



Institute of Particle Physics, University of  
València, Spain.

Institute of Physics, University of São Paulo,  
Brazil.



Disclosing  $D^* \bar{D}^*$  molecules in the  
 $B_c^- \rightarrow \pi^- J/\psi \omega$  decay

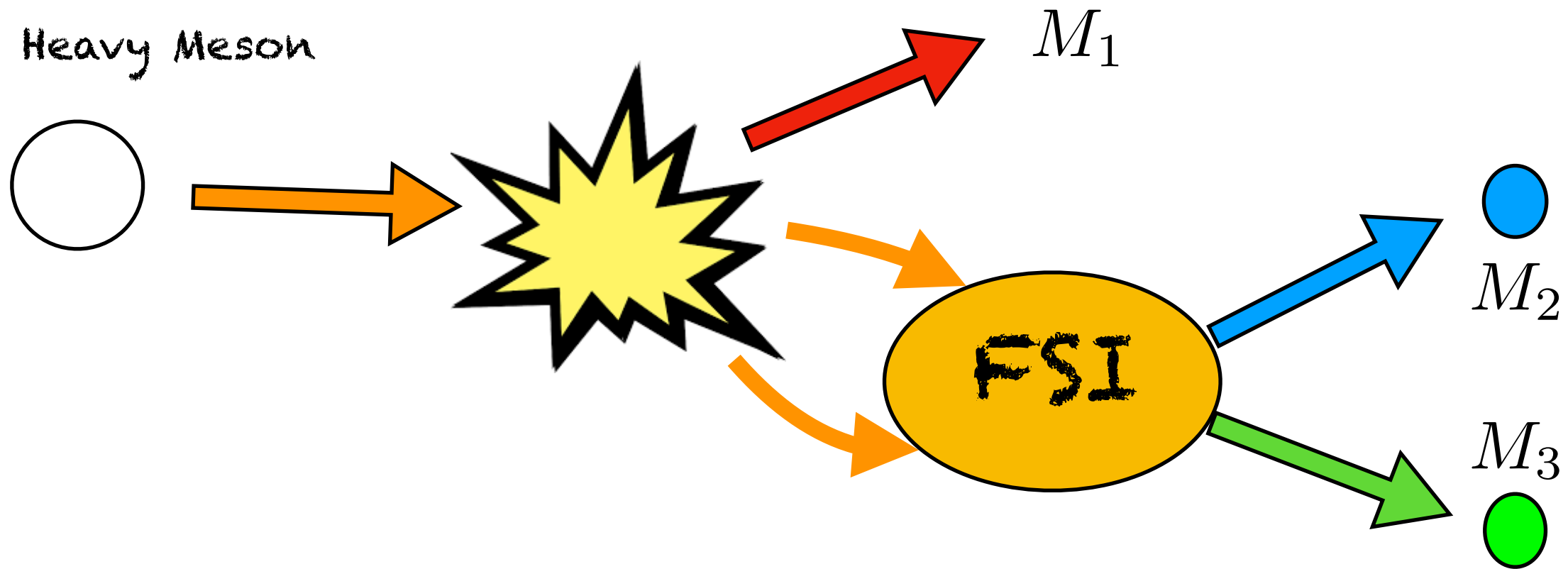
**Jorgivan M. Dias**

In collaboration with: **E. Oset**  
**LiangRong Dai**

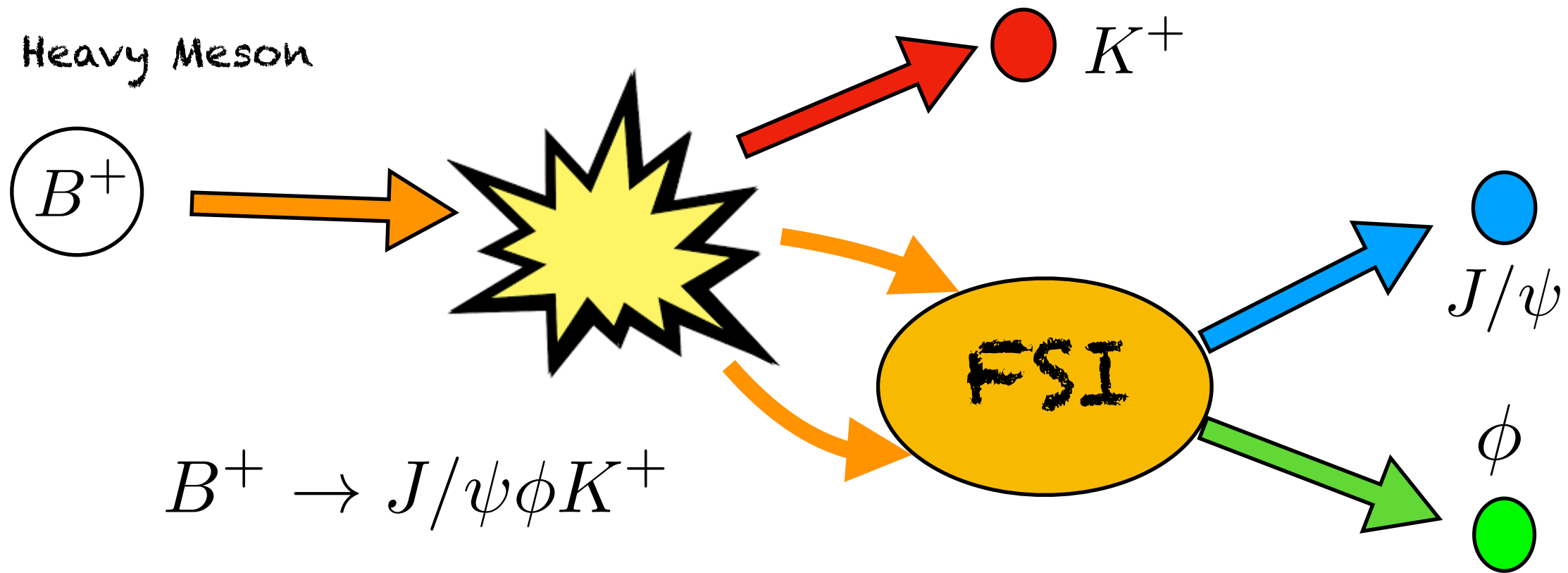


São Paulo Research Foundation

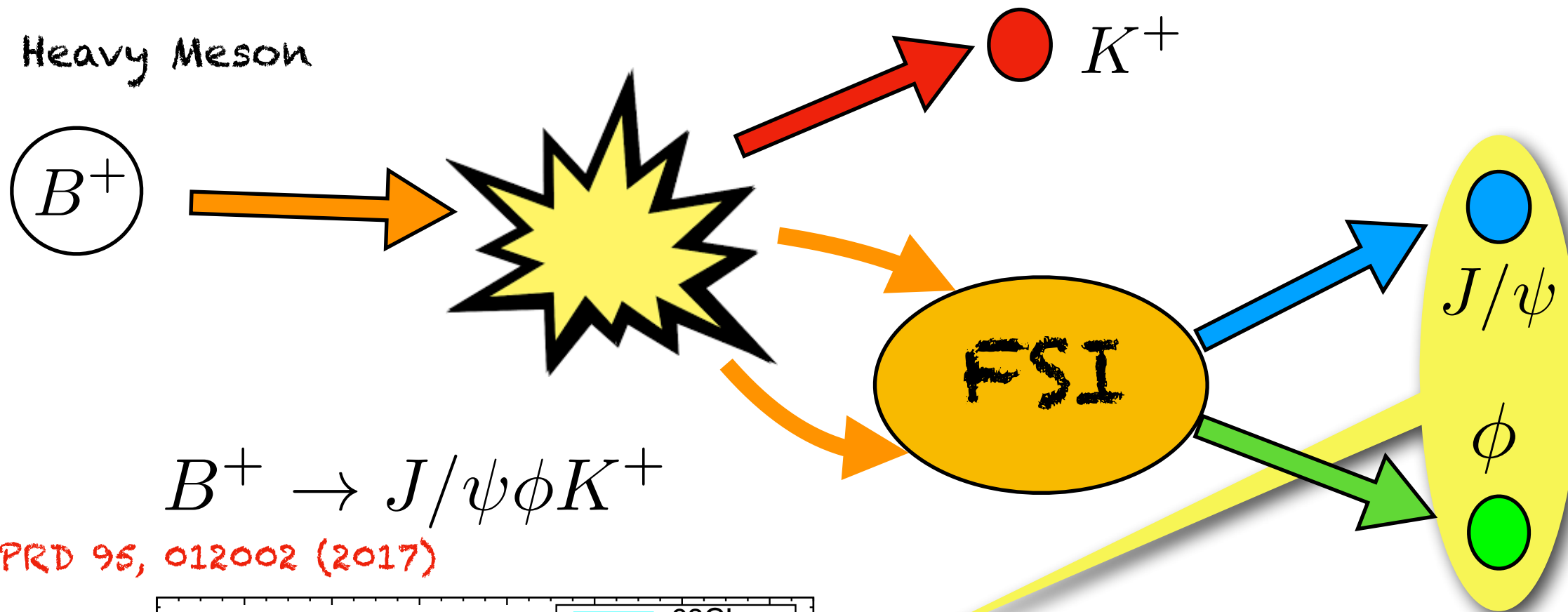
# Heavy meson decays



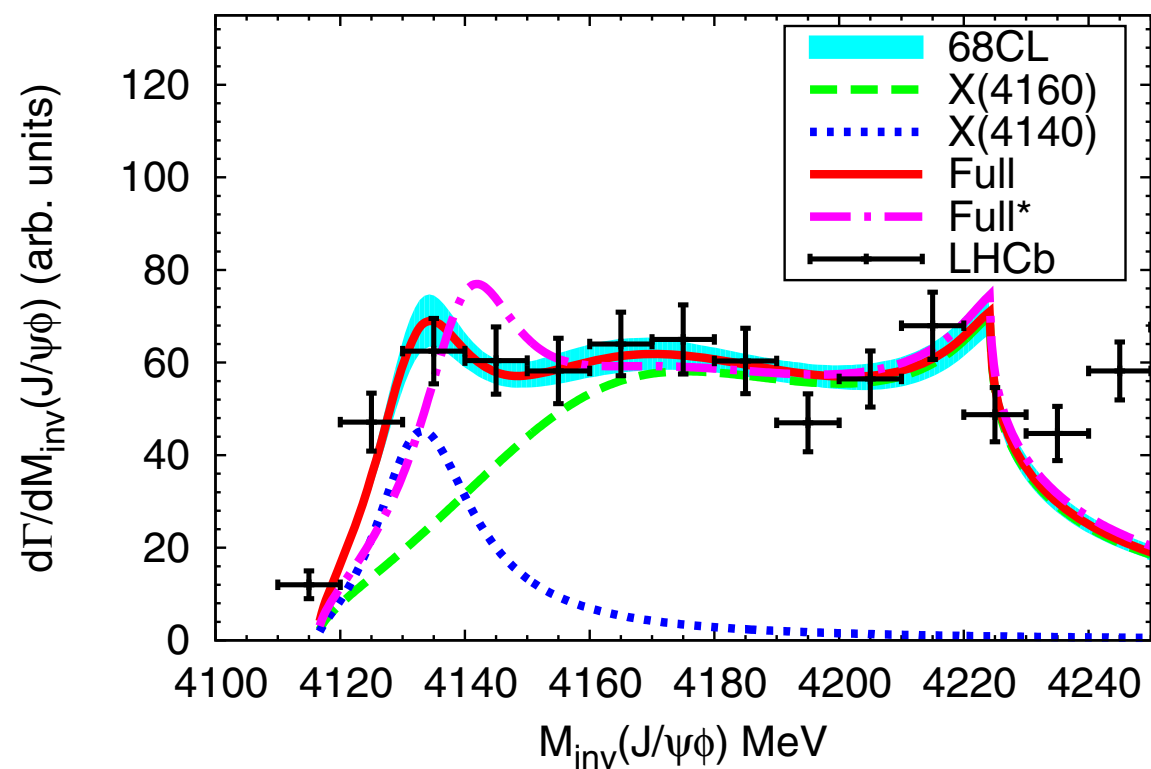
# Heavy meson decays



# Heavy meson decays

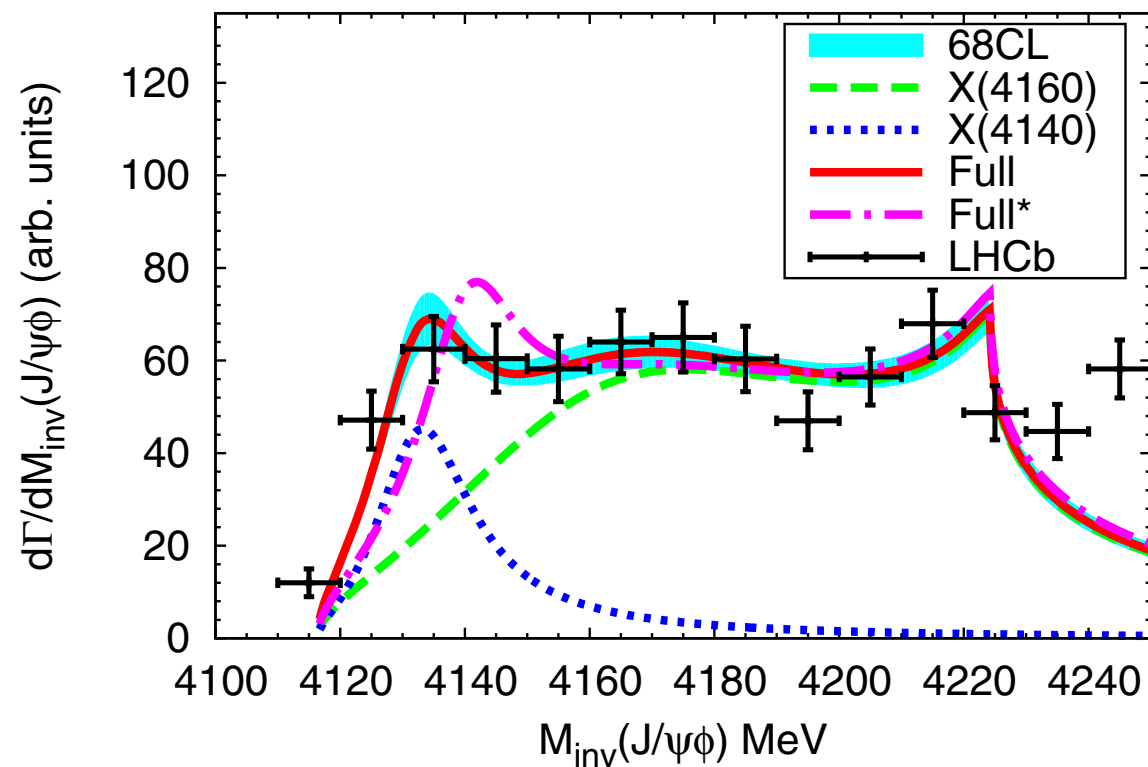
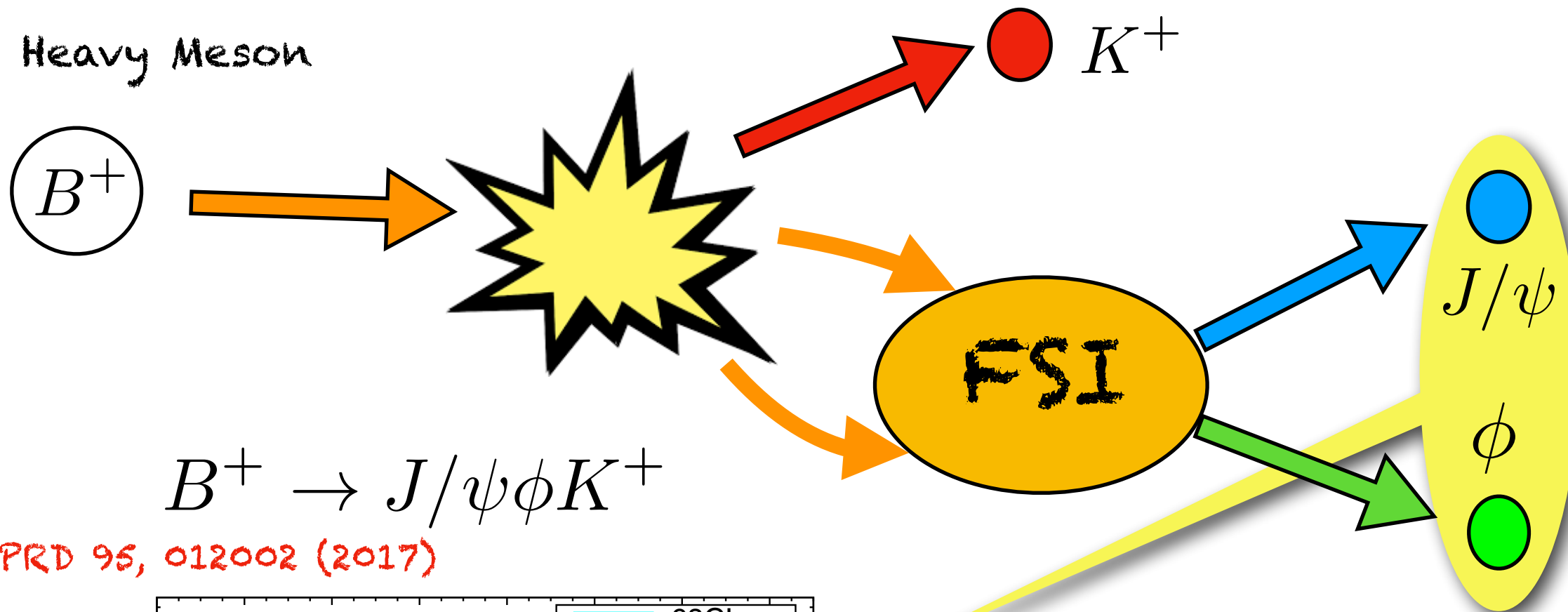


PRD 95, 012002 (2017)





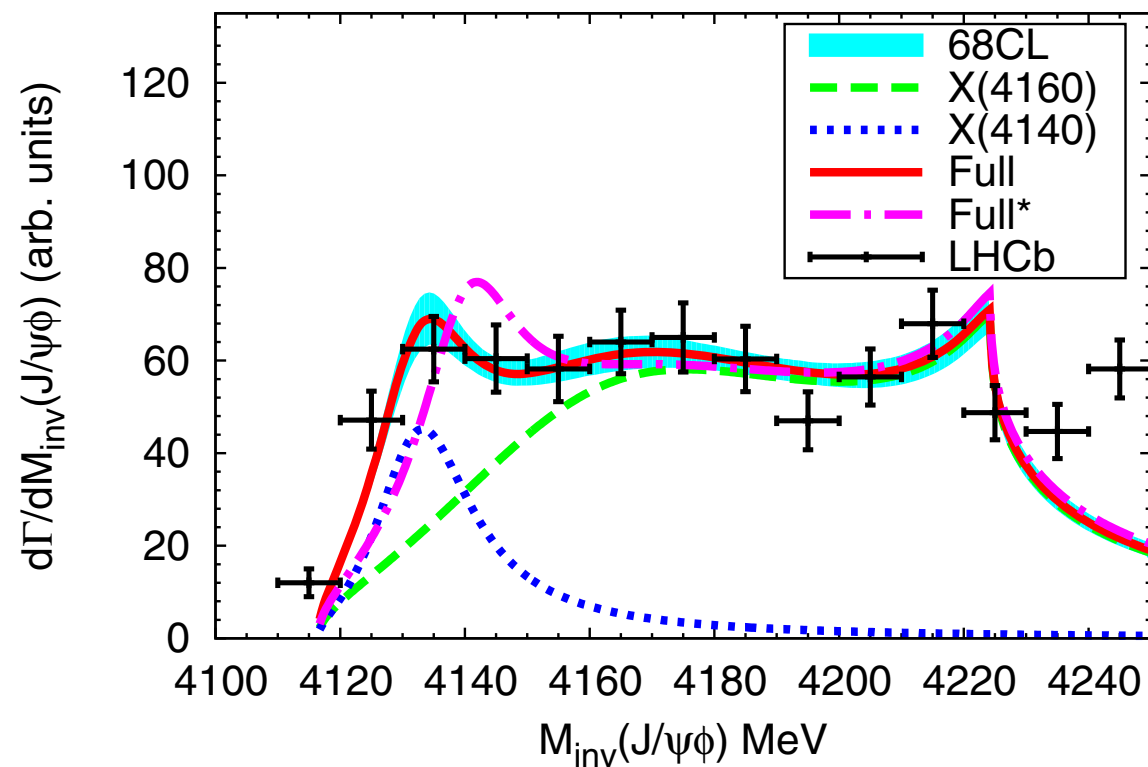
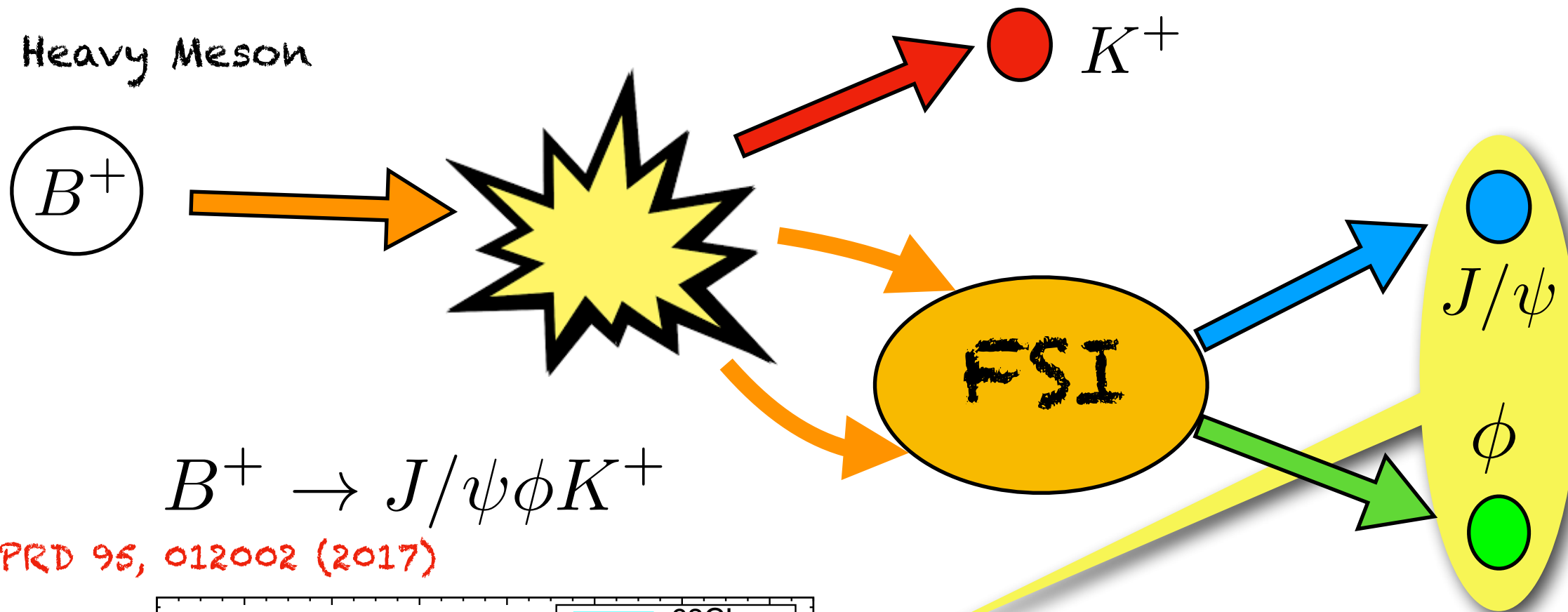
# Heavy meson decays



PRD 80, 114013 (2017)

$0^+(2^{++})$   
 $D_s^* \bar{D}_s^*$   
 $J/\psi \phi$   
 $\vdots$

# Heavy meson decays



PRD 80, 114013 (2017)

X(4160)

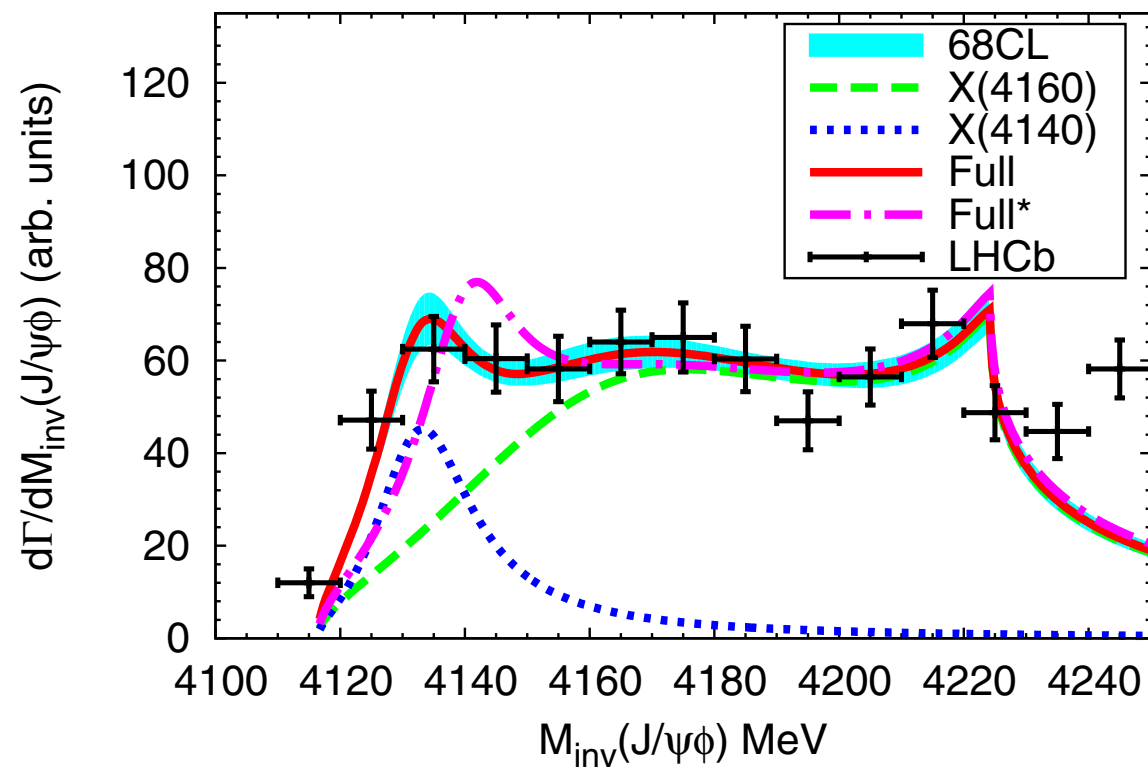
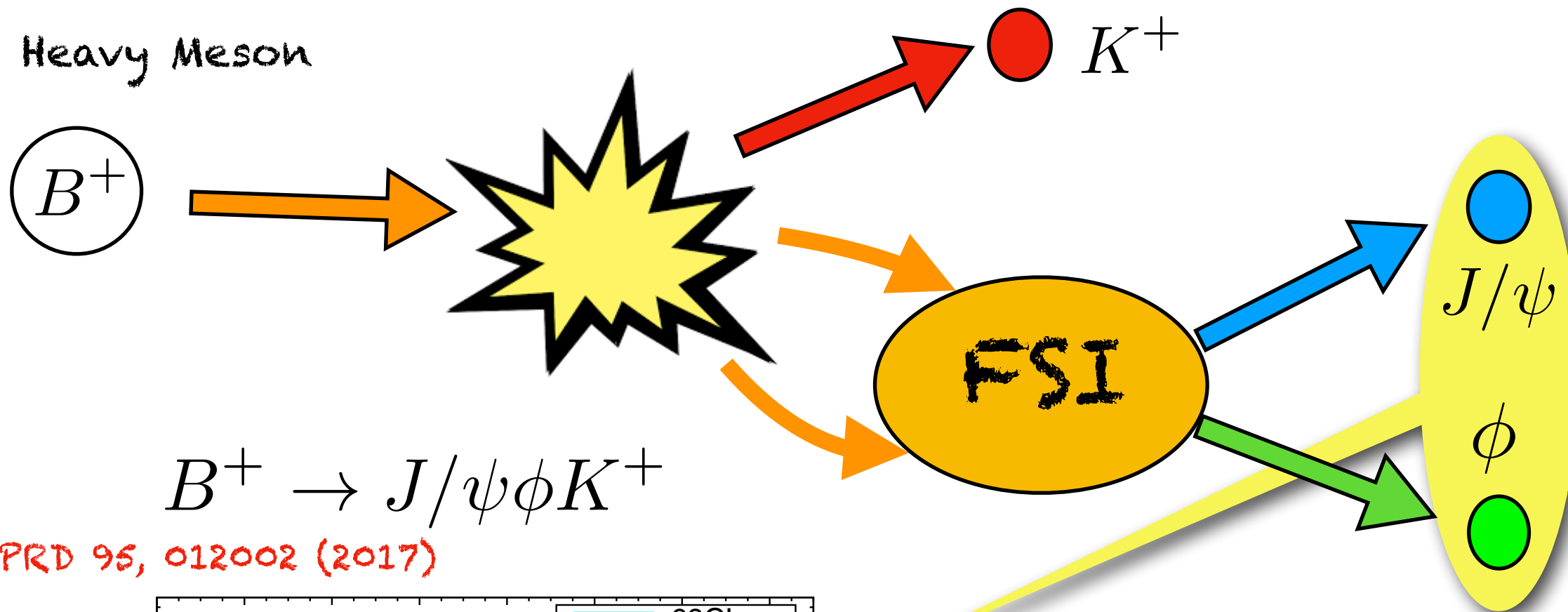
$0^+(2^{++})$

$D_s^* \bar{D}_s^*$

$J/\psi \phi$

⋮

# Heavy meson decays



PRD 80, 114013 (2017)

X(4160)

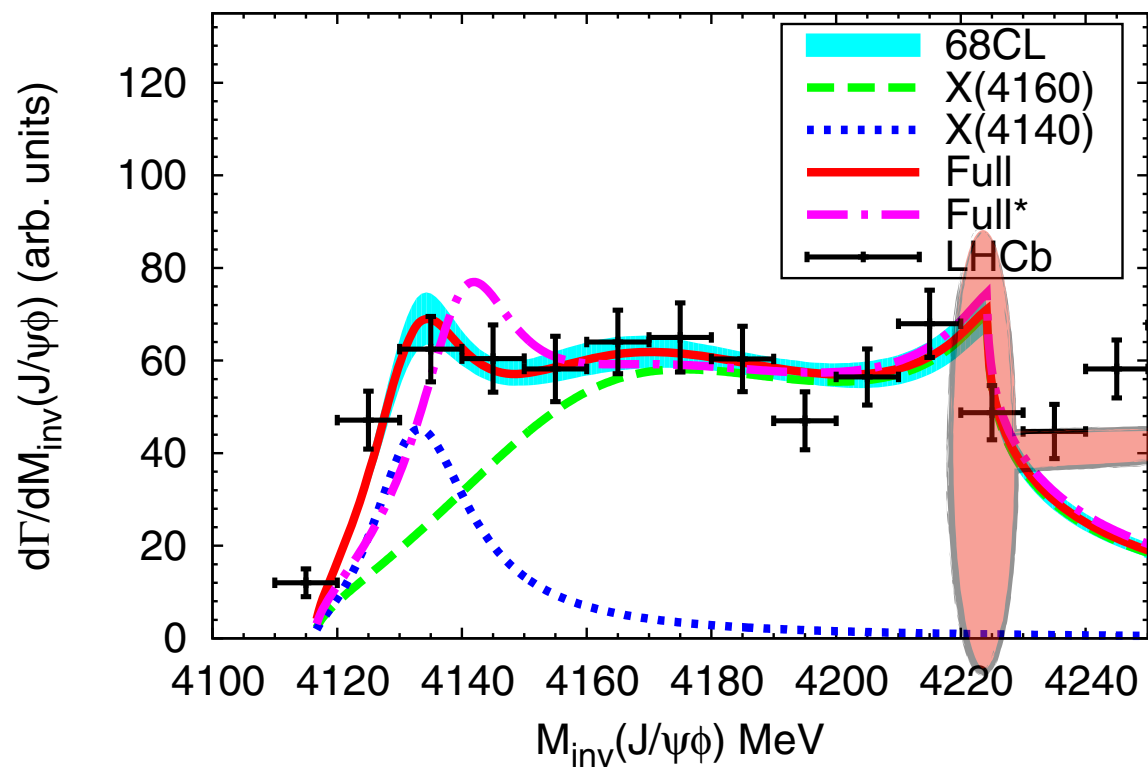
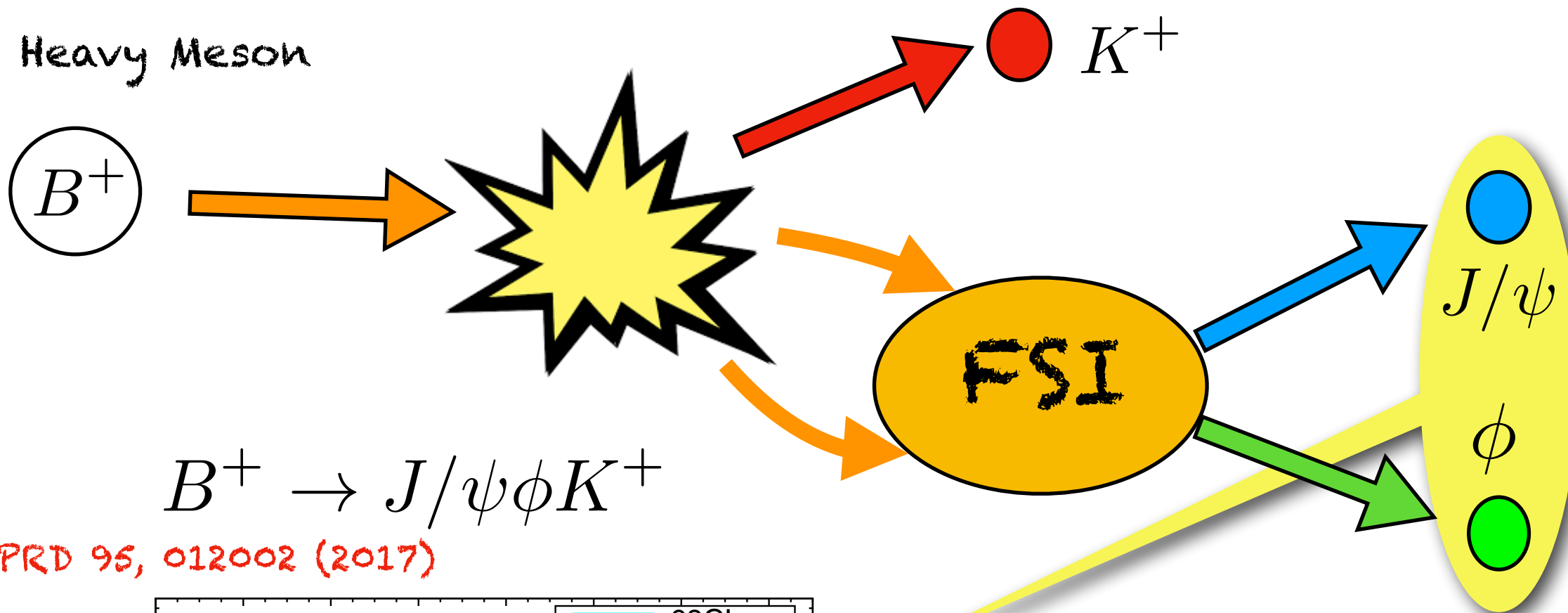
$0^+(2^{++})$

$D_s^* \bar{D}_s^*$

$J/\psi \phi$

⋮

# Heavy meson decays



PRD 80, 114013 (2017)

X(4160)

$0^+(2^{++})$

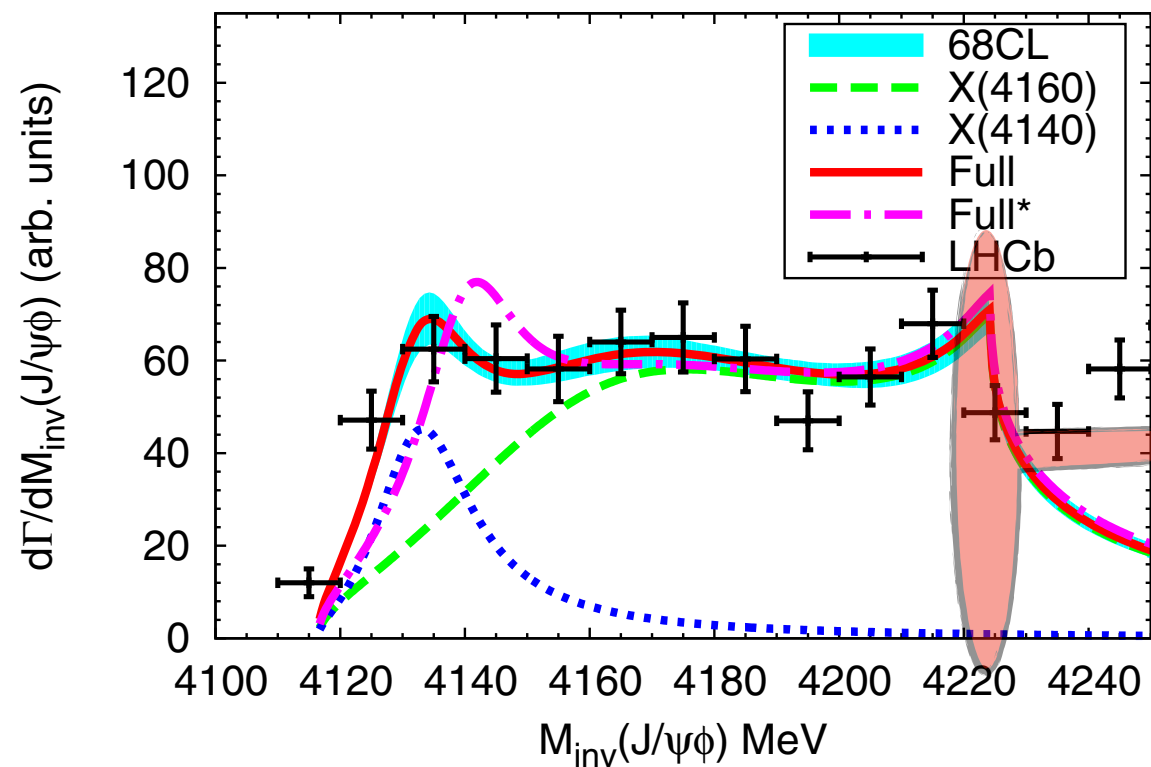
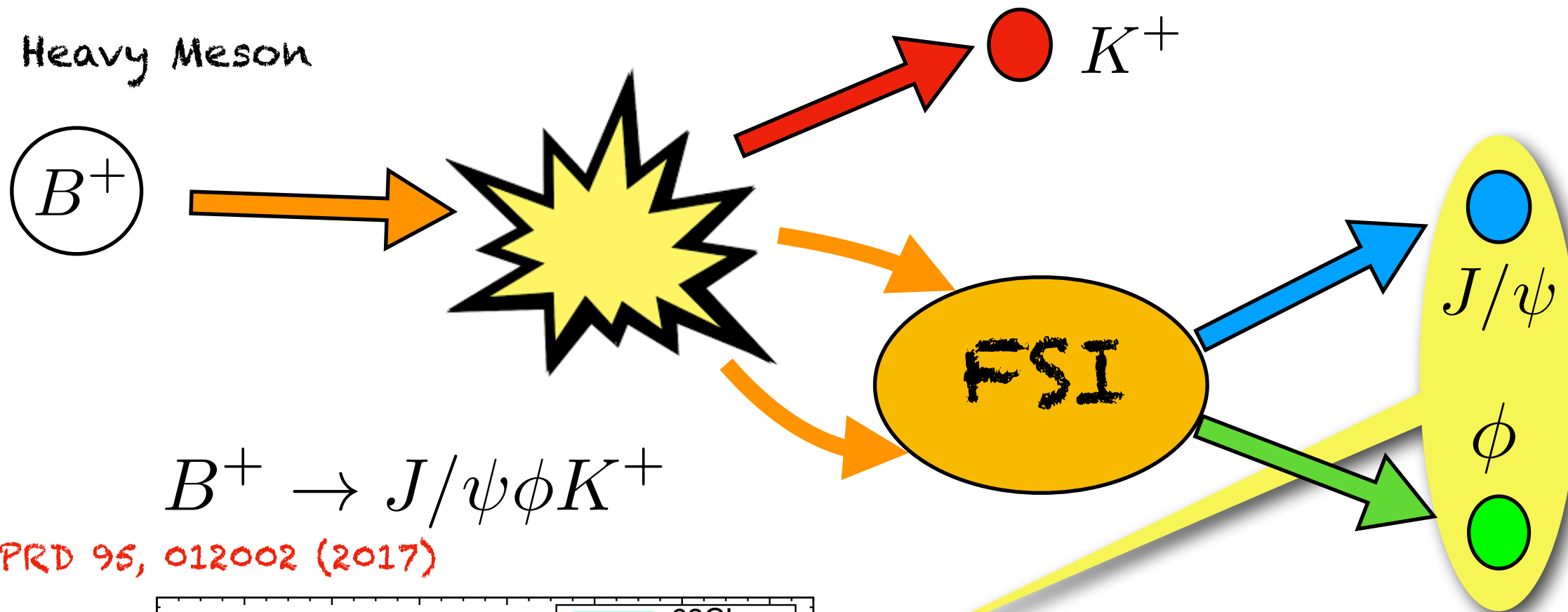
$D_s^* \bar{D}_s^*$

$J/\psi\phi$

⋮

Cusp!

# Heavy meson decays



PRD 80, 114013 (2017)

X(4160)

$0^+(2^{++})$

$D_s^* \bar{D}_s^*$

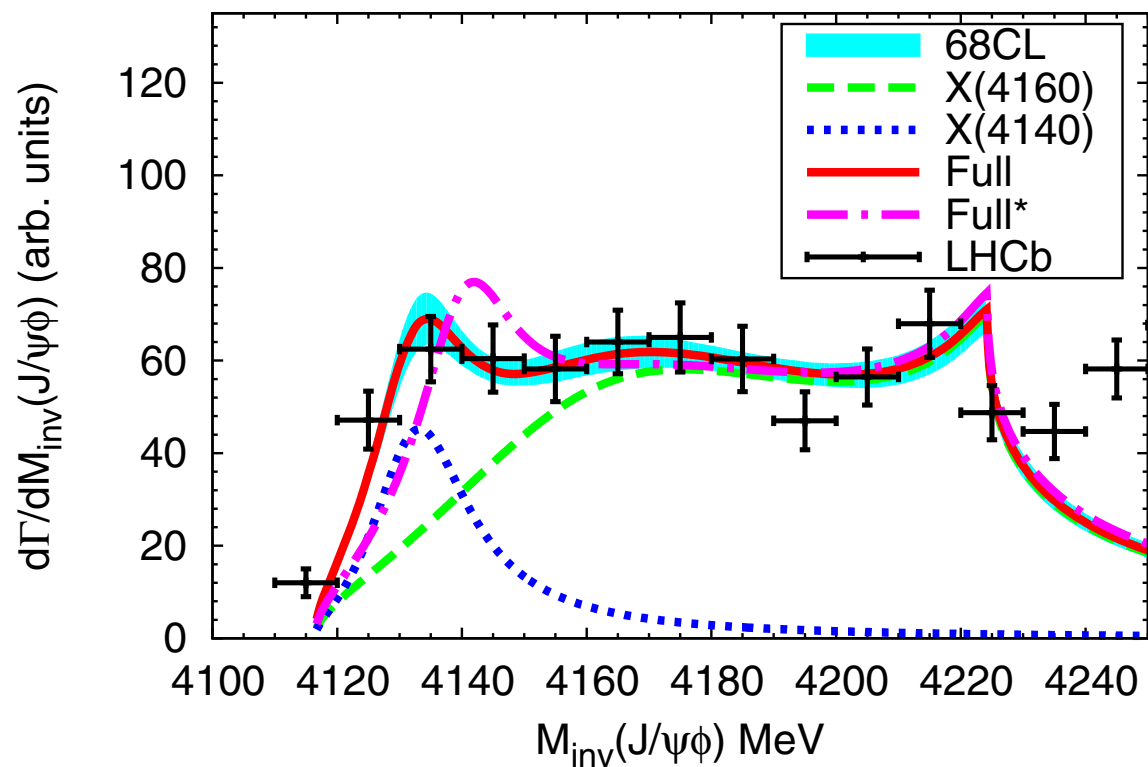
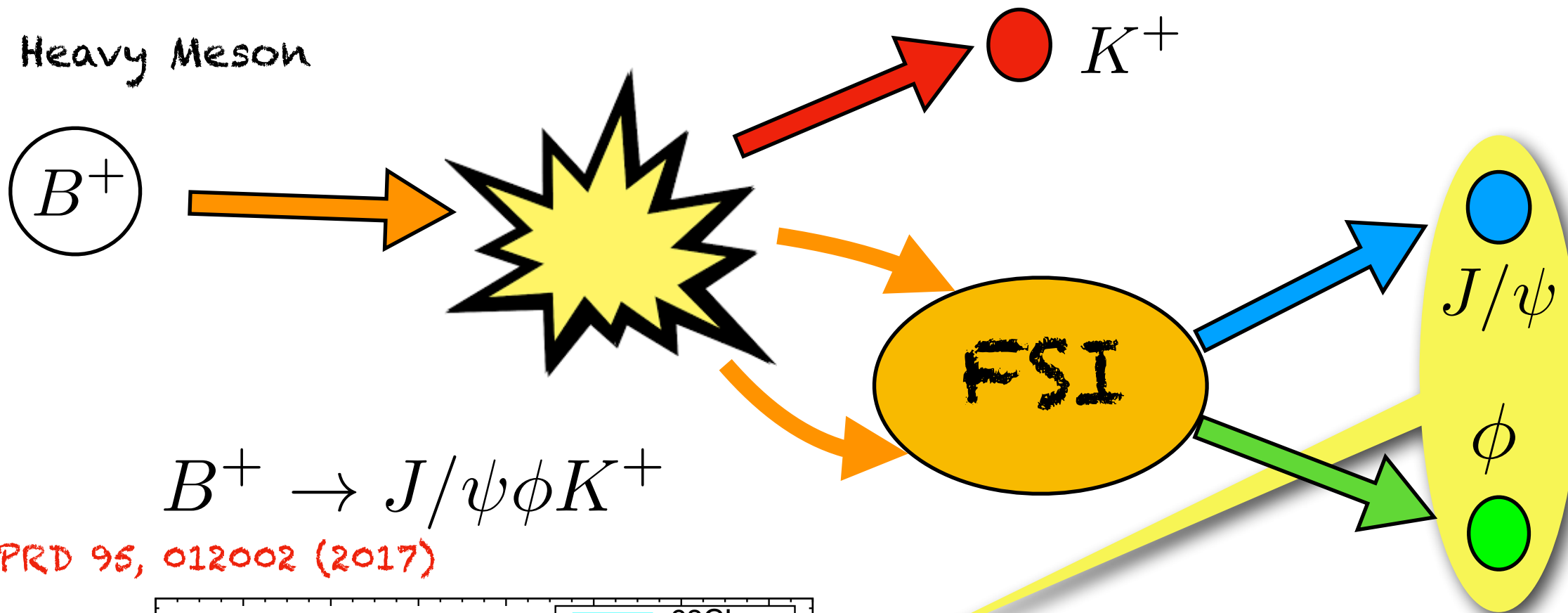
$J/\psi\phi$

⋮

Cusp!

So, we can look for this behavior to test the molecular nature of some states!

# Heavy meson decays



PRD 80, 114013 (2017)

$D^* \bar{D}^*$

$0^+(0^{++})$

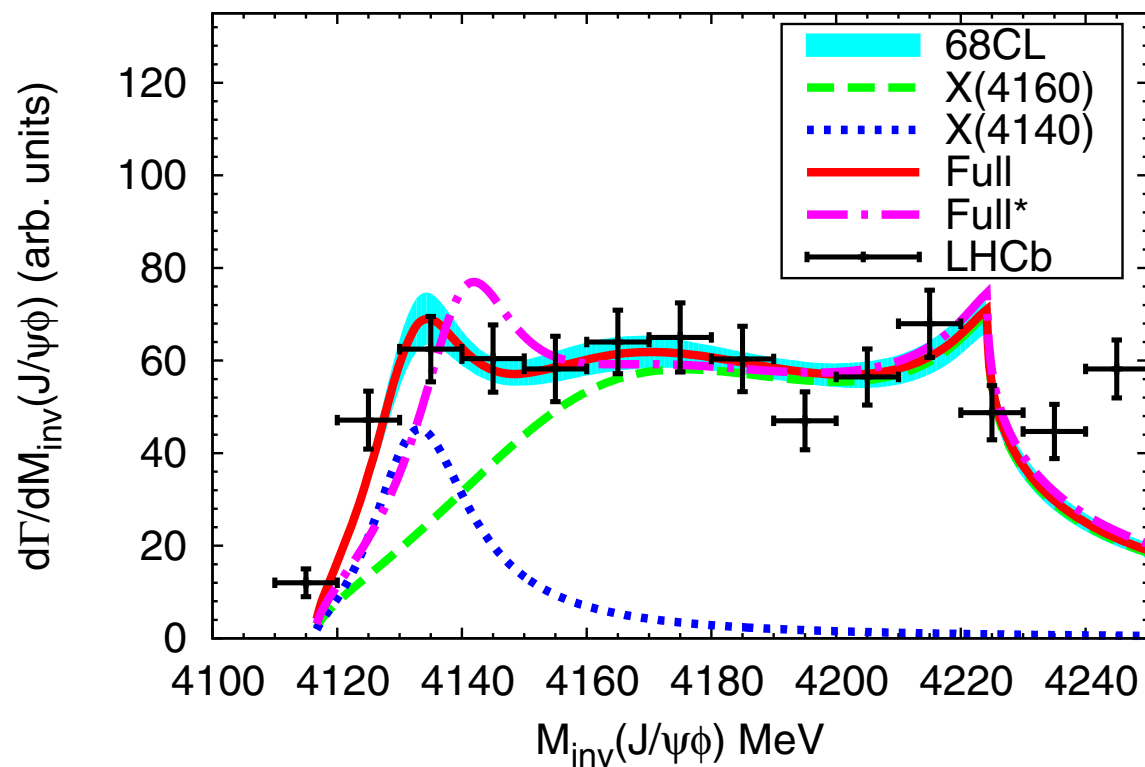
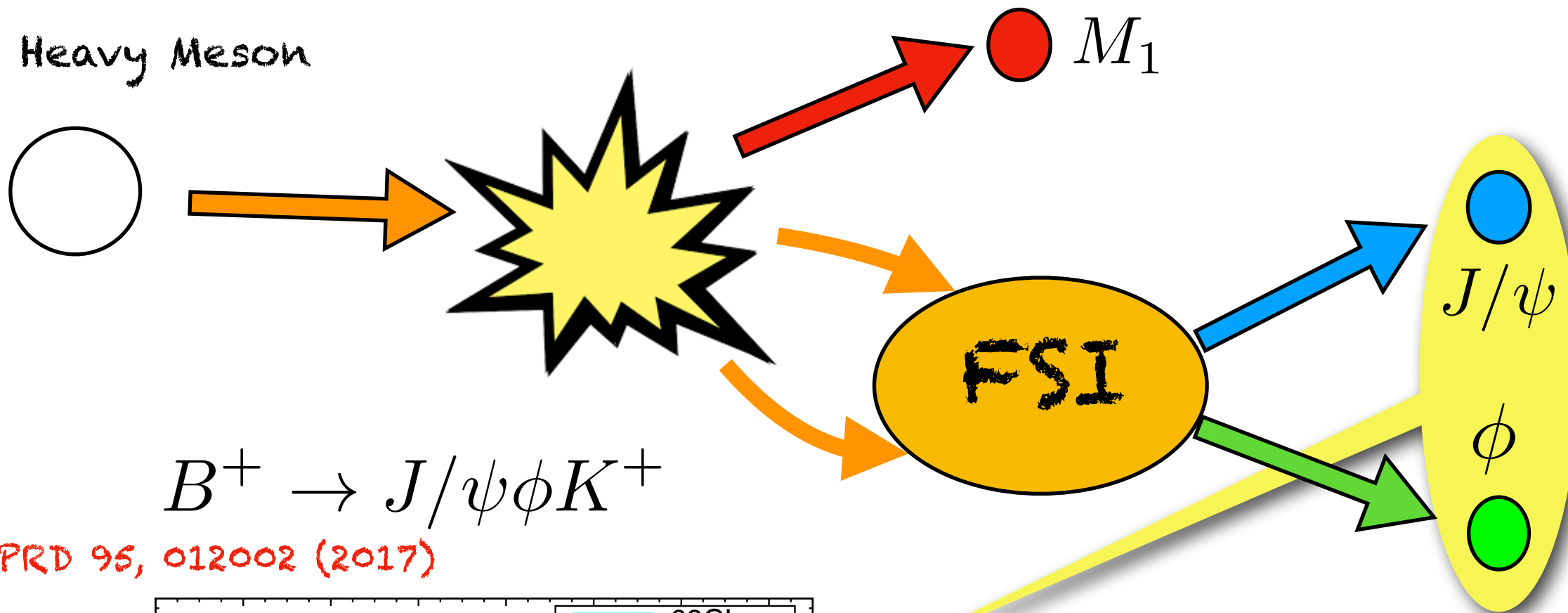
X(3940)

$0^+(2^{++})$

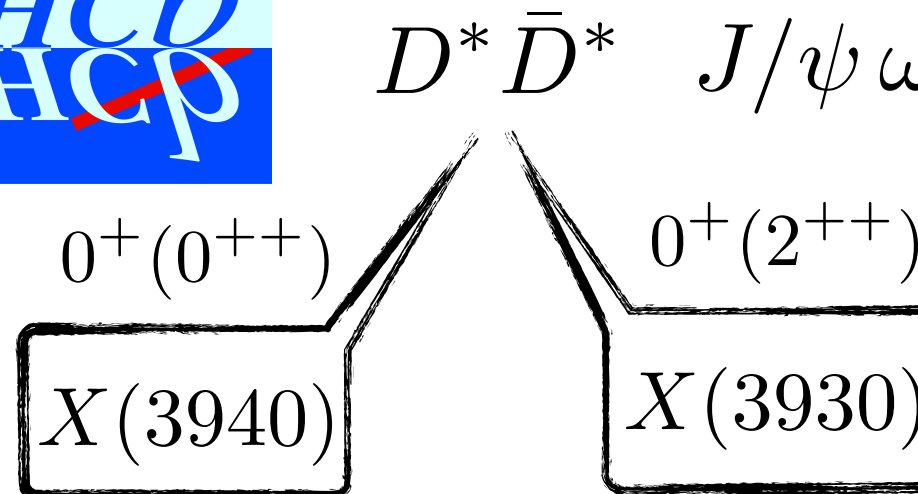
X(3930)



# Heavy meson decays

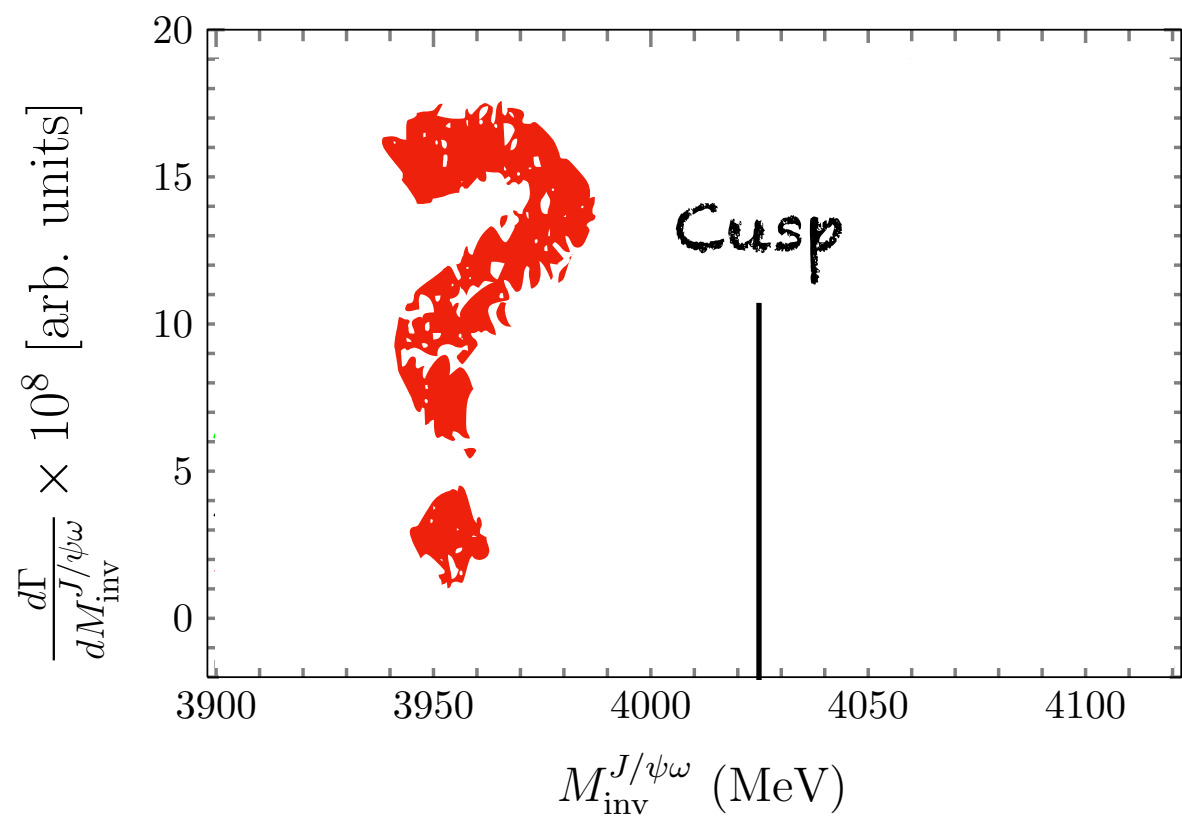
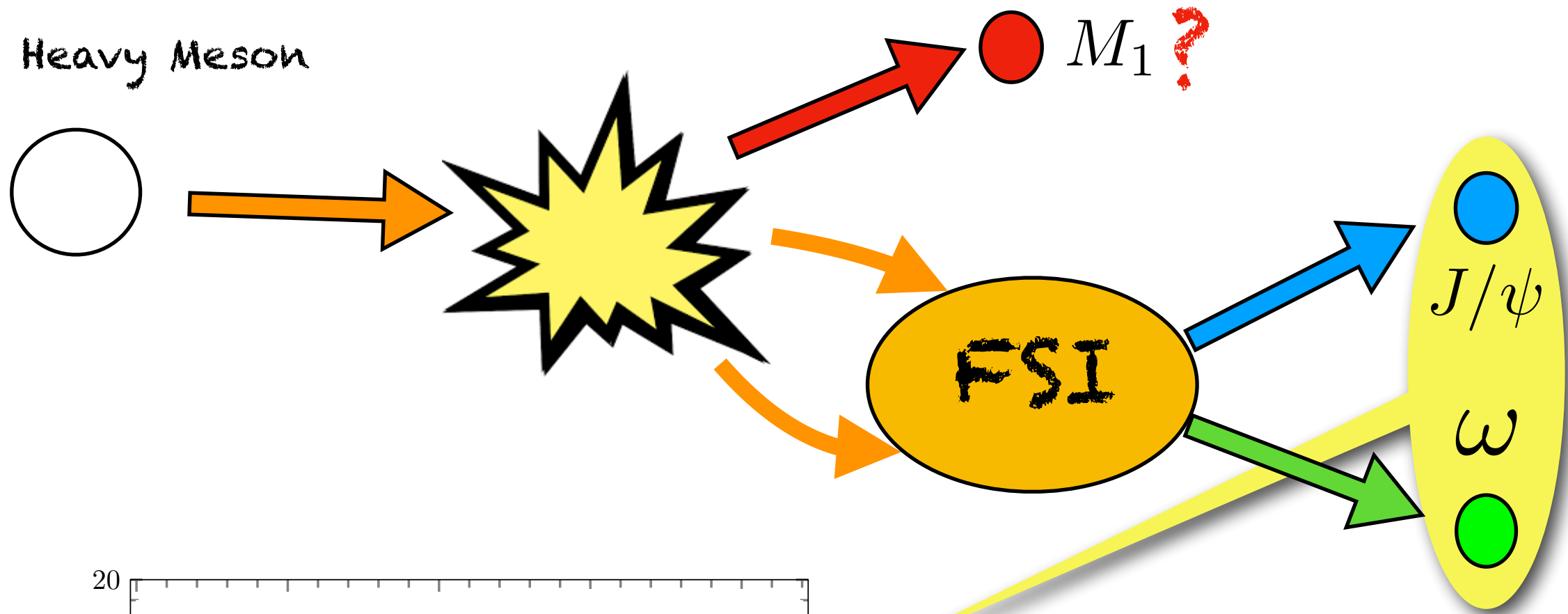


PRD 80, 114013 (2017)



Both states also couple to  $J/\psi \omega$

# Heavy meson decays



PRD 80, 114013 (2017)

$D^* \bar{D}^* \quad J/\psi \omega$

$0^+(0^{++})$

$X(3940)$

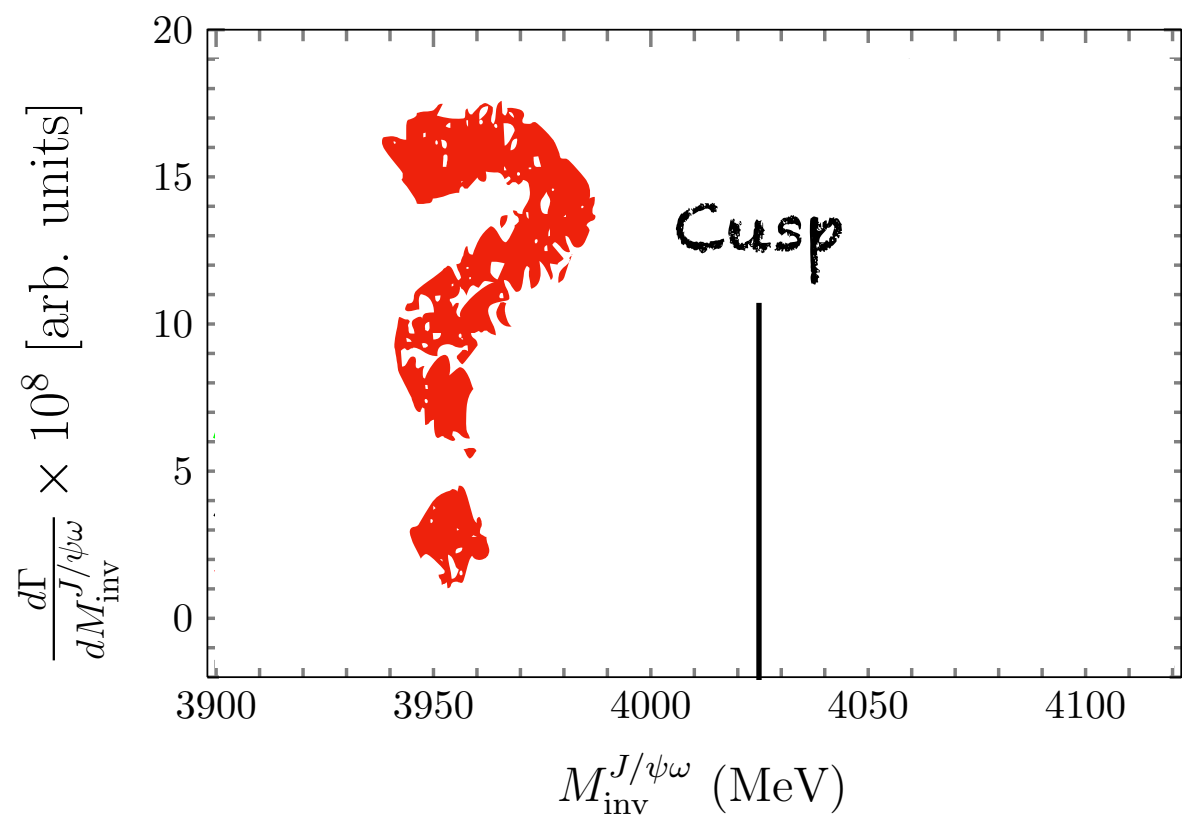
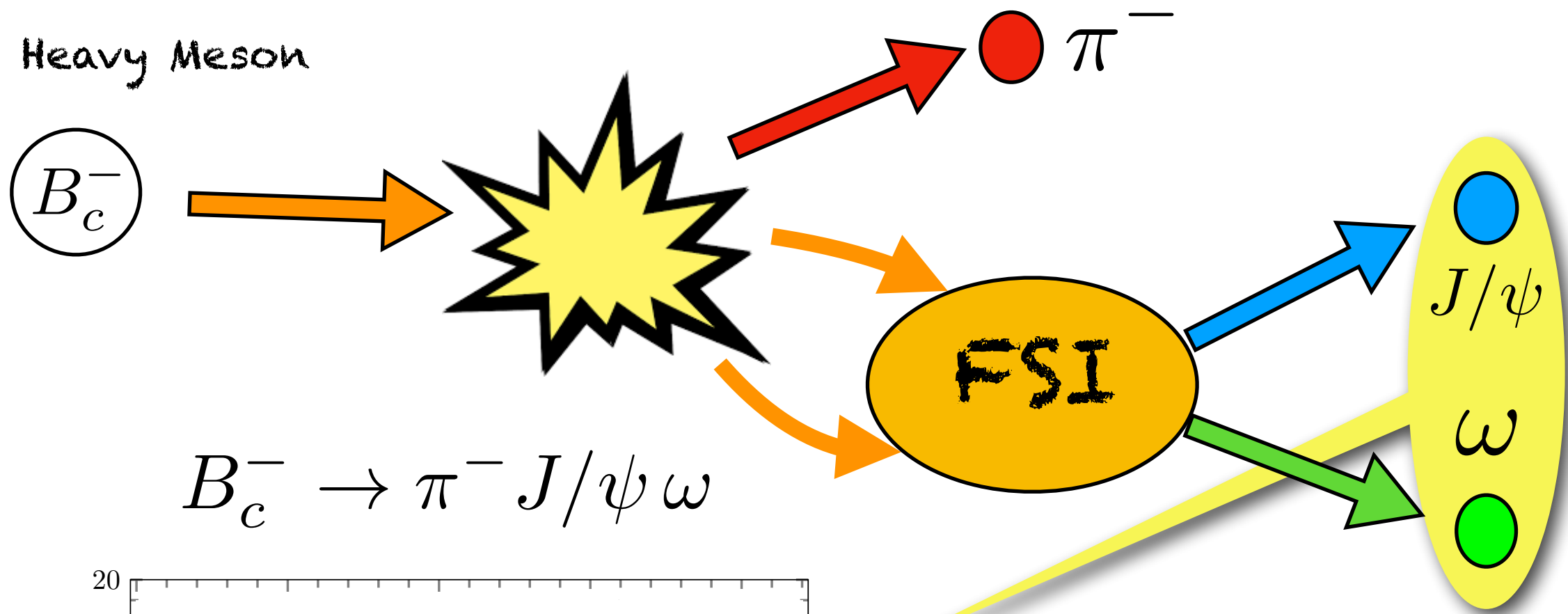
$0^+(2^{++})$

$X(3930)$

Both states also couple to  $J/\psi \omega$



# Heavy meson decays



PRD 80, 114013 (2017)

$D^* \bar{D}^* J/\psi \omega$

$0^+(0^{++})$


$X(3940)$

$0^+(2^{++})$

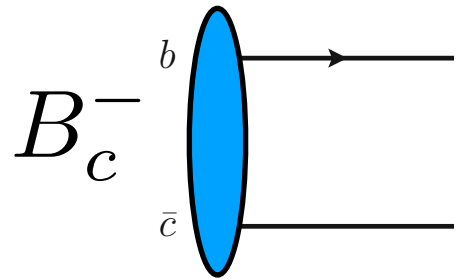
$X(3930)$

Both states also couple to  $J/\psi \omega$

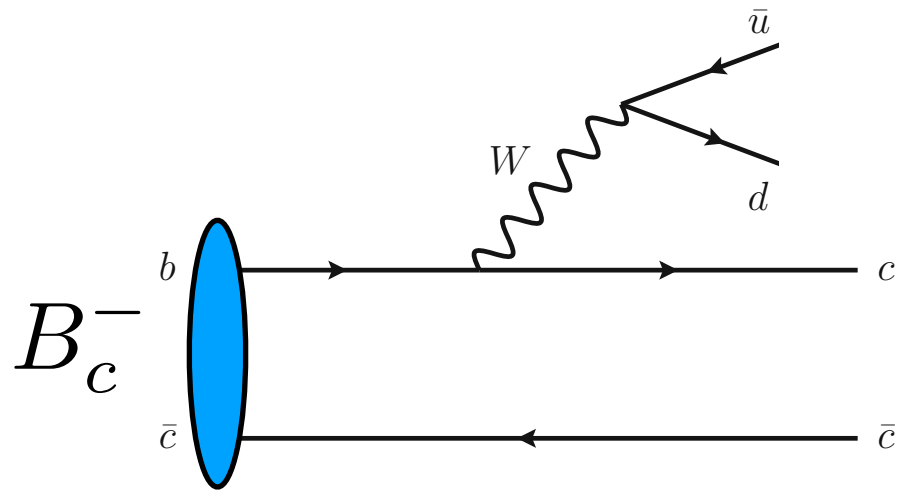
# Formalism...

$$B_c^{-} \begin{matrix} b \\ \bar{c} \end{matrix}$$


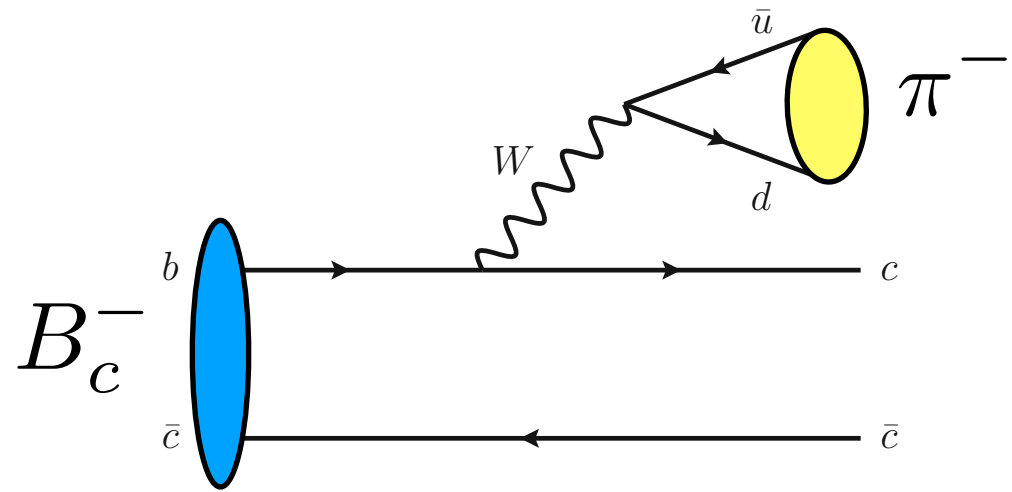
# Formalism...



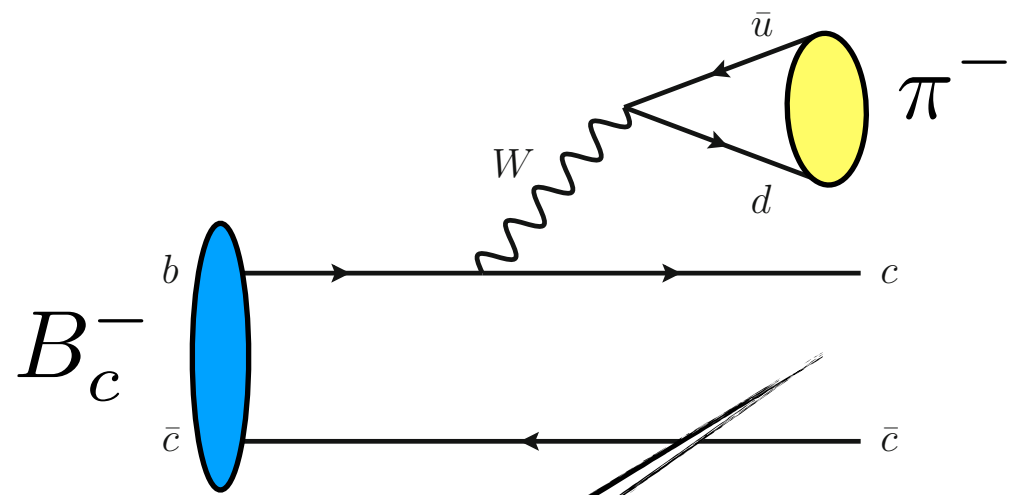
# Formalism...



# Formalism...



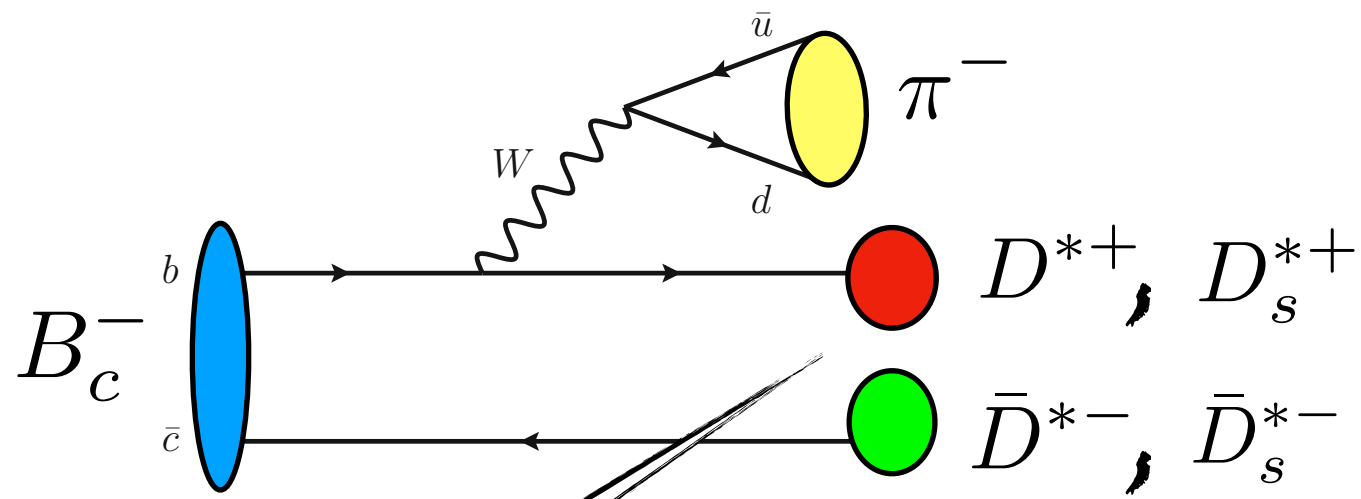
# Formalism...



Hadronized

$$\bar{u}u + \bar{d}d + \bar{s}s$$

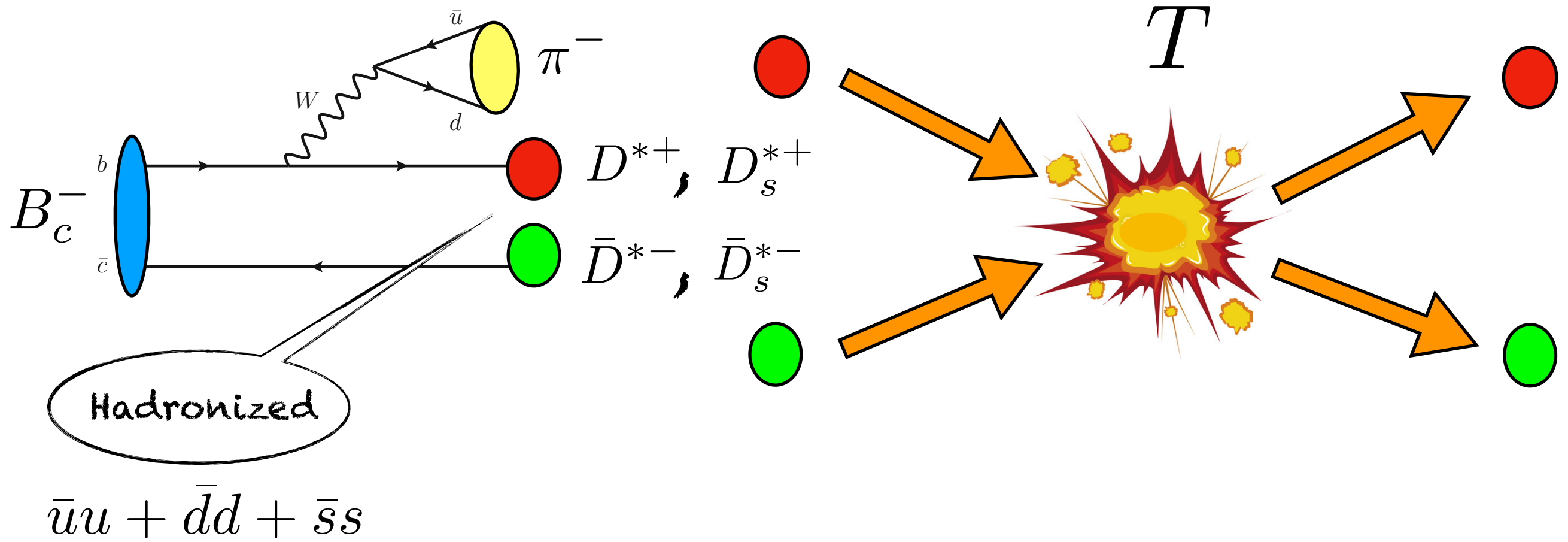
# Formalism...



Hadronized

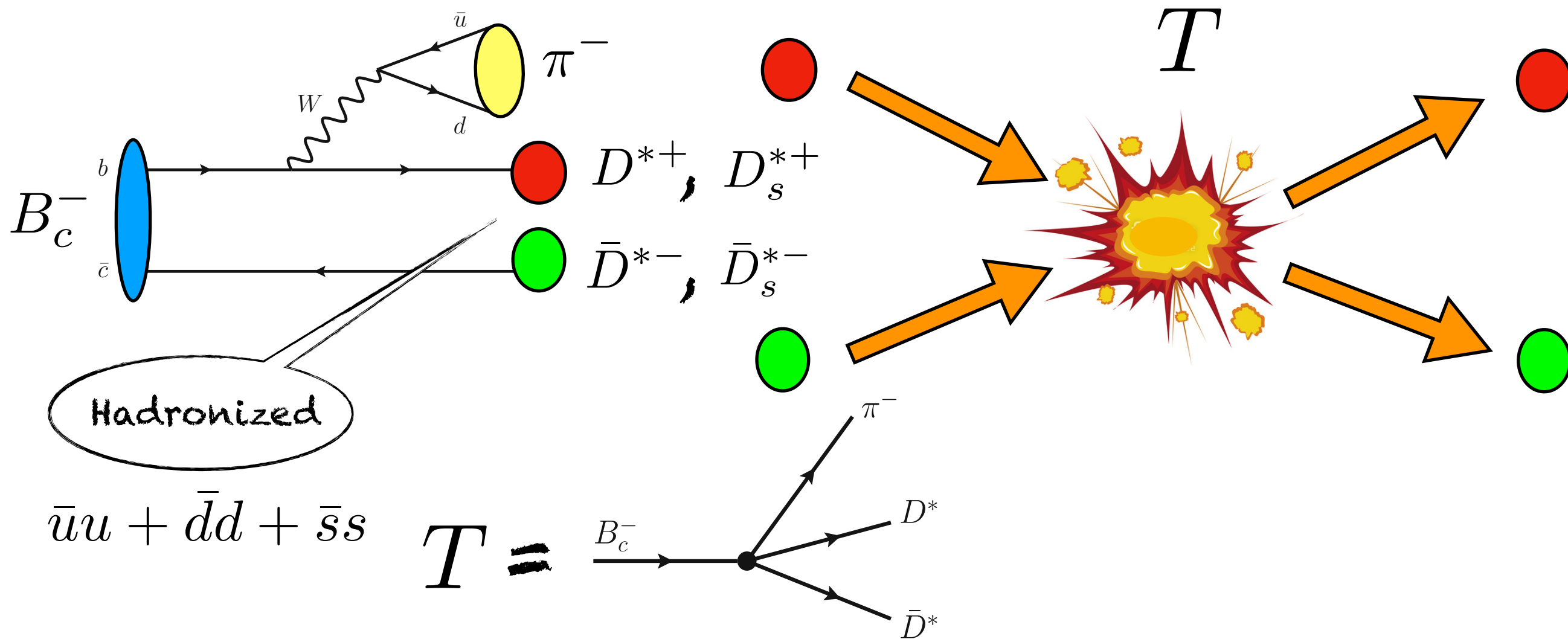
$$\bar{u}u + \bar{d}d + \bar{s}s$$

# Formalism...

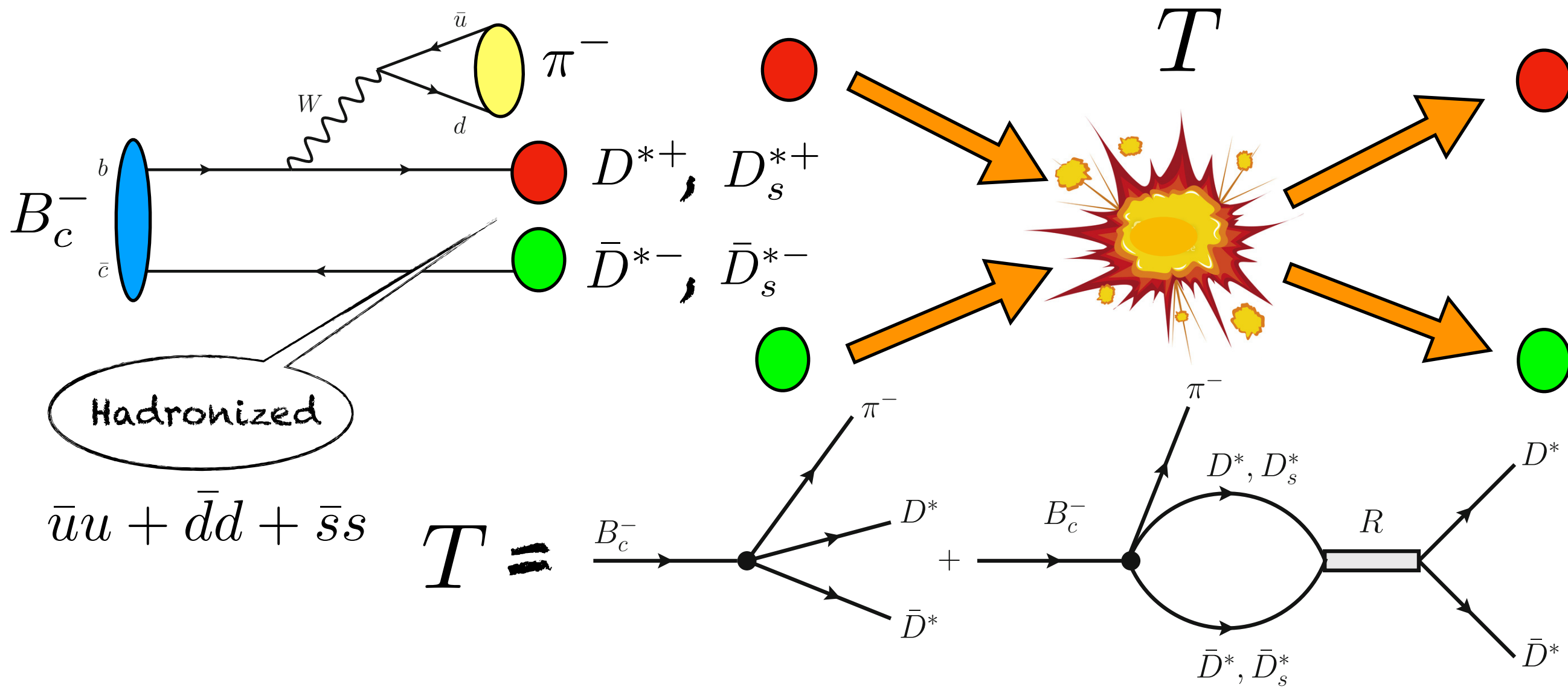




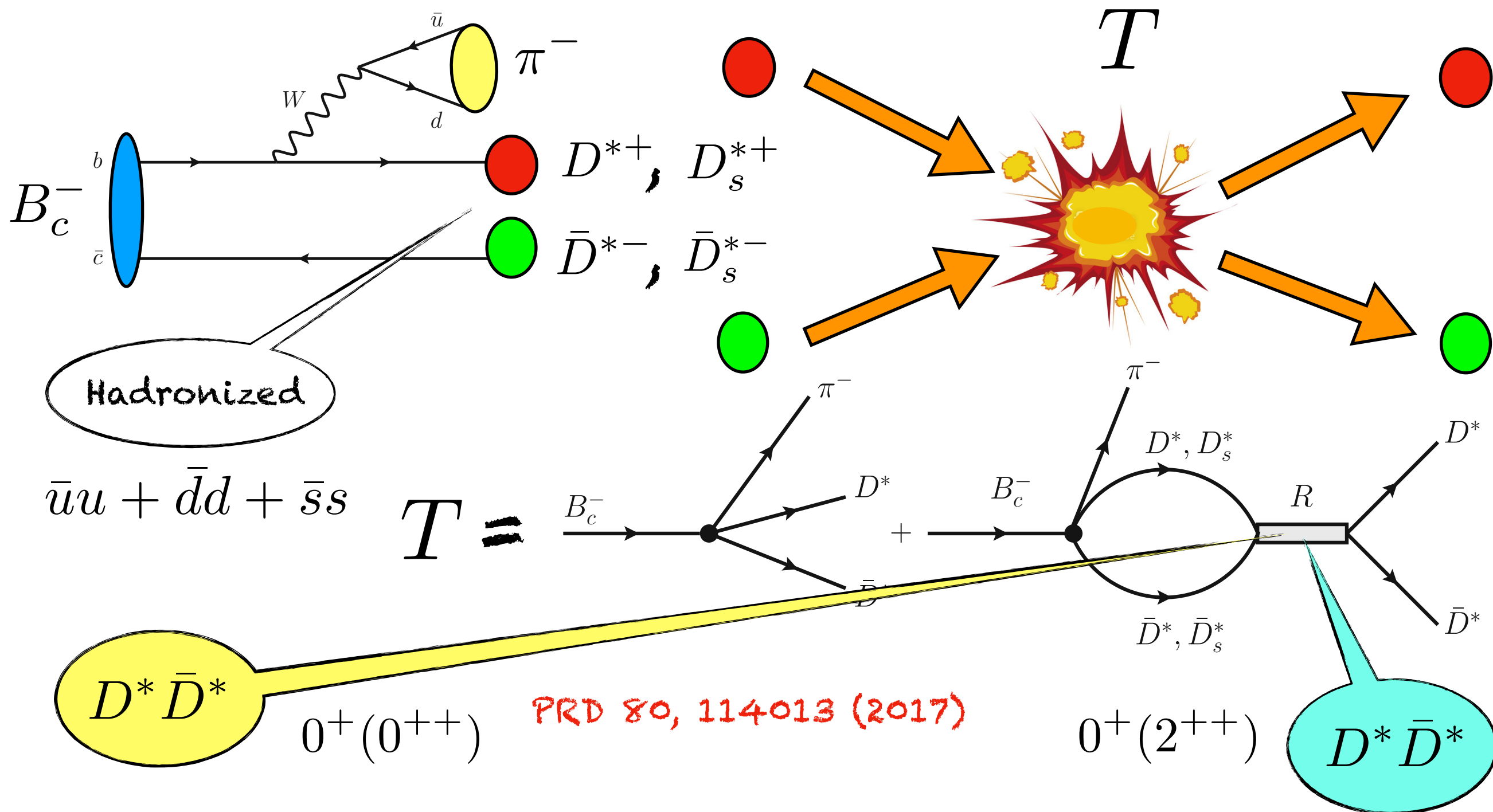
# Formalism...



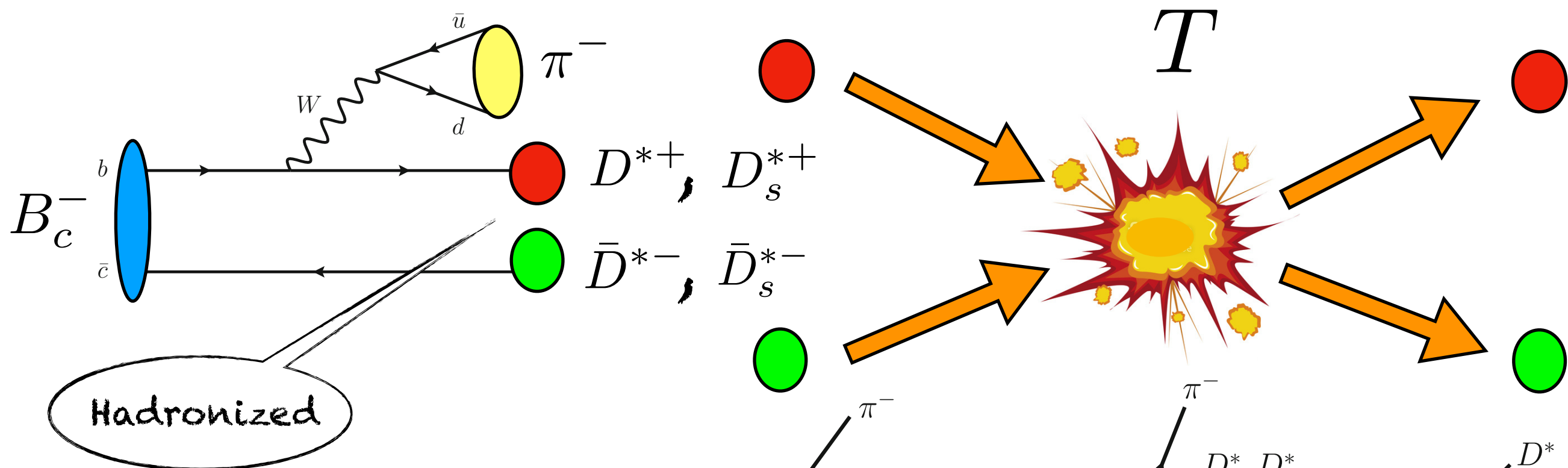
# Formalism...



# Formalism...

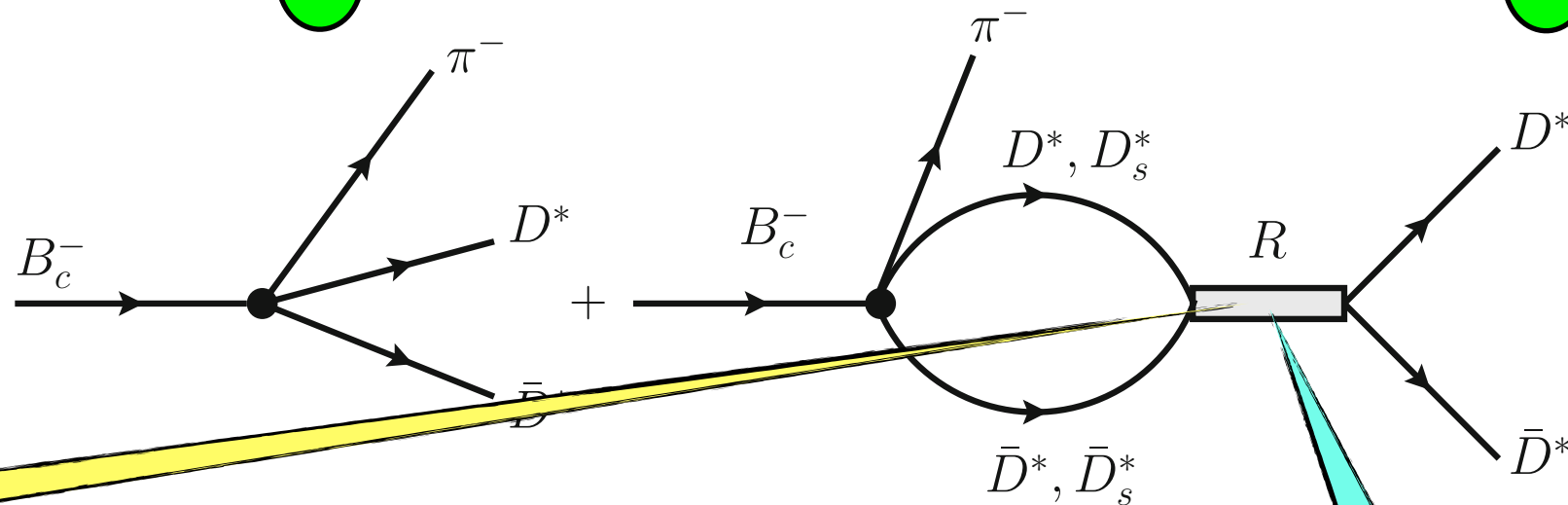


# Formalism...



$\bar{u}u + \bar{d}d + \bar{s}s$

$T =$



$D^* \bar{D}^*$  (yellow oval)

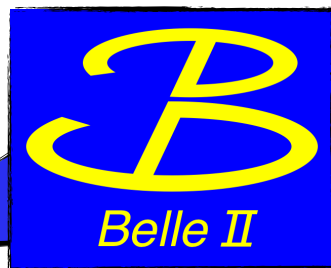
$0^+(0^{++})$

PRD 80, 114013 (2017)

$0^+(2^{++})$

$D^* \bar{D}^*$  (cyan oval)

$X(3940)$

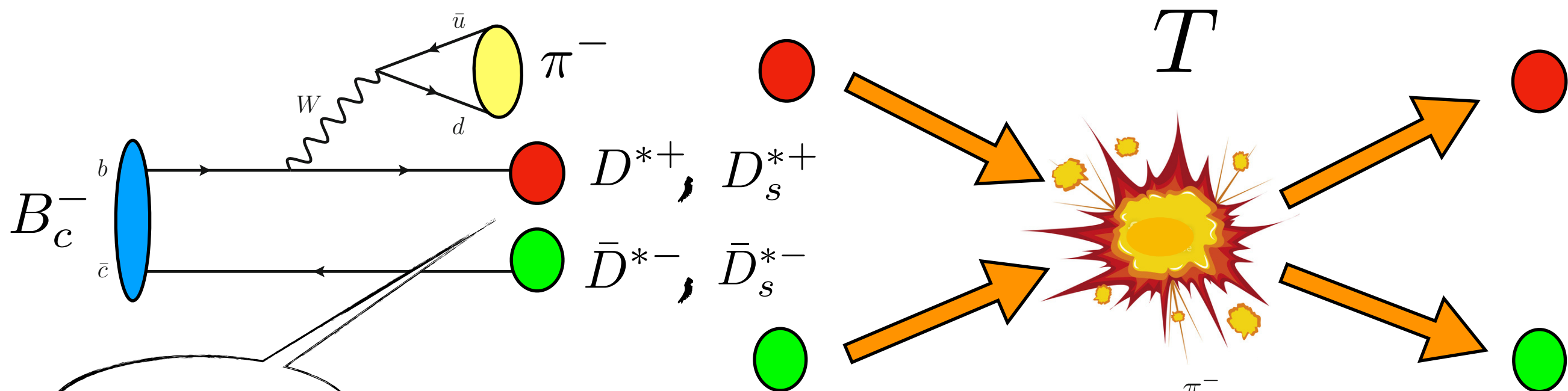


$X(3930)$

PRL 94, 182002 (2005) PRL 98, 082001 (2007)

PRL 98, 082001 (2007)

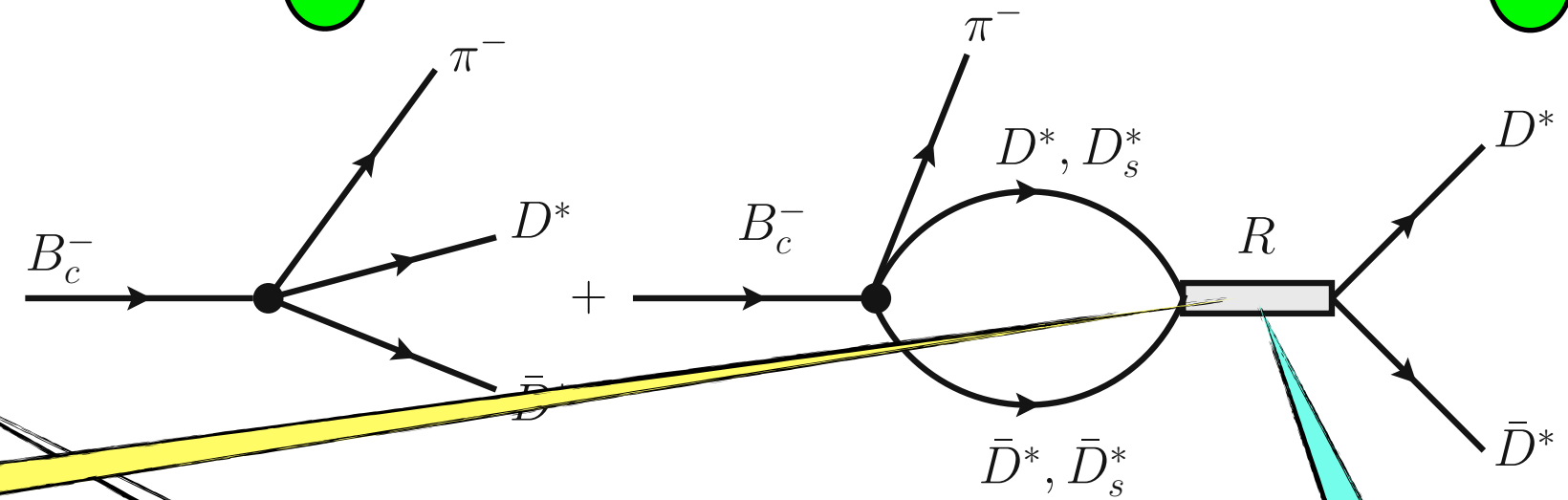
# Formalism...



Hadronized

$$\bar{u}u + \bar{d}d + \bar{s}s$$

$T =$



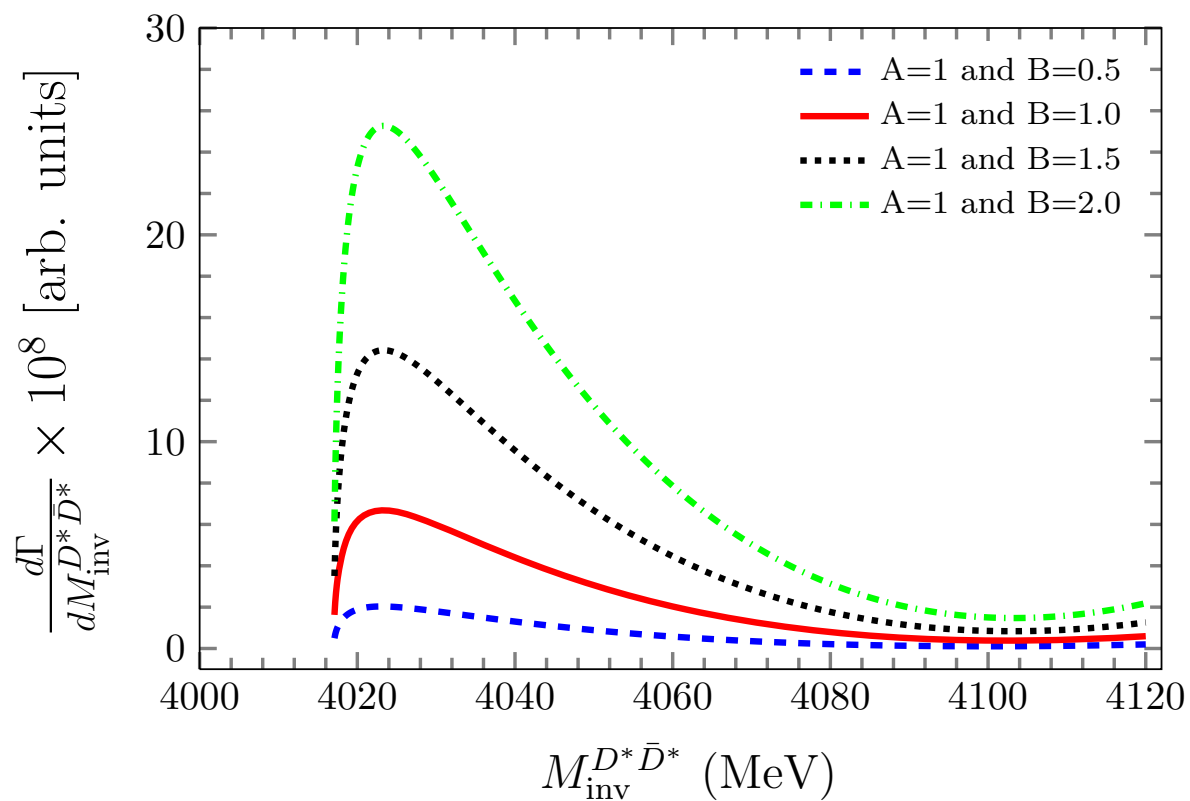
$D^* \bar{D}^*$   $0^+(0^{++})$

$0^+(2^{++})$

$D^* \bar{D}^*$

$$\frac{d\Gamma}{dM_{inv}^{D^* \bar{D}^*}} = \frac{1}{(2\pi)^3} \frac{k' p_{D^*}}{4M_{B_c}^2} |T|^2$$

# Results: $D^* \bar{D}^*$ distribution



$$T \sim A(\epsilon \cdot \epsilon')$$

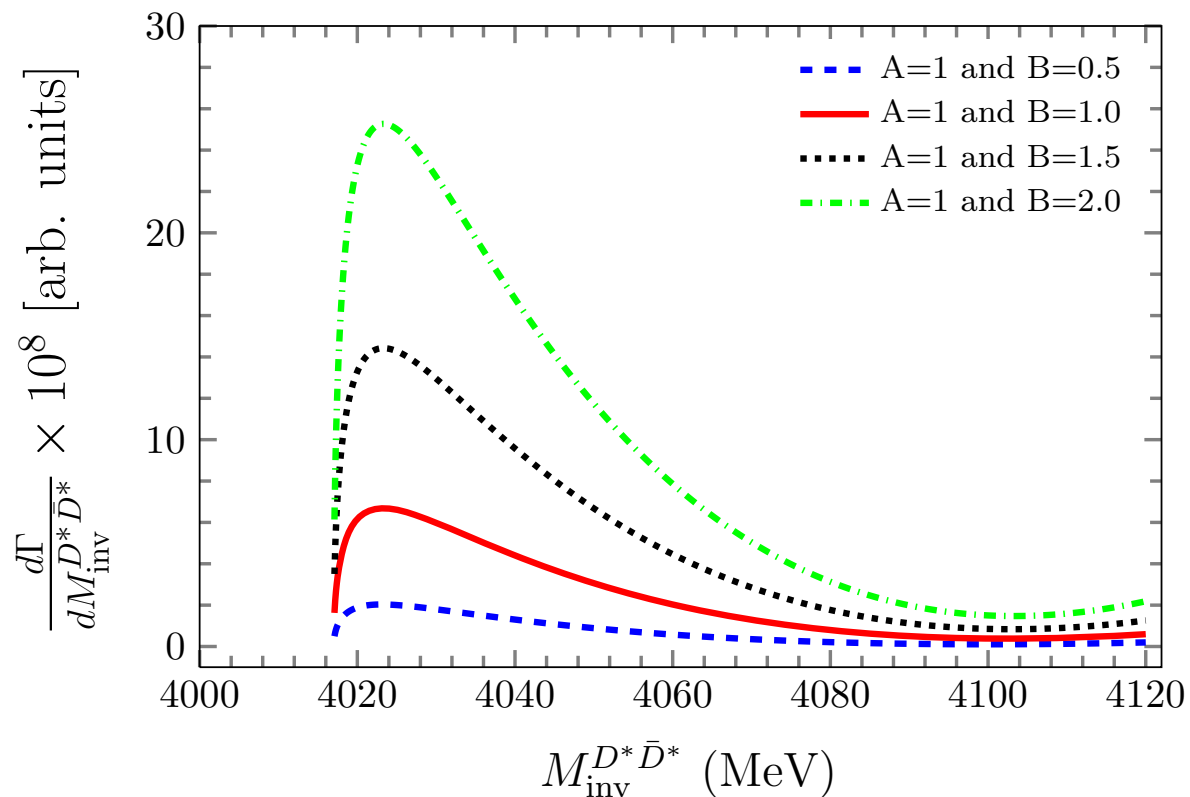
Production

$D^* \bar{D}^*$

$0^+(0^{++})$

$$\frac{d\Gamma}{dM_{inv}^{D^* \bar{D}^*}} = \frac{1}{(2\pi)^3} \frac{k' p_{D^*}}{4M_{B_c}^2} |T|^2$$

# Results: $D^* \bar{D}^*$ distribution



**Production**

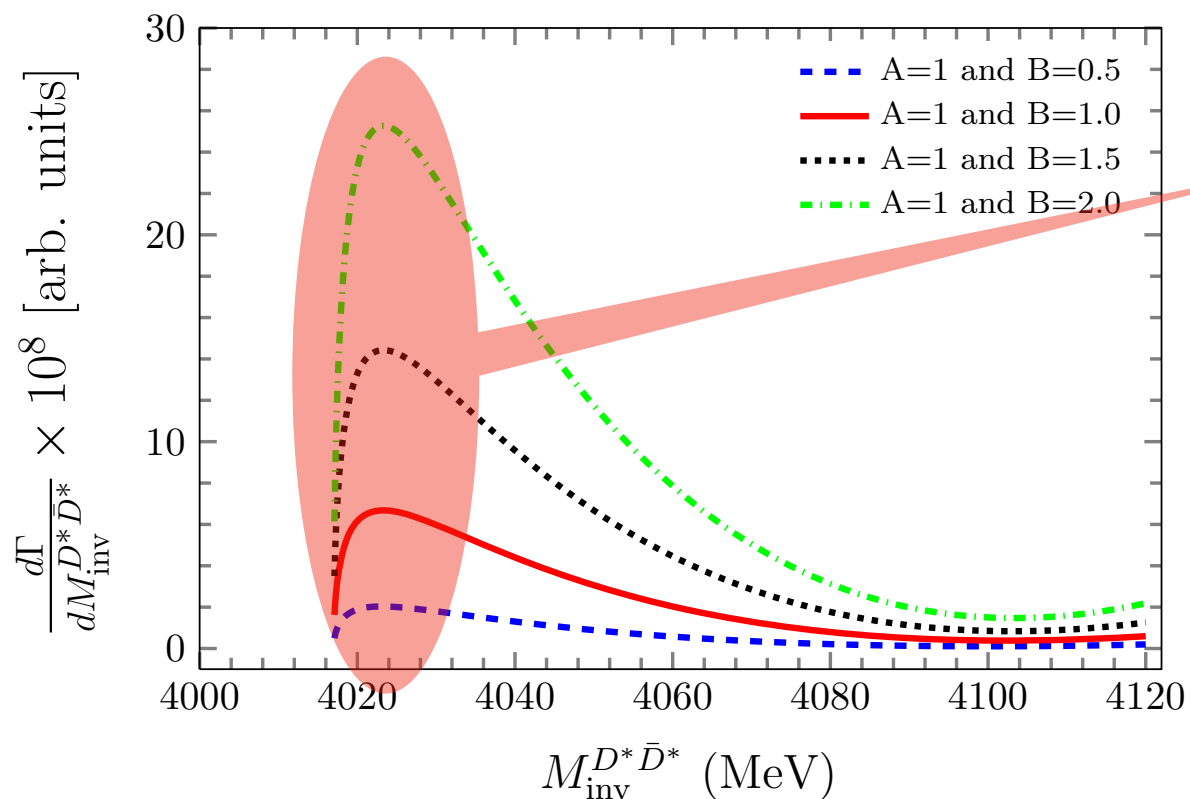
$$T \sim A(\epsilon \cdot \epsilon') + B \left[ (\epsilon \cdot \mathbf{k})(\epsilon' \cdot \mathbf{k}) - \frac{1}{3} |\mathbf{k}|^2 (\epsilon \cdot \epsilon') \right]$$

$D^* \bar{D}^*$   $0^+(0^{++})$   $0^+(2^{++})$   $D^* \bar{D}^*$

**Production**

$$\frac{d\Gamma}{dM_{inv}^{D^* \bar{D}^*}} = \frac{1}{(2\pi)^3} \frac{k' p_{D^*}}{4M_{B_c}^2} |T|^2$$

# Results: $D^* \bar{D}^*$ distribution



- Indicates an influence by a resonance below threshold

$$T \sim A(\epsilon \cdot \epsilon') + B \left[ (\epsilon \cdot \mathbf{k})(\epsilon' \cdot \mathbf{k}) - \frac{1}{3} |\mathbf{k}|^2 (\epsilon \cdot \epsilon') \right]$$

Production

$D^* \bar{D}^*$

$0^+(0^{++})$

$0^+(2^{++})$

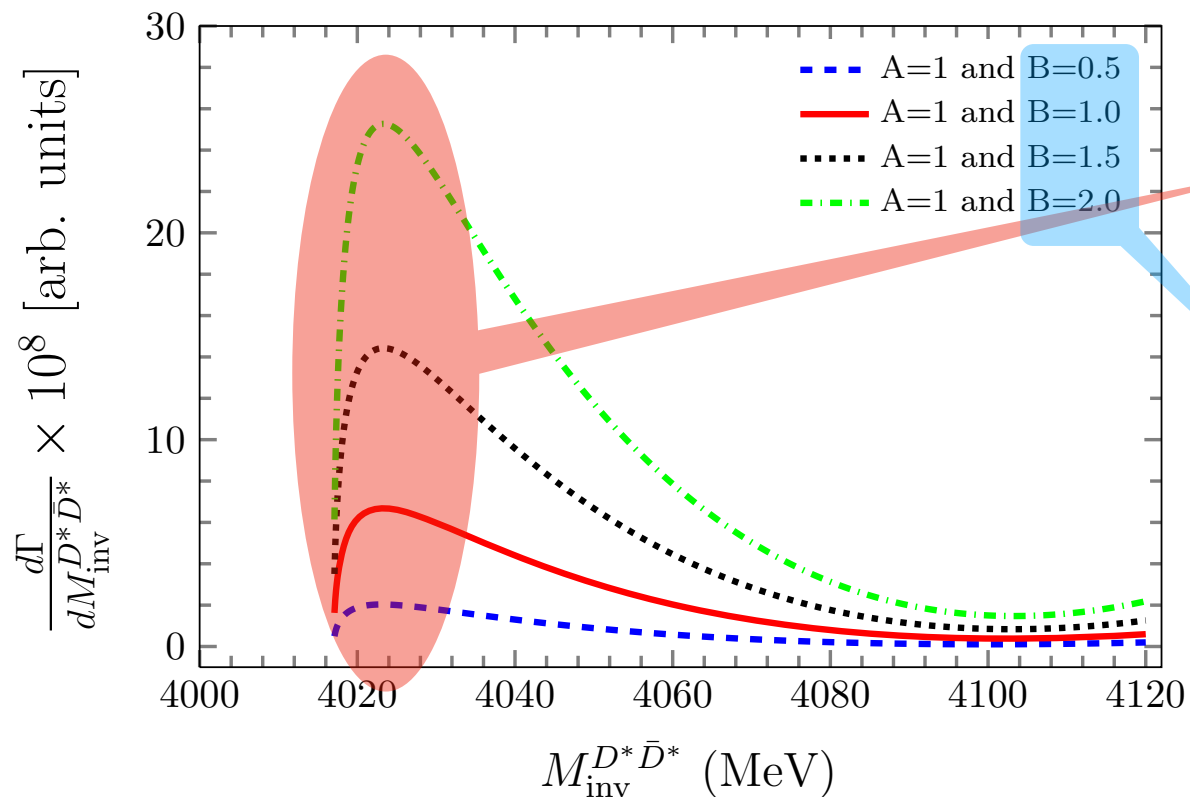
$D^* \bar{D}^*$

Production

$$\frac{d\Gamma}{dM_{inv}^{D^* \bar{D}^*}} = \frac{1}{(2\pi)^3} \frac{k' p_{D^*}}{4M_{B_c}^2} |T|^2$$



# Results: $D^* \bar{D}^*$ distribution



- Indicates an influence by a resonance below threshold

- It is influenced by the tensor resonance

$$T \sim A(\epsilon \cdot \epsilon') + B \left[ (\epsilon \cdot \mathbf{k})(\epsilon' \cdot \mathbf{k}) - \frac{1}{3} |\mathbf{k}|^2 (\epsilon \cdot \epsilon') \right]$$

Production

$D^* \bar{D}^*$

$0^+(0^{++})$

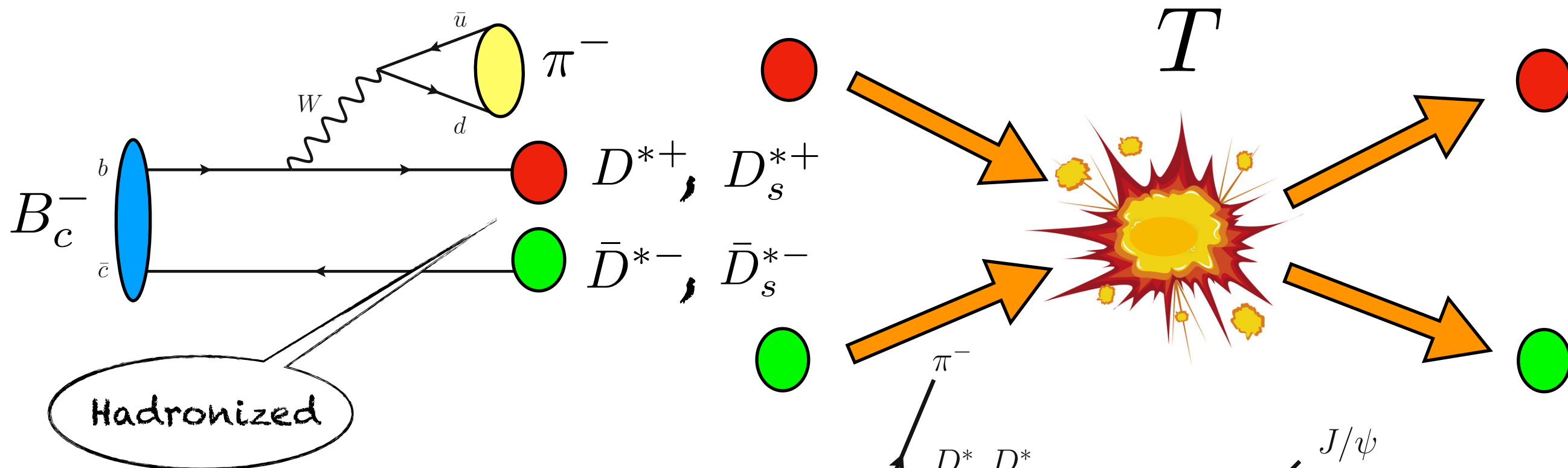
$0^+(2^{++})$

$D^* \bar{D}^*$

Production

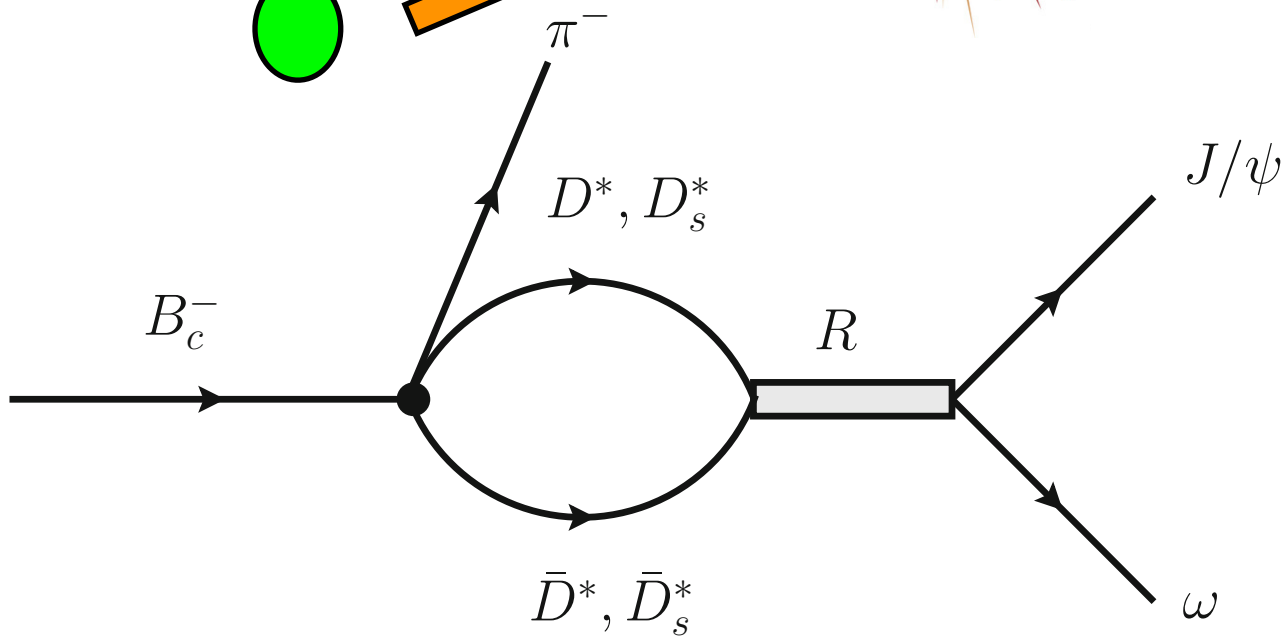
$$\frac{d\Gamma}{dM_{inv}^{D^* \bar{D}^*}} = \frac{1}{(2\pi)^3} \frac{k' p_{D^*}}{4M_{B_c}^2} |T|^2$$

# Formalism...

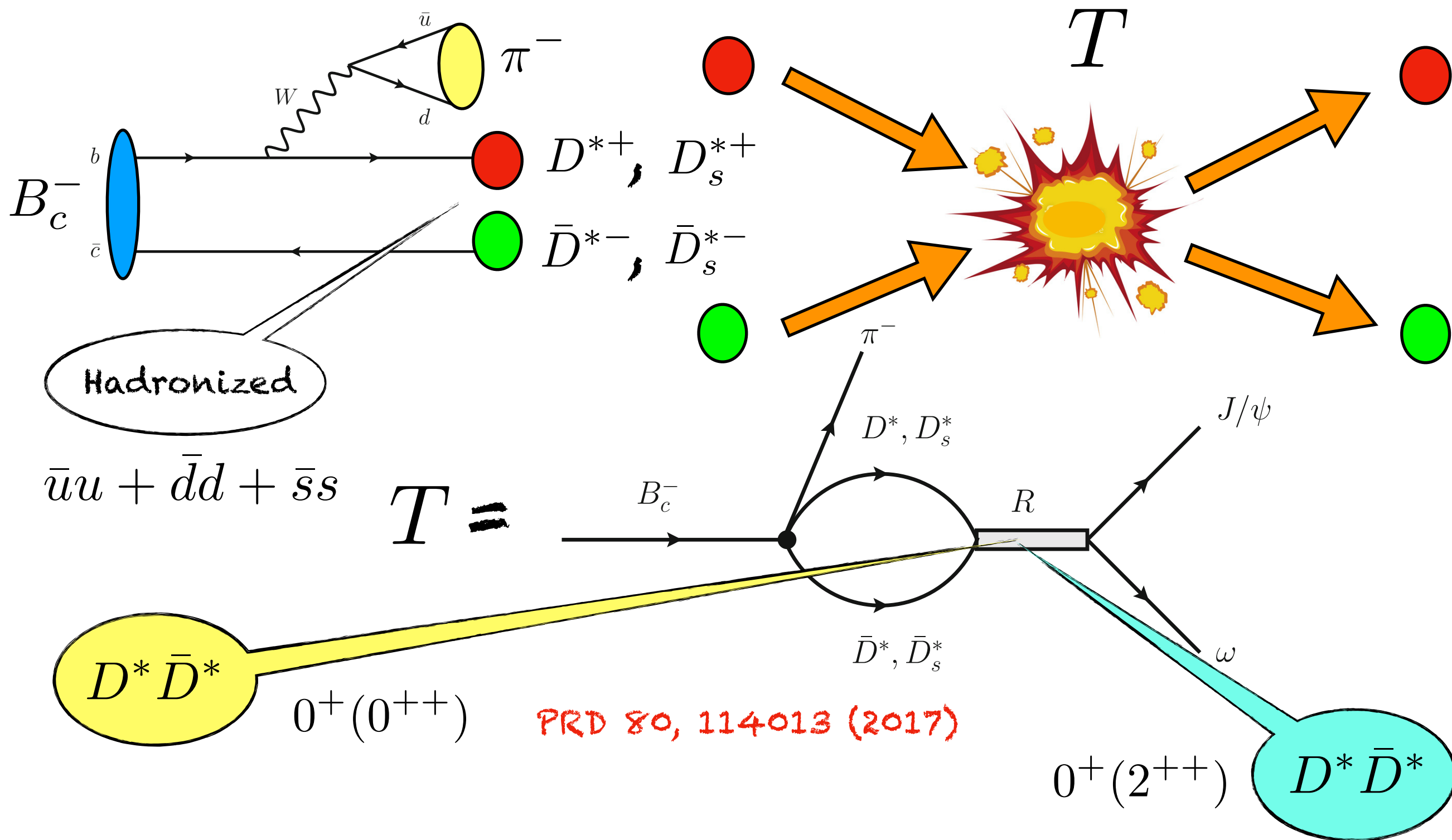


Hadronized  
 $\bar{u}u + \bar{d}d + \bar{s}s$

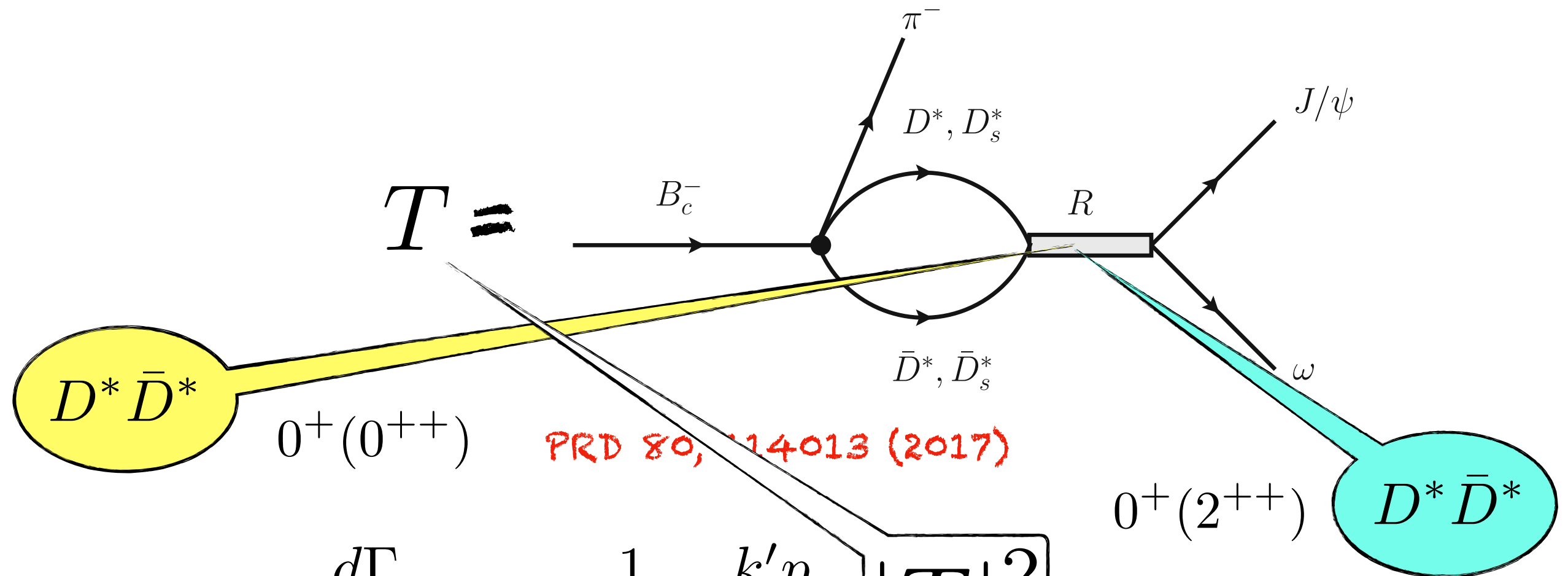
$T =$



# Formalism...

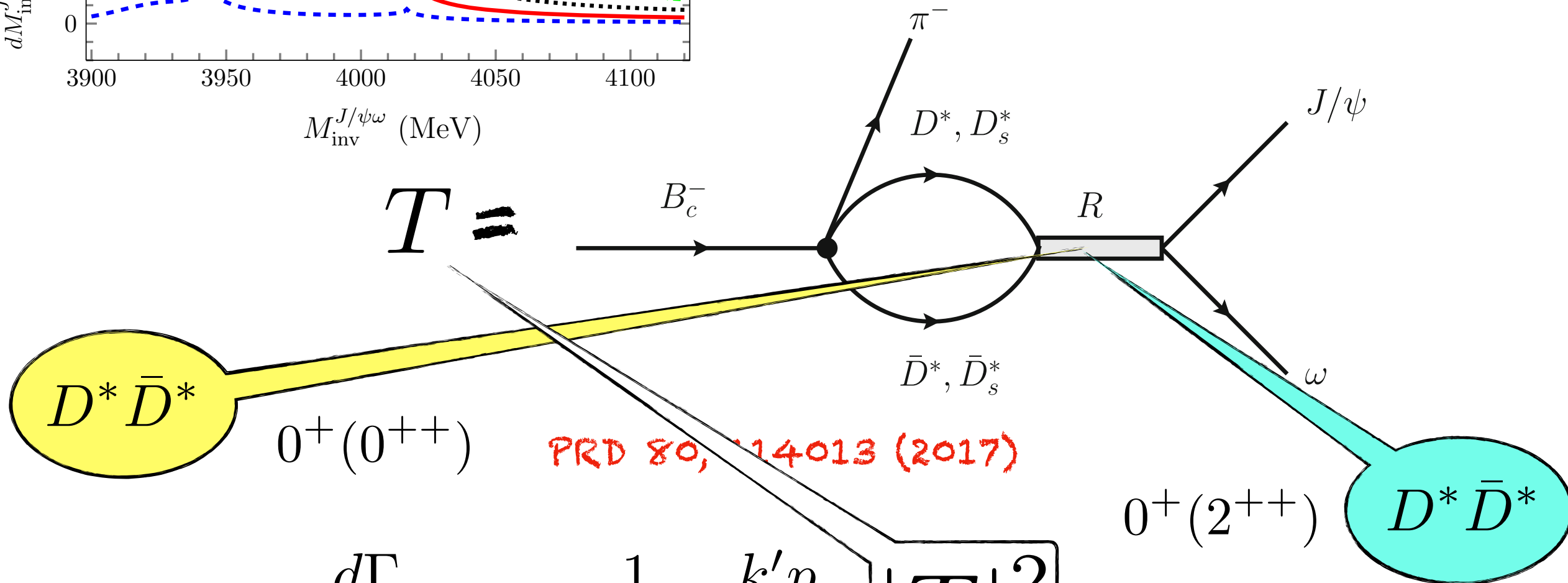
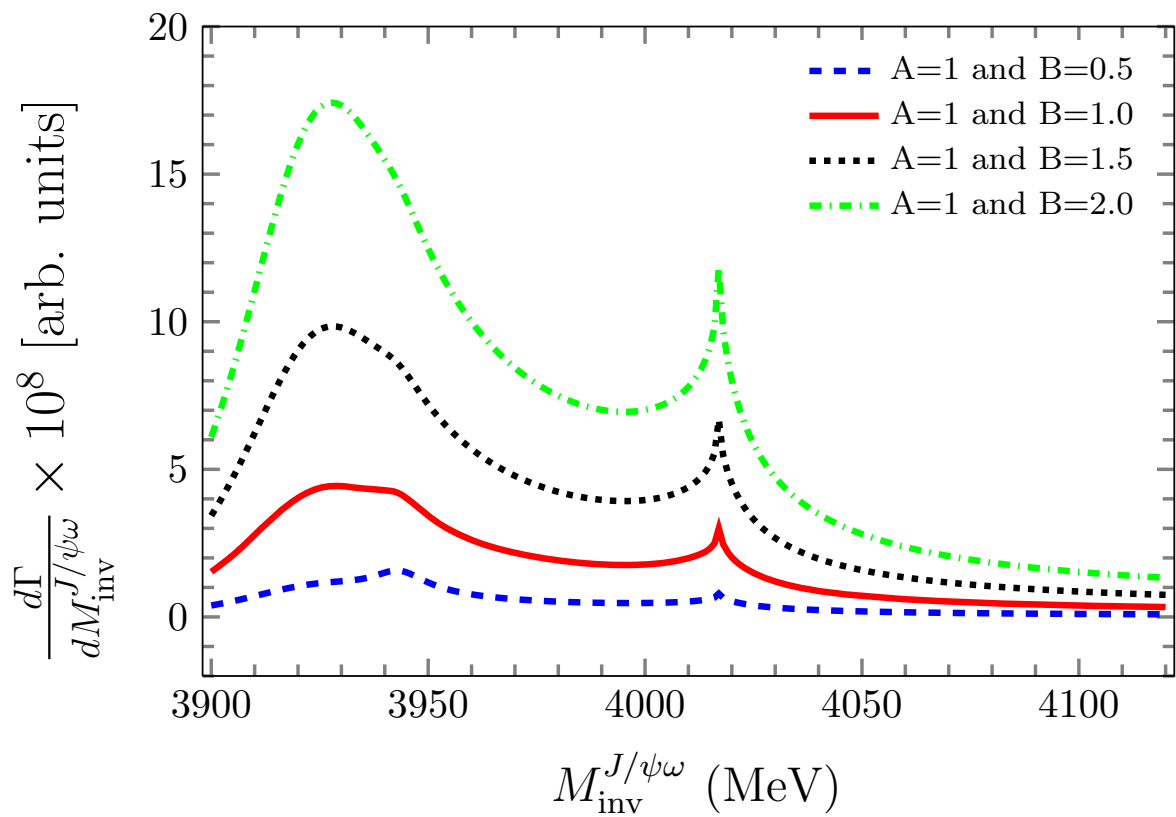


# Results: $J/\psi \omega$ distribution



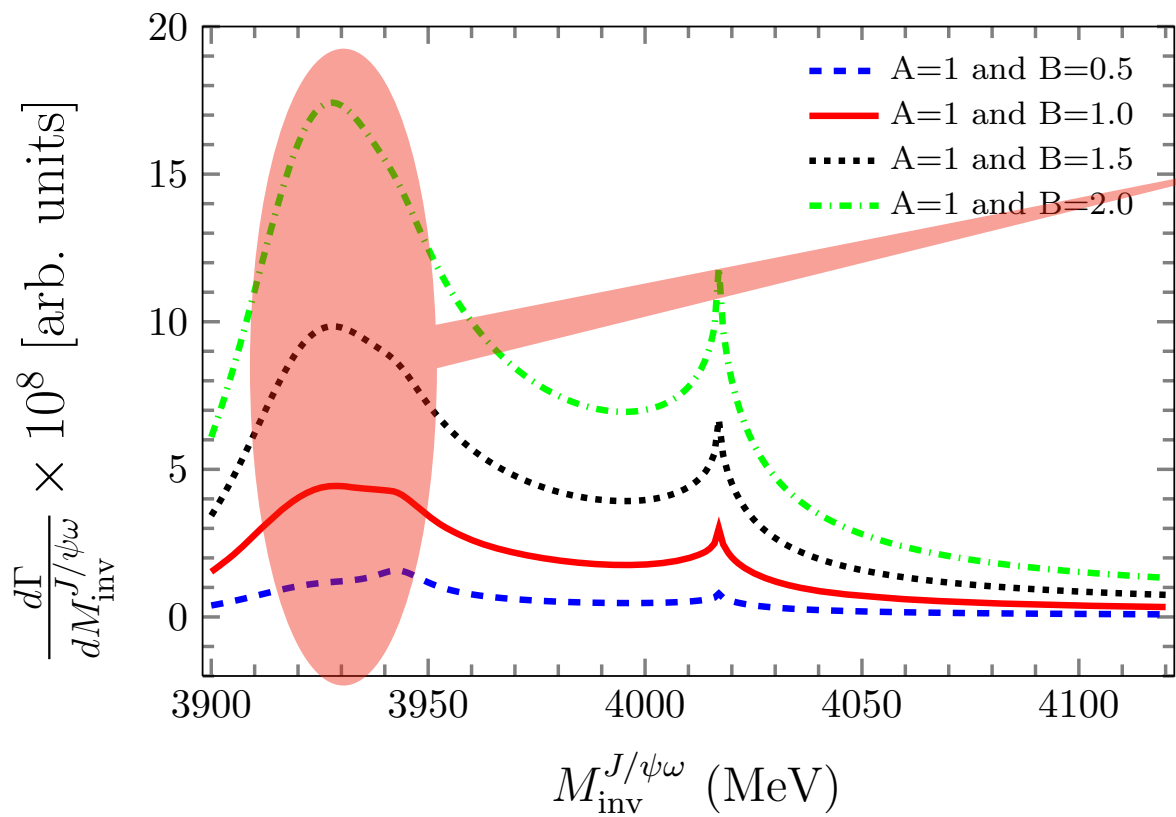
$$\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}} = \frac{1}{(2\pi)^3} \frac{k' p_\omega}{4M_{B_c}^2} |T|^2$$

# Results: $J/\psi \omega$ distribution

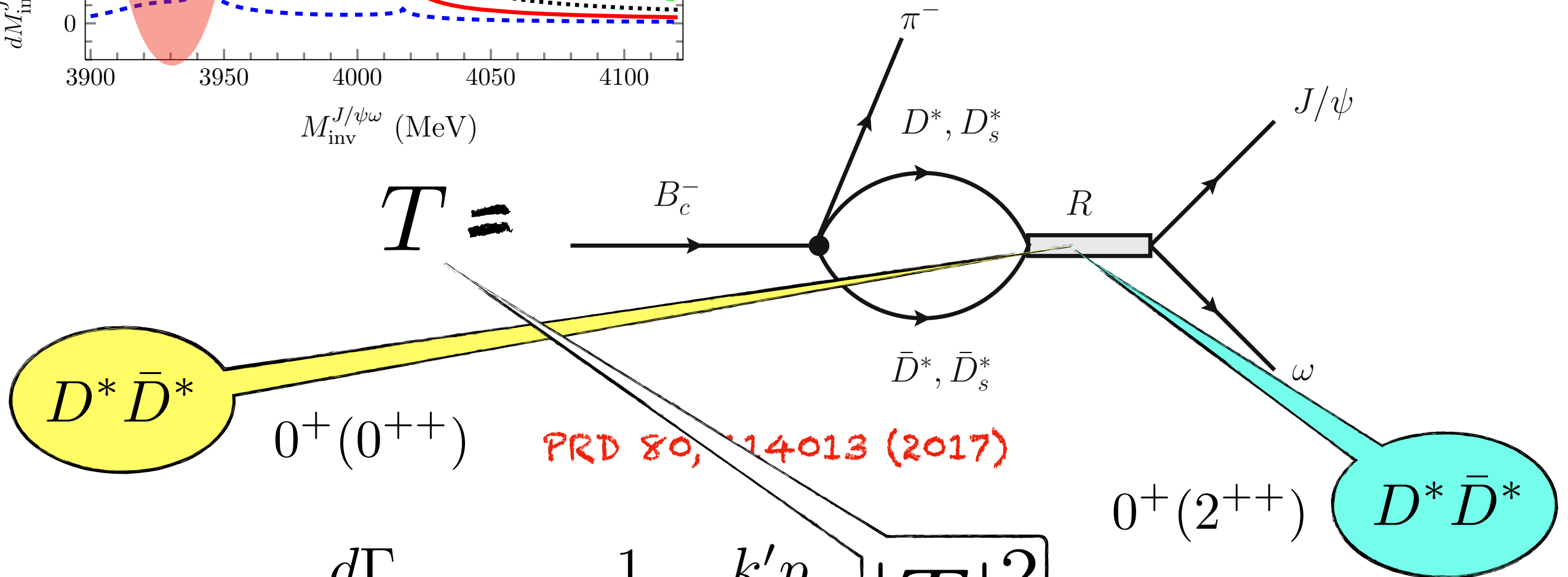


$$\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}} = \frac{1}{(2\pi)^3} \frac{k' p_\omega}{4M_{B_c}^2} |T|^2$$

# Results: $J/\psi \omega$ distribution

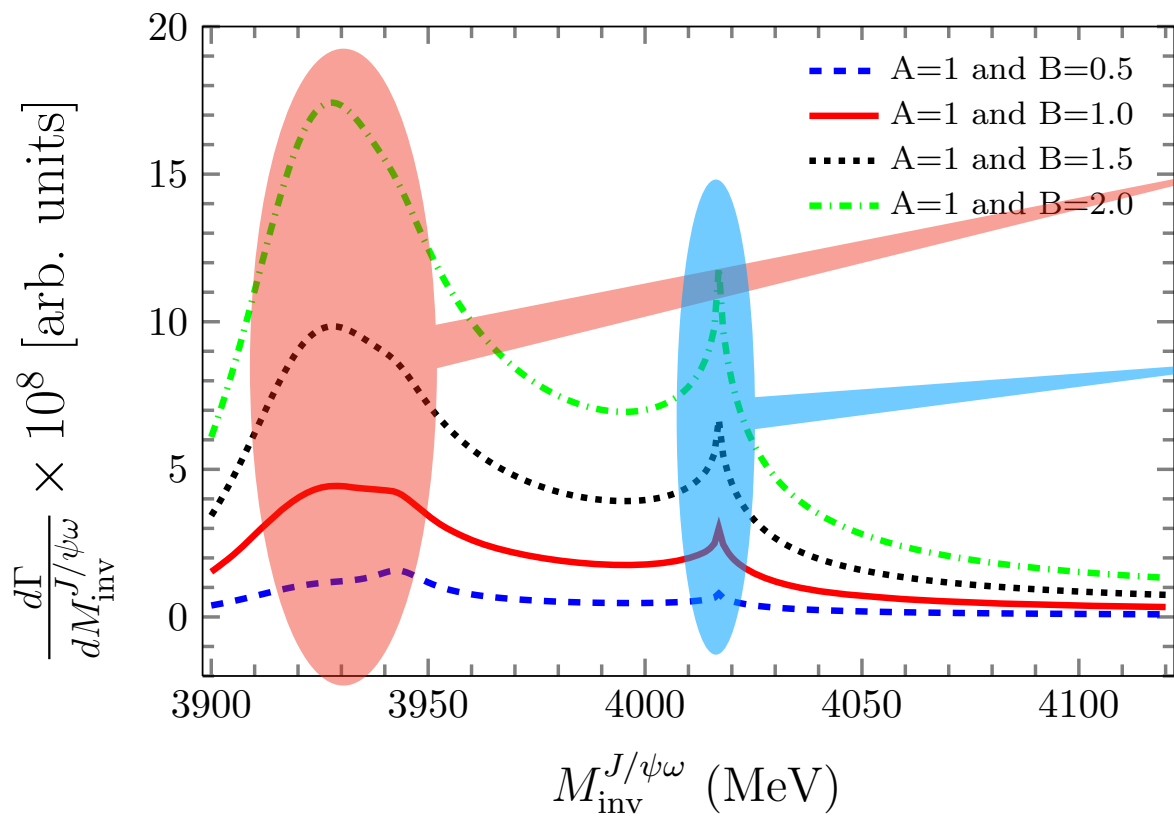


The two resonances merge into a broader one



$$\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}} = \frac{1}{(2\pi)^3} \frac{k' p_\omega}{4M_{B_c}^2} |T|^2$$

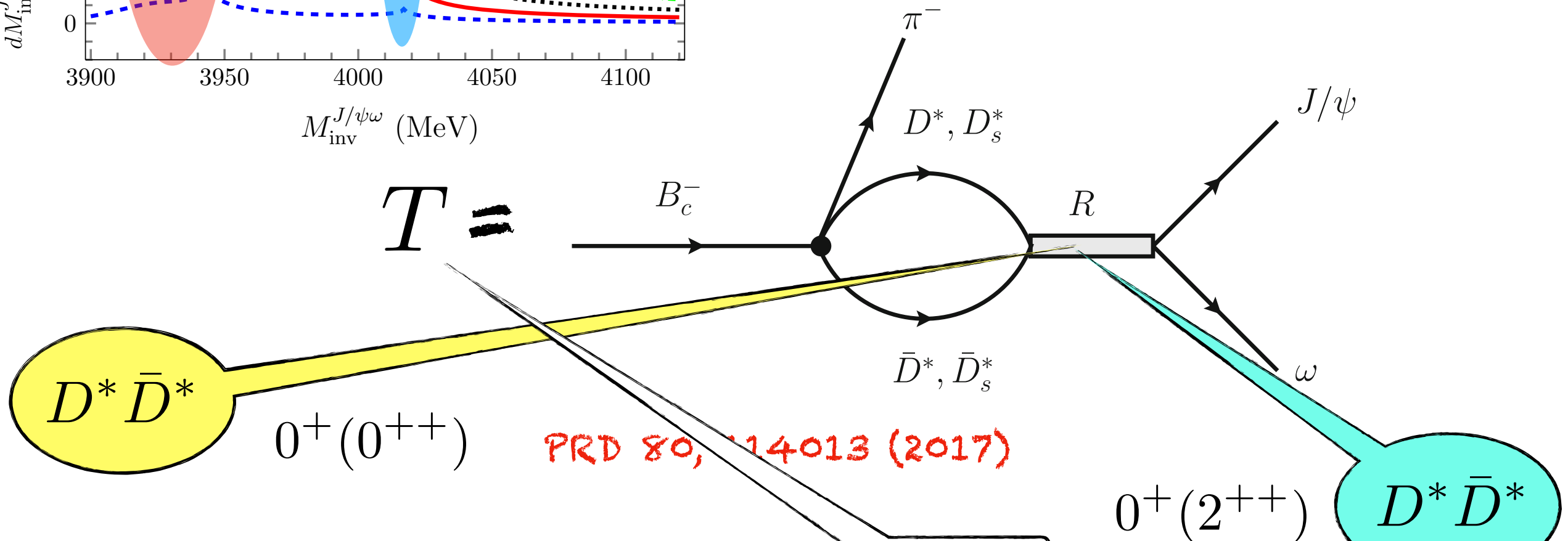
# Results: $J/\psi \omega$ distribution



- The two resonances merge into a broader one

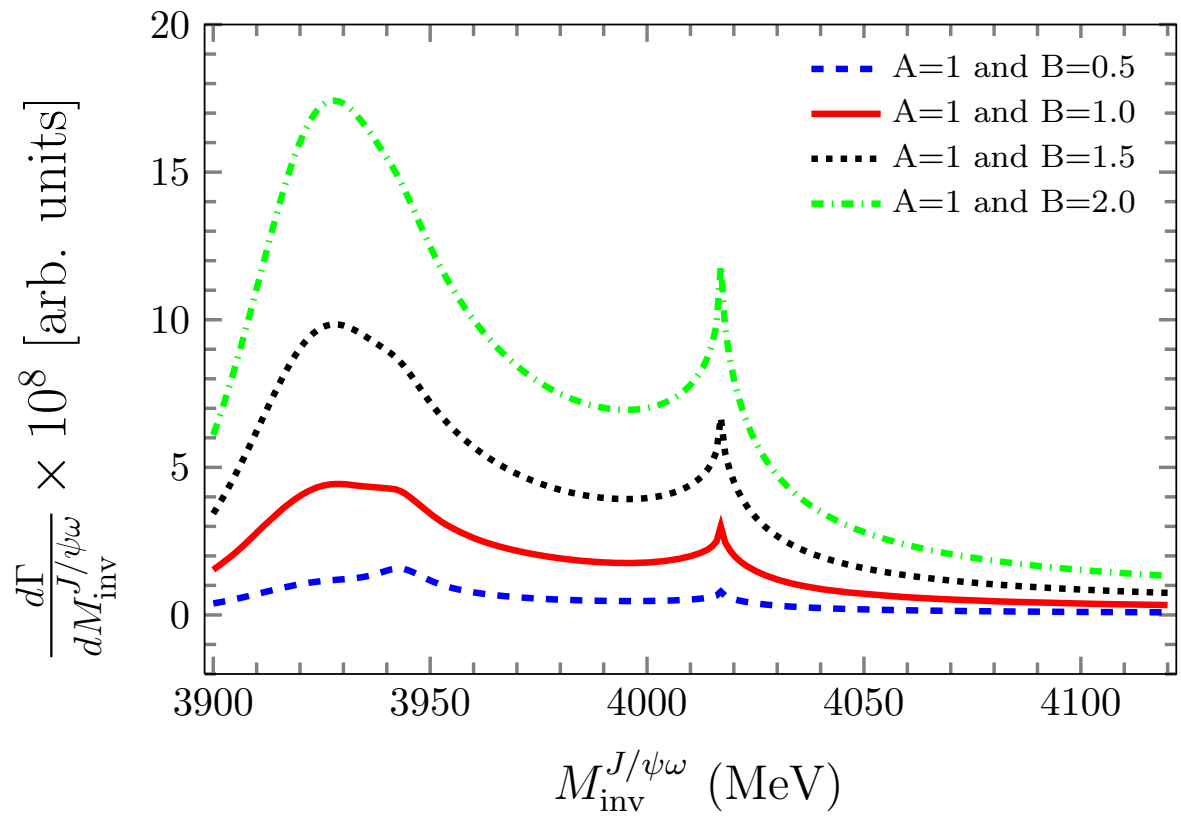
- Cusp at  $D^* \bar{D}^*$  threshold

- Its strength is influenced by the tensor resonance

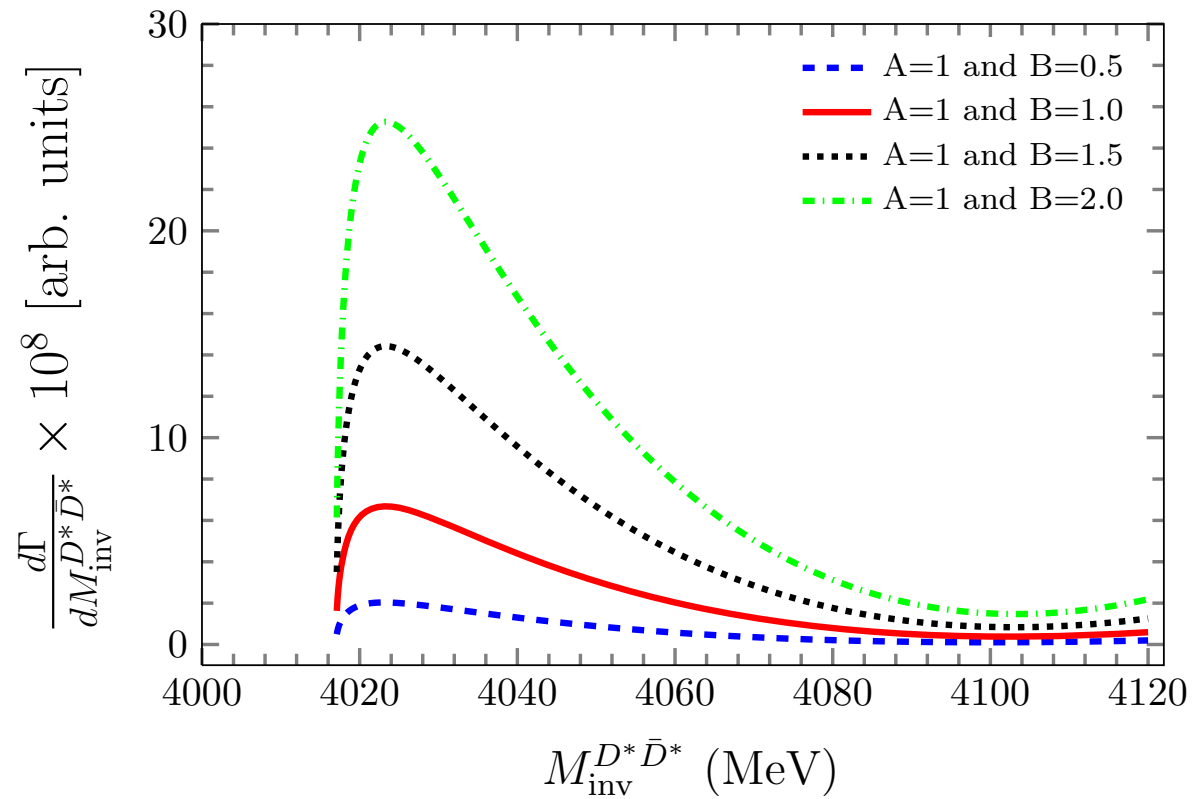


$$\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}} = \frac{1}{(2\pi)^3} \frac{k' p_\omega}{4M_{B_c}^2} |T|^2$$

# Results: Ratio between the distributions

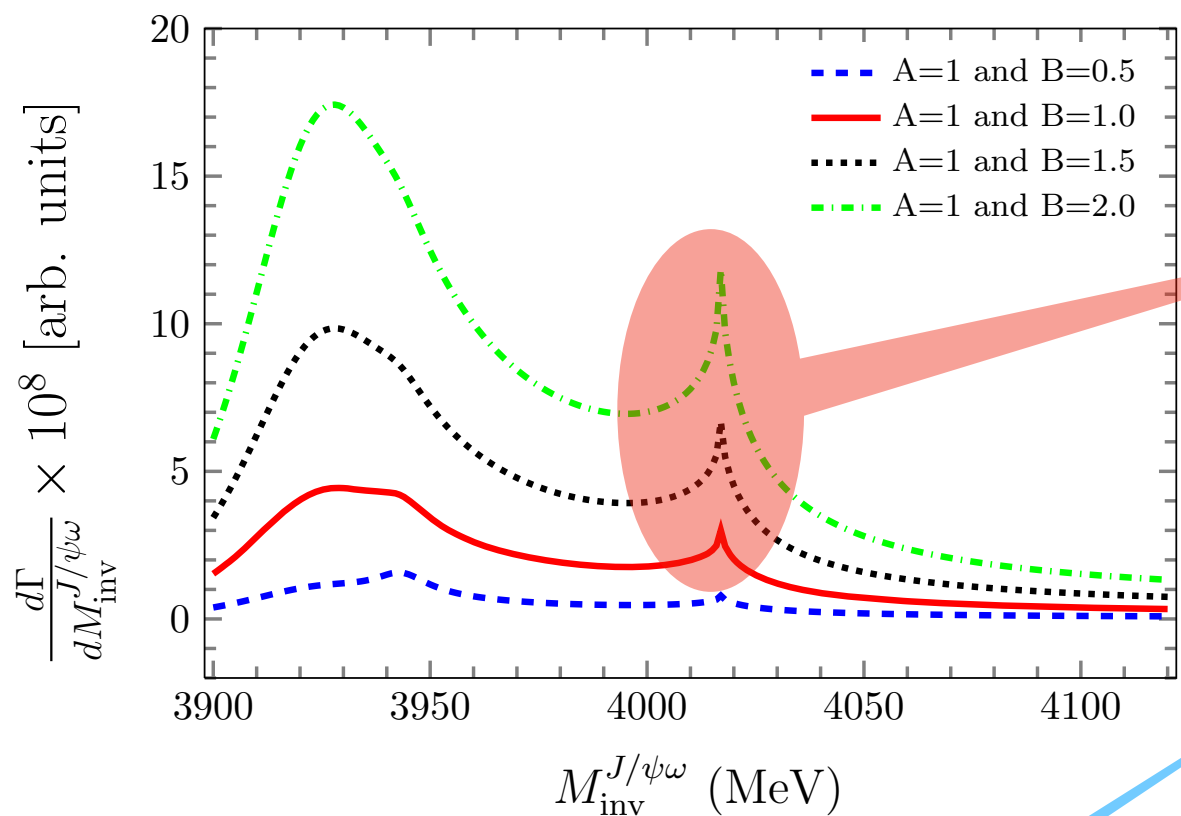


$$\frac{\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}} (cusp)}{\frac{d\Gamma}{dM_{inv}^{D^*\bar{D}^*}} (peak)} = R$$





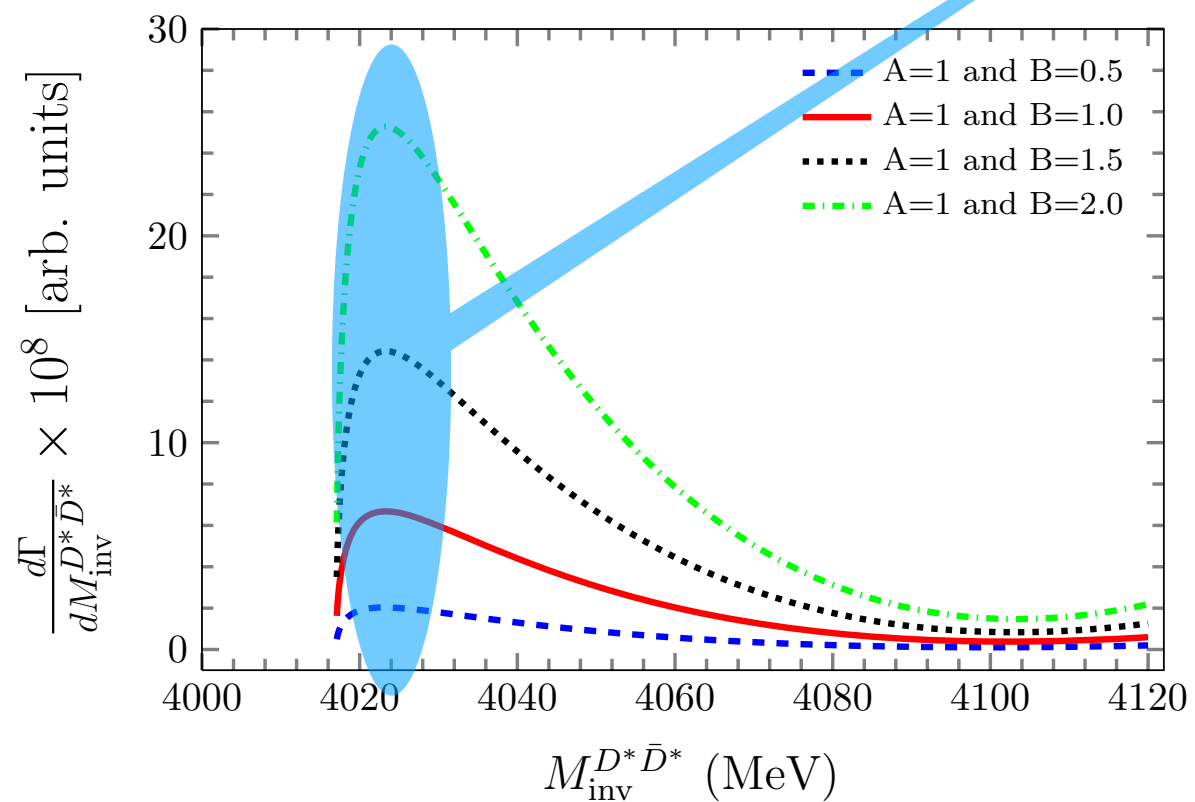
# Results: Ratio between the distributions



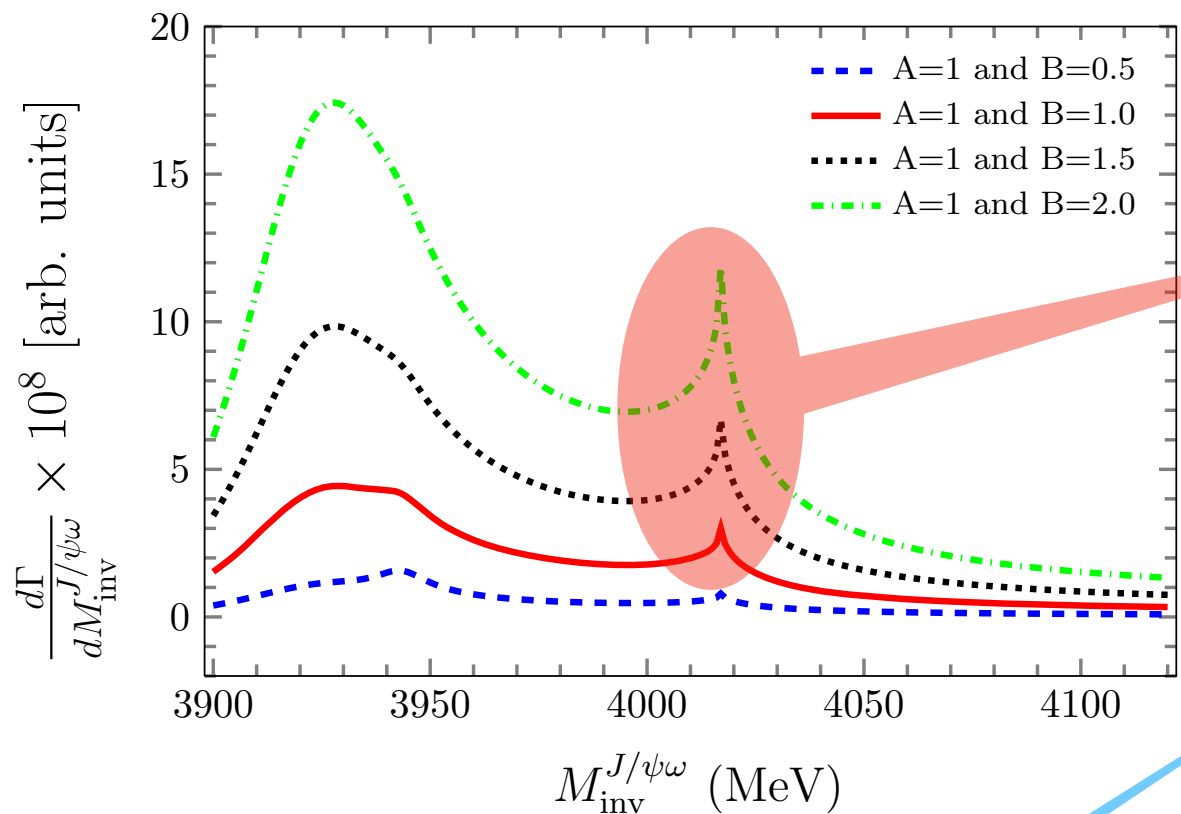
$$\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}} (cusp)$$

$$\frac{d\Gamma}{dM_{inv}^{D^*\bar{D}^*}} (peak)$$

$$= R$$



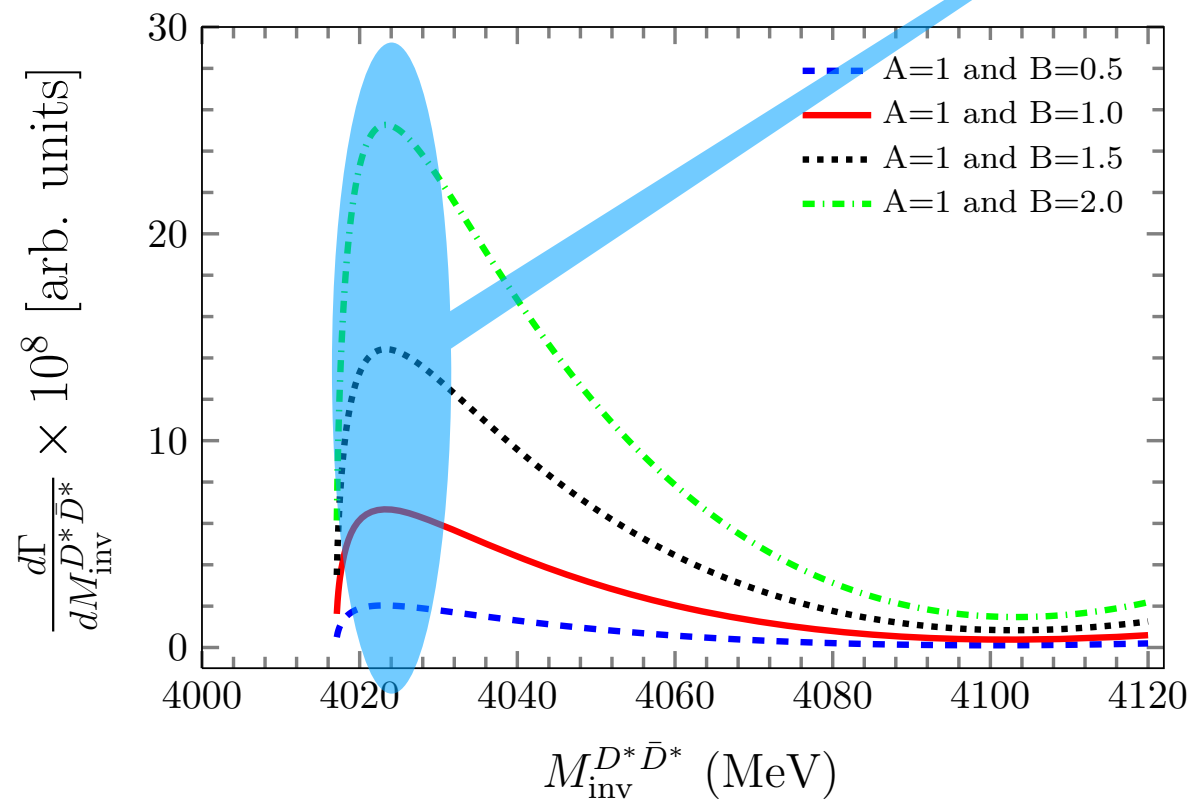
# Results: Ratio between the distributions



$$\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}} (cusp)$$

$$= R$$

$$\frac{d\Gamma}{dM_{inv}^{D^*\bar{D}^*}} (peak)$$



$A = 1.0$

$B = 0.5$

$B = 1.0$

$B = 1.5$

$B = 2.0$

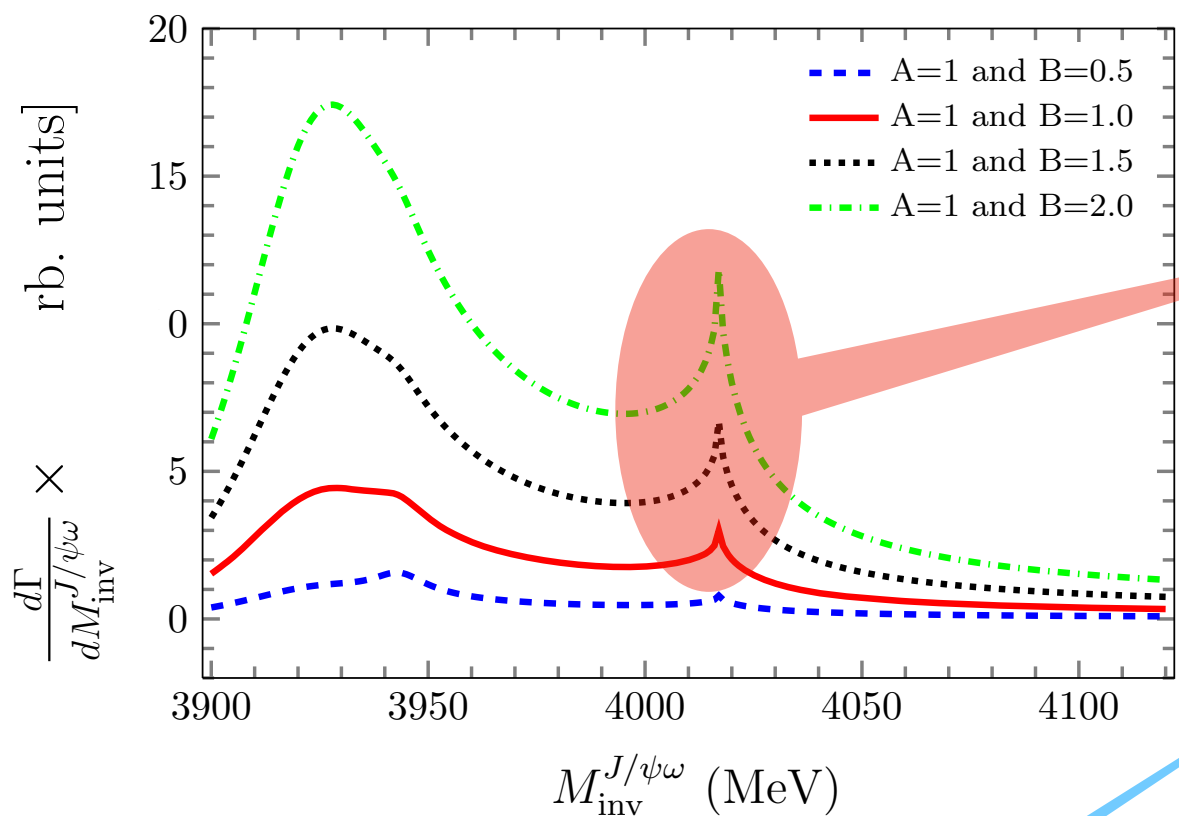
$R = 2.57$

$R = 2.22$

$R = 2.16$

$R = 2.13$

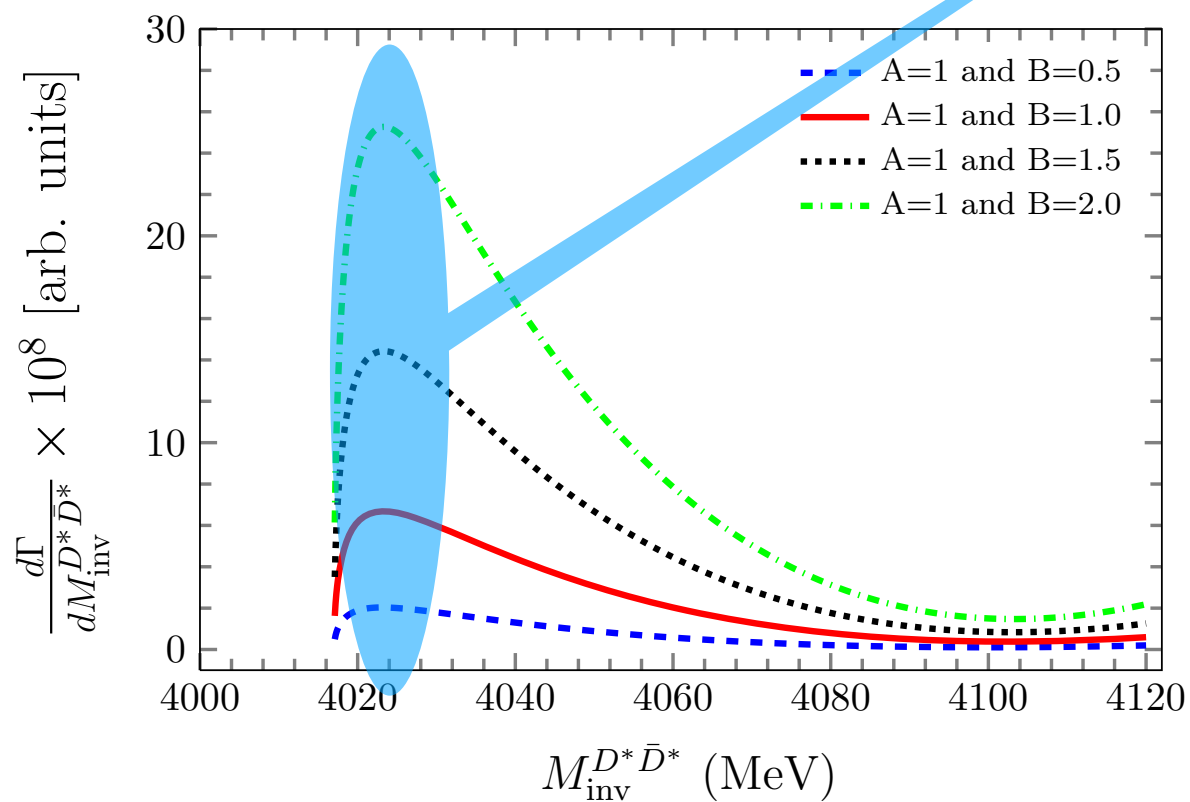
# Results: Ratio between the distributions



$$\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}} (cusp)$$

$$= R$$

$$\frac{d\Gamma}{dM_{inv}^{D^*\bar{D}^*}} (peak)$$



A = 1.0

B = 0.5

B = 1.0

B = 1.5

B = 2.0

R = 2.57

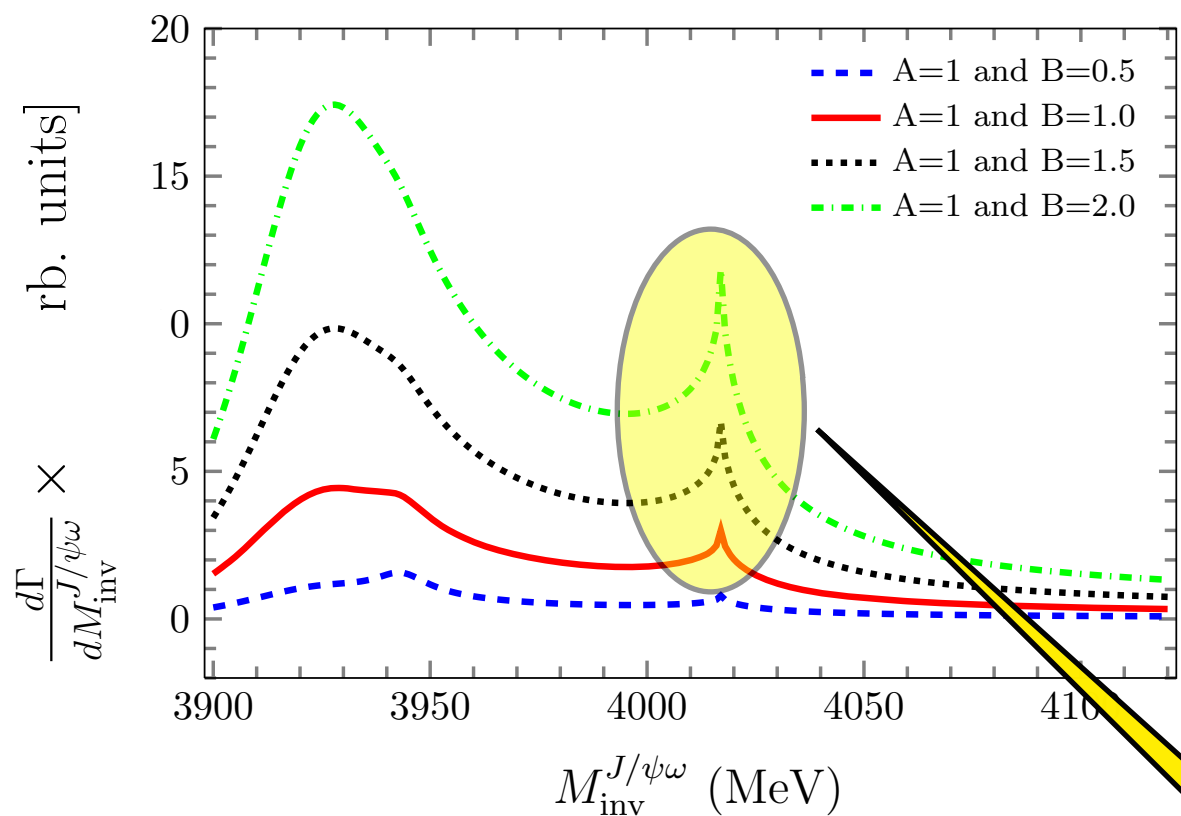
R = 2.22

R = 2.16

R = 2.13

— The ratio is relatively stable

# Results: Ratio between the distributions



$$\frac{\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}}(cusp)}{\frac{d\Gamma}{dM_{inv}^{D^*\bar{D}^*}}(peak)} = R$$

A = 1.0

B = 0.5

R = 2.57

B = 1.0

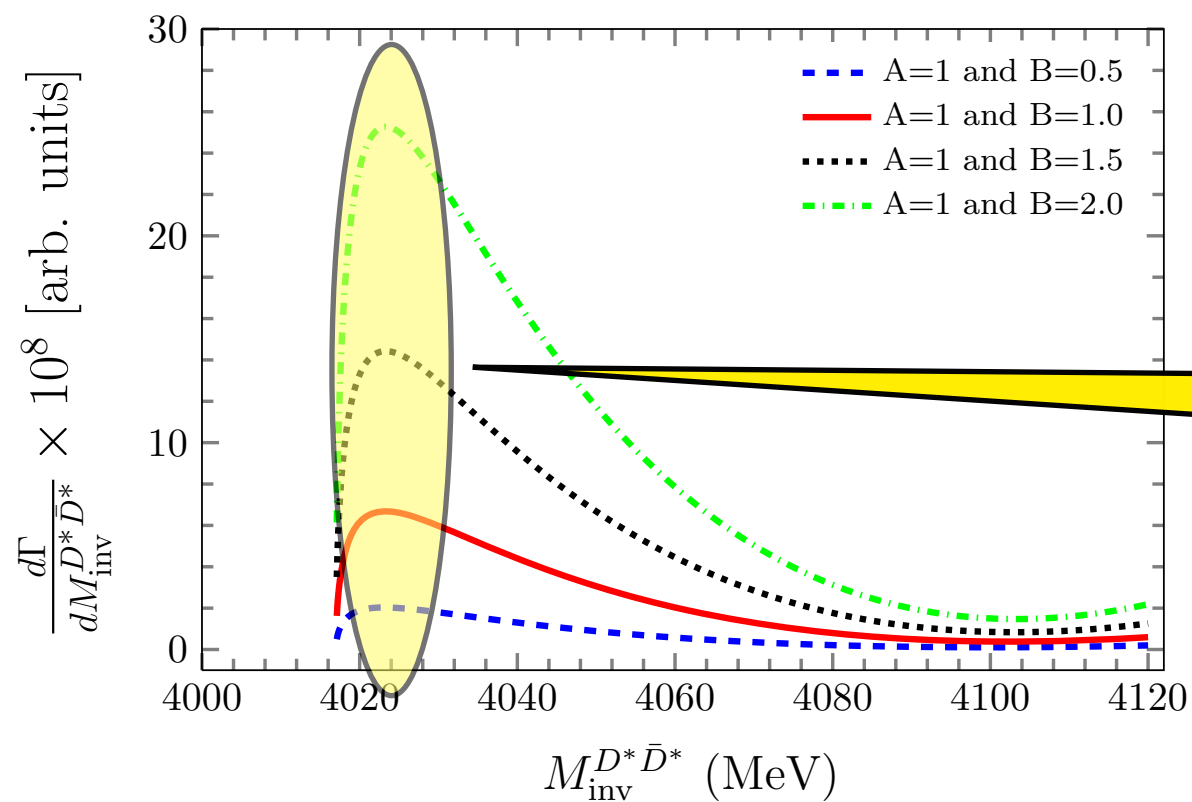
R = 2.22

B = 1.5

R = 2.16

B = 2.0

R = 2.13



- The ratio is relatively stable

Tensor state

# Summary and conclusions

- We have looked at  $B_c^- \rightarrow J/\psi \omega$  decay

$$\frac{d\Gamma}{dM_{inv}^{J/\psi\omega}}$$

is influenced by the  $X(3940)$  and  $X(3930)$  states

PRD 80, 114013 (2017)

$$0^+(0^{++})$$

$$0^+(2^{++})$$

- Both states couple mostly to  $D^* \bar{D}^*$

- In order to find support for this nature of these states:

1)  $J/\psi \omega$  is not the main channel, but  $D^* \bar{D}^*$ .

As consequence, a cusp appears!

2) The states influence the  $D^* \bar{D}^*$  distribution

Thank you for your attention!