3686)$ data (dots with error bar) and $\psi(3770)$ data (red histogram).

Measurement of $\chi_{c1,2}$ resonance parameters at LHCb

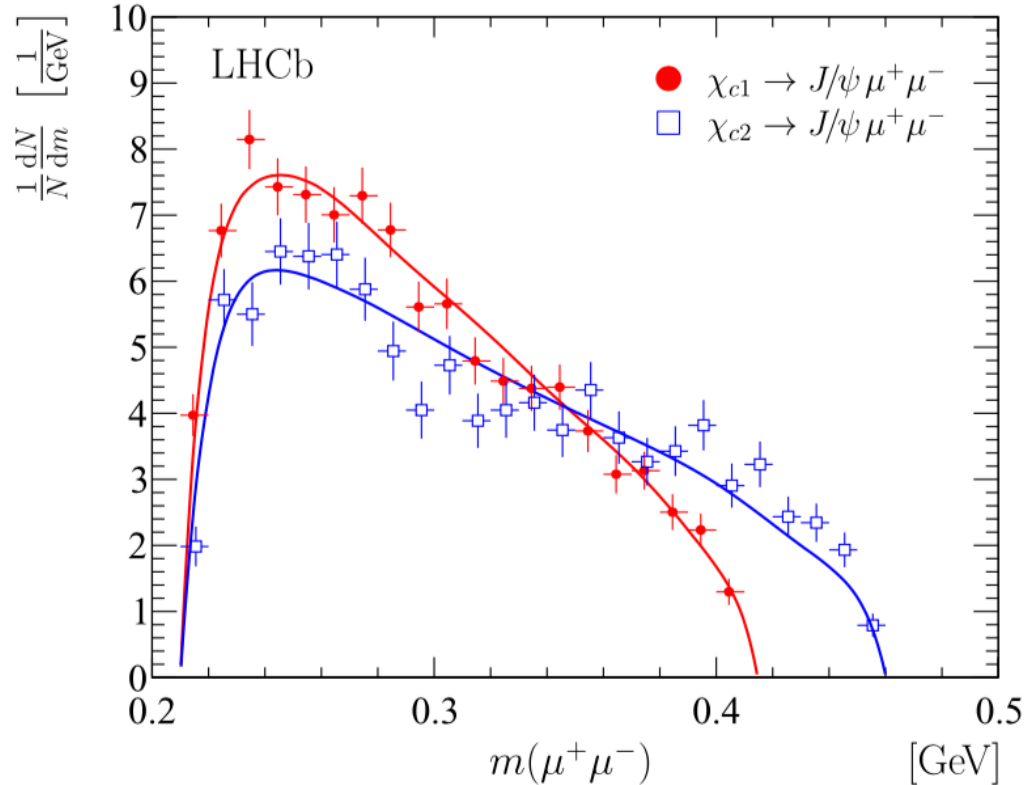


FIG. 2. Background-subtracted $m(\mu^+ \mu^-)$ distribution for $\chi_{c1} \rightarrow J/\psi \mu^+ \mu^-$ (solid red circles) and $\chi_{c2} \rightarrow J/\psi \mu^+ \mu^-$ (open blue squares) decays. The distributions are normalized to the unit area. The curves show the expected distribution from the simulation, which uses the model described in Ref. [29].

Observation of $X^*(3860)$ or $\chi_{c0}(2P)$

K. CHILIKIN *et al.*

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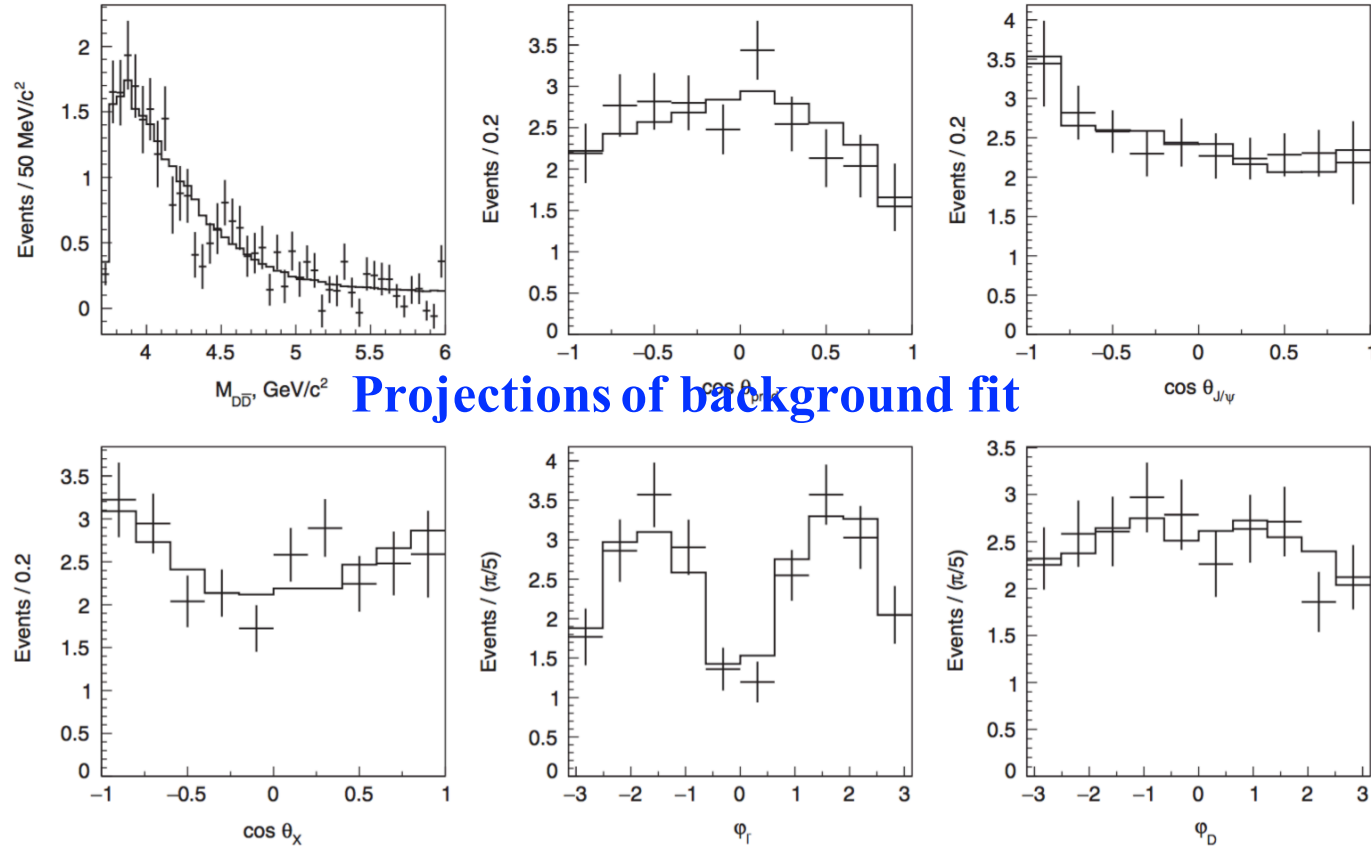


FIG. 5. Projections of the background fit results onto $M_{D\bar{D}}$ and angular variables. The points with error bars are data, and the solid line is the fit result.