

# **Complementarity of the beauty and charm hadron physics**

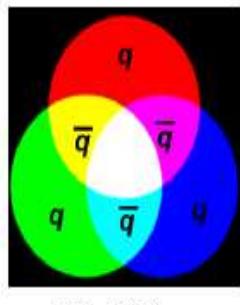
**Alex Bondar  
Novosibirsk, NSU/BINP  
Belle Collaboration**



(Novosibirsk, May 21, 2018)

# QCD

$$\mathcal{L}_{\text{QCD}} = \sum_{q=u,d,s,c,b,t} \bar{q} (i\gamma_\mu D^\mu - m_q) q - \frac{1}{4} F^{\mu\nu} F_{\mu\nu}$$



$SU(3)_{\text{color}}$   
**Gluons** with  
 color-anticolor charge

Expect hadrons with gluons as constituents:

- **Hybrids:**  $(qqg), (qqqg), \dots$
- **Glueballs:**  $(gg), \dots$

1973

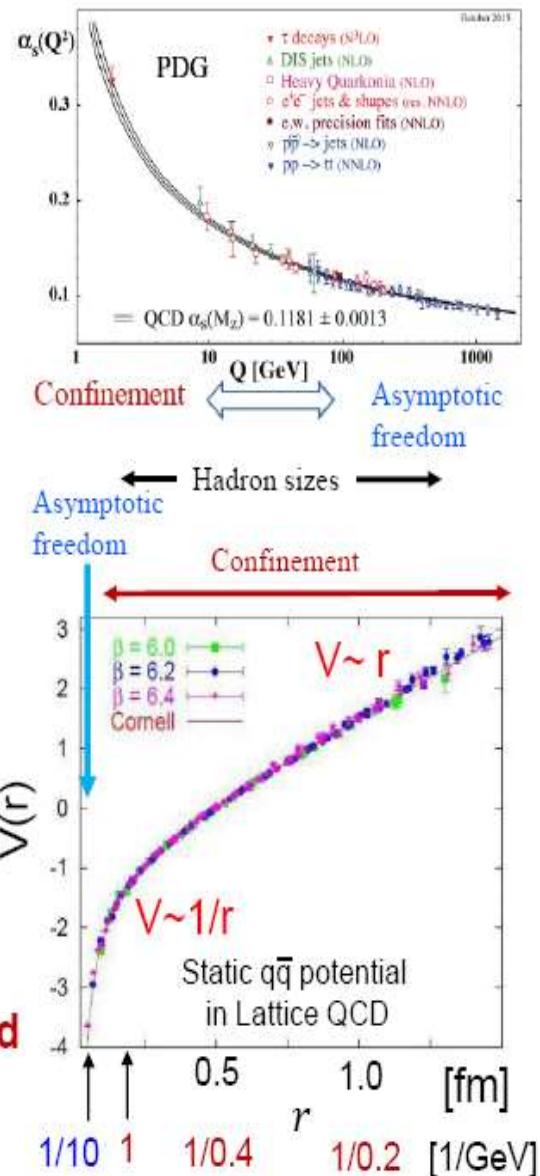


Hadrons = Non-perturbative QCD

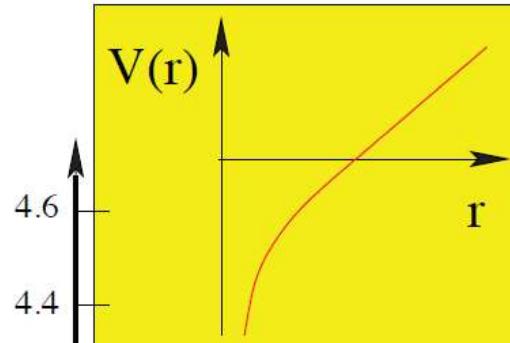
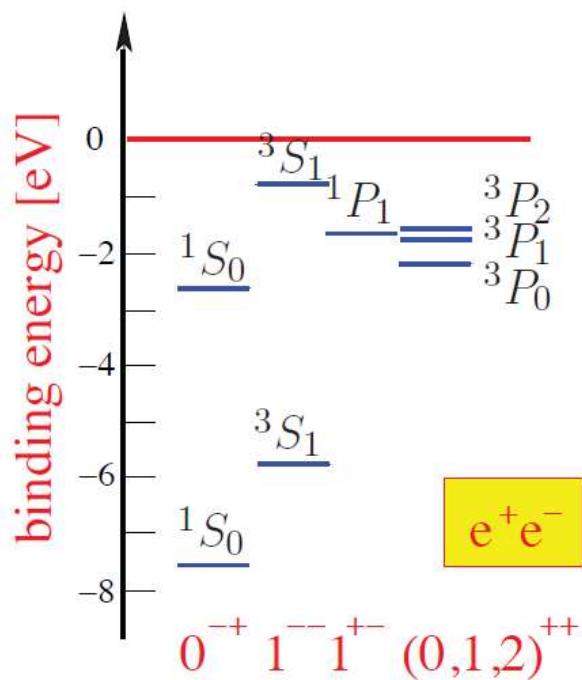
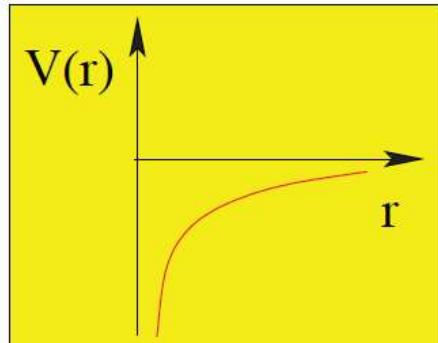
Lattice QCD works well for lowest-excitations of  $(qq), (qqq)$ .

Only approximate lattice simulations for **unstable** higher excitations.

We have to **rely on data and QCD-motivated phenomenology** when trying to understand more complex hadronic structures.

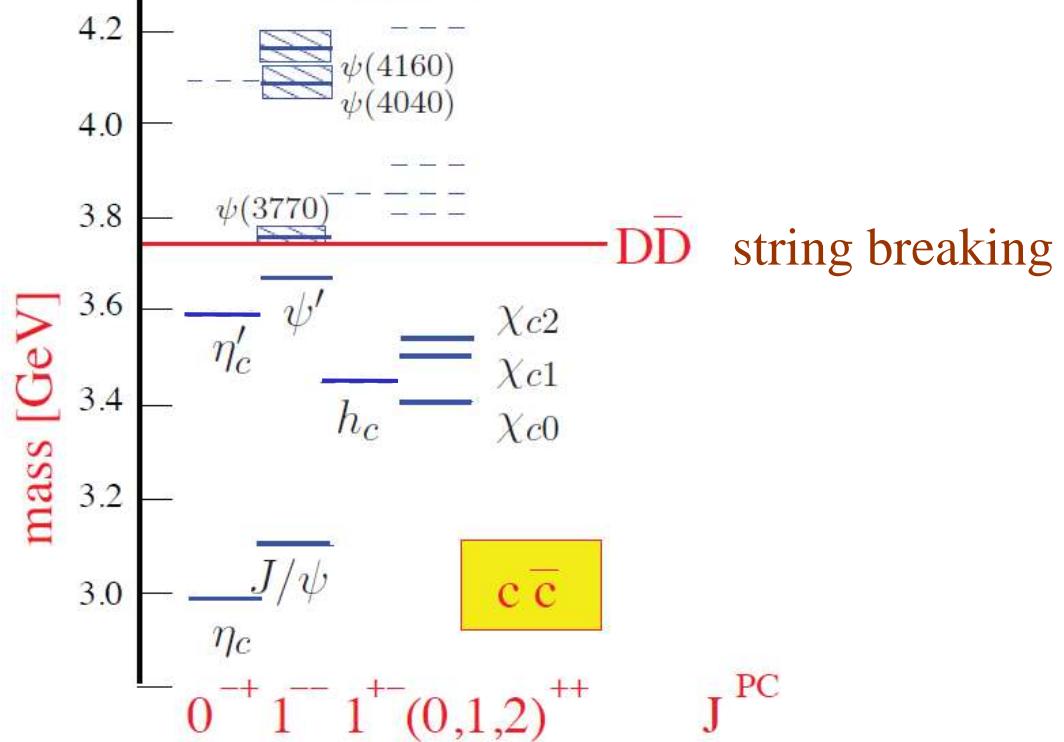


Classification of  $c\bar{c}$  and  $b\bar{b}$  levels is the same as in positronium: L, S,  $n_r$ :

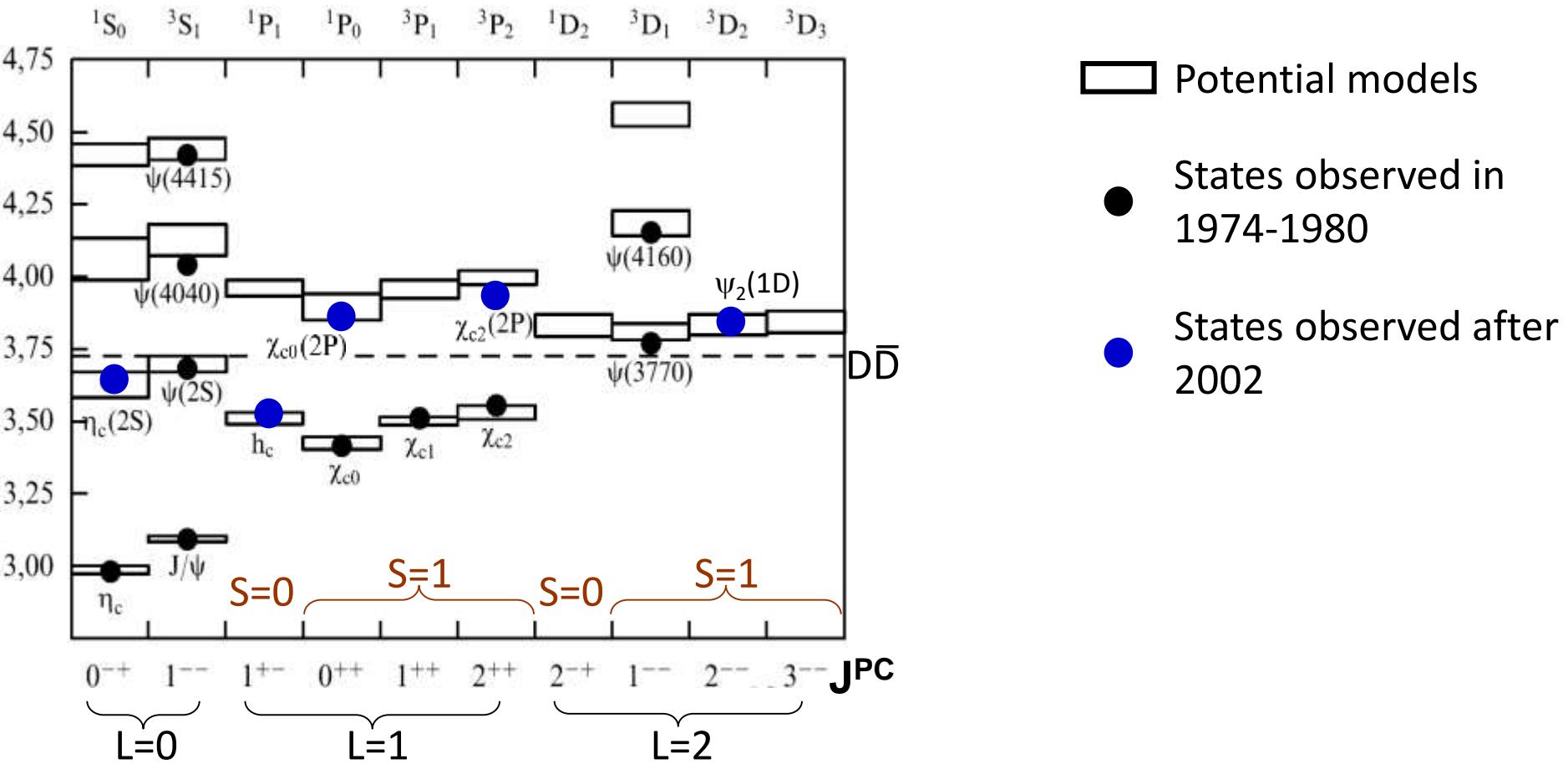


confinement  
chromoelectric tube

asymptotic freedom  
one-gluon exchange

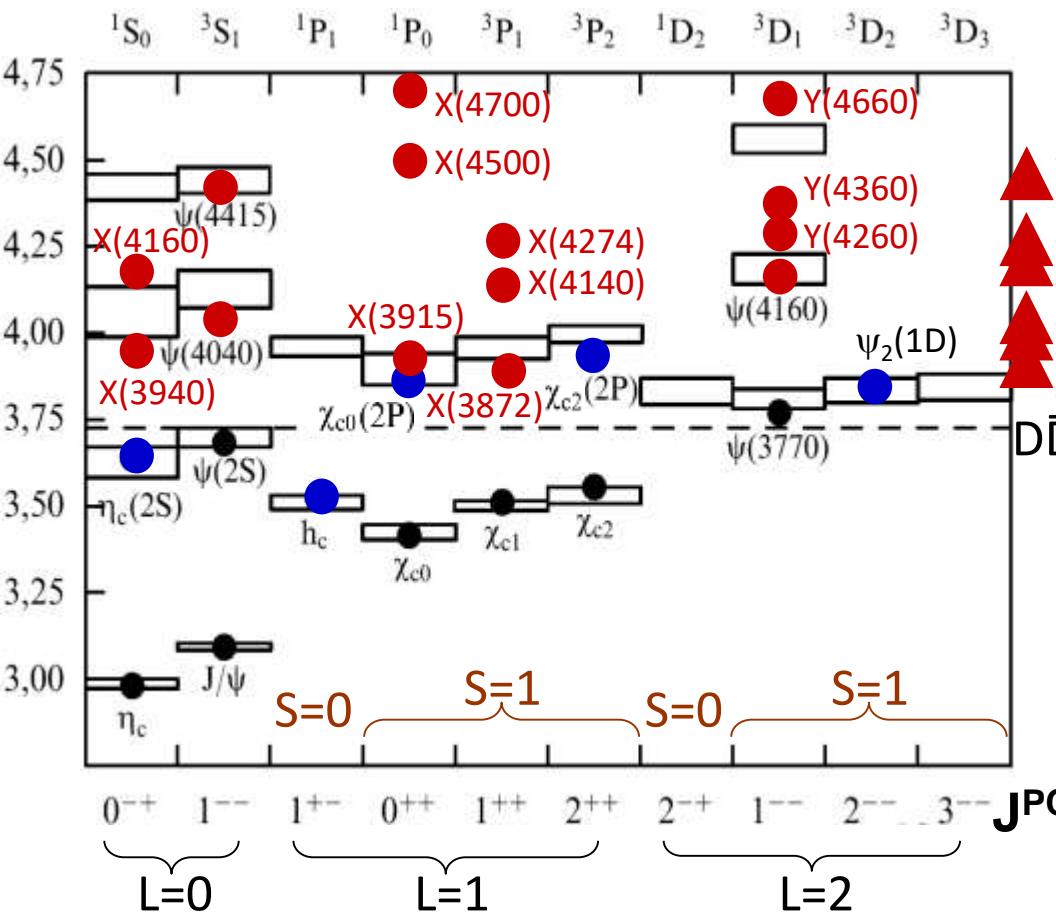


# Charmonium table



States below  $D\bar{D}$  threshold are narrow (annihilation or  $\rightarrow$  other charmonia)  
 States above  $D\bar{D}$  threshold are broad ( $\rightarrow D\bar{D}, D\bar{D}^*, \dots$ )

# Charmonium table



- ◻ Potential models
- States observed in 1974-1980
- States observed after 2002
- States with unexpected properties
- ▲  $Z^+ = |\bar{c}u\bar{d}\rangle$   
*manifestly “exotic”*

States below  $D\bar{D}$  threshold are narrow (annihilation or  $\rightarrow$  other charmonia)  
 States above  $D\bar{D}$  threshold are broad ( $\rightarrow D\bar{D}, D\bar{D}^*, \dots$ )

# Multiquark states conceived already at the birth of the Quark Model

Volume 8, number 3

PHYSICS LETTERS

1 February 1964

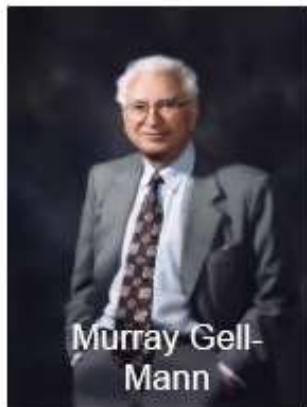
## A SCHEMATIC MODEL OF BARYONS AND MESONS \*

M. GELL-MANN

*California Institute of Technology, Pasadena, California*

Received 4 January 1964

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $b$  if we assign to the triplet  $t$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ . We then refer to the members  $u^{\frac{1}{3}}$ ,  $d^{-\frac{1}{3}}$ , and  $s^{-\frac{1}{3}}$  of the triplet as "quarks" 6) and the members of the anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqqq)$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(q\bar{q}\bar{q})$ , etc. It is assuming that the lowest baryon configuration  $(qqq)$  gives just the representations 1, 8, and 10 that have been observed, while



Murray Gell-Mann

8419/TH.412

21 February 1964

AN  $SU_3$  MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING

II \*)

G. Zweig

CERN—Geneva

\*) Version I is CERN preprint 8102/TH.401, Jan. 17, 1964.

...

- 6) In general, we would expect that baryons are built not only from the product of three mesas,  $AAA$ , but also from  $\overline{AAA}$ ,  $\overline{AA}AAA$ , etc., where  $\overline{A}$  denotes an anti-ace. Similarly, mesons could be formed from  $\overline{AA}$ ,  $\overline{AAA}$  etc. For the low mass mesons and baryons we will assume the simplest possibilities,  $\overline{AA}$  and  $AAA$ , that is, "deuces and treys".

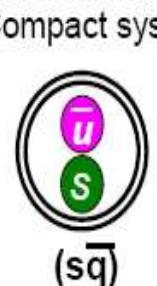


George Zweig

# Conventional and “exotic” hadrons

## Conventional

Strong binding.  
Compact systems.



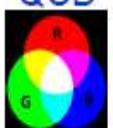
$K \text{ meson}$



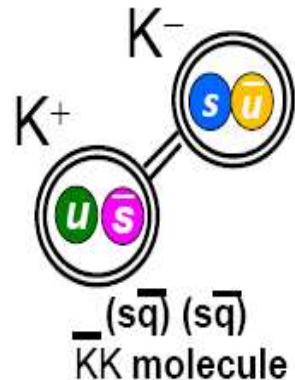
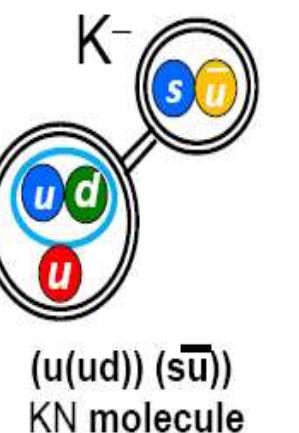
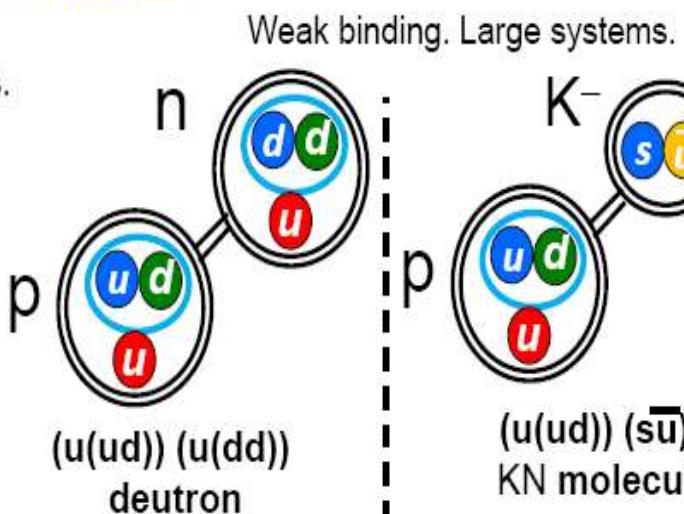
$\Lambda \text{ baryon}$

Meson and baryons  
motivated Quark Model

and  
QCD



Baryonic  
molecules exist



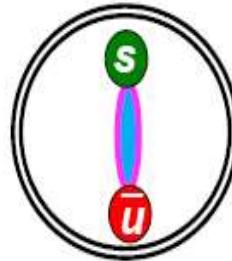
Are molecular forces in such  
systems strong enough to  
create bound states, or  
pronounced effects?

## “Exotic”

Strong binding. Compact systems.



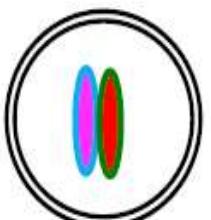
$((\bar{q}(sq))(qq))$   
pentaquark



$(s\bar{q}g)$   
Hybrid meson



$((\bar{s}q)(sq))$   
tetraquark

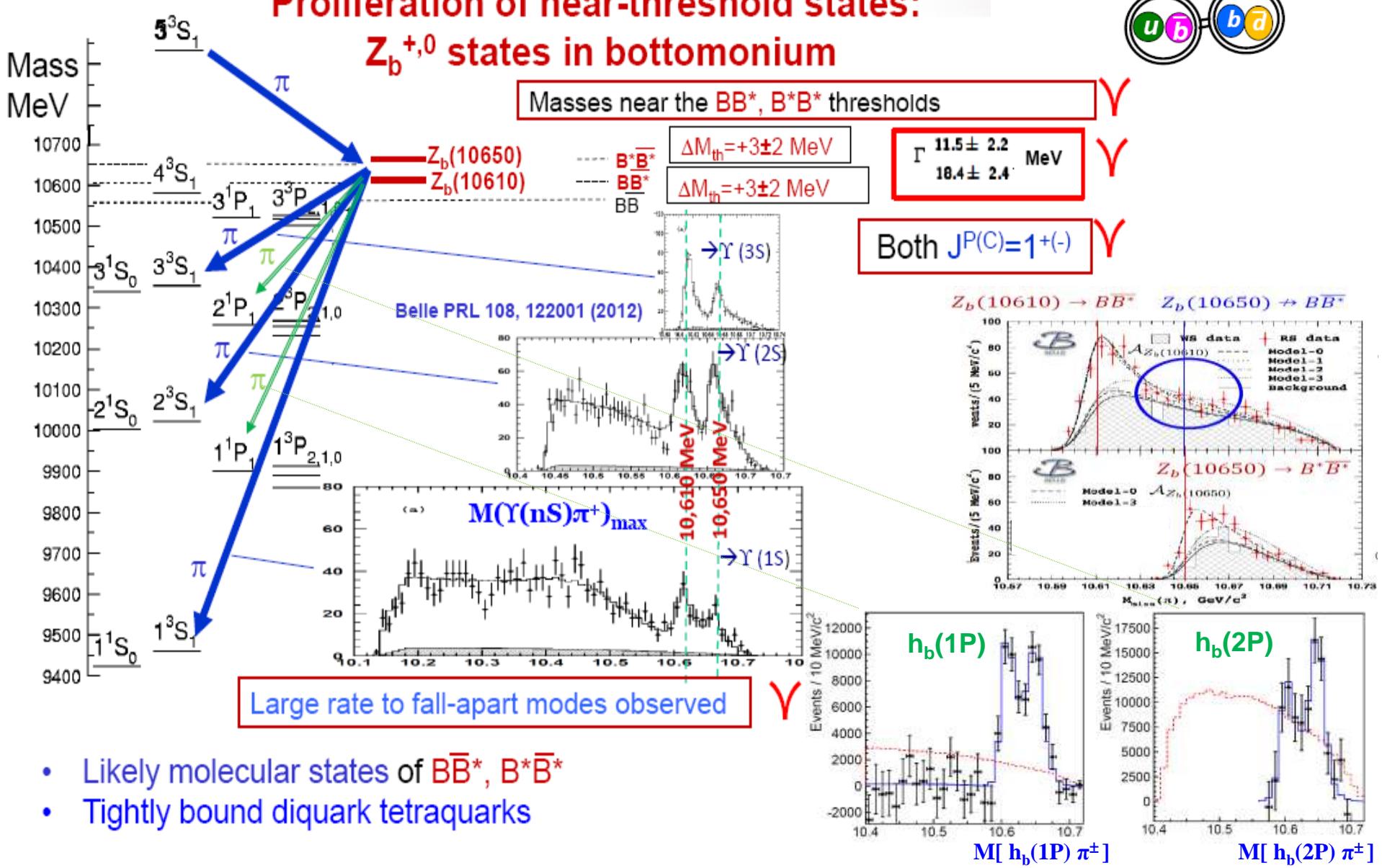


$(gg)$   
Glueball

QCD predicts attractive forces in  
some of such configurations.  
Do they live long enough to produce  
observable states/effects ?

Firmly  
expected  
in QCD

## Proliferation of near-threshold states: $Z_b^{+,0}$ states in bottomonium



- Likely molecular states of  $B\bar{B}^*$ ,  $B^*\bar{B}^*$
- Tightly bound diquark tetraquarks

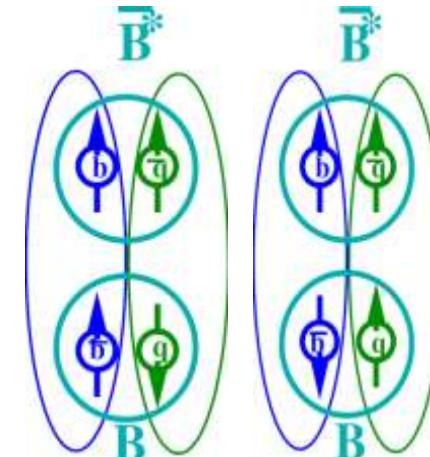
# Heavy quark structure in $Z_b$

A.B.,A.Garmash,A.Milstein,R.Mizuk,M.Voloshin PRD84 054010 (arXiv:1105.4473)

Wave func. at large distance –  $B(*)B^*$

$$|Z'_b\rangle = \frac{1}{\sqrt{2}} \mathbf{0}_{bb}^- \otimes \mathbf{1}_{Qq}^- - \frac{1}{\sqrt{2}} \mathbf{1}_{bb}^- \otimes \mathbf{0}_{Qq}^-$$

$$|Z_b\rangle = \frac{1}{\sqrt{2}} \mathbf{0}_{bb}^- \otimes \mathbf{1}_{Qq}^- + \frac{1}{\sqrt{2}} \mathbf{1}_{bb}^- \otimes \mathbf{0}_{Qq}^-$$



Explains

- Why  $h_b\pi\pi$  is unsuppressed relative to  $\Upsilon\pi\pi$
- Relative phase  $\sim 0$  for  $\Upsilon$  and  $\sim 180^\circ$  for  $h_b$
- Production rates of  $Z_b(10610)$  and  $Z_b(10650)$  are similar
- Dominant decays to  $B(*)B^*$
- Similar structures in  $\Psi\pi$  and  $h_c\pi$

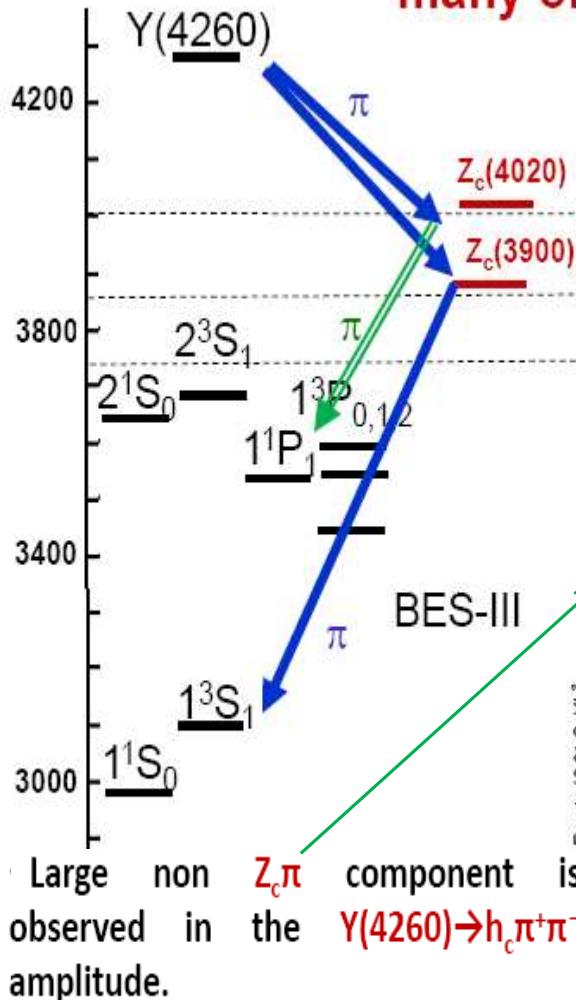
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## Other Possible Explanations

- Coupled channel resonances (I.V.Danilkin et al, arXiv:1106.1552)
- Cusp (D.Bugg Europhys.Lett.96 (2011),arXiv:1105.5492)
- Tetraquark (M.Karlener, H.Lipkin, arXiv:0802.0649)

# More near-threshold states: many of $Z_c^{+,0}$ charmonium states

- Expected from  $Z_b$  states and Heavy Quark Symmetry



Masses a few MeV above the  $D\bar{D}^*$ ,  $D^*\bar{D}^*$  thresholds

$$D^*\bar{D}^* \quad \Delta M_{th} = +7 \pm 2 \text{ MeV}$$

$$D\bar{D}^* \quad \Delta M_{th} = +11 \pm 3 \text{ MeV}$$

$$\Gamma \quad 13 \pm 5 \text{ MeV}$$

$$28.1 \pm 2.6$$

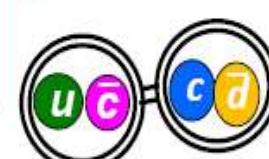
$$J^P(C) = 1^{+(-)}$$

(established only for  $Z_c(3900)$ )

Large rate to fall-apart modes

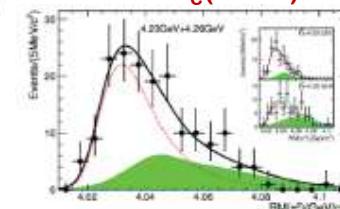
$$\frac{\Gamma[Z_c(4025)\rightarrow D^*D^*]}{\Gamma[Z_c(4020)\rightarrow \pi h_c]} \sim 9.$$

$$\frac{\Gamma[Z_c(3900)\rightarrow DD^*]}{\Gamma[Z_c(3900)\rightarrow \pi J/\psi]} = 6.2 \pm 1.1_{\text{stat}} \pm 2.7_{\text{sys}}$$



Charged and neutral versions detected /  $G=1^+$

$Z_c(4025)$



Molecular states of  $D\bar{D}^*$ ,  $D^*\bar{D}^*$ ?  
Diquark tetraquarks?

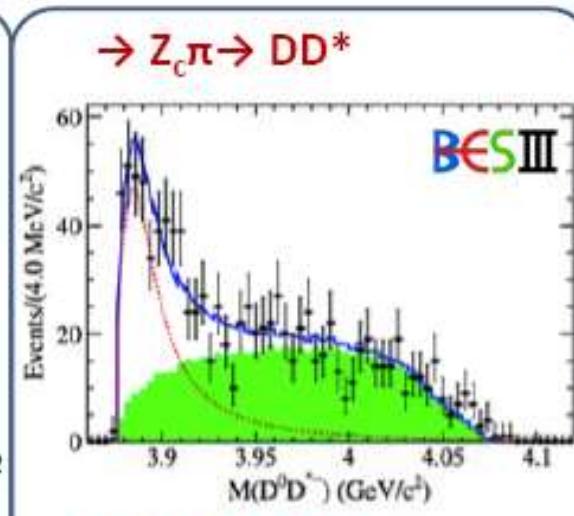
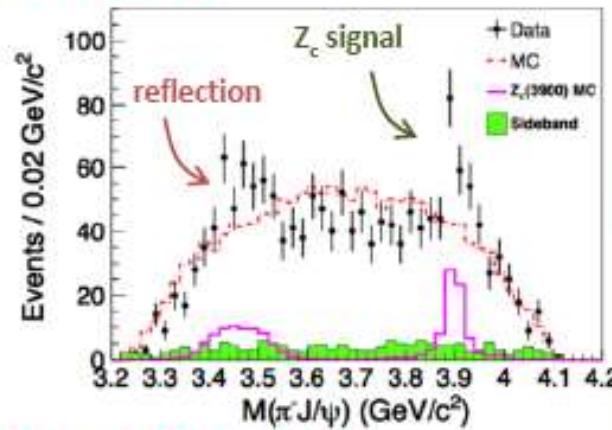
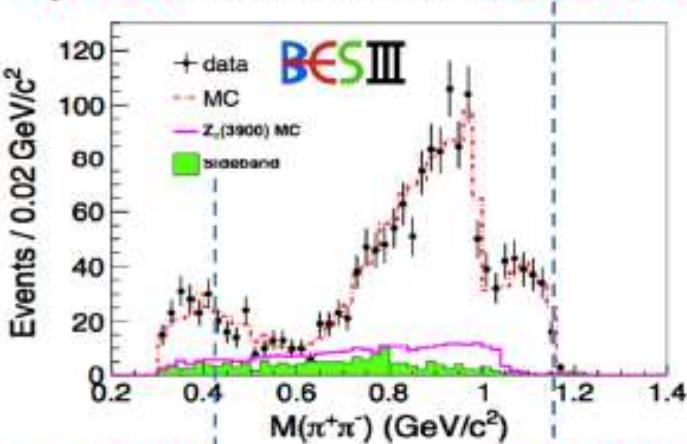
No sign of  $Z_c(4025)$  decay in  $DD^*$

# Charm vs Beauty: I

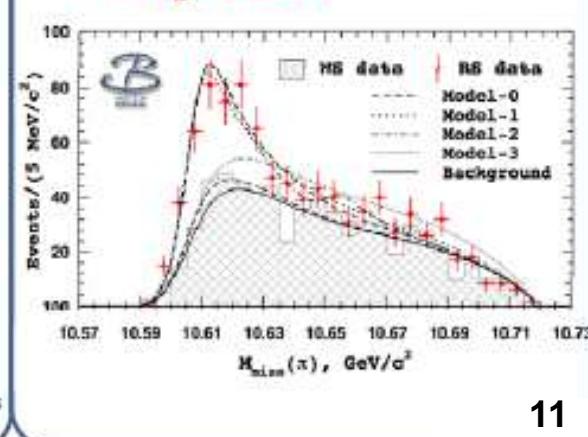
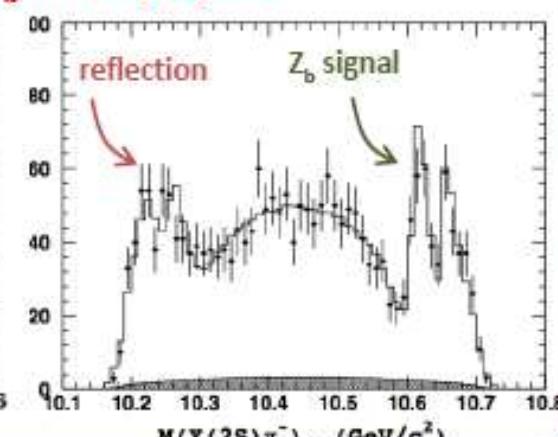
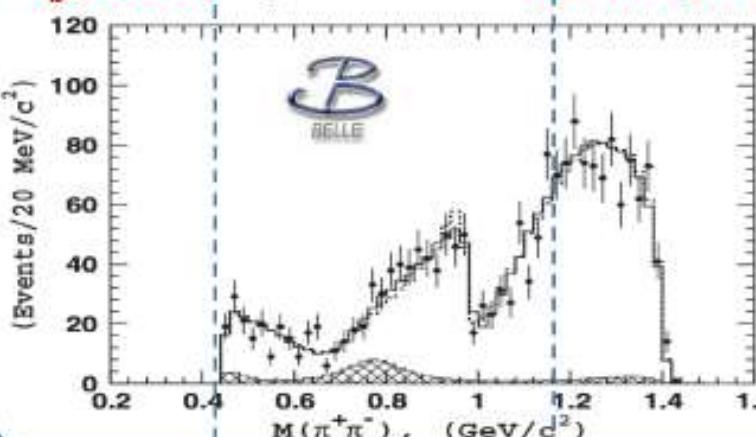
## What is in common?

- $\Upsilon(10860)/\Upsilon(4260)$  demonstrates anomalously large coupling to  $\Upsilon\pi^+\pi^-/\Psi\pi^+\pi^-$  and  $h_b\pi^+\pi^-/h_c\pi^+\pi^-$  final states.  $J^P = 1^+$  for both, PRL119 (2017), 072001

$Z_c(3900)$  is produced in  $\Upsilon(4260) \rightarrow Z_c\pi \rightarrow \Psi\pi^+\pi^-$



$Z_b(10610)$  is produced in  $\Upsilon(10860) \rightarrow Z_b\pi \rightarrow \Upsilon(nS)\pi^+\pi^-$



# Charm vs Beauty: II

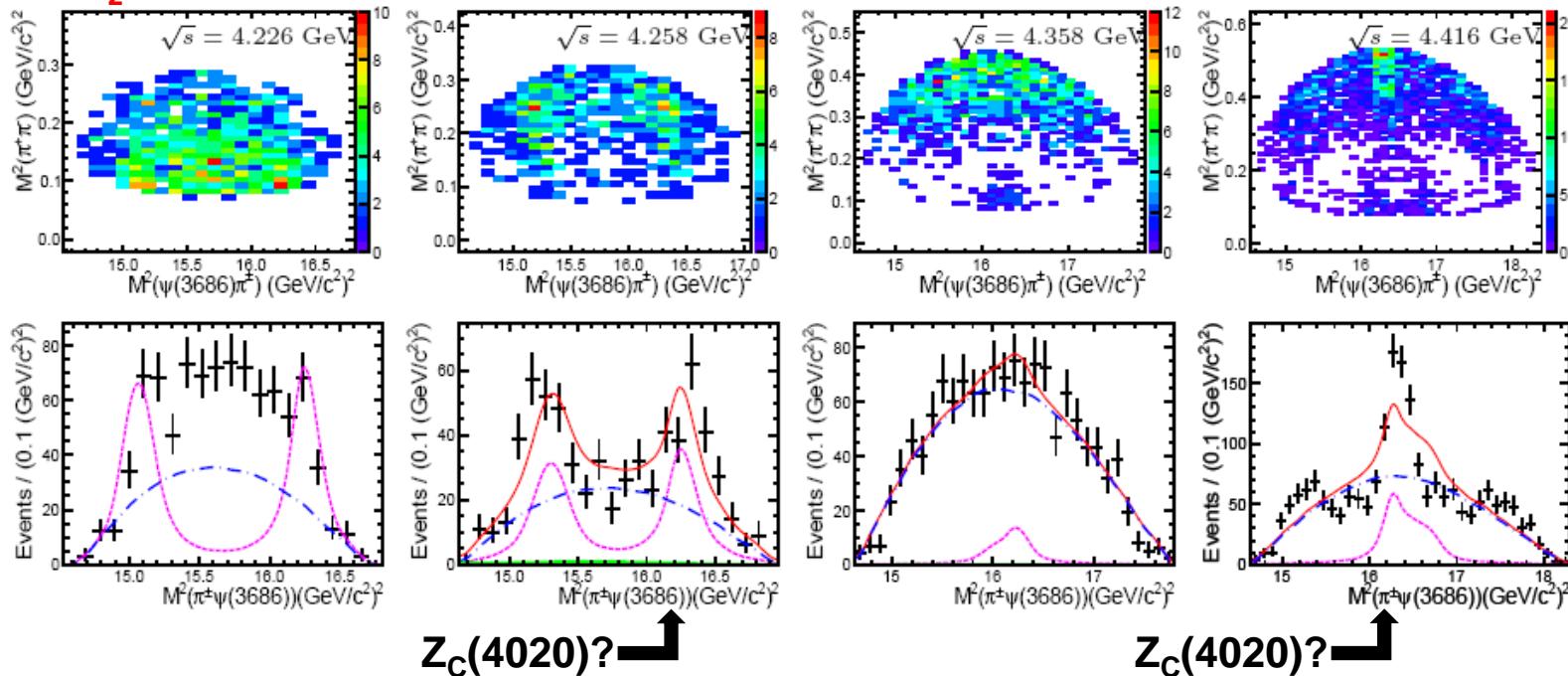
## What is different?

- Both  $Z_b(10610)$  and  $Z_b(10650)$  isotriplets are observed in the  $\Upsilon(nS)\pi$ , ( $n=1,2,3$ ) and  $h_b\pi$  final states.

BESIII, PRD96 (2017), 032004

$$M_z = 4032.1 \pm 2.4 \text{ MeV}/c^2$$

$$\Gamma_z = 26.1 \pm 5.3 \text{ MeV}$$

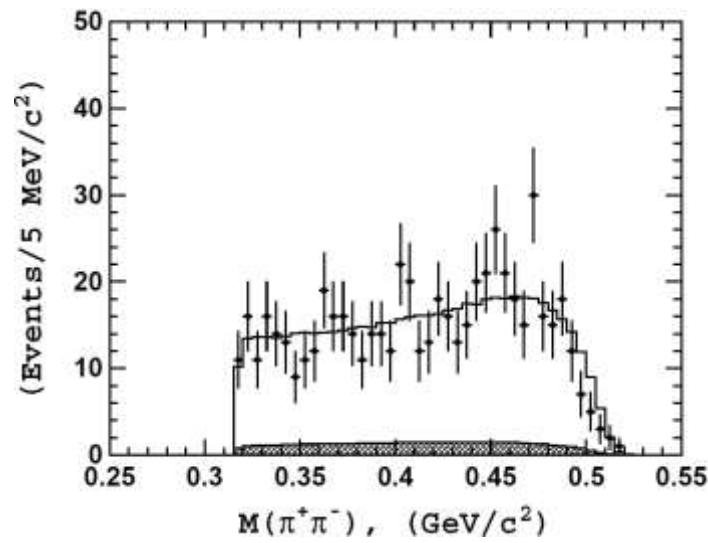
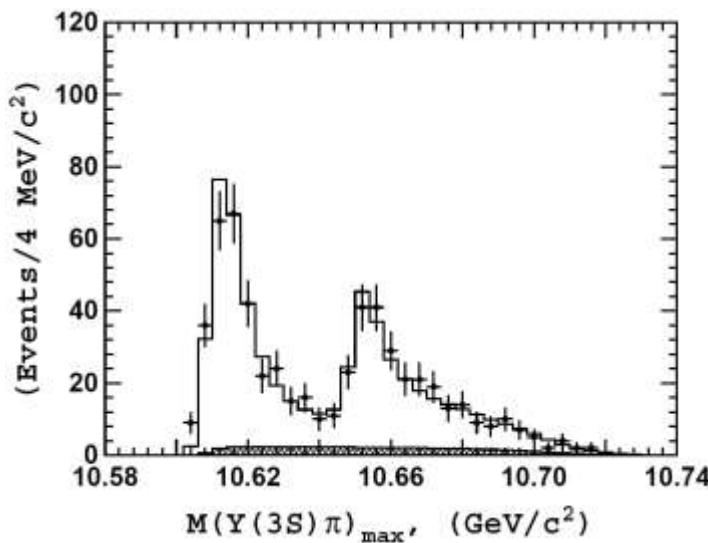
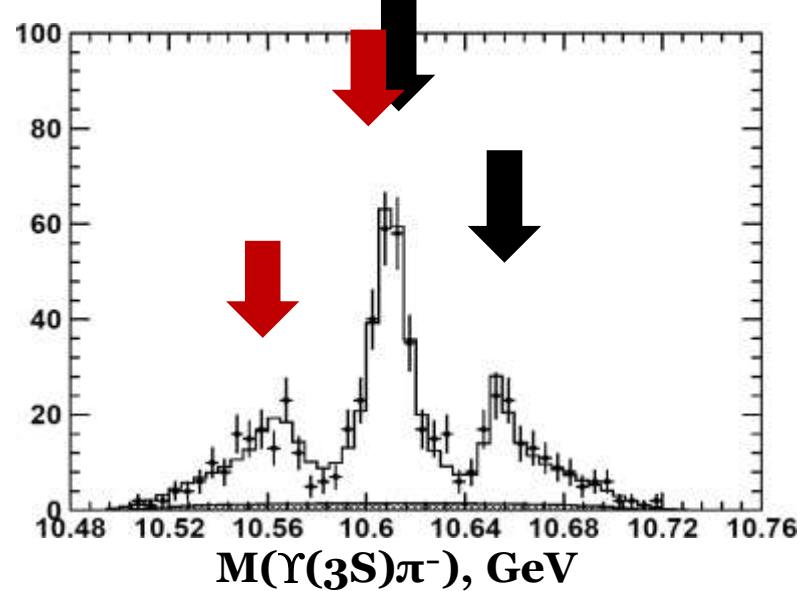
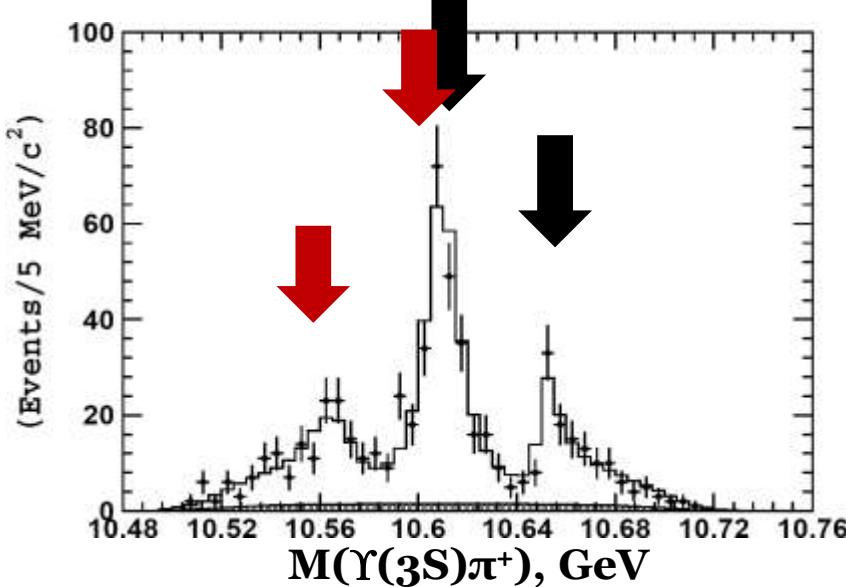


Mass, width not determined properly since did not allow for  
 $Z_c$  – NR bkg interference hinted by the Dalitz plot. This is likely  
 $Z_c(4020) \rightarrow \psi(2S)\pi^+$  expected from  $Z_b(10650) \rightarrow \Upsilon(2S)\pi^+$

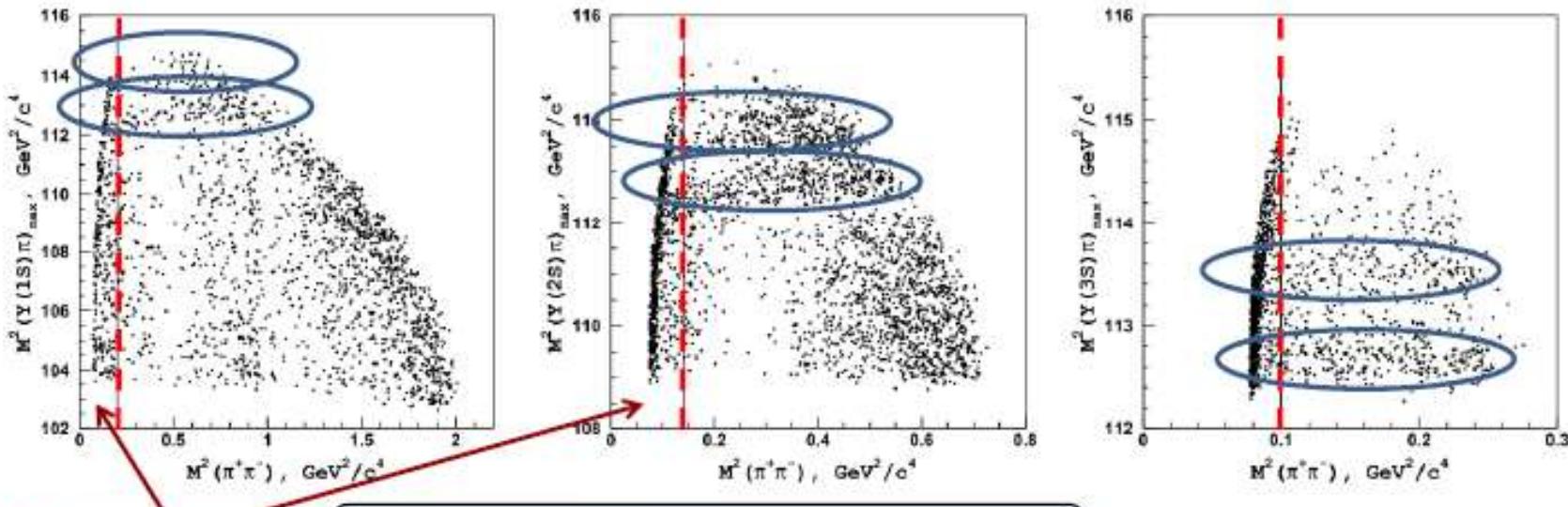
1

AB

# Results: $\Upsilon(3S)\pi^+\pi^-$



# Amplitude Analysis of $\Upsilon(nS)\pi^+\pi^-$



Photon conversions

Flatte:  $m = 950 \text{ MeV}/c^2$ ;  $g_{\pi\pi} = 0.23$ ;  $g_{KK} = 0.73$   
From the analysis of  $B \rightarrow K\pi\pi$  by Belle

D-wave Breit-Wigner

$$S(s_1, s_2) = |A_{Z_{b1}} + A_{Z_{b2}} + A_{NR} + A_{f_0(980)} + A_{f_2(1275)}|^2$$

$$A_{Z_{bi}} = \frac{\sqrt{M_i \Gamma_i}}{M_i^2 - s_1 + i M_i \Gamma_i} + \frac{a_i e^{i \phi_i} \sqrt{M_i \Gamma_i}}{M_i^2 - s_2 + i M_i \Gamma_i}$$

$$s_i \equiv M_{\pi_i \Upsilon}^2$$

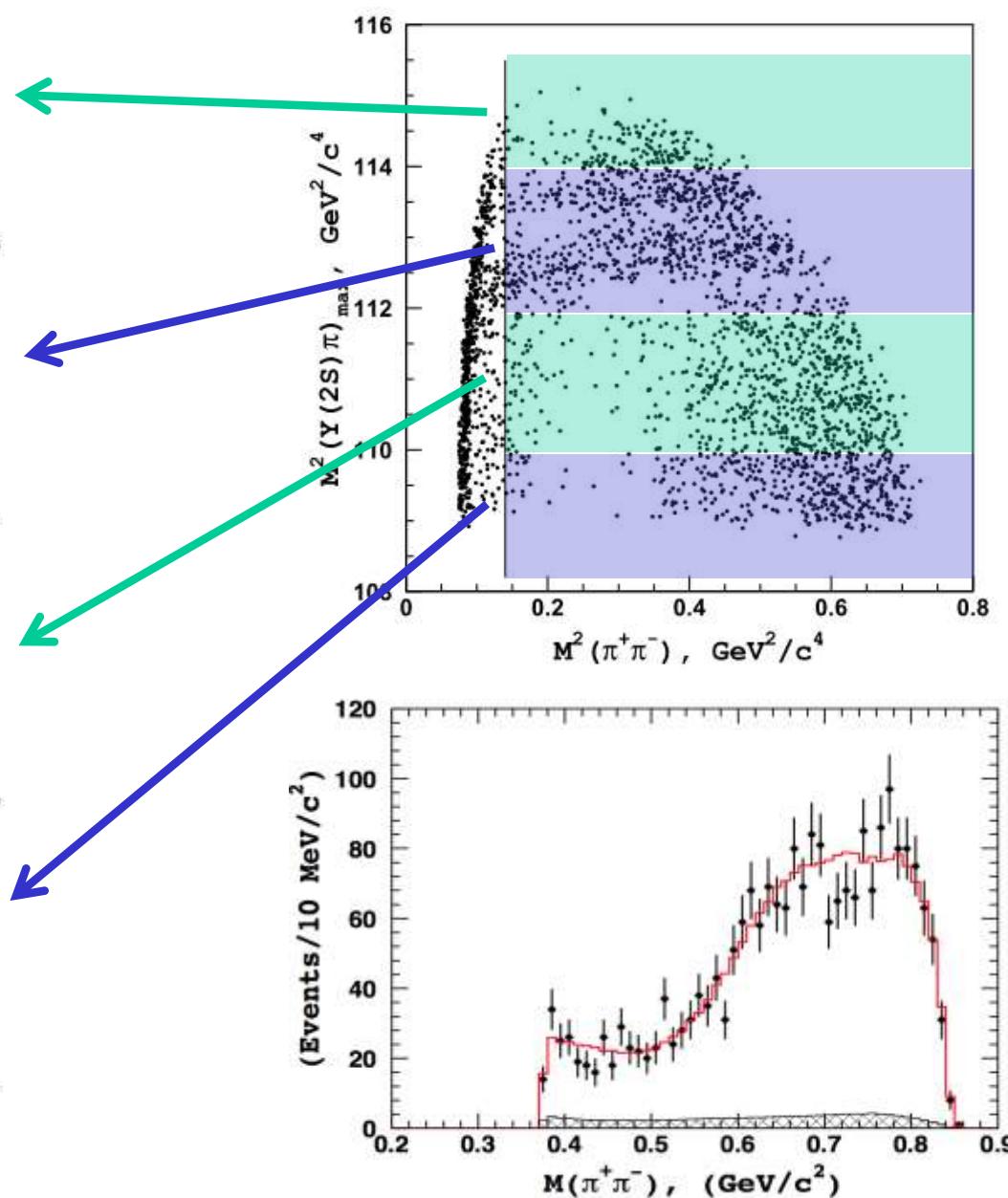
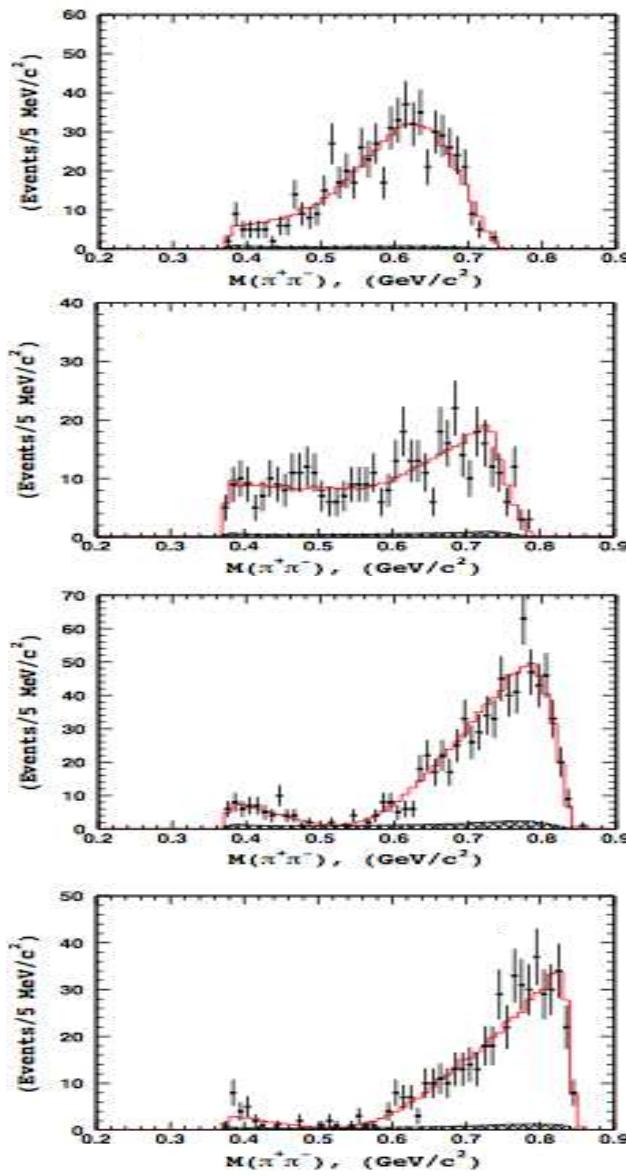
$$A_{NR} = c_1 + c_2 m_{\pi\pi}^2$$

M.B. Voloshin, Prog. Part. Nucl. Phys. 61:455, 2008.  
M.B. Voloshin, Phys. Rev. D74:054022, 2006.

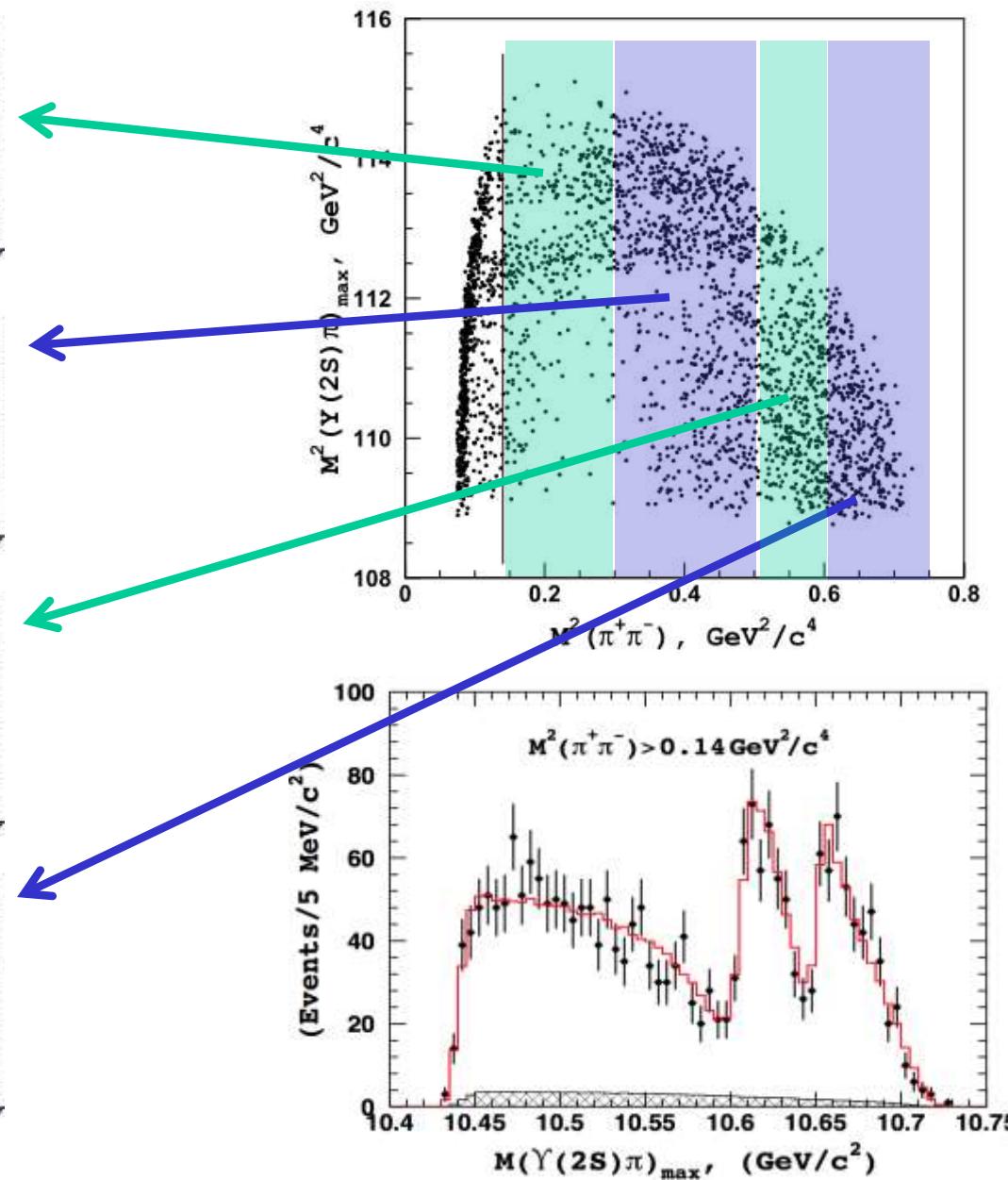
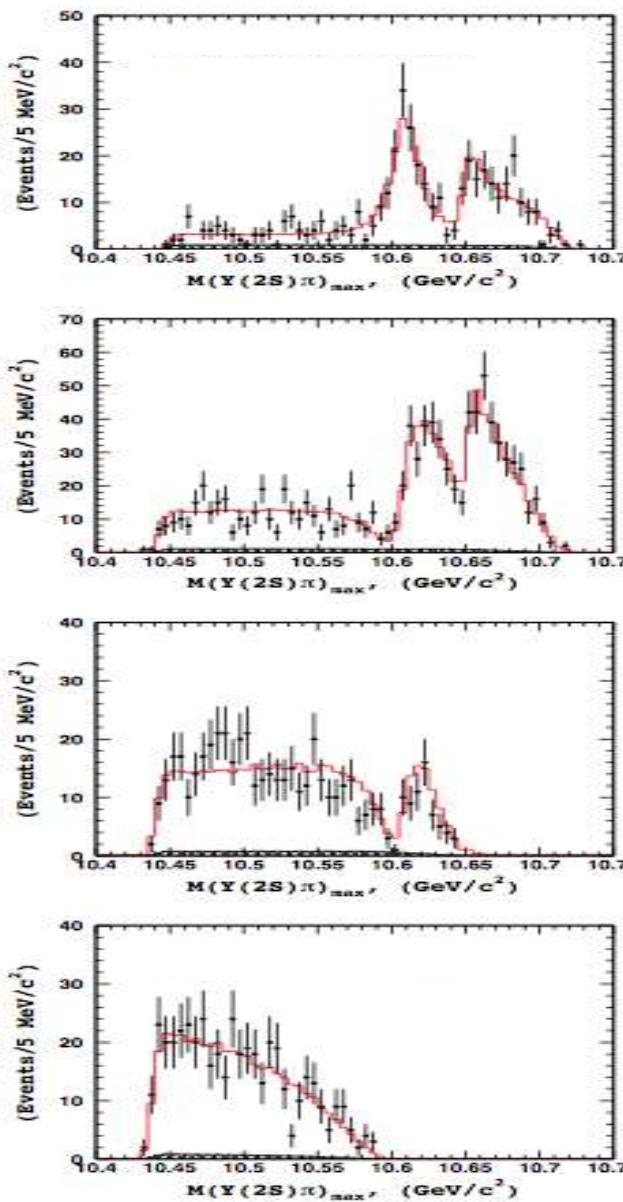
Combinatorial background is parameterized as a constant.

Unbinned ML fit to signal Dalitz plots

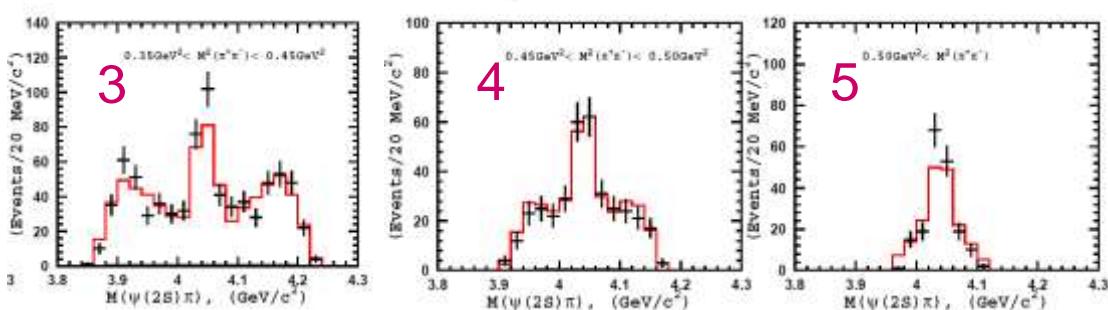
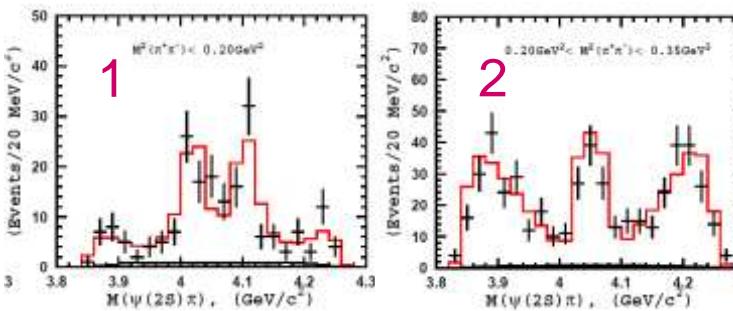
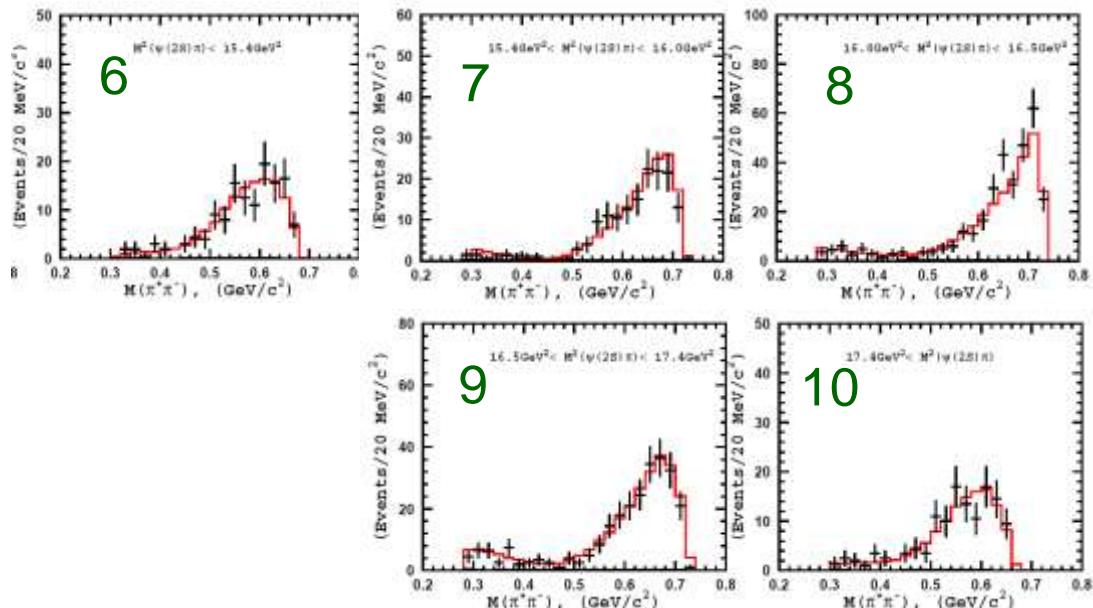
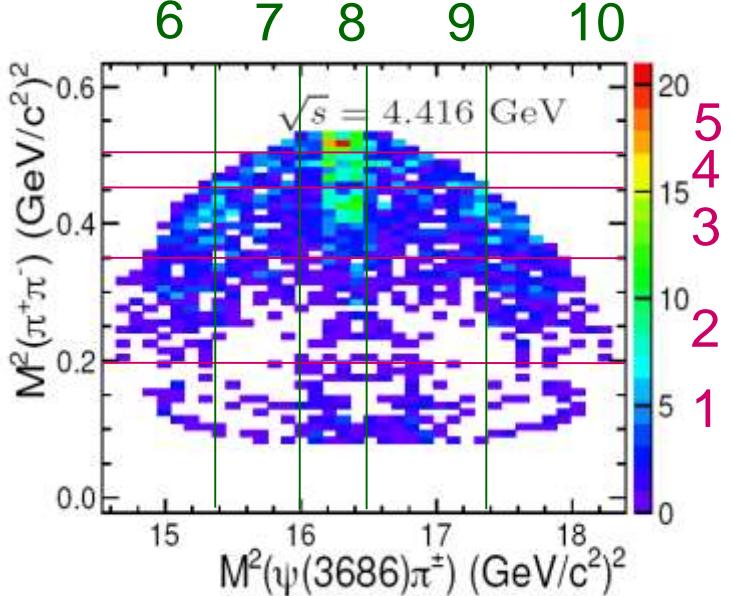
# $\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$ Results



# $\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$ Results



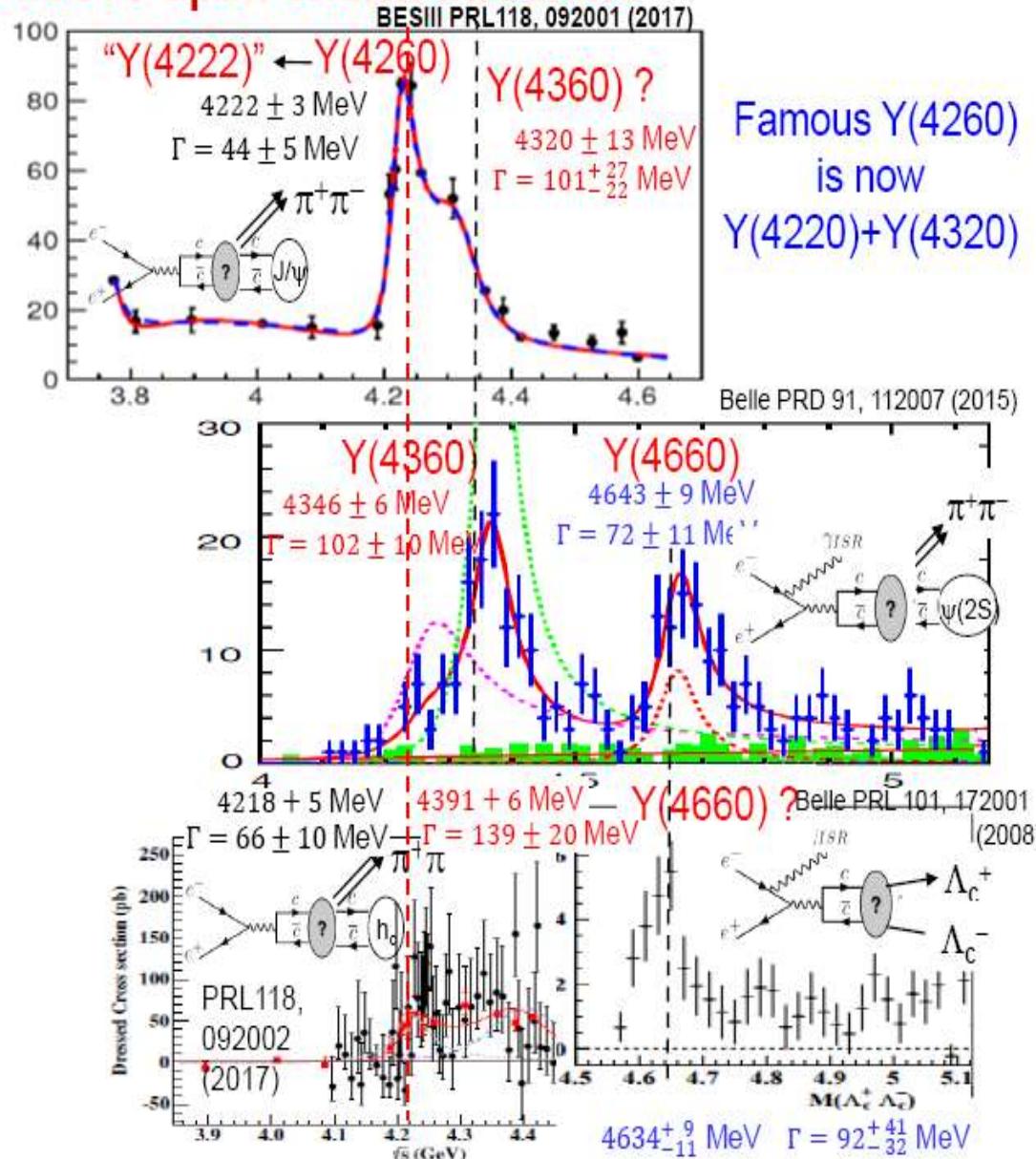
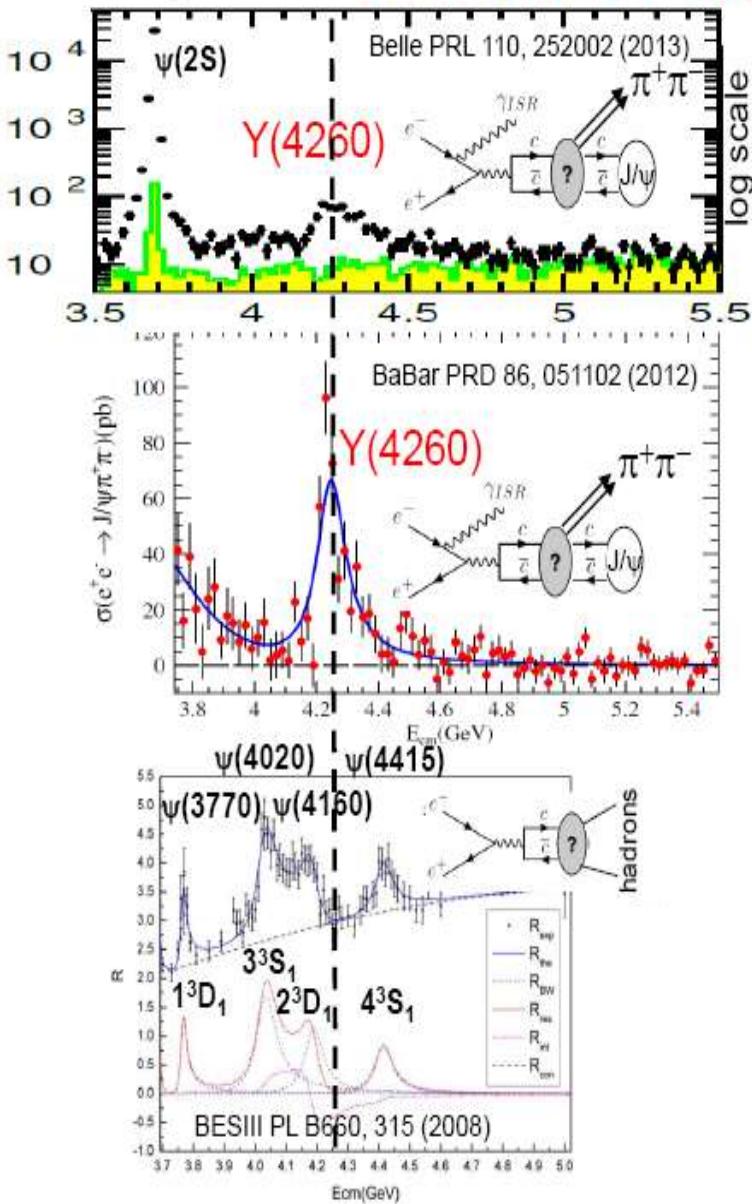
# Toy Fit of BESIII data at 4.416 GeV



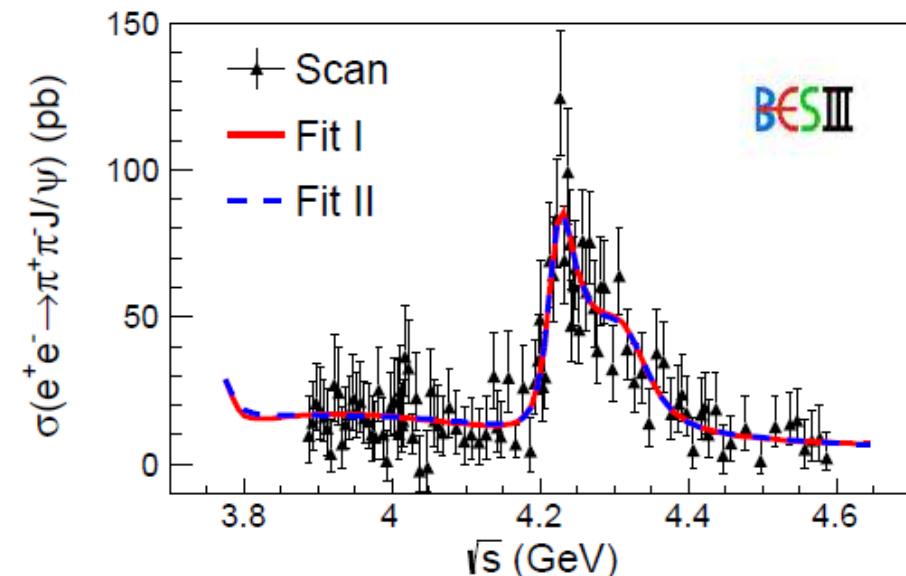
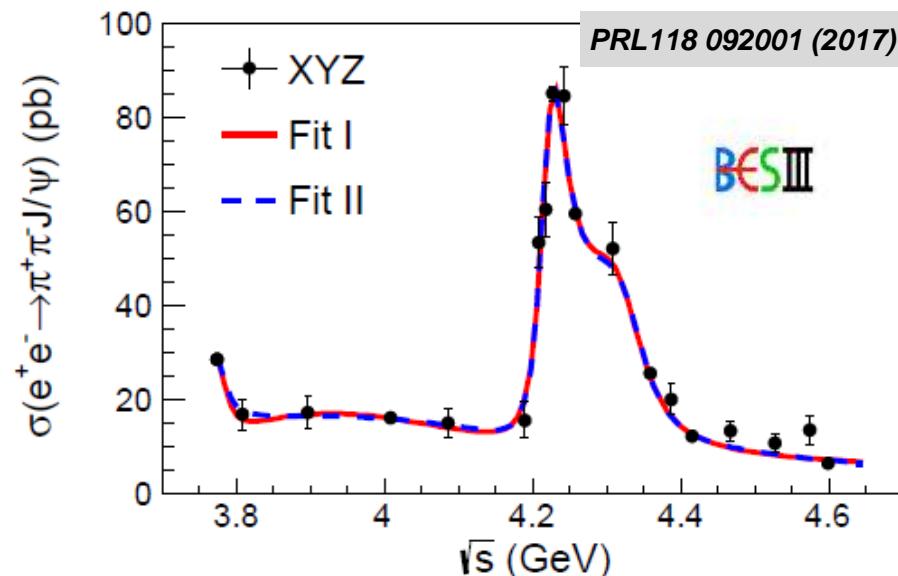
**Toy Fit Results:**  
 $M_z = 4019 \pm 1.9 \text{ MeV}/c^2$   
 $\Gamma_z = 29 \pm 4 \text{ MeV}$   
**Fit Fraction**  $12 \pm 3.7\%$

First observed by BaBar in 2005

# Anomalous 1<sup>-</sup> states above open charm threshold



# New precise measurements of $e^+e^- \rightarrow \pi^+\pi^- J/\psi$

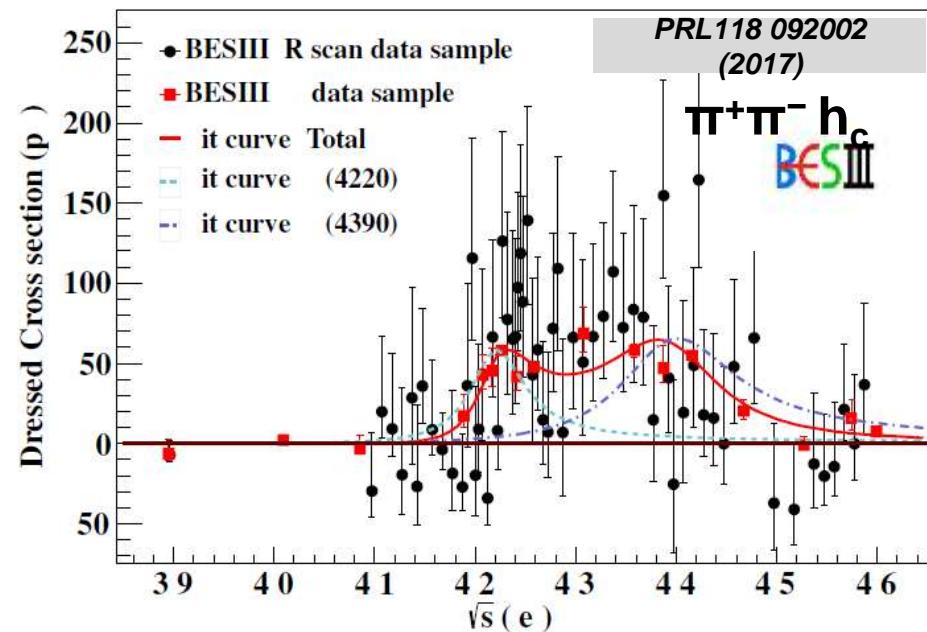
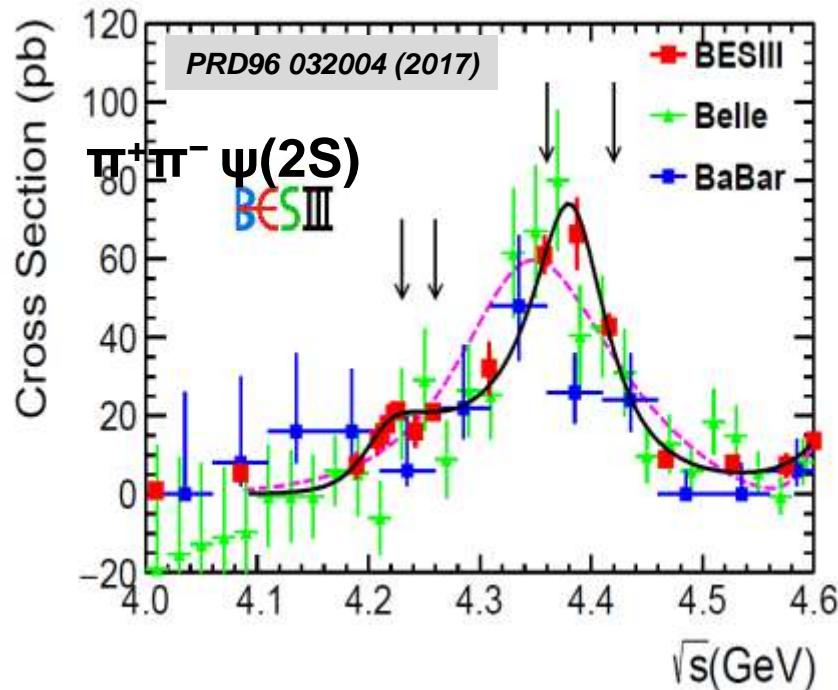


$e^+e^- \rightarrow \pi^+\pi^- J/\psi$  cross section is inconsistent with a single pick of **Y(4260)**

Two peaks are favored over one peak by 7.6  $\sigma$

	M, GeV/c <sup>2</sup>	$\Gamma$ , MeV	Decay mode
X(4260), PDG	4230±8	55±19	$\pi^+\pi^- J/\psi$
Y(4220), BESIII	4222.0±3.1±1.4	44.1±4.3±2.0	$\pi^+\pi^- J/\psi$
X(4360), PDG	4341±8	102±9	$\pi^+\pi^- \psi(2S)$
Y(4360), BESIII	4320.0±10.4±7.0	101.4 <sup>+25.3</sup> <sub>-19.7</sub> ±10.2	<u><math>\pi^+\pi^- J/\psi</math></u>

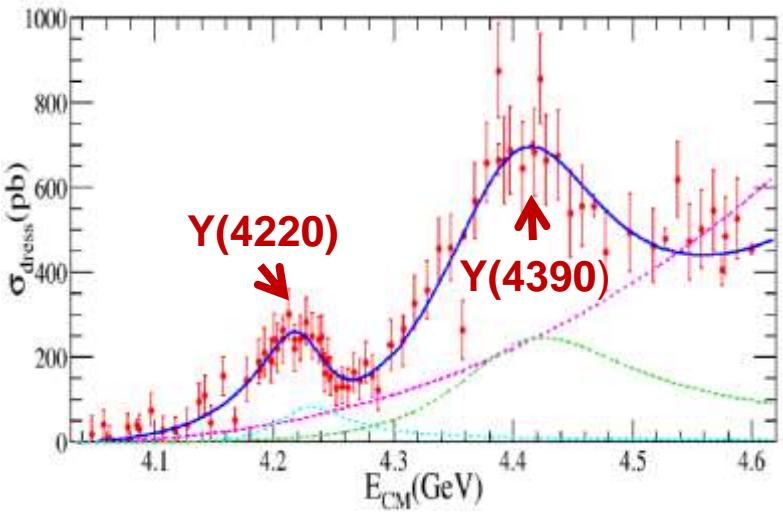
# New precise measurements of $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$ , $\pi^+\pi^- h_c$



BESIII confirms line shape in  $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$

	M, GeV/c <sup>2</sup>	$\Gamma$ , MeV	Decay mode
Y(4220)	$4209.5 \pm 7.4 \pm 1.4$	$80.1 \pm 24.6 \pm 2.9$	$\pi^+\pi^-\psi(2S)$
Y(4220)	$4218.4^{+5.5}_{-4.5} \pm 0.9$	$66.0^{+12.3}_{-8.3} \pm 0.4$	$\pi^+\pi^- h_c$
Y(4390)	$4383.8 \pm 4.2 \pm 0.8$	$84.2 \pm 12.5 \pm 2.1$	$\pi^+\pi^-\psi(2S)$
Y(4390)	$4391.5^{+6.3}_{-6.8} \pm 0.9$	$139.5^{+16.2}_{-20.6} \pm 0.6$	$\pi^+\pi^- h_c$
X(4360), PDG	<u><math>4341 \pm 8</math></u>	<u><math>102 \pm 9</math></u>	<u><math>\pi^+\pi^-\psi(2S)</math></u>

# BESIII: $e^+e^- \rightarrow D^0D^{*-}\pi^+$

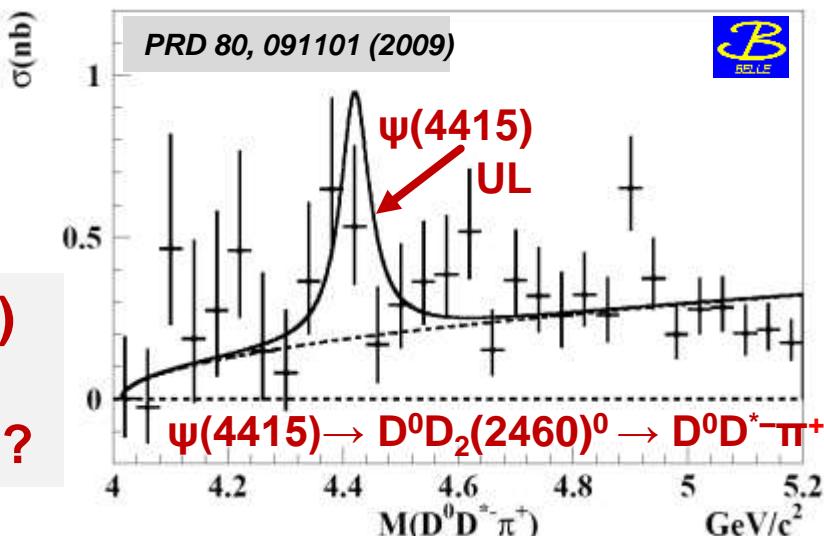


$Y(4390)$   
or  
 $\Psi(4415)$ ?

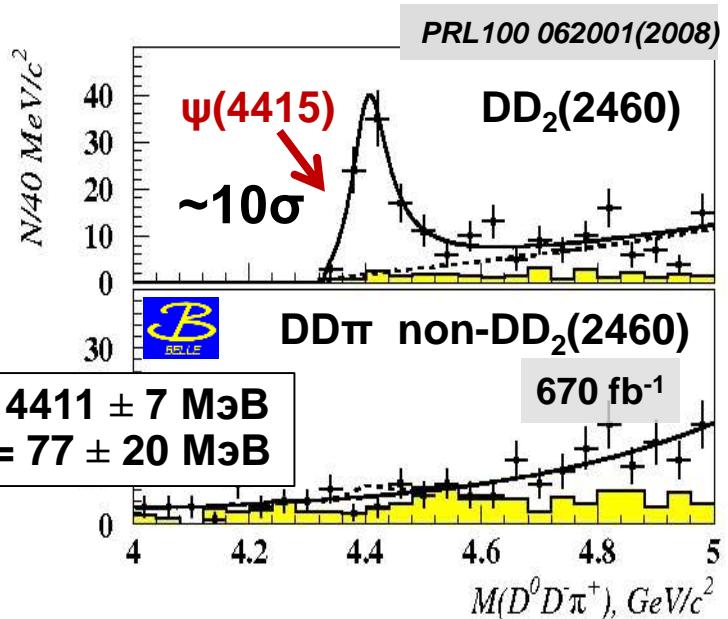
Parameters	SolutionI	SolutionII	SolutionIII	SolutionIV
$c (10^{-4})$			$5.5 \pm 0.6$	
$M_1 (\text{MeV}/c^2)$	$\boxed{\Psi(4220)}$	$4224.8 \pm 5.6$		
$\Gamma_1 (\text{MeV})$		$72.3 \pm 9.1$	<small>BESIII Preliminary</small>	
$M_2 (\text{MeV}/c^2)$	$\boxed{\Psi(4390)}$	$4400.1 \pm 9.3$		
$\Gamma_2 (\text{MeV})$		$181.7 \pm 16.9$		
$\Gamma_1^{\text{el}} (\text{eV})$	$62.9 \pm 11.5$	$7.2 \pm 1.8$	$81.6 \pm 15.9$	$9.3 \pm 2.7$
$\Gamma_2^{\text{el}} (\text{eV})$	$88.5 \pm 15.8$	$55.3 \pm 8.7$	$551.9 \pm 85.3$	$344.9 \pm 70.6$
$\phi_1$	$-2.1 \pm 0.1$	$2.8 \pm 0.3$	$-0.9 \pm 0.1$	$-2.3 \pm 0.2$
$\phi_2$	$1.9 \pm 0.3$	$2.3 \pm 0.2$	$2.3 \pm 0.1$	$-1.9 \pm 0.1$

$\Psi(4415) \rightarrow D^0 D_2(2460)^0 \rightarrow D^0 D^- \pi^+$   
 $\Psi(4415) \rightarrow D^0 D_2(2460)^0 \rightarrow D^0 D^{*-} \pi^+$   
 UL due to limited statistics

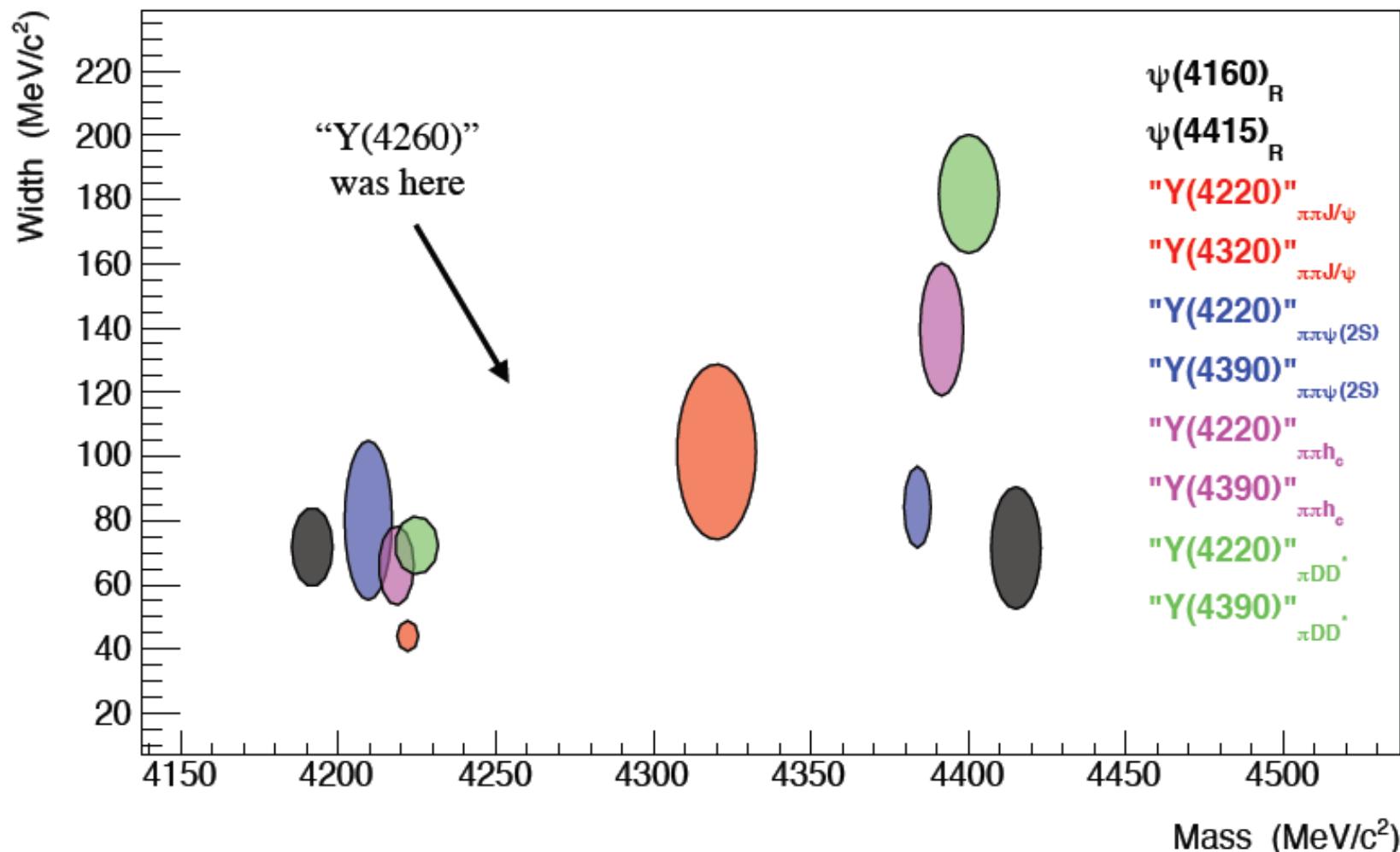
# Belle: $e^+e^- \rightarrow D^0D^{*-}\pi^+$



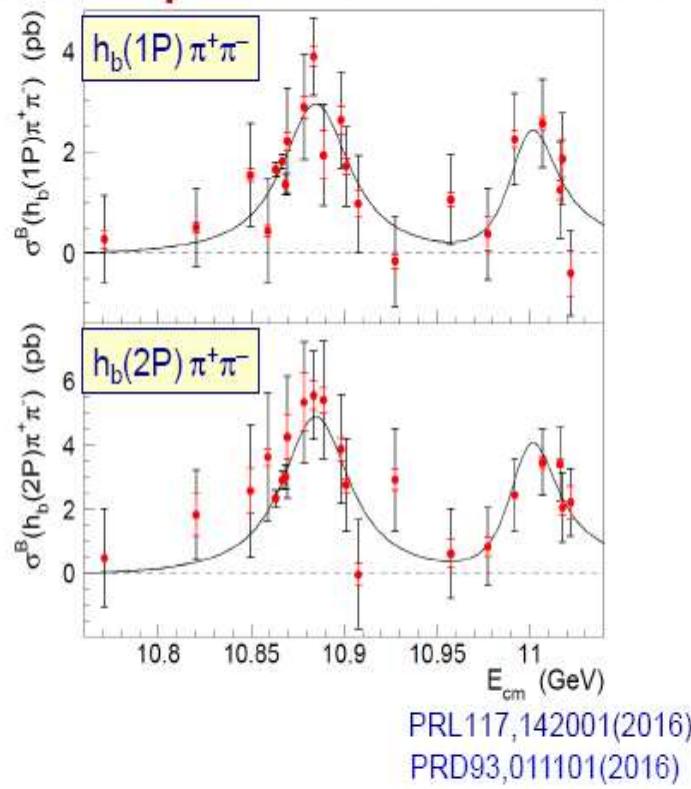
# Belle: $e^+e^- \rightarrow D^0D^- \pi^+$



## Parameters of the Peaks in $e^+e^-$ Cross Sections

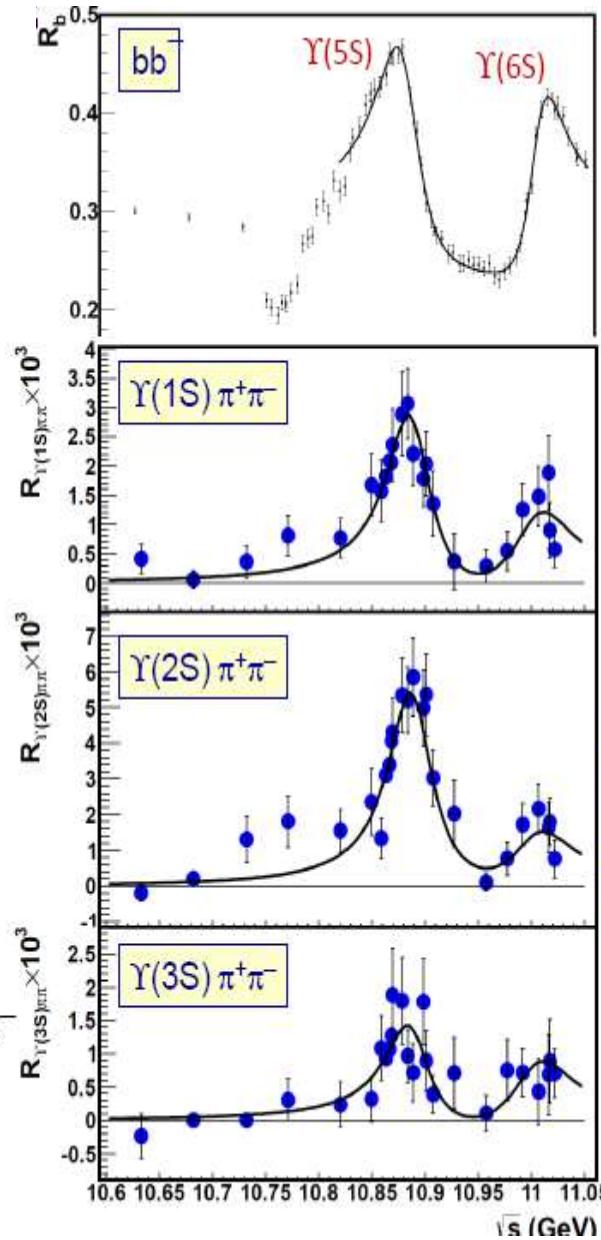


## Anomalous behavior of $1^-$ states above open bottom threshold



$e^+e^- \rightarrow \Upsilon(1S,2S,3S)\pi^+\pi^-$  and  $h_b(1P,2P)\pi^+\pi^-$  proceed via  $\Upsilon(5S), \Upsilon(6S)$

Unlike in charmonium!



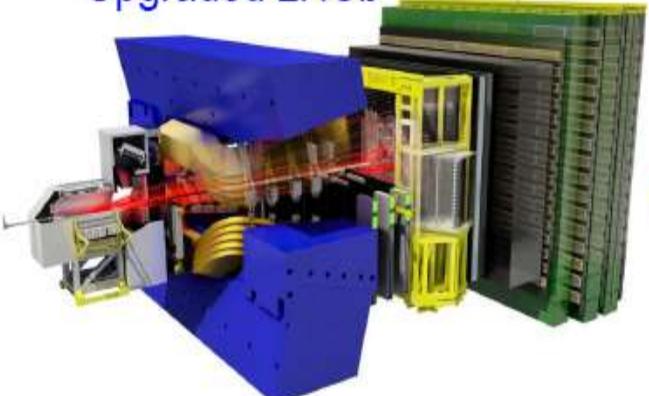
However,  $\Upsilon(5S), \Upsilon(6S) \rightarrow \Upsilon(1S,2S,3S)\pi^+\pi^-$  widths are 100 larger than  $\Upsilon(3S), \Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$   
OZI-rule violation

Also widths for  $\Upsilon(5S), \Upsilon(6S) \rightarrow h_b(1P), h_b(2P)\pi^+\pi^-$  are comparable, but require heavy quark spin flip  
HQSS violation

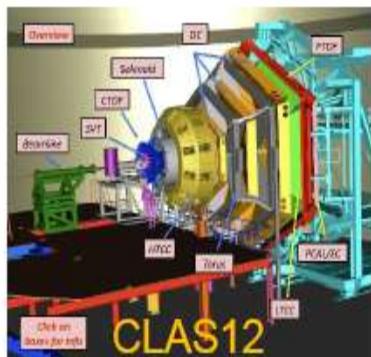
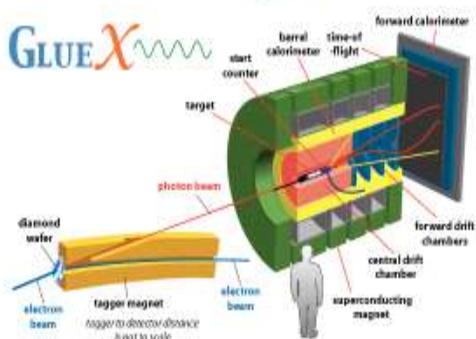
Like in charmonium!

- Need more data to settle the phenomenological disputes
- More data are forthcoming!

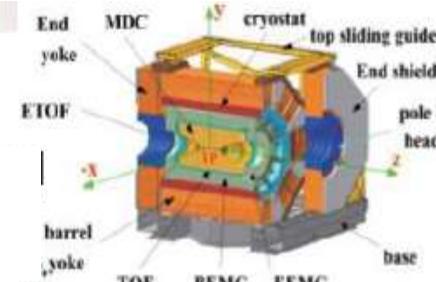
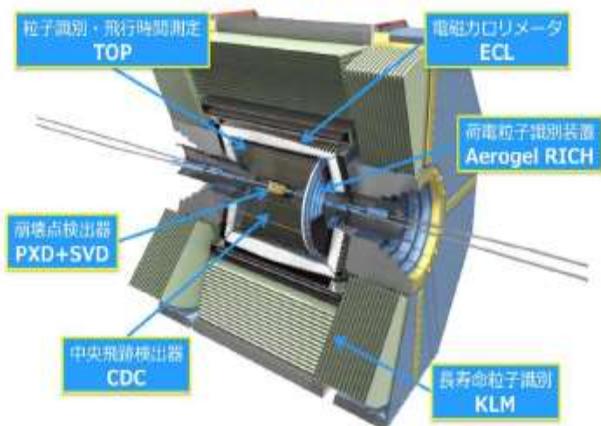
Upgraded LHCb



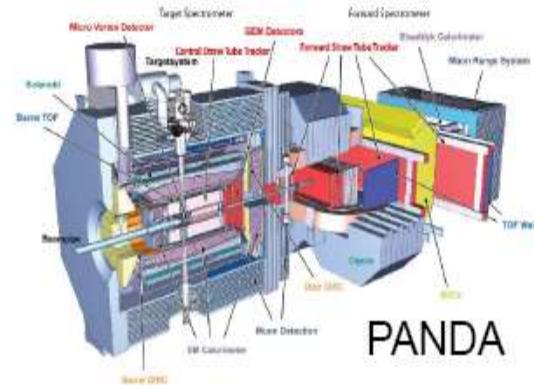
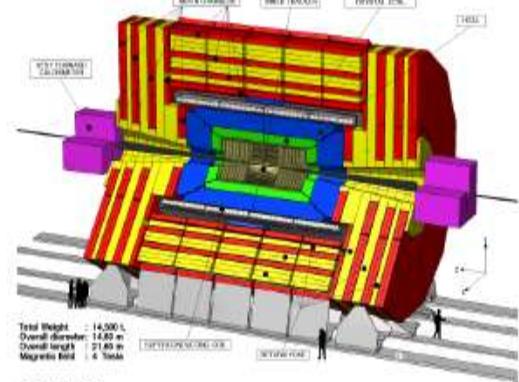
GLUE X



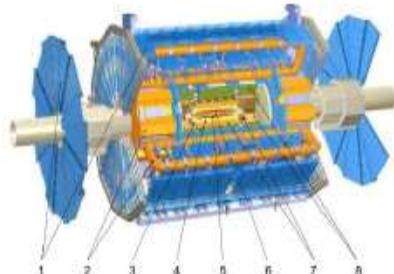
Belle II 測定器



CMS



ATLAS



PANDA

and other...

# Back up slides

# Quarkonium Basics

c, b -quarks are heavy:

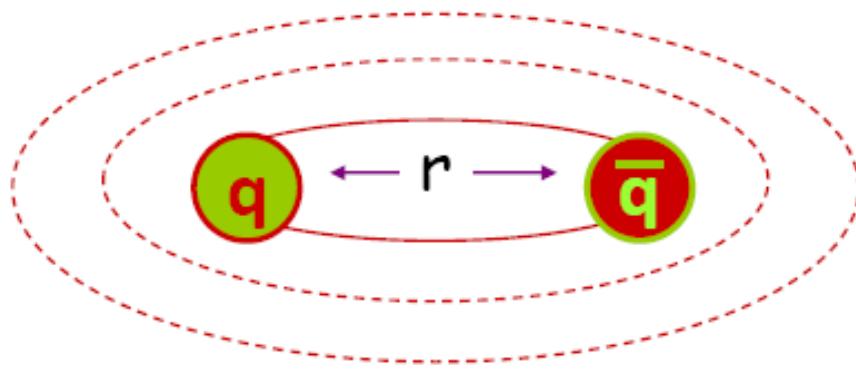
$$m_c \sim 1.5 \text{ GeV} \sim 1.6 m_p ;$$

$$m_b \sim 4.5 \text{ GeV} \sim 4.8 m_p ;$$

velocities are small:

$$v/c \sim 1/4 \text{ (for } b\bar{b}, v/c \sim 0.1)$$

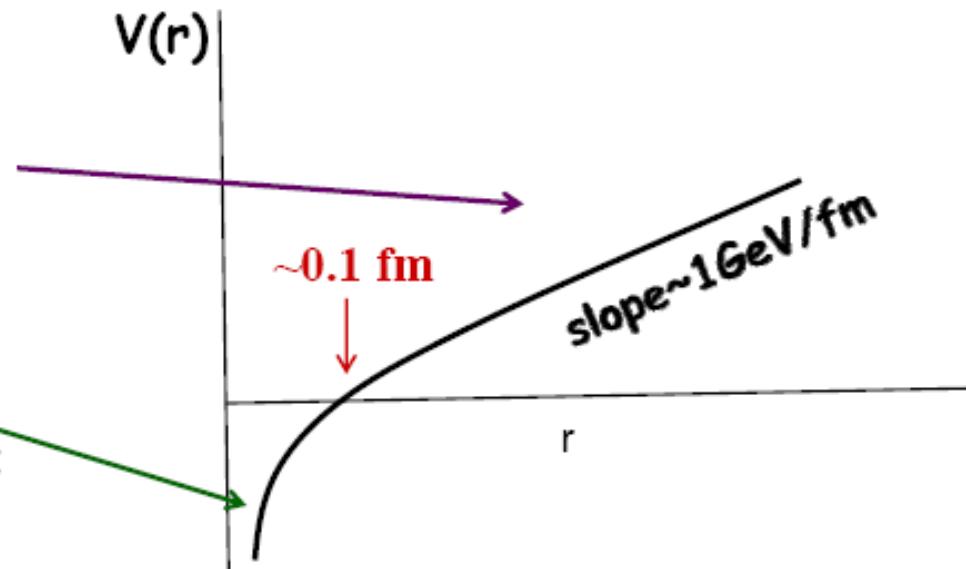
non-relativistic QM applies

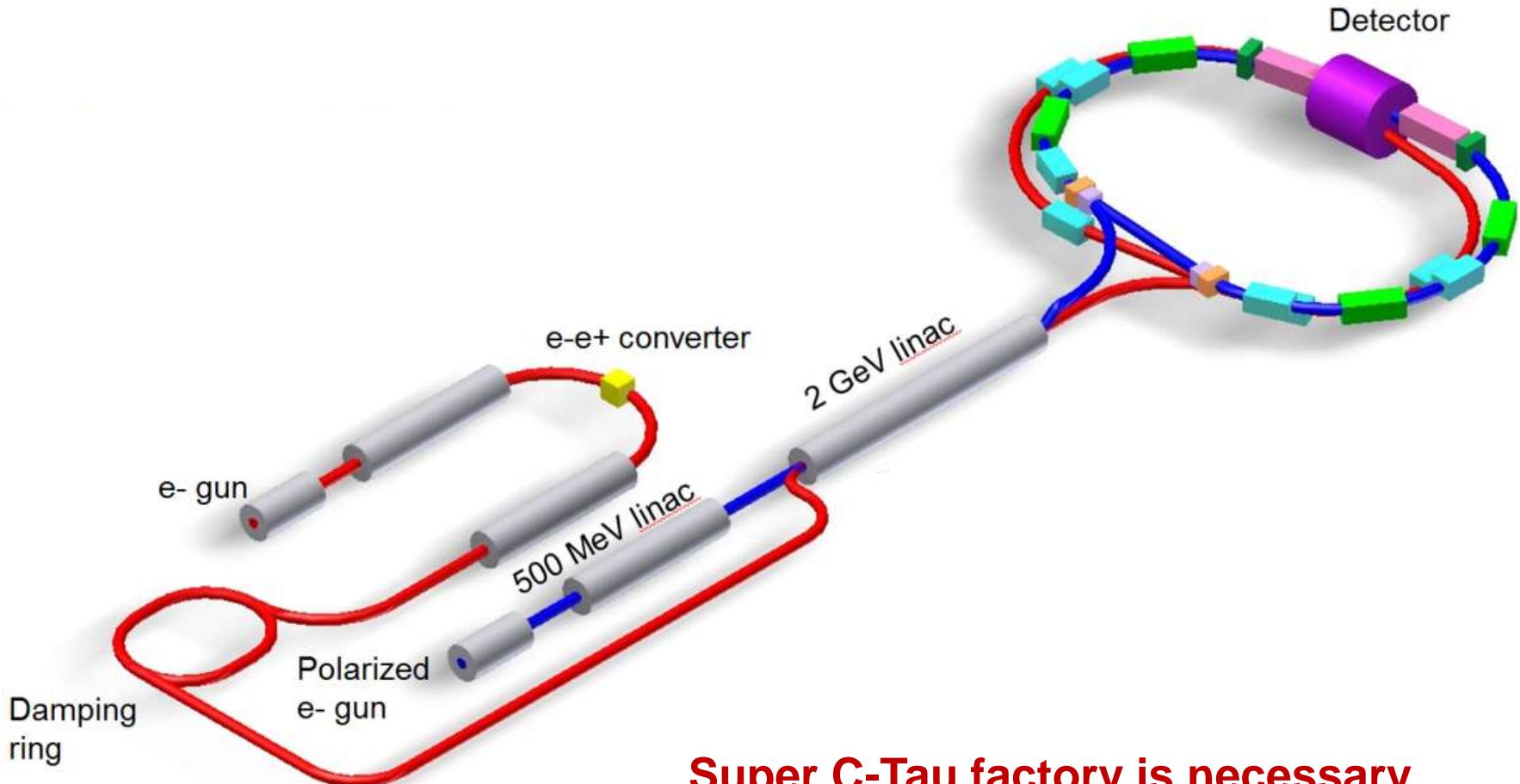


$$-\frac{\hbar^2}{2m_r} \nabla^2 \Psi + V(r) \Psi = E \Psi$$

linear "confining"  
long distance component

$1/r$  "coulombic"  
short distance component



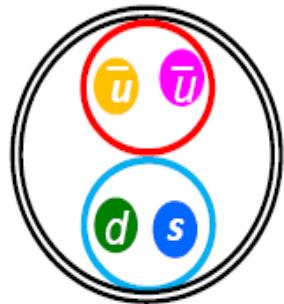


**Super C-Tau factory is necessary instrument for future studies of the highly excited quarkonium**

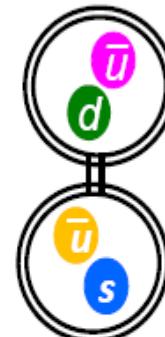
## Tetraquarks vs meson-meson molecules

- The same quark content can, in principle, create a meson-meson molecule or a tetraquark
- However, mass spectrum from these two types of bindings are very different

$(\bar{q}\bar{q})(qq)$   
tetraquark

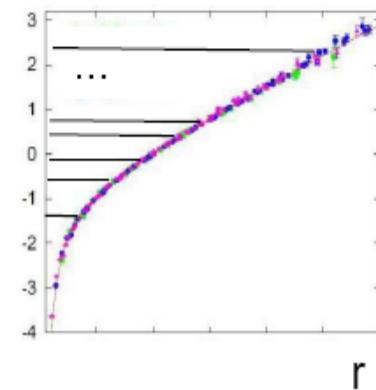


$(q\bar{q})-(q\bar{q})$   
meson-meson molecule



We don't know if either one exist ("exotic hadron")

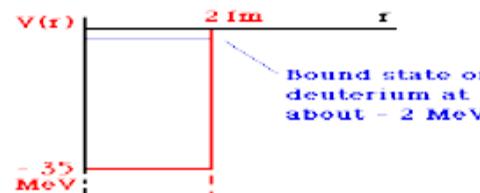
$V(r)$



Very rich mass spectrum expected!

However, states can be undetectable if extremely broad.

Typically expect only one state  $n=1, L=0$ .

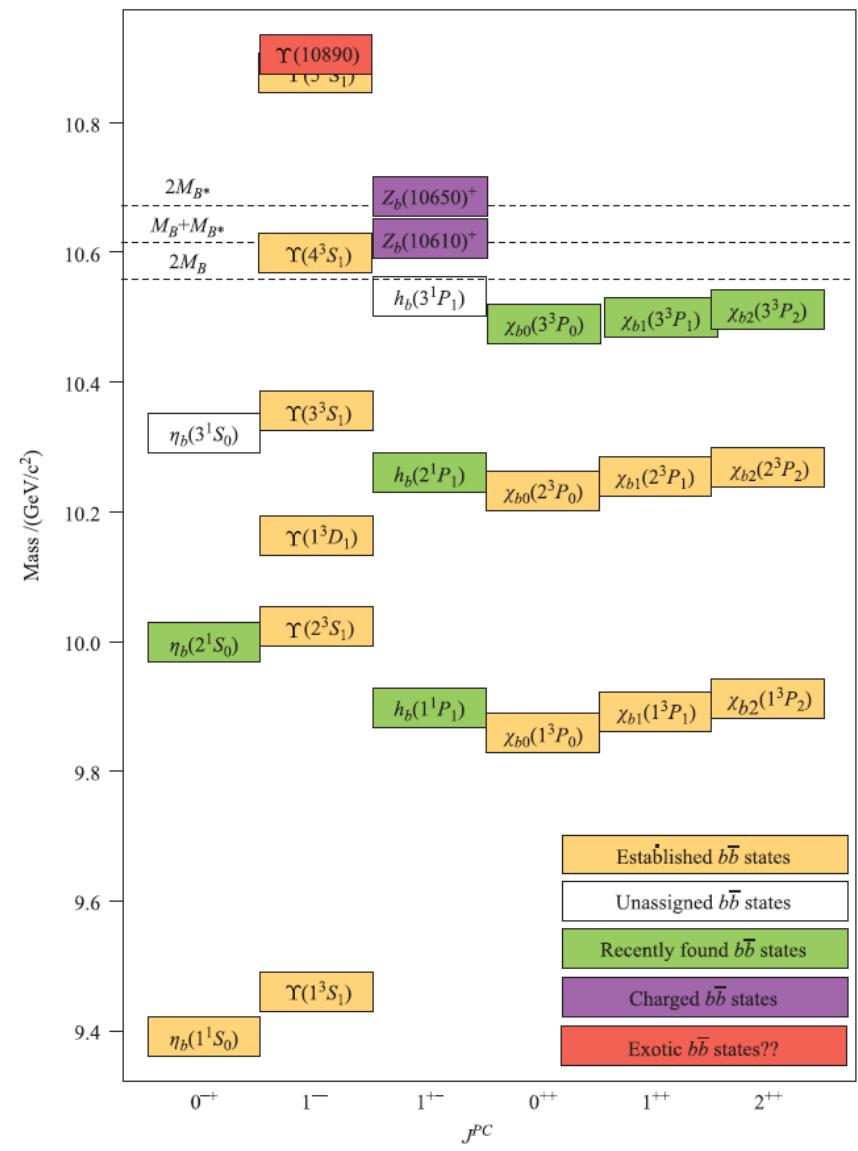
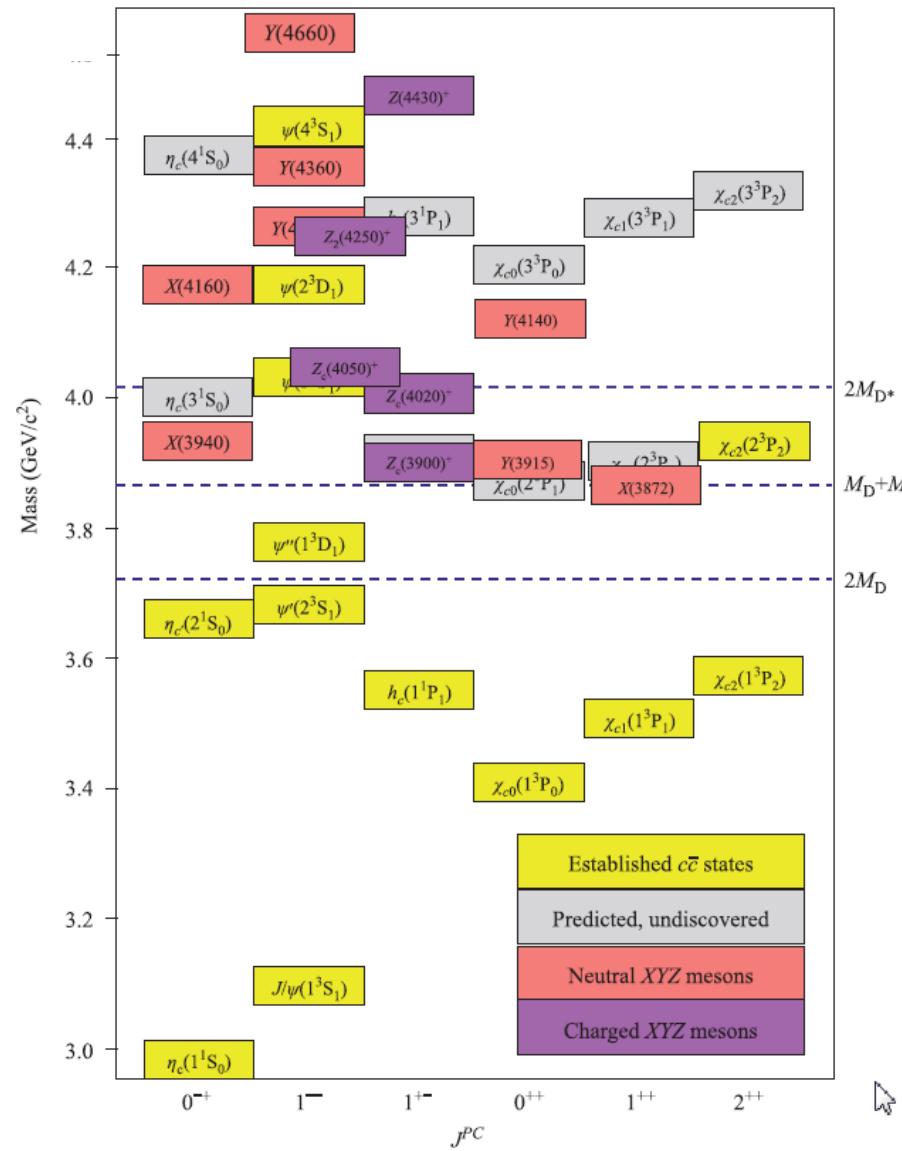


Fall apart prevented by spatial separation – long-lived states if below threshold.

Mass and  $J^P$  fairly constrained from the constituents.

# Very reach experimental field

From S. Olsen,  
arXiv:1411.7738



# Beginning of the XYZ saga

## The X(3872) & other charmonium puzzles

Stephen Lars Olsen  Institute for Basic Science Daejeon, KOREA

Workshop on Exotic Hadrons at 6<sup>th</sup> International Conference on New Frontiers in Physics, Kolymbari, Greece, Aug. 21-23, 2017

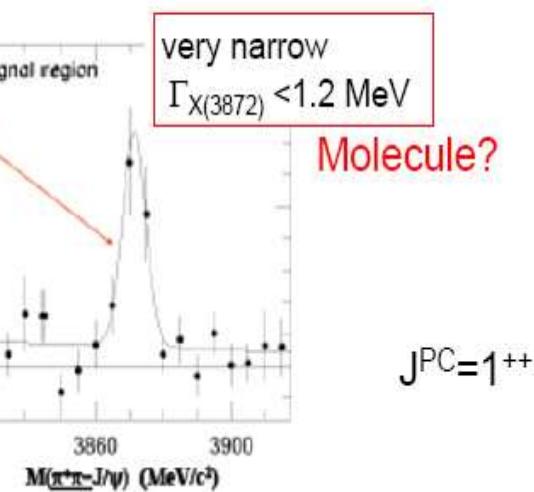
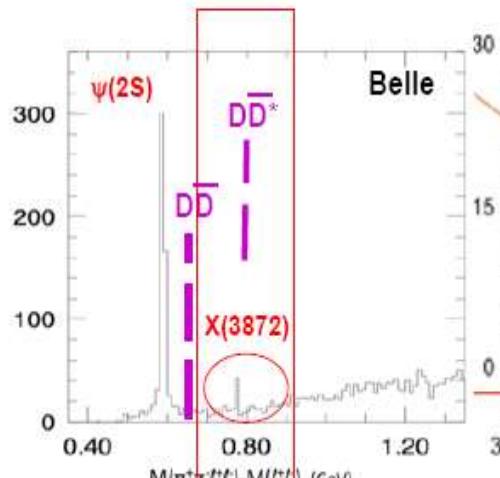
Phys.Rev.Lett. 91 (2003) 262001

The most cited Belle paper (1470 citations)

Observation of a narrow charmonium-like state in exclusive

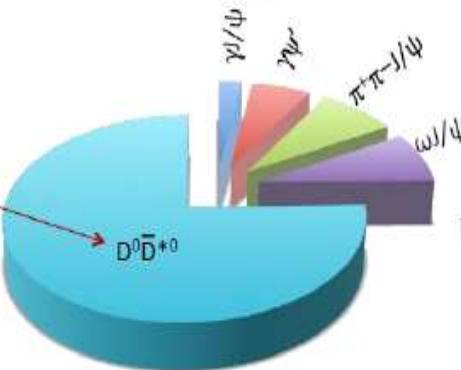
$B^\pm \rightarrow K^\pm \pi^+ \pi^- J/\psi$  decays

S.-K. Choi,<sup>5</sup> S. L. Olsen,<sup>6</sup> K. Abe,<sup>7</sup> T. Abe,<sup>7</sup> I. Adachi,<sup>7</sup> Byoung Sup Ahn,<sup>14</sup>  
H. Aihara,<sup>43</sup> K. Akai,<sup>7</sup> M. Akatsu,<sup>20</sup> M. Akemoto,<sup>7</sup> Y. Asano,<sup>48</sup> T. Aso,<sup>47</sup> V. Aulchenko,<sup>1</sup> ...



$J^{PC}=1^{++}$

strong  $D\bar{D}^*$  coupling



Preference for  $\gamma\psi'$  over  $\gamma J/\psi$  points to  $2^3P_1$  component

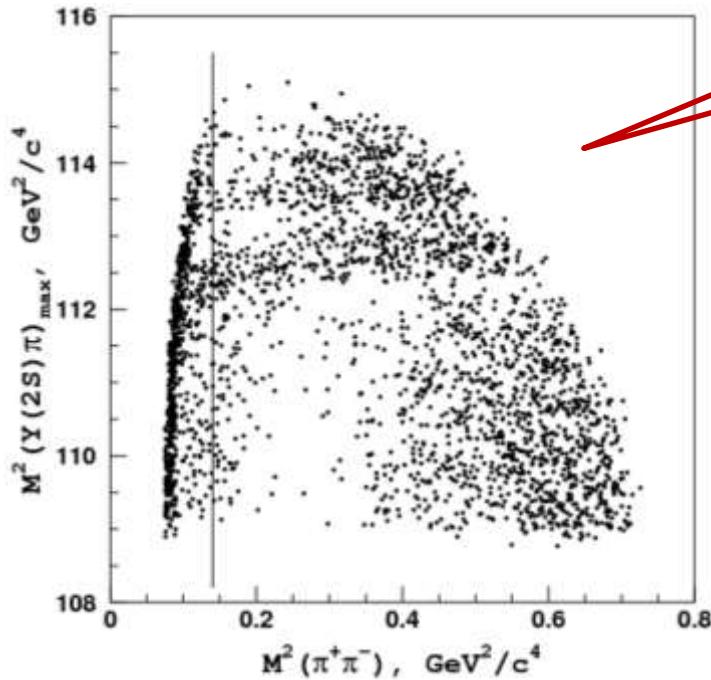
$\chi_{c1}'$ ?

Large isospin violation in these decays,

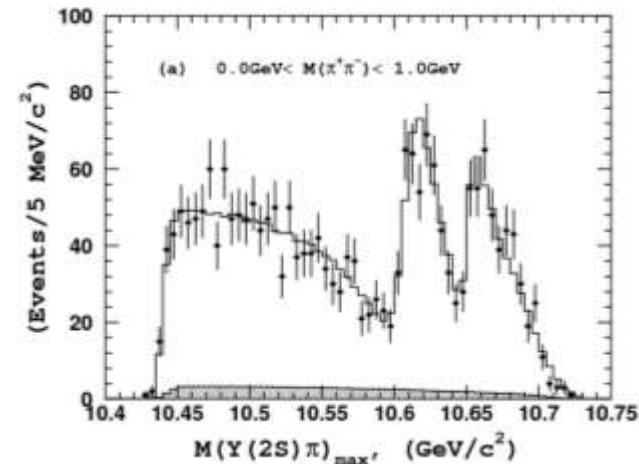
due to  
 $m(D^0)-m(D^-)$ ?  
Molecule?

Huge fall-apart mode from the resonance tail above the  $D^0 \bar{D}^{*0}$  threshold  
Molecule?

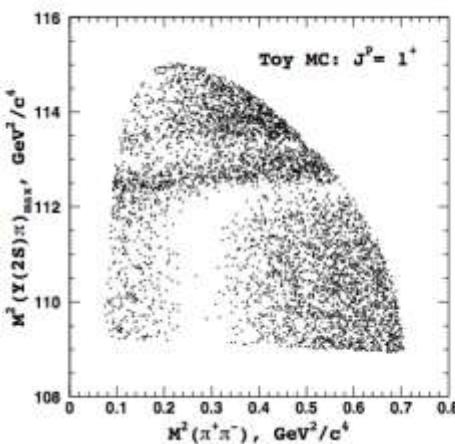
# $\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$ : $J^P$ Results



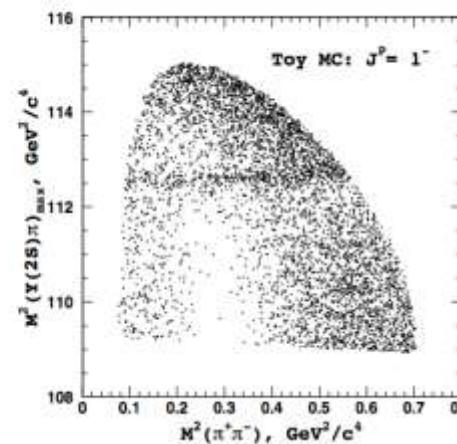
$\Upsilon(2S)\pi^+\pi^-$  Data



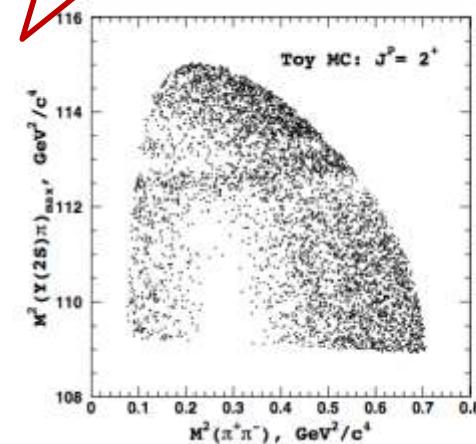
Toy MC with various  $J^P$



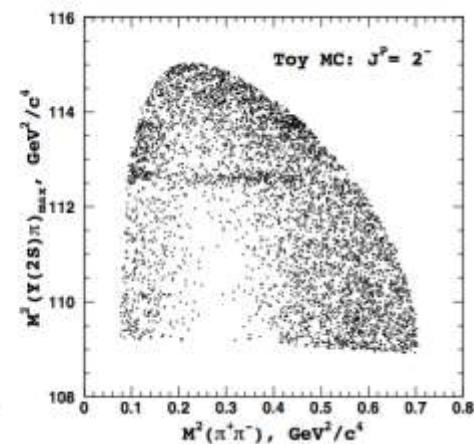
$J^P = 1^+$



$J^P = 1^-$

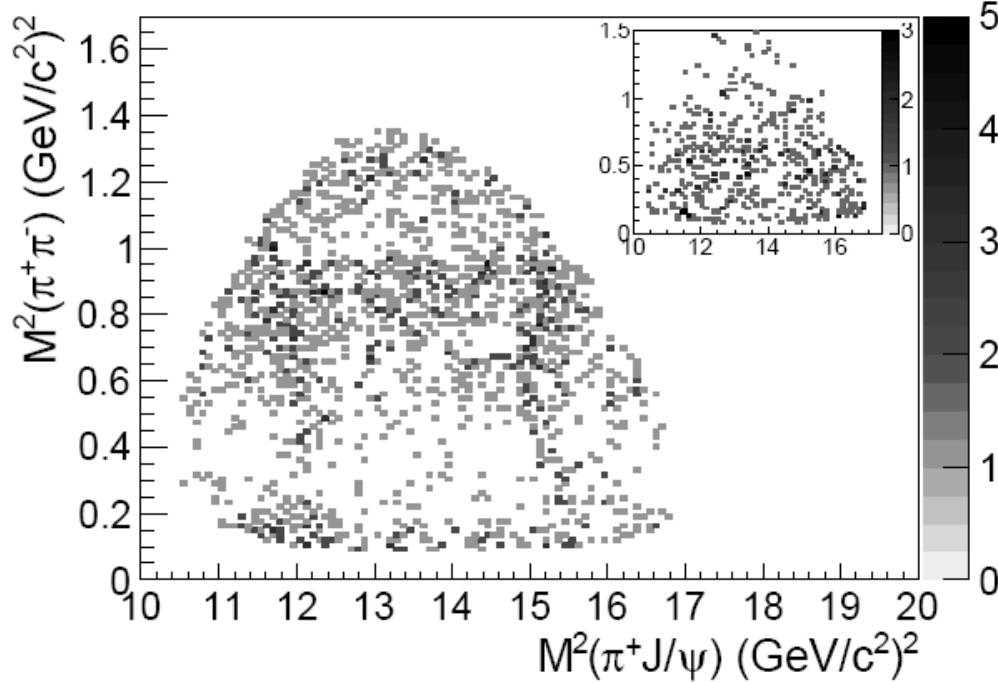


$J^P = 2^+$



$J^P = 2^-$

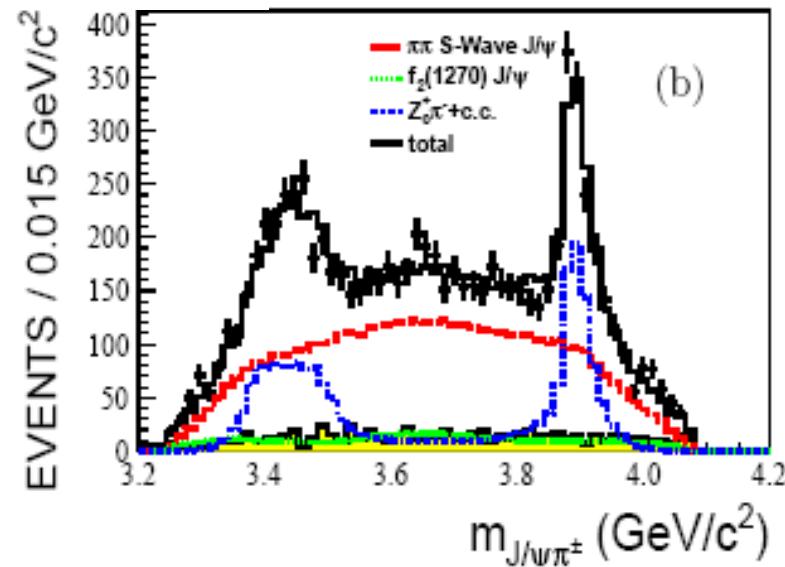
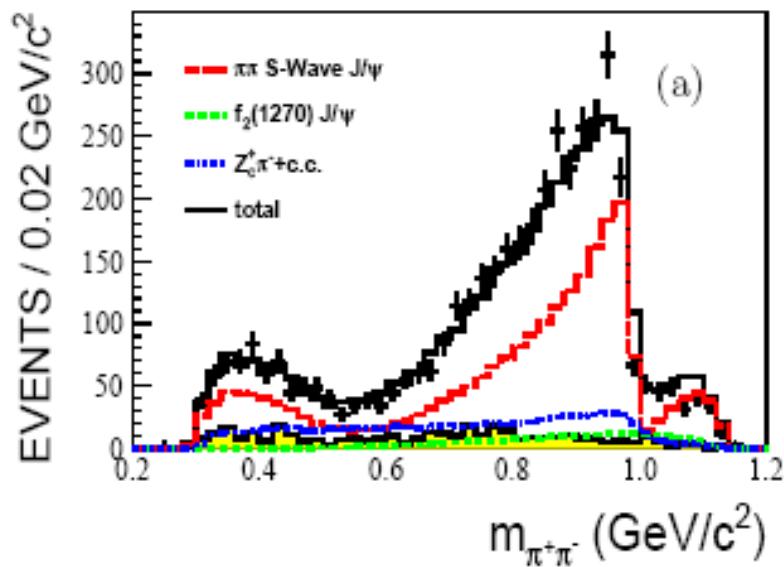
# BESIII $e^+e^- \rightarrow \pi^+\pi^- J/\psi$ at 4260 MeV

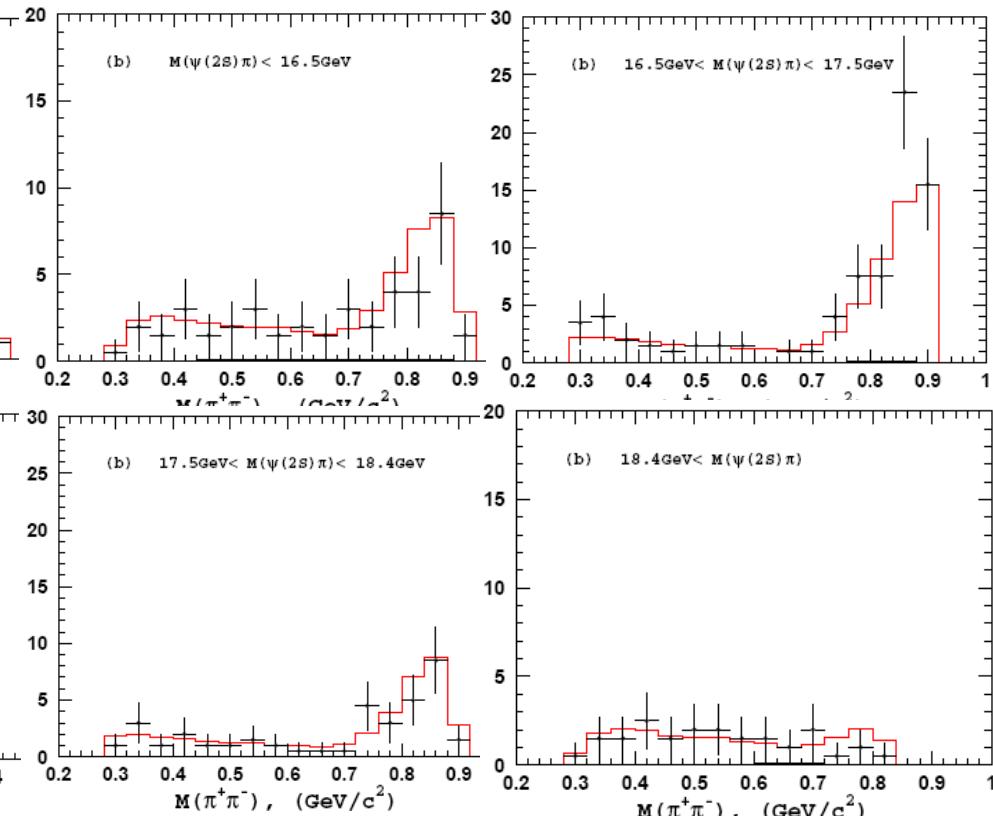
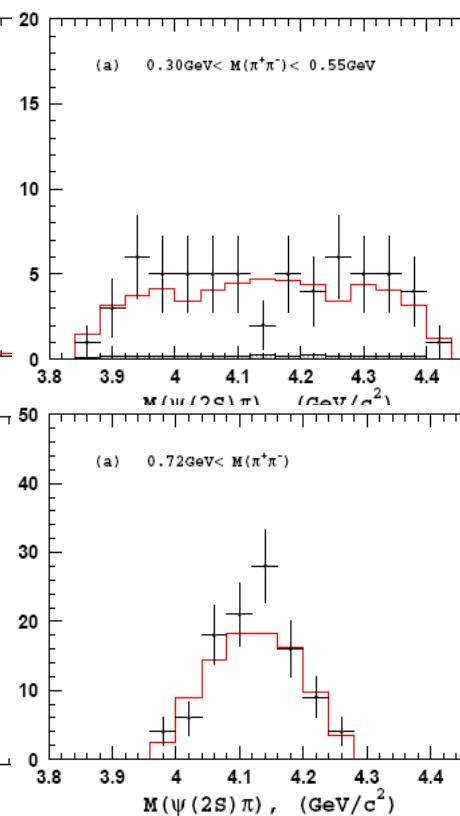
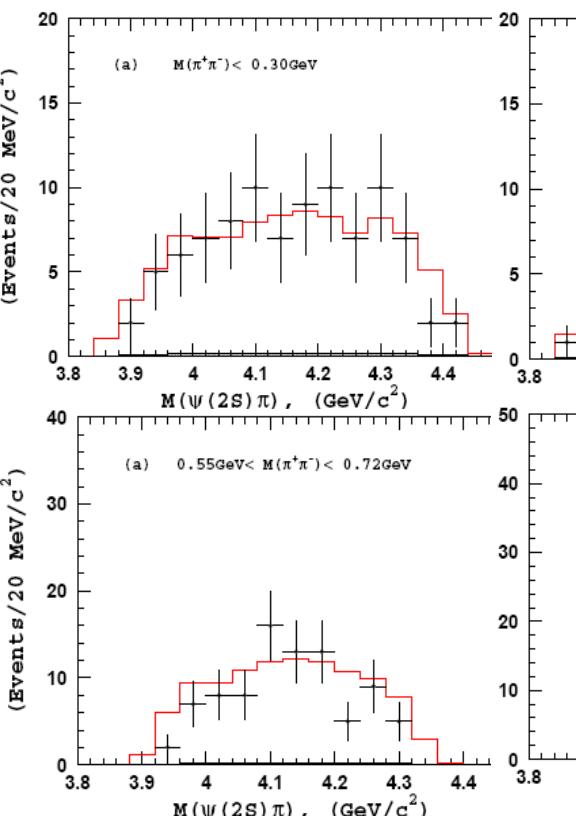
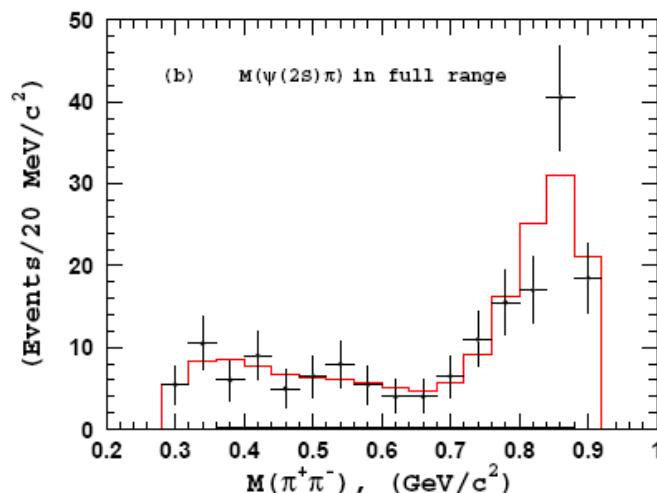
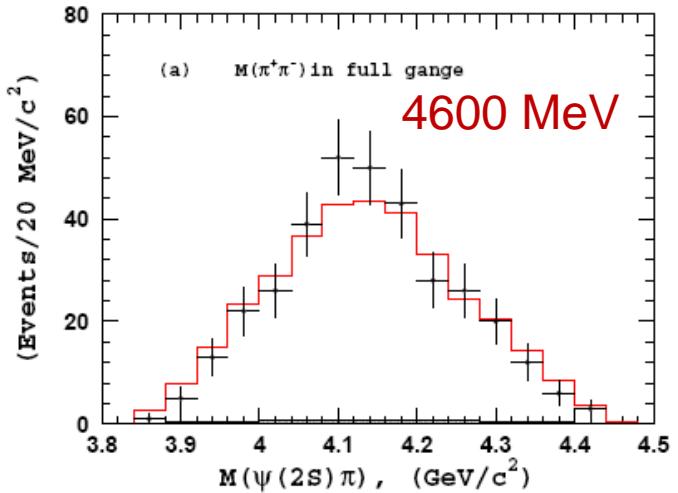


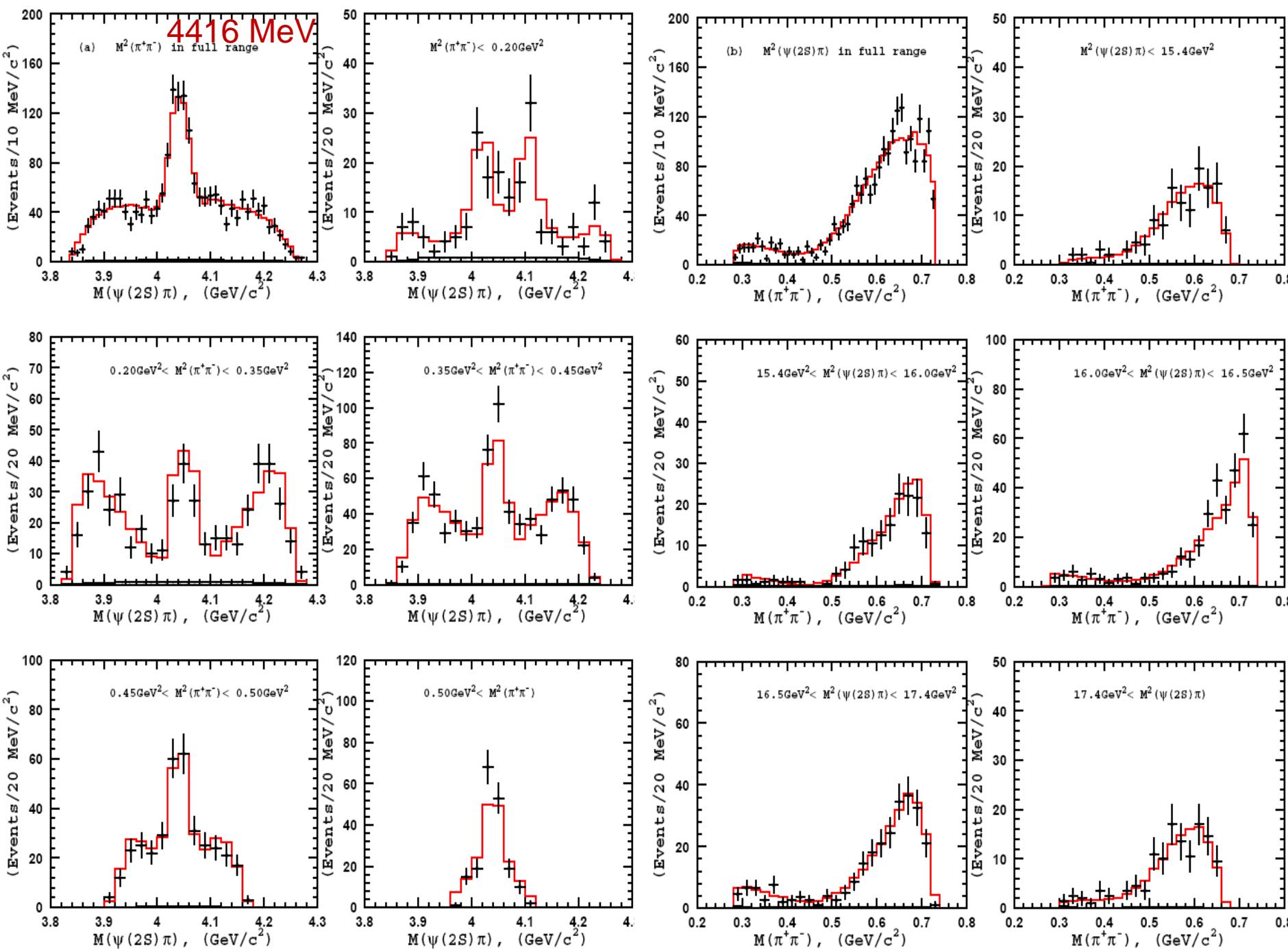
$$M_z = 3901.5 \pm 2.7 \pm 38.0 \text{ MeV}/c^2$$

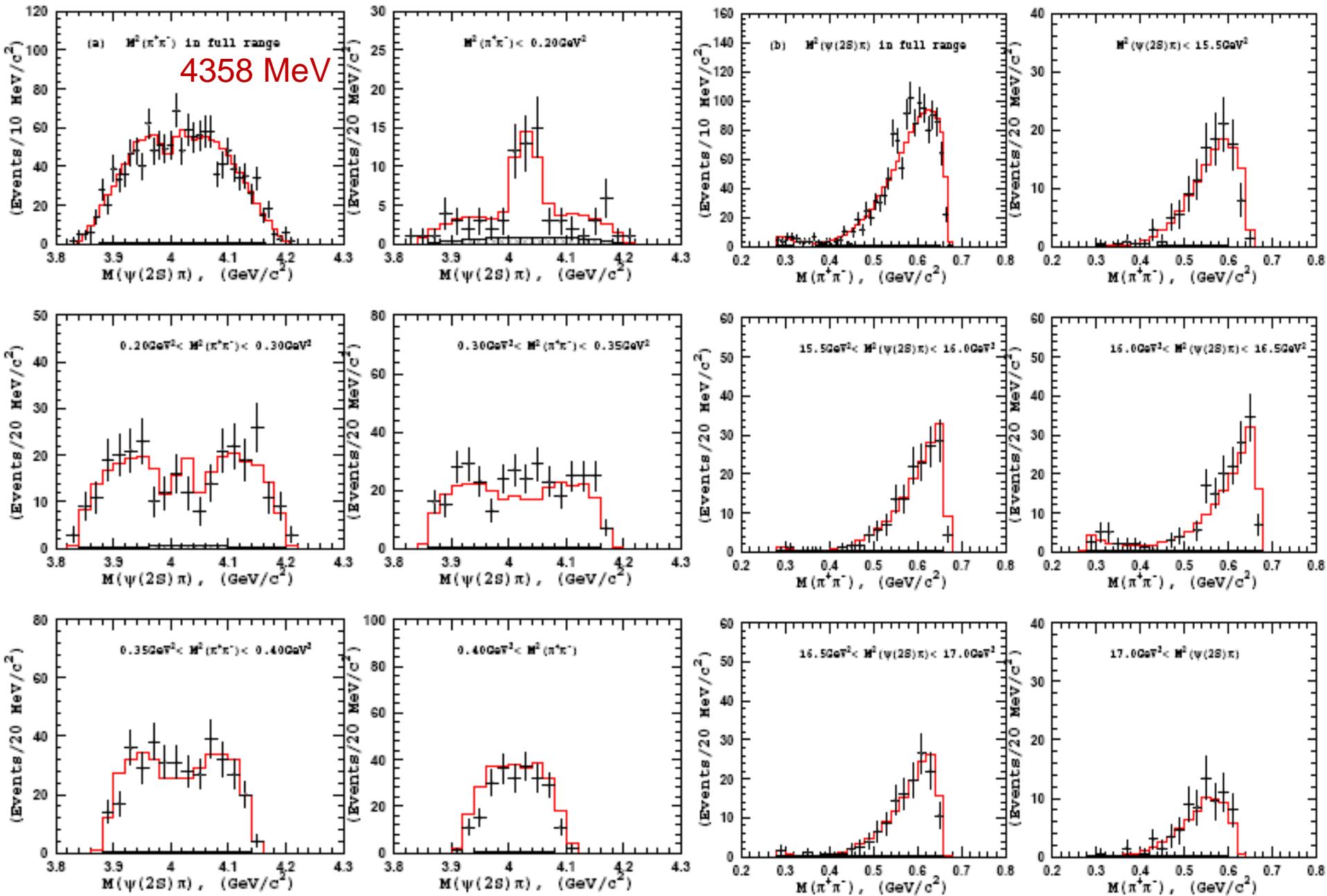
$$\Gamma_z = 51.8 \pm 4.6 \pm 36.0 \text{ MeV}$$

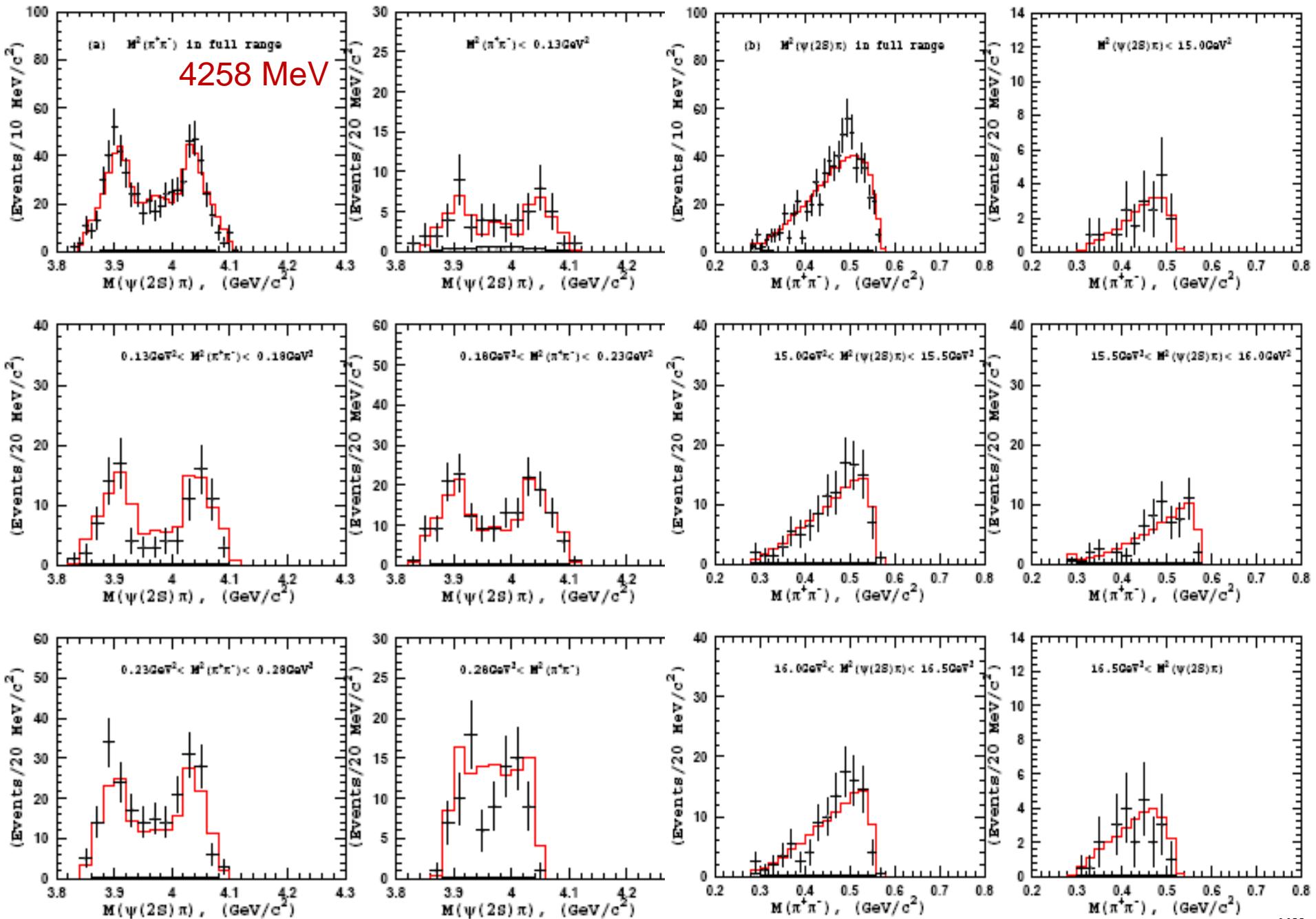
$$J^P = 1^+$$

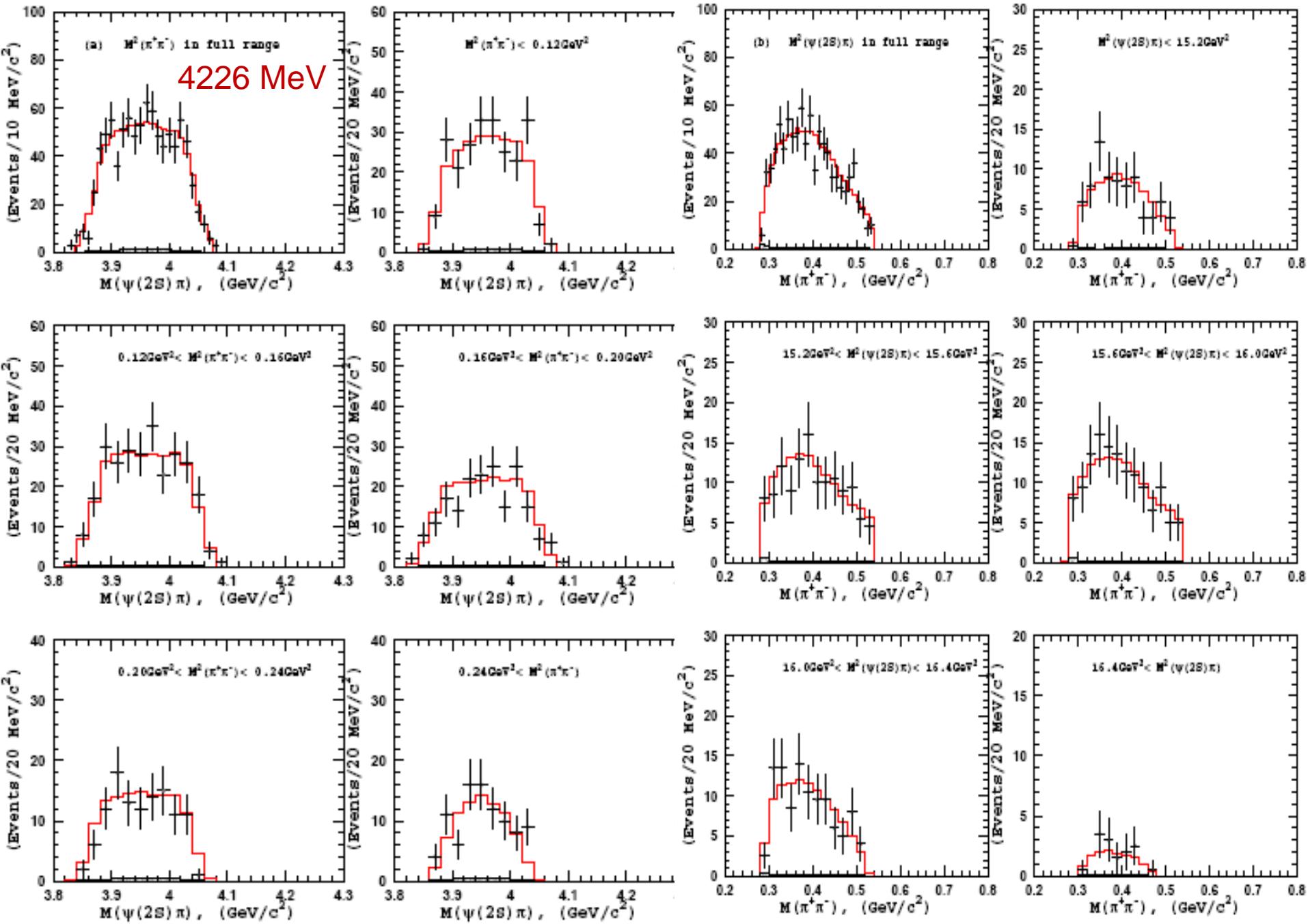






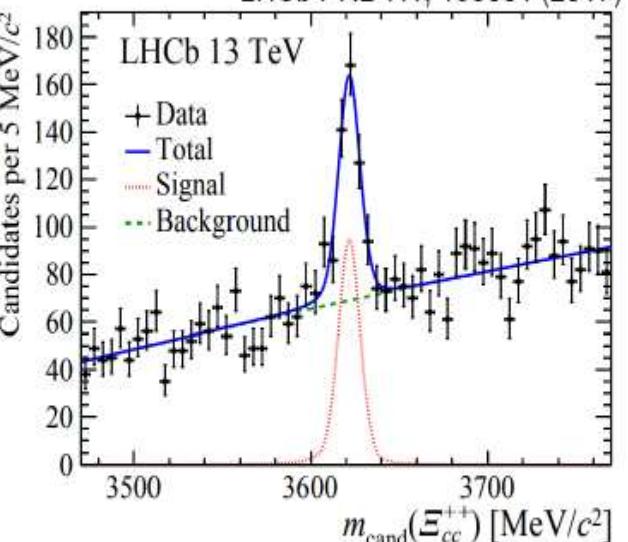






## Doubly heavy systems

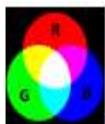
baryon



Karliner,Rosner PRD90,094007 (2014)

State	Quark content	$M(J = 1/2)$	$M(J = 3/2)$
$\Xi_{cc}^{(*)}$	$ccq$	$3627 \pm 12$	$3690 \pm 12$
$\Xi_{bc}^{(*)}$	$b[cq]$	$6914 \pm 13$	$6969 \pm 14$
$\Xi'_{bc}$	$b(cq)$	$6933 \pm 12$	...
$\Xi_{bb}^{(*)}$	$bbq$	$10162 \pm 12$	$10184 \pm 12$

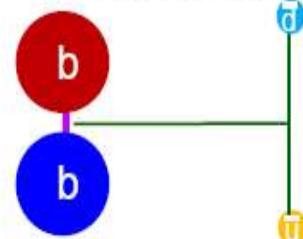
LHCb:  $3621 \pm 1$



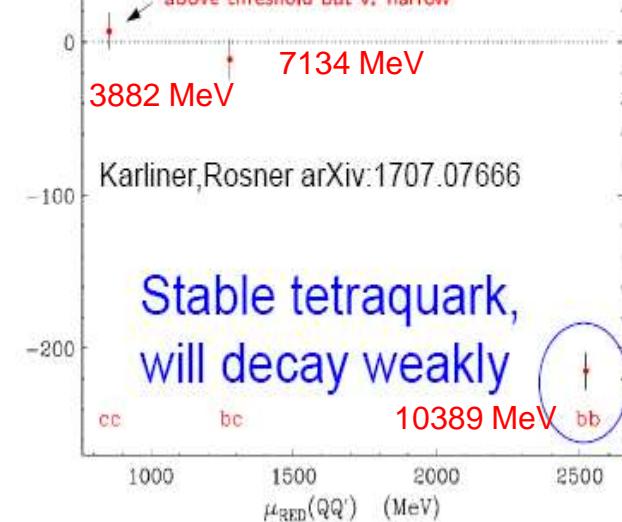
the same toolkit



tetraquark



The lightest  $1^+$  state

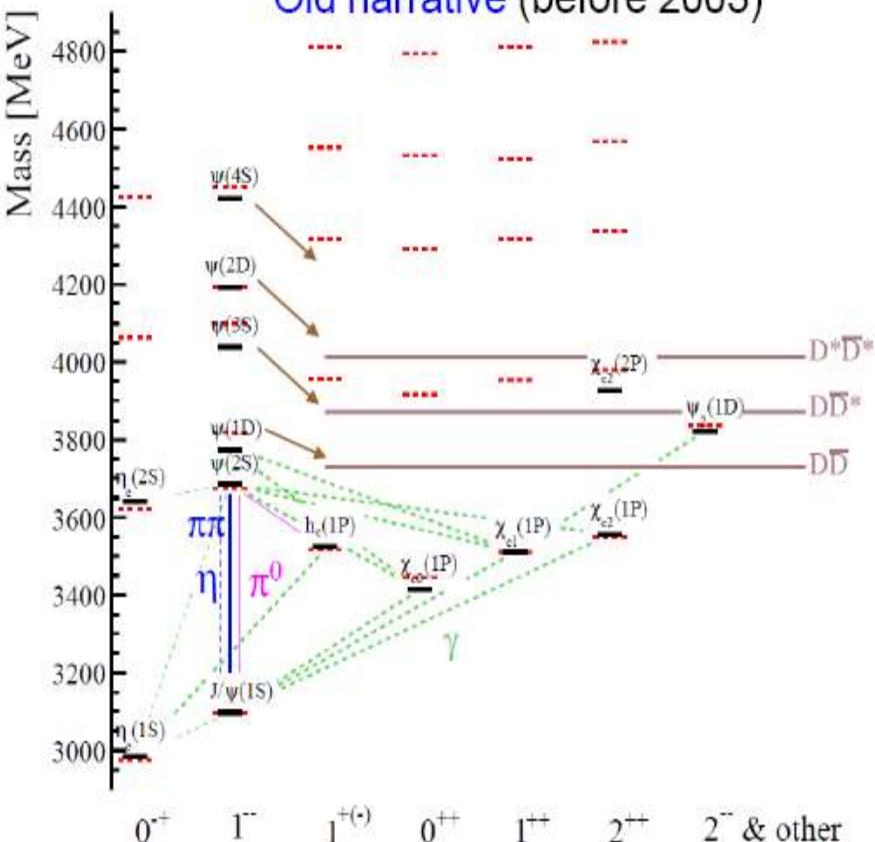


Consistent results predicted by  
LQCD:

Francis,Hudspith,Lewis,Maltman  
PRL 1118,142001 (2017)

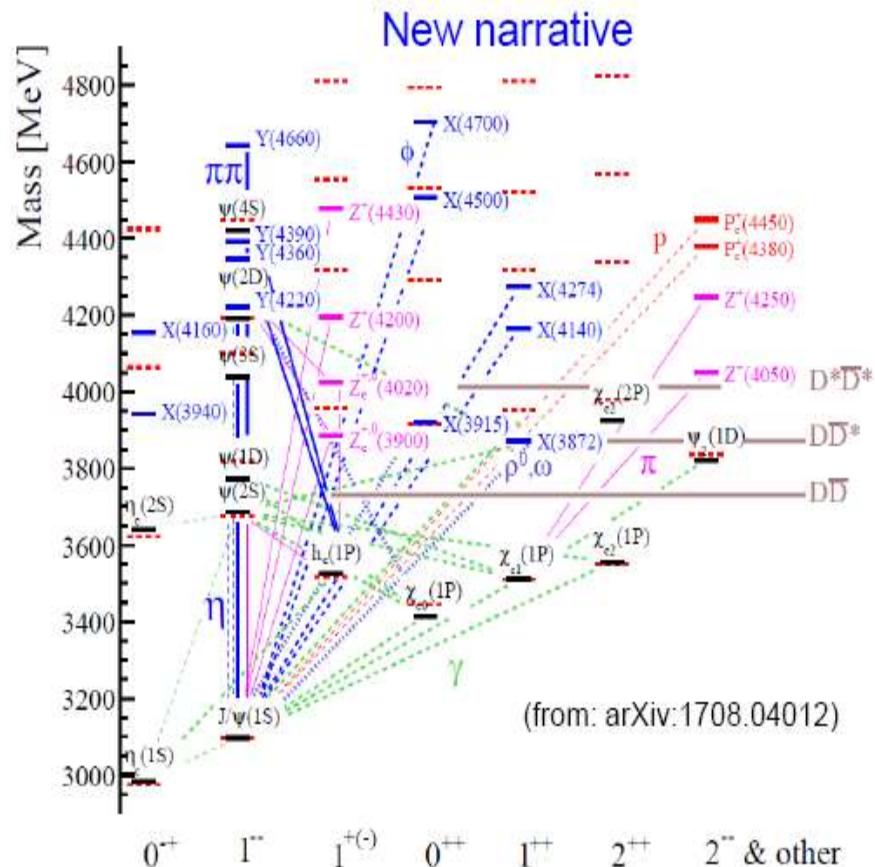
## Summary I

### Old narrative (before 2003)



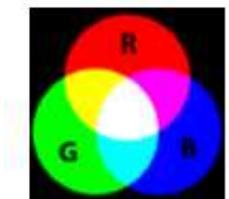
Mesons are  $(q\bar{q})$  bound states.

### New narrative



Mesons are **predominantly**  $(q\bar{q})$  bound states below the open flavor threshold. They are more complex structures above it, and we have not yet understood them.

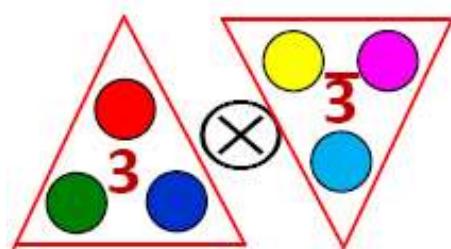
# Mesons from quarks & antiquarks in QCD



color triplet

color antitriplet

color singlet



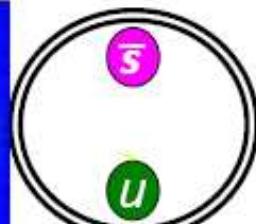
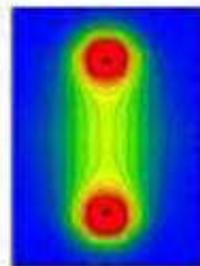
quark    antiquark

$q$

$\bar{q}$

( $q\bar{q}$ ) meson  
e.g.  $K^+$

Color flux tube  
stretched between  
quark and antiquark  
with attractive  
potential



attractive color force

color octet

$$\begin{pmatrix} 1 \\ \sqrt{2} \\ 1 \\ \sqrt{2} \end{pmatrix} \begin{matrix} \text{Red} \\ \text{Yellow} \\ \text{Blue} \\ \text{Cyan} \end{matrix}$$

$$\begin{pmatrix} i \\ \sqrt{2} \\ i \\ \sqrt{2} \end{pmatrix} \begin{matrix} \text{Red} \\ \text{Yellow} \\ \text{Blue} \\ \text{Cyan} \end{matrix}$$

$$\begin{pmatrix} 1 \\ \sqrt{2} \\ -2 \\ \sqrt{6} \end{pmatrix} \begin{matrix} \text{Blue} \\ \text{Magenta} \\ \text{Green} \\ \text{Yellow} \end{matrix}$$

$$\begin{pmatrix} 1 \\ \sqrt{2} \\ -1 \\ \sqrt{2} \end{pmatrix} \begin{matrix} \text{Green} \\ \text{Magenta} \\ \text{Blue} \\ \text{Yellow} \end{matrix}$$

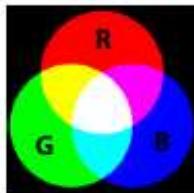
$$\begin{pmatrix} 1 \\ \sqrt{2} \\ 1 \\ \sqrt{2} \end{pmatrix} \begin{matrix} \text{Green} \\ \text{Blue} \\ \text{Red} \\ \text{Magenta} \end{matrix}$$

$$\begin{pmatrix} i \\ \sqrt{2} \\ i \\ \sqrt{2} \end{pmatrix} \begin{matrix} \text{Green} \\ \text{Blue} \\ \text{Red} \\ \text{Magenta} \end{matrix}$$

repulsive color force

quarks will pull apart in any  
octet configuration

gluons happen to belong  
to the color octet

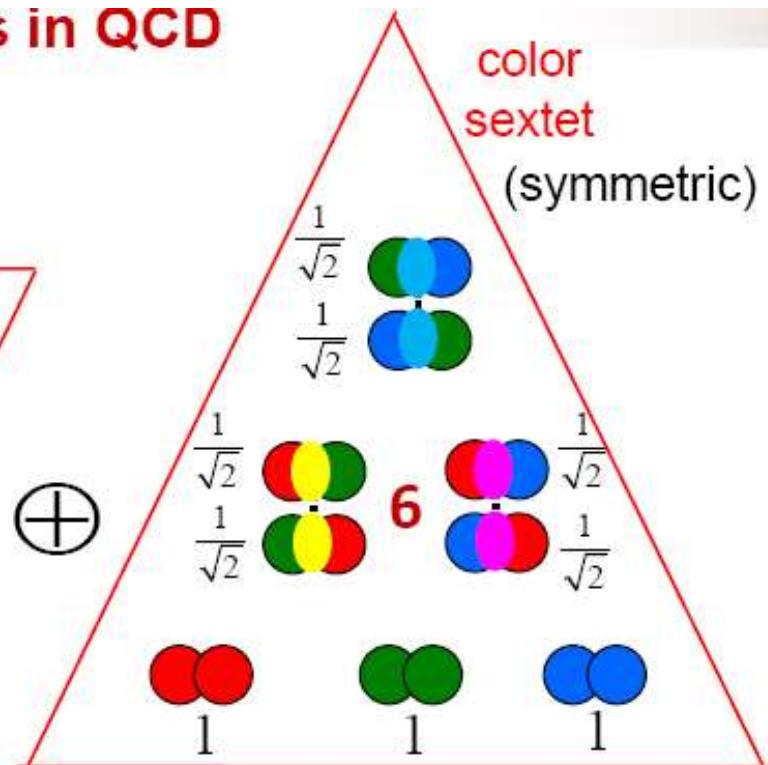
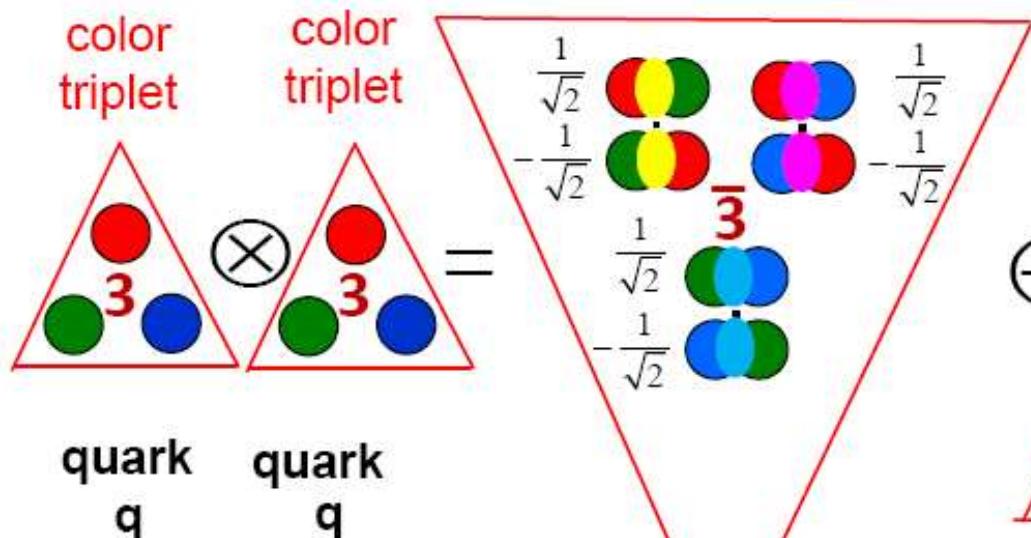


## (Colored) diquarks in QCD

(antisymmetric)

color

antitriplet



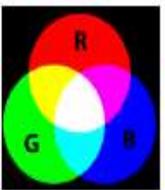
Color flux tube  
stretched between  
the quarks and  
extending to other  
color partners



(qq) diquark



Not a particle, just a  
building block in  
QCD

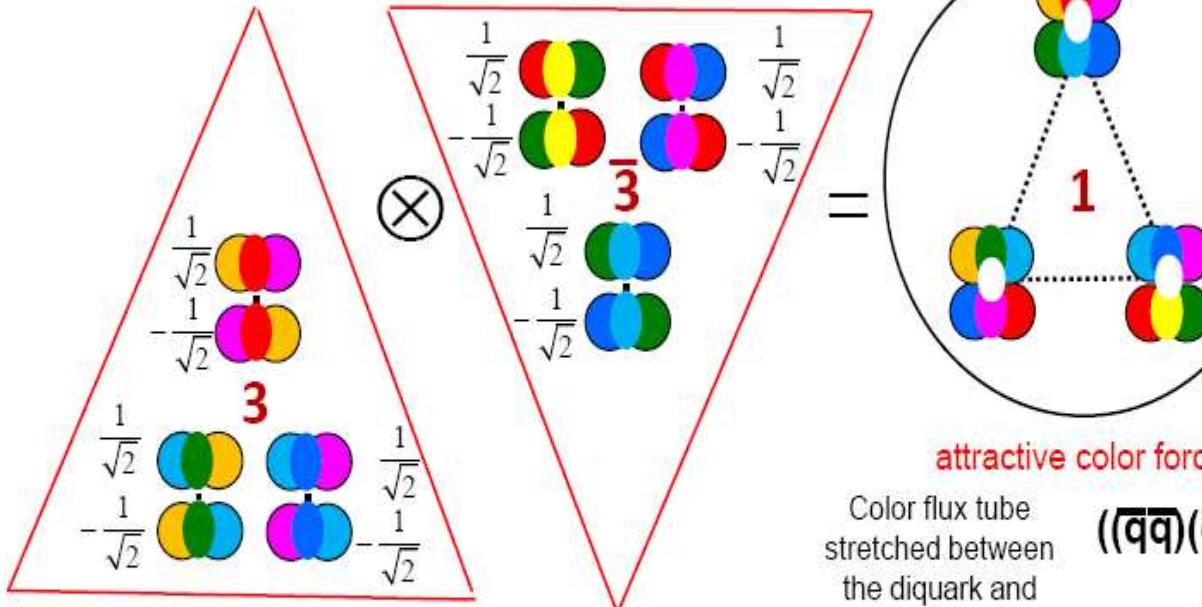


## Diaquarks can make tetraquarks!

color triplet

color antitriplet

color singlet



attractive color force

$(\bar{q}q)$  diantiquark

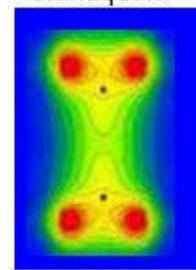
$\uparrow$

attractive color force

$(qq)$  diquark

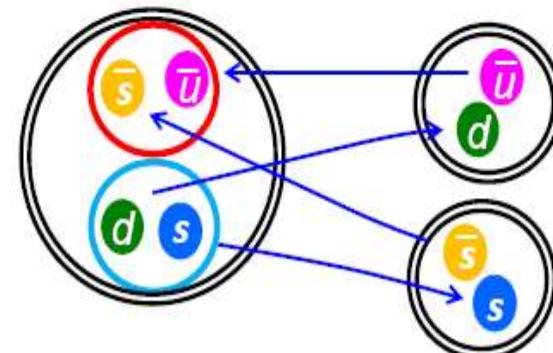
$\uparrow$

Color flux tube  
stretched between  
the diquark and  
diantiquark

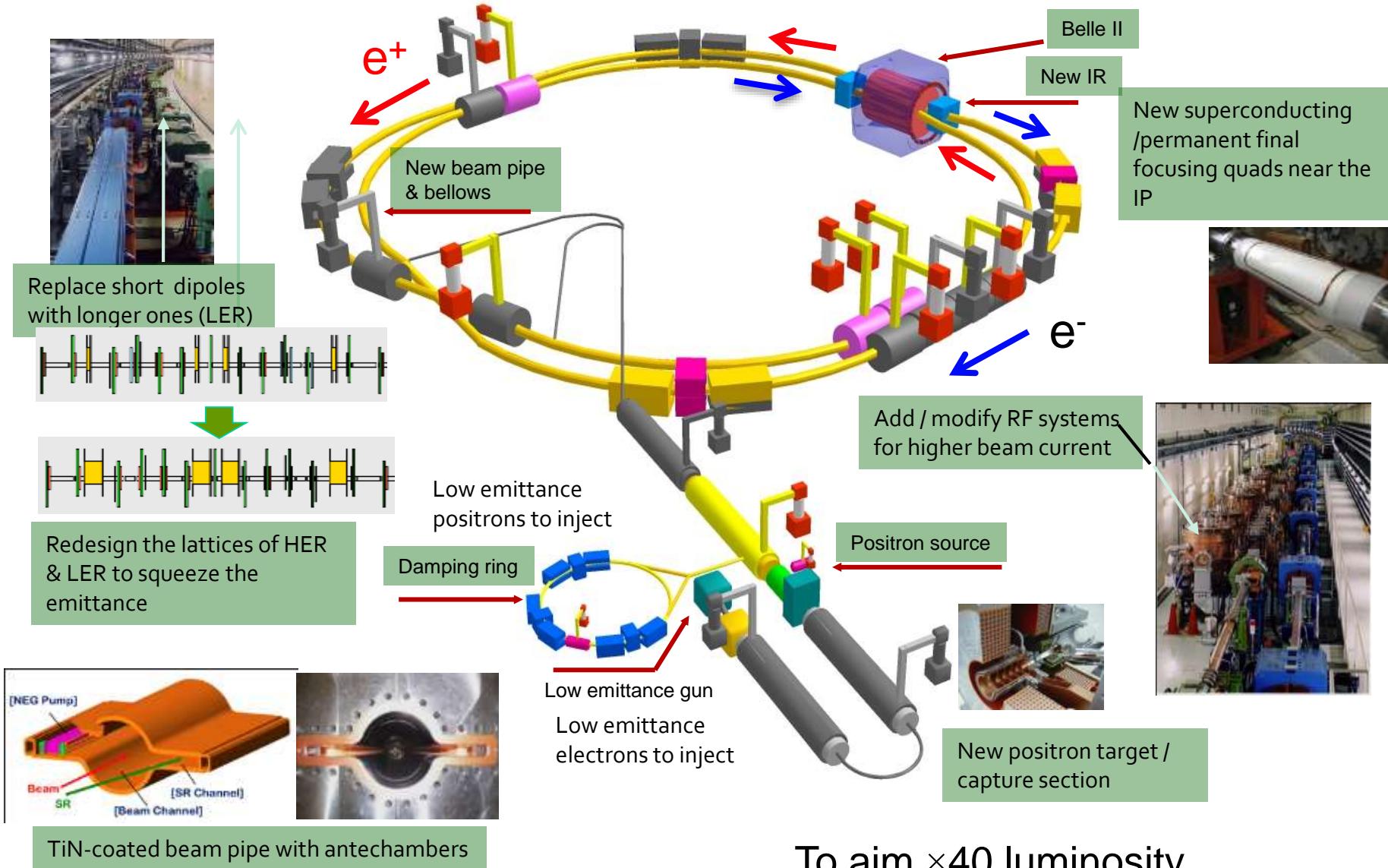


However, it is not clear if an efficient mechanisms to suppress the fall-apart mode to two mesons exists, especially when all quarks are light.

$(\bar{q}q)(qq)$  tetraquark

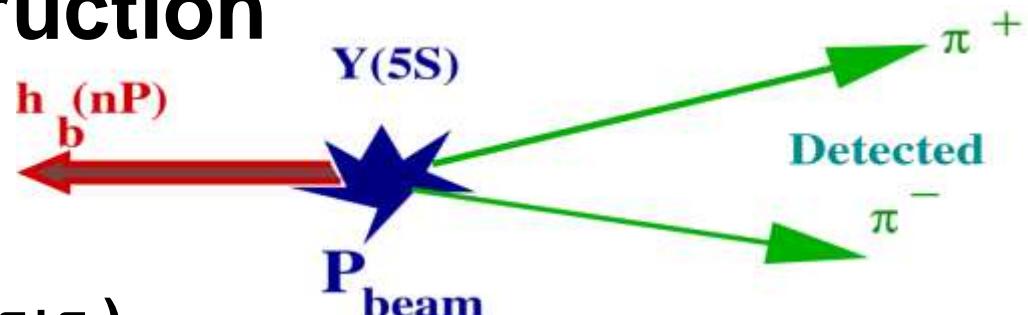


# SuperKEKB



# $h_b$ reconstruction

Missing mass to  $\pi\pi$  system

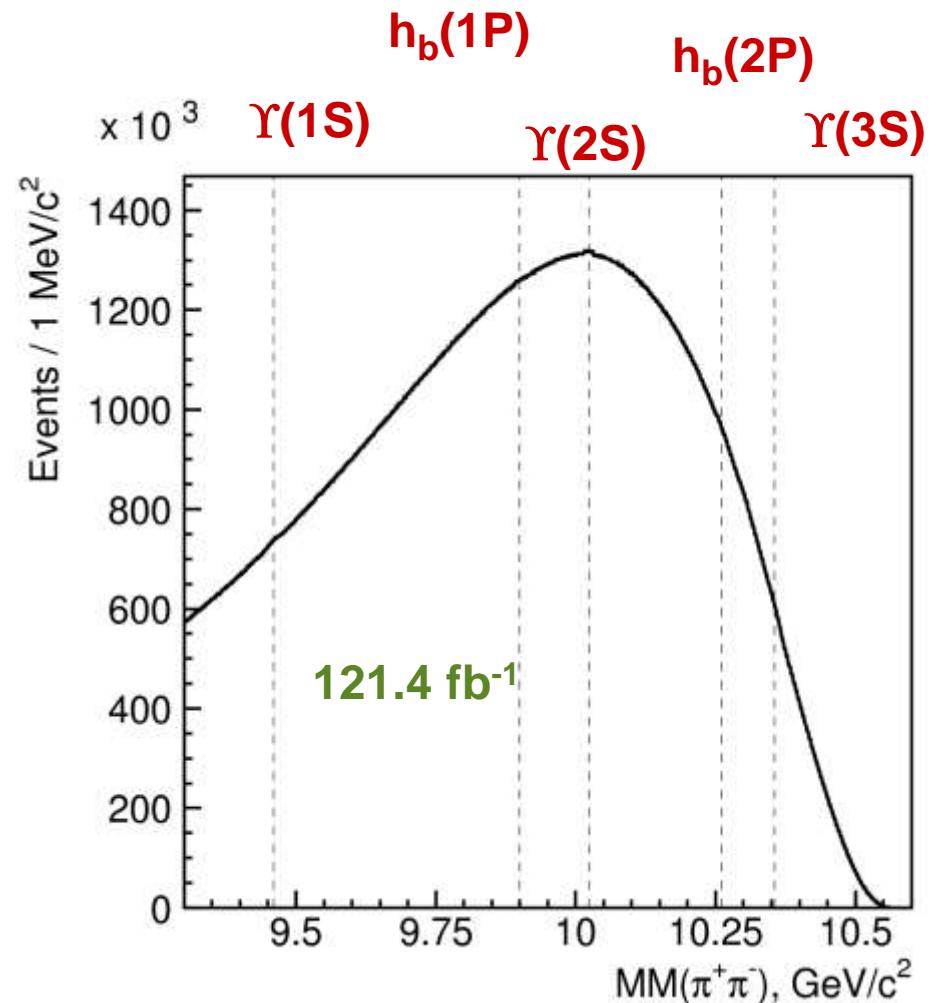


$$M_{hb(nP)} = \sqrt{(P_{Y(5S)} - P_{\pi^+\pi^-})^2} \equiv MM(\pi^+\pi^-)$$

**Simple selection :**  
 $\pi^+\pi^-$  : good quality, positively identified

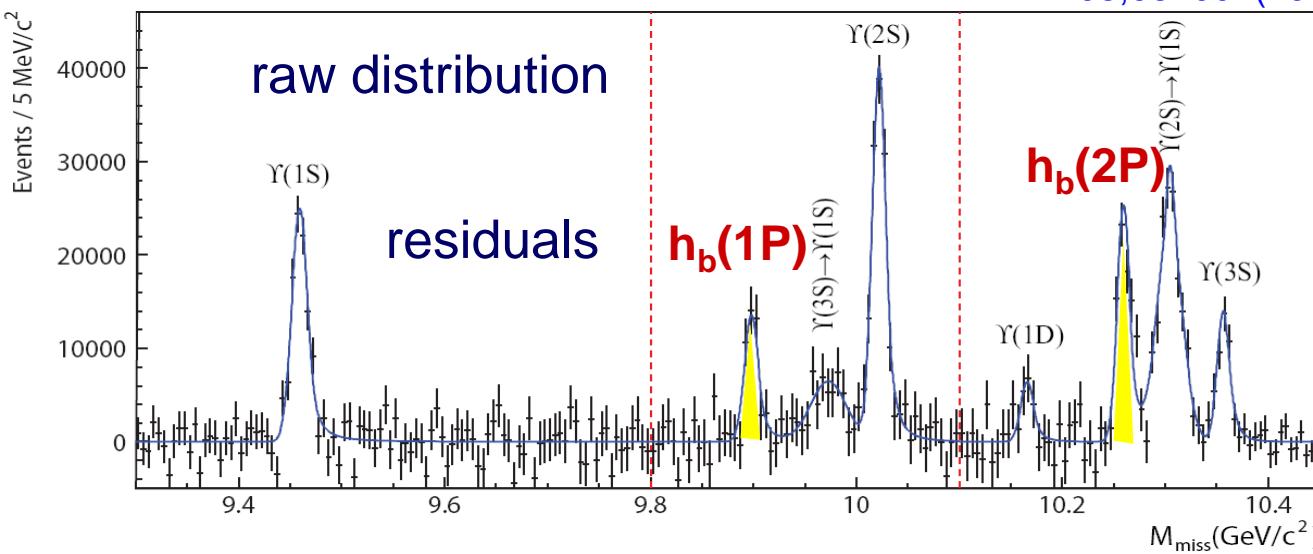
Suppression of continuum events  
FW R2<0.3

⇒ Search for  $h_b(nP)$  peaks  
in  $MM(\pi^+\pi^-)$  spectrum



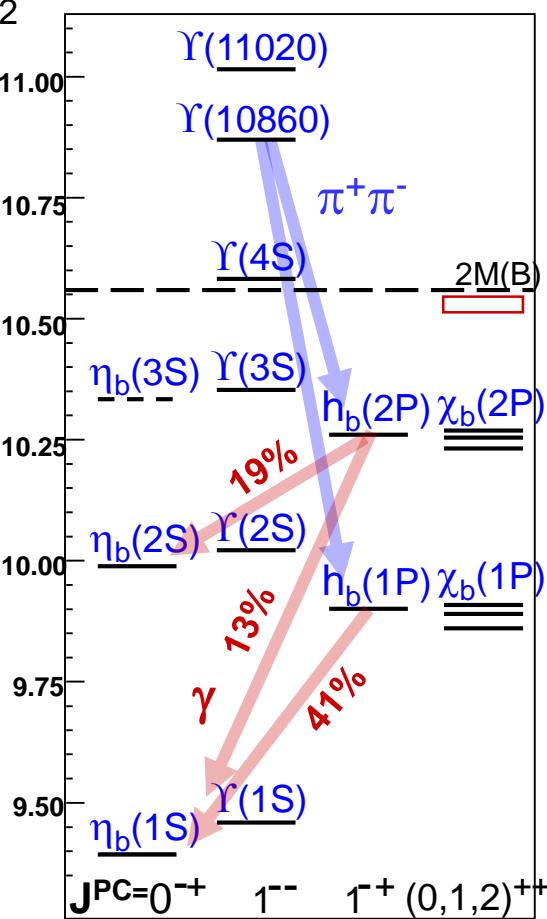
# Observation of $h_b(1P,2P)$

$e^+e^- \rightarrow \gamma(5S) \rightarrow h_b(nP) \pi^+\pi^-$  reconstructed, use  $M_{miss}(\pi^+\pi^-)$



$$\sqrt{(P_{e^+e^-} - P_{\pi^+\pi^-})^2}$$

PRL108,032001(2012)



$\Delta M_{HF}(1P) = +0.8 \pm 1.1 \text{ MeV}$  consistent with zero,  
 $\Delta M_{HF}(2P) = +0.5 \pm 1.2 \text{ MeV}$  as expected

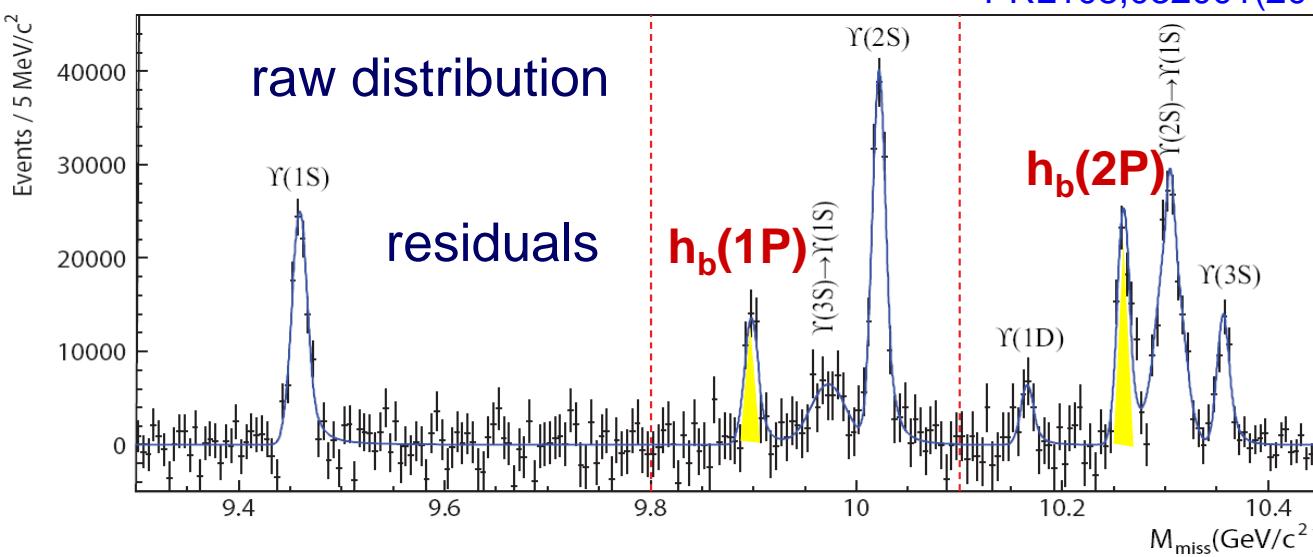
Large  $h_b(1,2P)$  production rates

c.f. CLEO  $e^+e^- \rightarrow \psi(4170) \rightarrow h_c \pi^+\pi^-$

$h_b(nP)$  decays are a source of  $\eta_b(mS)$

# Observation of $h_b(1P,2P)$

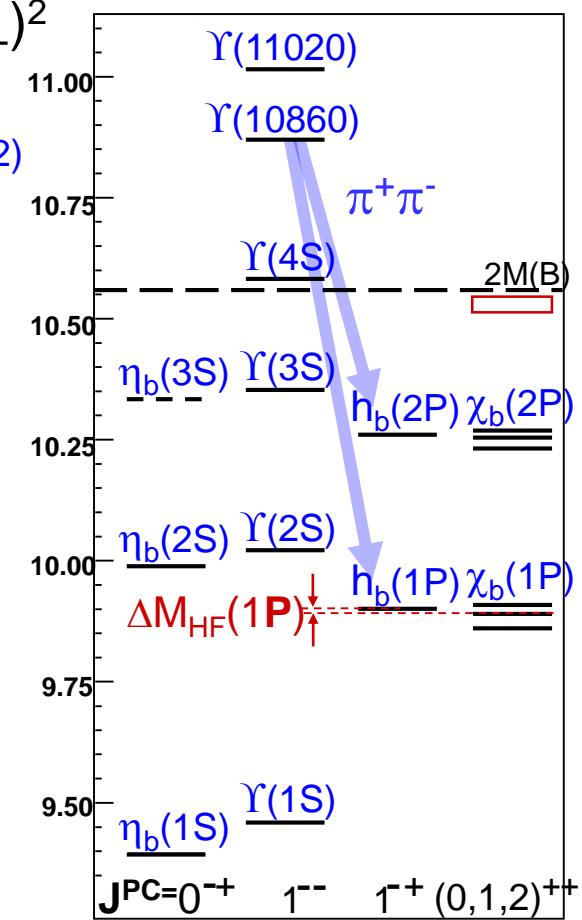
$e^+e^- \rightarrow \gamma(5S) \rightarrow X \pi^+\pi^-$  reconstructed, use  $M_{\text{miss}}(\pi^+\pi^-)$



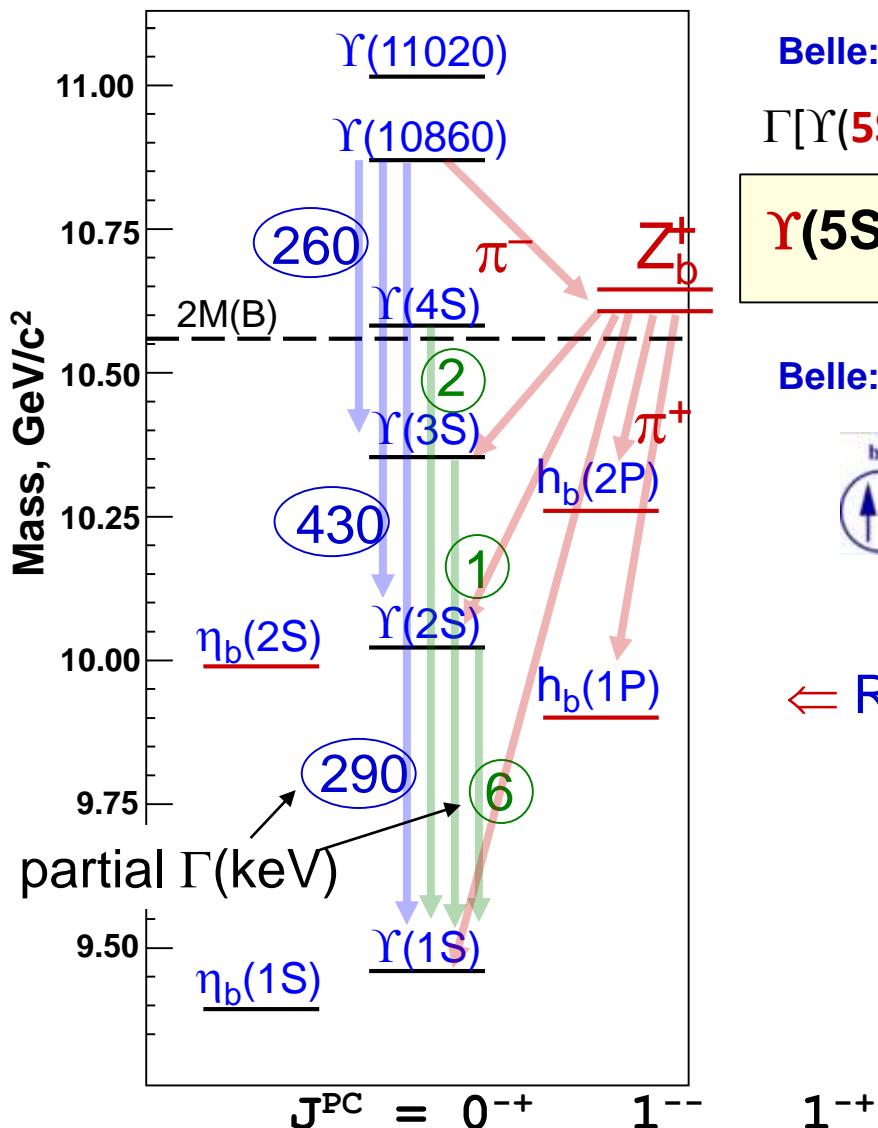
$\Delta M_{\text{HF}}(1P) = +0.8 \pm 1.1 \text{ MeV}$  consistent with zero,  
 $\Delta M_{\text{HF}}(2P) = +0.5 \pm 1.2 \text{ MeV}$  as expected

Large  $h_b(1,2P)$  production rates

c.f. CLEO  $e^+e^- \rightarrow \psi(4170) \rightarrow h_c \pi^+\pi^-$



# Anomalies in $\Upsilon(5S) \rightarrow (\bar{b}\bar{b})\pi^+\pi^-$ transitions



Belle: PRL100, 112001 (2008)  $\sim 100$

$\Gamma[\Upsilon(5S) \rightarrow \Upsilon(1,2,3S)\pi^+\pi^-] \gg \Gamma[\Upsilon(4,3,2S) \rightarrow \Upsilon(1S)\pi^+\pi^-]$

$\Upsilon(5S) \rightarrow h_b(1,2P)\pi^+\pi^-$  are **not suppressed**

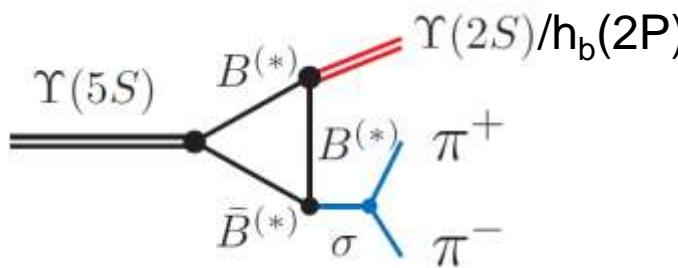
Belle: PRL108, 032001 (2012)



expect suppression  $\sim \Lambda_{\text{QCD}}/m_b$

~~Heavy Quark Symmetry~~

↔ Rescattering of on-shell  $B^{(*)}\bar{B}^{(*)}$  ?



$h_b$  production mechanism?  $\Upsilon(5S) \rightarrow h_b(1,2P)\pi^+\pi^-$  are **not suppressed** due to  $Z_b$  intermediate states! But it's not enough for  $\Upsilon(nS)\pi^+\pi^-$ .

Y(?S)

$$\left| Z_b \right\rangle = \frac{1}{\sqrt{2}} \mathbf{0}_{bb}^- \otimes \mathbf{1}_{Qq}^- - \frac{1}{\sqrt{2}} \mathbf{1}_{bb}^- \otimes \mathbf{0}_{Qq}^-$$

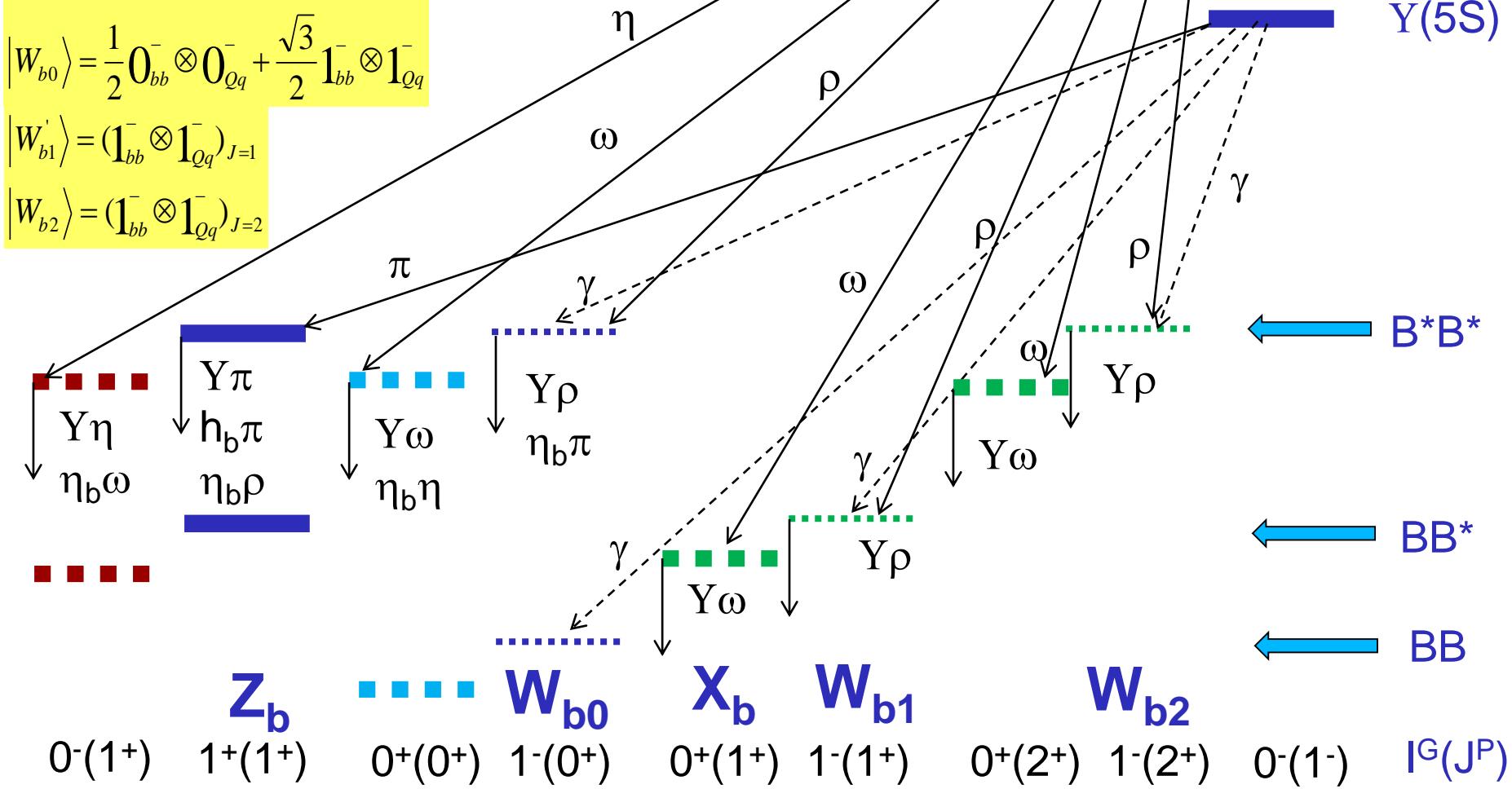
$$\left| Z_b \right\rangle = \frac{1}{\sqrt{2}} \mathbf{0}_{bb}^- \otimes \mathbf{1}_{Qq}^- + \frac{1}{\sqrt{2}} \mathbf{1}_{bb}^- \otimes \mathbf{0}_{Qq}^-$$

$$\left| W_{b0} \right\rangle = \frac{\sqrt{3}}{2} \mathbf{0}_{bb}^- \otimes \mathbf{0}_{Qq}^- - \frac{1}{2} \mathbf{1}_{bb}^- \otimes \mathbf{1}_{Qq}^-$$

$$\left| W_{b0} \right\rangle = \frac{1}{2} \mathbf{0}_{bb}^- \otimes \mathbf{0}_{Qq}^- + \frac{\sqrt{3}}{2} \mathbf{1}_{bb}^- \otimes \mathbf{1}_{Qq}^-$$

$$\left| W_{b1} \right\rangle = (\mathbf{1}_{bb}^- \otimes \mathbf{1}_{Qq}^-)_{J=1}$$

$$\left| W_{b2} \right\rangle = (\mathbf{1}_{bb}^- \otimes \mathbf{1}_{Qq}^-)_{J=2}$$



# Tetraquark?

M ~ 10.2 – 10.3 GeV

Ying Cui, Xiao-lin Chen, Wei-Zhen Deng,  
Shi-Lin Zhu, High Energy Phys.Nucl.Phys.31:7-13, 2007  
(hep-ph/0607226)

M ~ 10.5 – 10.8 GeV

Tao Guo, Lu Cao, Ming-Zhen Zhou, Hong Chen, (1106.2284)

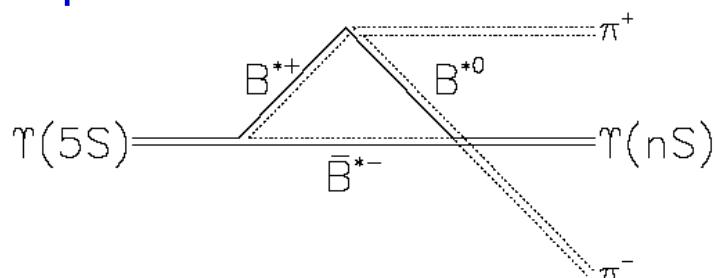
M ~ 9.4, 11 GeV

M.Karliner, H.Lipkin, (0802.0649)

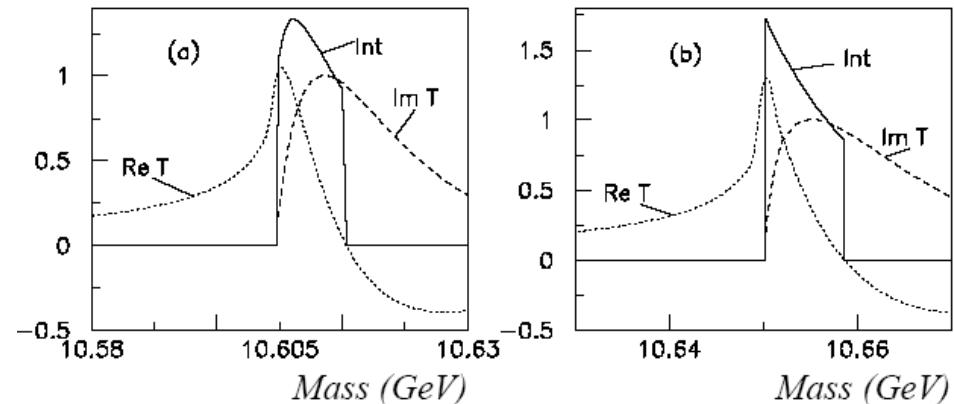
# Cusp?

D.Bugg Europhys.Lett.96 (2011) (arXiv:1105.5492)

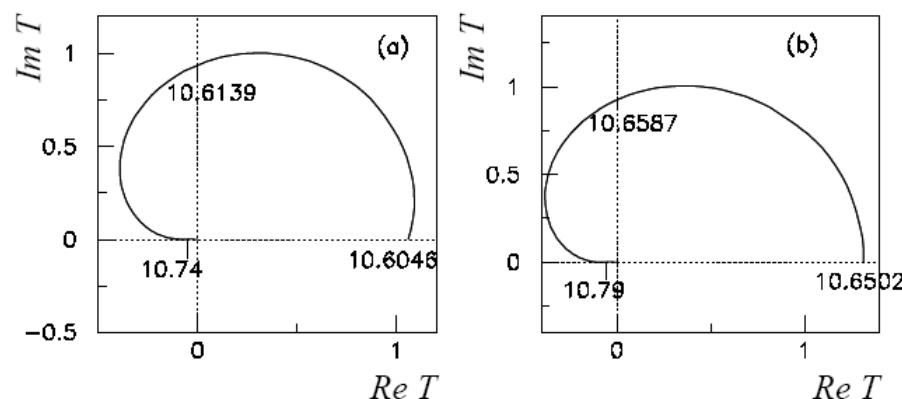
Amplitude



Line-shape

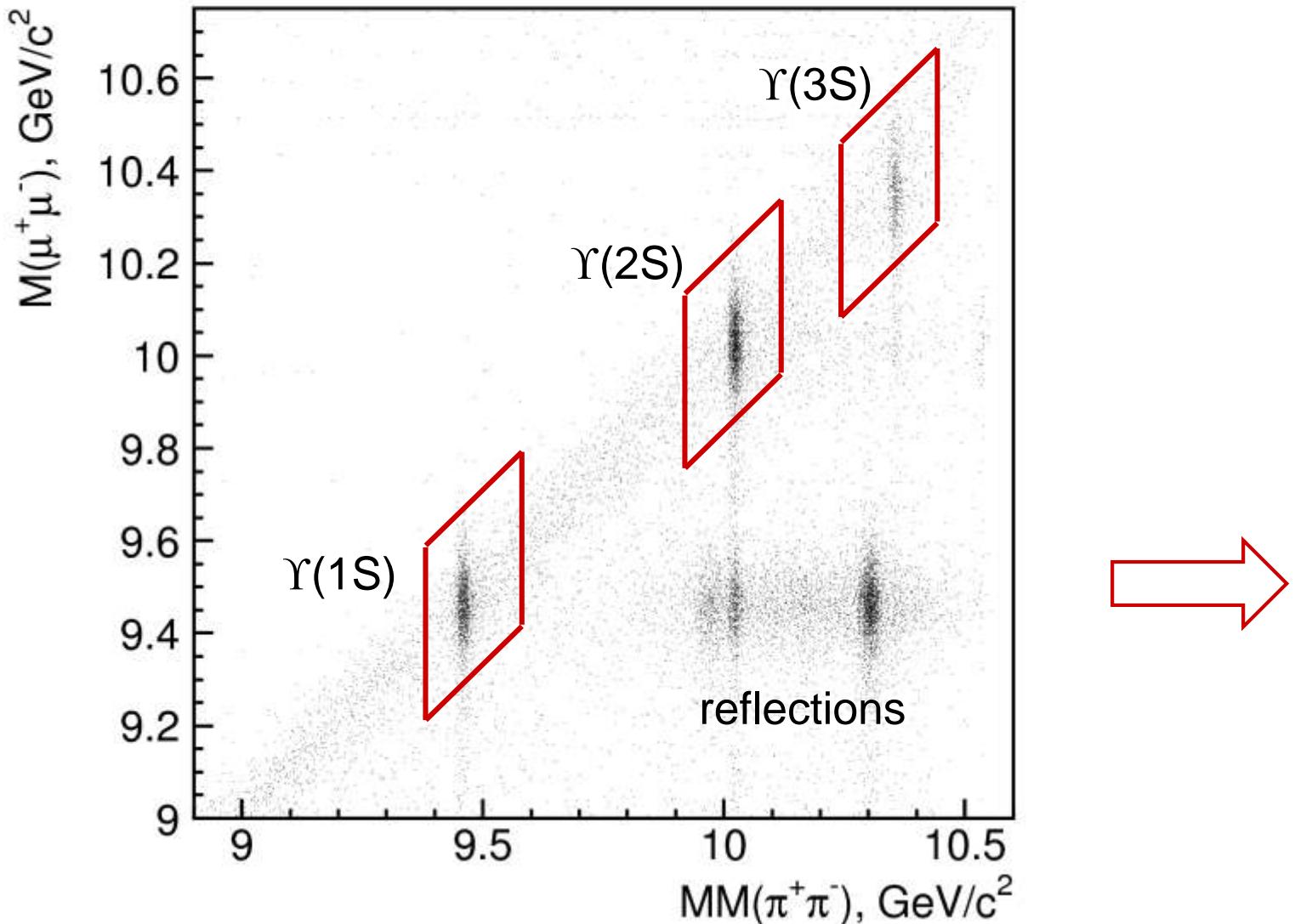


Not a resonance

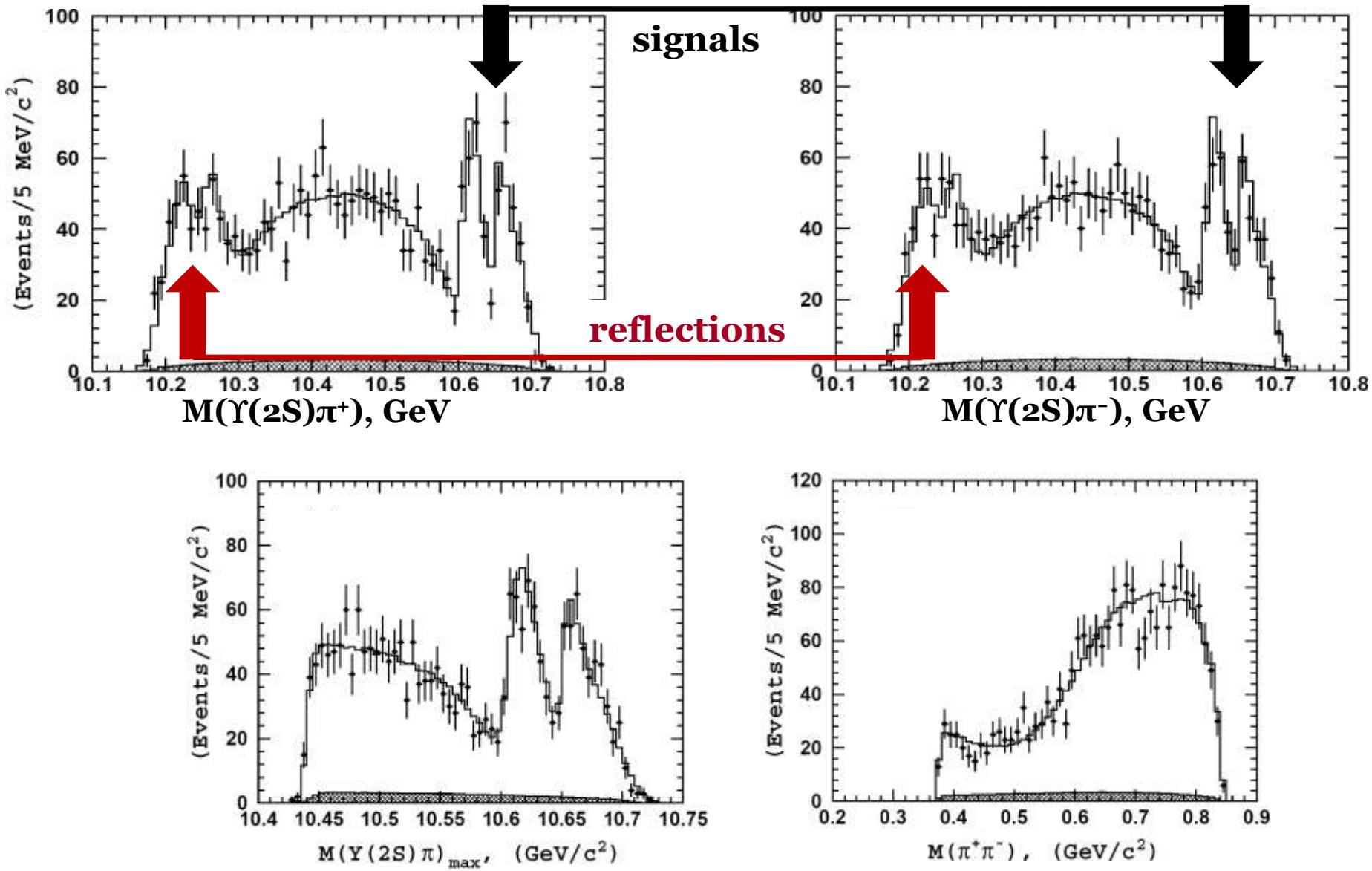


# Exclusive $\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^-$

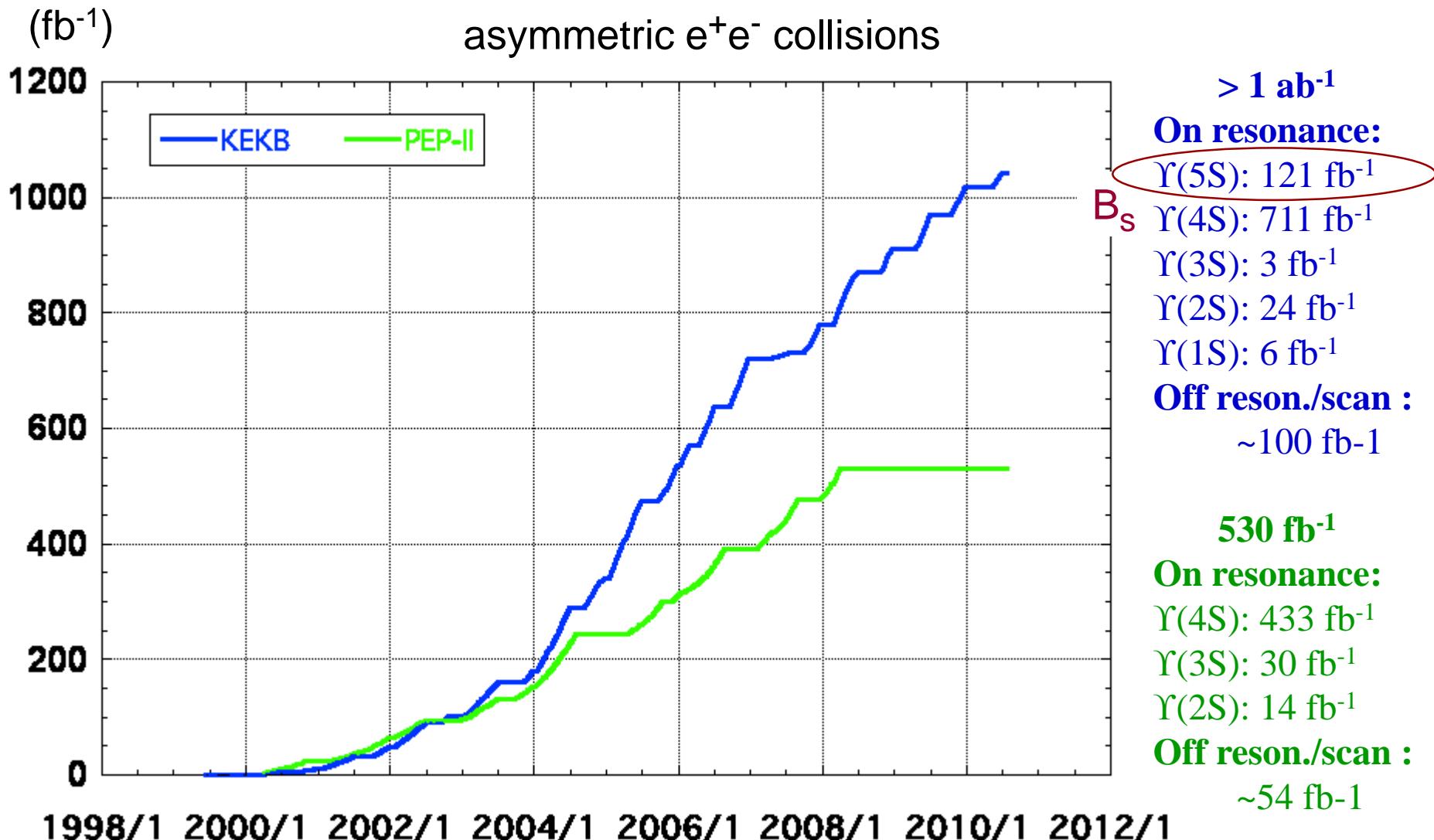
$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi^+ \pi^-$       ( $n = 1, 2, 3$ )  
 $\Upsilon(nS) \rightarrow \mu^+ \mu^-$



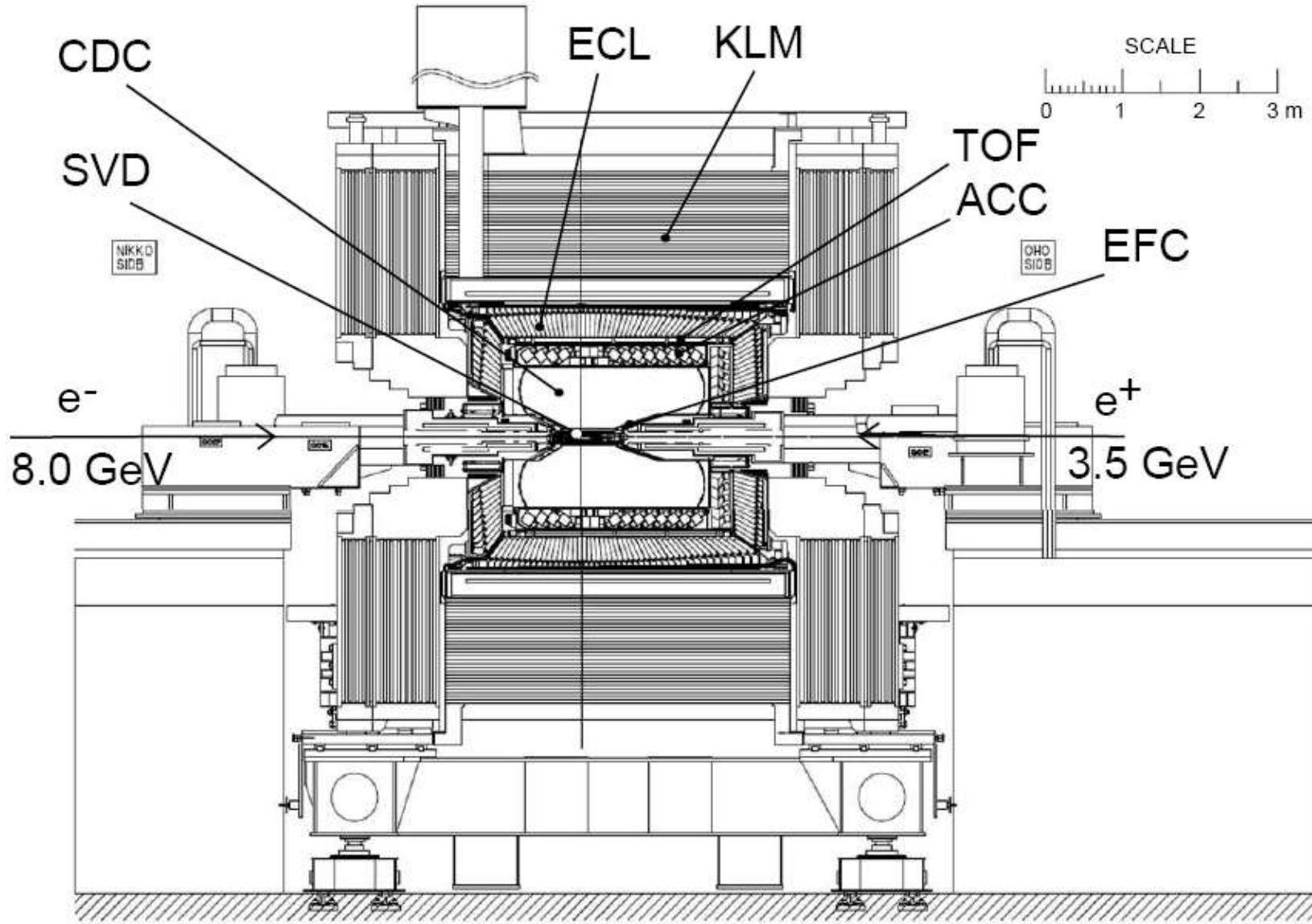
# Results: $\Upsilon(2S)\pi^+\pi^-$



# Integrated Luminosity at B-factories



# Belle Detector



# Heavy quarkonium – approximately a non-relativistic system.

System	Ground triplet state			$(v/c)^2$
	Name	Mass, MeV	$\Gamma$ , MeV	
<b>POSITRONIUM</b>				
$e^+e^-$	Ortho-	1	$5 \cdot 10^{-15}$	$\sim 0.0001$
<b>QUARKONIUM</b>				
$u\bar{u}, d\bar{d}$	$\rho$	800	150	$\sim 1.0$
$s\bar{s}$	$\phi$	1000	4	$\sim 0.8$
$c\bar{c}$	$\psi$	3100	0.09	$\sim 0.25$
$b\bar{b}$	$\Upsilon$	9500	0.05	$\sim 0.08$

Good approximation for heavy quarkonium – potential models.

# Puzzles of $\Upsilon(5S)$ decays

Anomalous production of  $\Upsilon(nS)\pi^+\pi^-$  with  $21.7 \text{ fb}^{-1}$

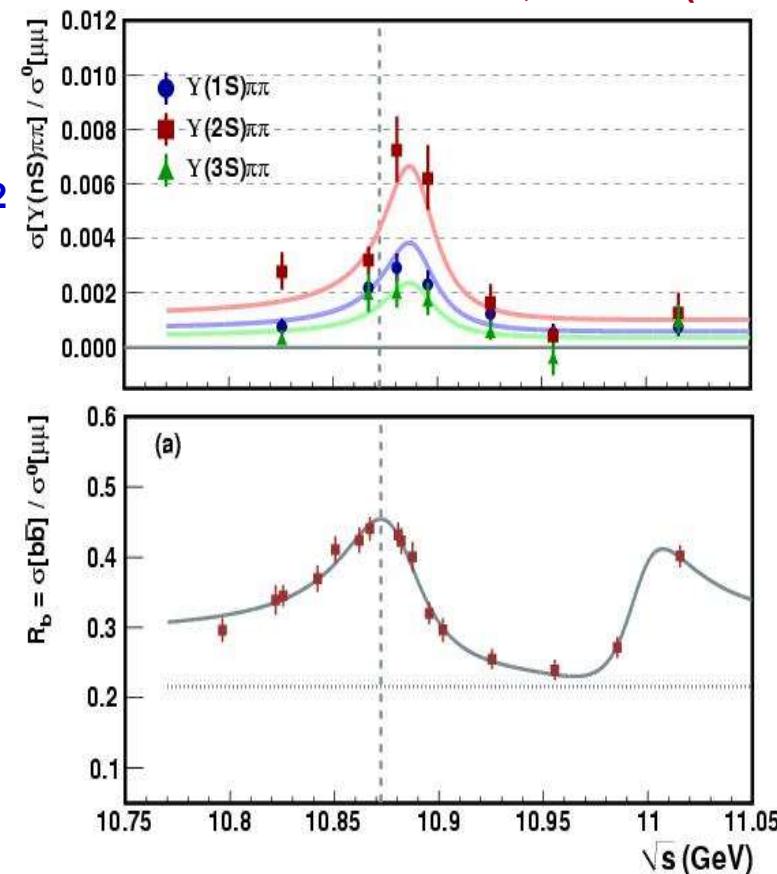
PRD82,091106R(2010)

PRL100,112001(2008)

	$\Gamma(\text{MeV})$
$\Upsilon(5S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	$0.59 \pm 0.04 \pm 0.09$
$\Upsilon(5S) \rightarrow \Upsilon(2S)\pi^+\pi^-$	$0.85 \pm 0.07 \pm 0.16$
$\Upsilon(5S) \rightarrow \Upsilon(3S)\pi^+\pi^-$	$0.52^{+0.20}_{-0.17} \pm 0.10$
$\Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0060
$\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0009
$\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-$	0.0019

$10^2$

Dedicated energy scan  $\Rightarrow$   
shapes of  $R_b$  and  $\sigma(\Upsilon\pi\pi)$  different



$\Upsilon(5S)$  is very interesting and not yet understood  
Finally Belle recorded  $121.4 \text{ fb}^{-1}$  data set at  $\Upsilon(5S)$