Prospects for Charm Physics at a Super τ-charm Factory

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The state of the second

with thanks to Hajime Muramatsu and Roy Briere

The Importance of Charm

new physics (1) Of the flavored hadronic systems with mixing — K(s), D(c), B(b) — the D system is the only system involving heavy up-type quarks:
 ⇒ *it provides sensitivity to different new physics phenomena* (2) Mixing (found) and CP violation (not found) are small in the charm system:
 ⇒ *deviations from SM expectations could be dramatic*

weak (3) Flavor physics relies on global constraints derived from all systems (e.g., the CKM matrix elements, and inputs from one system into another):
 charm is an essential piece of a larger flavor physics program

(4) Weak physics and strong physics can be separated in charm leptonic and semi-✓ leptonic decays:

strong physics

 \Rightarrow charm decays offer opportunities for precision QCD

(5) Many rare decays have backgrounds from "long-distance" hadronic processes:
 ⇒ a spotlight is placed on less-understood aspects of QCD

Current Experimental Landscape

EXPERIMENTS	DATA	FEATURES
<u>High-energy pp collisions</u> LHCb	5 fb ⁻¹ (8 × 10 ¹²)	huge rates time-dependent decays large backgrounds difficult neutral reconstruction
<u>Asymmetric e+e- at Υ(4S)</u> BaBar Belle	550 fb ⁻¹ (8 × 10 ⁸) 1 ab ⁻¹ (13 × 10 ⁸)	large rates some time resolution mostly clean environment neutrals are no problem
<u>e+e- at ψ(3770) (and D_sD_s(*))</u> CLEOc BESIII	0.8 fb ⁻¹ (5 × 10 ⁶) 3 fb ⁻¹ (2 × 10 ⁷)	small rates no time resolution extremely clean quantum correlations best for neutrals/missing particles (also charmonium)

 \Rightarrow there is currently a delicate balance...

Future Experimental Landscape

EXPERIMENTS

High-energy pp collisions LHCb Upgrades DATA

5 fb⁻¹ (8 × 10¹²) 50/300 fb⁻¹ (run III/IV)

FEATURES

huge rates time-dependent decays large backgrounds difficult neutral reconstruction

Asymmetric e^+e^- at $\Upsilon(4S)$

BaBar Belle Belle II 550 fb⁻¹ (8 × 10⁸) 1 ab⁻¹ (13 × 10⁸) 50 ab⁻¹ large rates some time resolution mostly clean environment neutrals are no problem

<u>e+e- at $\psi(3770)$ (and $D_sD_s^{(*)}$)</u> CLEOc BESIII **\tau-charm factory**

0.8 fb⁻¹ (5 × 10⁶) 3 fb⁻¹ (2 × 10⁷) × ~100 luminosity small rates no time resolution extremely clean quantum correlations best for neutrals/missing particles (also charmonium)

\Rightarrow with the τ -charm factory, maintain this important balance.



 \Rightarrow with the τ -charm factory, maintain this important balance.

Future Experimental Landscape

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High-energy pp collisions LHCb **Upgrades** DATA

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\Rightarrow with the τ -charm factory, maintain this important balance.

Strengths of LHCb: *mixing in* $D^0 \rightarrow K^+\pi^-$



LHCb, "Updated determination of $D^0-\bar{D}^0$ mixing and CP violation parameters with $D^0 \to K^+\pi^-$ decays," PRD 97, 031101(R) (2018) **But D.** y' depends on δ .

Strengths of LHCb: *mixing in* $D^0 \rightarrow K^+\pi^-\pi^+\pi^-$

Terminology/Formulae/Definitions: Tagging the $D^0: D^{*+} \to D^0 \pi_s^+$ Cabibbo-favored decay: $D^0 \to K^- \pi^+ \pi^+ \pi^-$ Cabibbo-suppressed decay: $D^0 \to K^+ \pi^- \pi^+ \pi^-$ Mixing then decay: $D^0 \to \bar{D}^0 \to K^+ \pi^- \pi^+ \pi^-$ Time-dependent ratio starting with D^0 :

$$R^{+}(t) \equiv \frac{N(K^{+}\pi^{-}\pi^{+}\pi^{-})(t)}{N(K^{-}\pi^{+}\pi^{+}\pi^{-})(t)}$$

$$\approx \frac{|A(D^{0} \to K^{+}3\pi)(t) + A(D^{0} \to \bar{D}^{0} \to K^{+}3\pi)(t)|^{2}}{|A(D^{0} \to K^{-}3\pi)(t)|^{2}}$$

$$\approx r_{K3\pi}^{2} + r_{K3\pi}R_{K3\pi}y'_{K3\pi}\frac{t}{\tau} + \frac{x^{2} + y^{2}}{4}(\frac{t}{\tau})^{2}$$

where

$$x'_{K3\pi} \equiv x \cos \delta_{K3\pi} + y \sin \delta_{K3\pi}$$
$$y'_{K3\pi} \equiv y \cos \delta_{K3\pi} - x \sin \delta_{K3\pi}$$

and x, y are mixing parameters

and $\delta_{K3\pi}$ is an average strong phase

and $R_{K3\pi}$ is a coherence factor:

$$R_{K3\pi}e^{-i\delta_{K3\pi}} \equiv <\cos\delta > + i < \sin\delta >$$

LHCb, "First observation of $D^0-\bar{D}^0$ oscillations in $D^0 \to K^+\pi^-\pi^+\pi^-$ decays and measurement of the associated coherence parameters," PRL 116, 241801 (2016)



But D. Dependence on another strong phase and a coherence factor.

Strengths of LHCb: *amplitude analysis of* $D^0 \rightarrow K^+\pi^-\pi^+\pi^-$

Terminology/Formulae/Definitions: Tagging the $D^0: D^{*+} \to D^0 \pi_s^+$ Cabibbo-favored decay: $D^0 \to K^- \pi^+ \pi^+ \pi^-$ Cabibbo-suppressed decay: $D^0 \to K^+ \pi^- \pi^+ \pi^-$ Mixing then decay: $D^0 \to \bar{D}^0 \to K^+ \pi^- \pi^+ \pi^-$ Time-dependent ratio starting with D^0 :

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$$\approx r_{K3\pi}^{2} + r_{K3\pi}R_{K3\pi}y'_{K3\pi}\frac{t}{\tau} + \frac{x^{2} + y^{2}}{4}(\frac{t}{\tau})^{2}$$

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$$R_{K3\pi}e^{-i\delta_{K3\pi}} \equiv <\cos\delta > + i < \sin\delta >$$

LHCb, "Studies of the resonance structure in $D^0 \to K^{\mp} \pi^{\pm} \pi$

A. Massive statistics (tagging with π and μ):



Strengths of LHCb: rare decay $D^0 \rightarrow h^+h^-\mu^+\mu^-$



Observations of rare decays O(10⁻⁷): $B(D^{0} \rightarrow \pi^{+}\pi^{-}\mu^{+}\mu^{-}) = (9.64 \pm 0.48 \pm 0.51 \pm 0.97) \times 10^{-7}$ $B(D^{0} \rightarrow K^{+}K^{-}\mu^{+}\mu^{-}) = (1.54 \pm 0.27 \pm 0.09 \pm 0.16) \times 10^{-7}$ But note: largest systematic errors are due to normalization branching fractions: relative to K-\pi^+\mu^+(LHCb), relative to K-\pi^+\pi^+\mu^- (CLEO)
LHCb, "Observation of D⁰ meson decays to \pi^+\pi^-\mu^+\mu^- and K^+K^-\mu^+\mu^- final states," PRL 119, 181805 (2017)
Bhort distance: Long distance: Long distance: Long distance: Long distance: Long distance: Long distance: $U^0 \left\{ \begin{array}{c} \mu^+ \\ \mu^- \\ \mu^-$

Strengths of LHCb: rare decay $D^0 \rightarrow \mu^+\mu^-$



Tightest upper limits $O(10^{-9})$:

But note: standard model expectation depends on $\gamma\gamma$:

$$\mathcal{B}(D^0 \to \mu^+ \mu^-) < 6.2 \times 10^{-9}$$

 $\mathcal{B}(D^0 \to \mu^+ \mu^-) \approx (2.7 \times 10^{-5}) \times \mathcal{B}(D^0 \to \gamma \gamma)$

LHCb, "Search for the rare decay $D^0 \rightarrow \mu^+ \mu^-$," PLB 725, 15 (2013)

Strengths of BaBar/Belle(II): rare decay $D^0 \rightarrow \gamma \gamma$

A. Big statistics; B. Sensitivity to neutral final states

Search for $D^0 \rightarrow \gamma \gamma$ to access FCNC $c \rightarrow u \gamma$:



Belle, "Search for the rare decay $D^0 \to \gamma \gamma$ at Belle," PRD 93, 051102(R) (2016)

Strengths of BaBar/Belle(II): *CP violation in* $D^+ \rightarrow \pi^+ \pi^0$





Mode	$\mathcal{B}_{\mathrm{mode}}/\mathcal{B}_{\mathrm{Normalization}}$ (%)	This result \mathcal{B} (%)	\mathcal{A}_{CP} (%)
$D^0 \rightarrow K^+ K^-$	$10.41 \pm 0.11 \pm 0.12$	$0.407 \pm 0.004 \pm 0.005 \pm 0.008$	
$D^0 \rightarrow K^0_S K^0_S$	$0.41 \pm 0.04 \pm 0.02$	$0.0160 \pm 0.0017 \pm 0.0008 \pm 0.0003$	
$D^0 \rightarrow \pi^+ \pi^-$	$3.70 \pm 0.06 \pm 0.09$	$0.145 \pm 0.002 \pm 0.004 \pm 0.003$	
$D^0 o \pi^0 \pi^0$	$2.06 \pm 0.07 \pm 0.10$	$0.081 \pm 0.003 \pm 0.004 \pm 0.002$	
$D^0 \rightarrow K^- \pi^+$	100	3.9058 external input	$0.5 \pm 0.4 \pm 0.9$
$D^0 \rightarrow K^0_S \pi^0$	$30.4 \pm 0.3 \pm 0.9$	$1.19 \pm 0.01 \pm 0.04 \pm 0.02$	
$D^0 \to K_S^{0} \eta$	$12.3 \pm 0.3 \pm 0.7$	$0.481 \pm 0.011 \pm 0.026 \pm 0.010$	
$D^0 o \pi^{ ilde 0} \eta$	$1.74 \pm 0.15 \pm 0.11$	$0.068 \pm 0.006 \pm 0.004 \pm 0.001$	
$D^0 \rightarrow K^0_S \eta'$	$24.3 \pm 0.8 \pm 1.1$	$0.95 \pm 0.03 \pm 0.04 \pm 0.02$	
$D^0 ightarrow \pi^{ec 0} \eta^\prime$	$2.3 \pm 0.3 \pm 0.2$	$0.091 \pm 0.011 \pm 0.006 \pm 0.002$	
$D^0 \rightarrow \eta \eta$	$4.3 \pm 0.3 \pm 0.4$	$0.167 \pm 0.011 \pm 0.014 \pm 0.003$	
$D^0 o \eta \eta'$	$2.7 \pm 0.6 \pm 0.3$	$0.105 \pm 0.024 \pm 0.010 \pm 0.002$	
$D^+ \rightarrow K^- \pi^+ \pi^+$	100	9.1400 external input	$-0.1 \pm 0.4 \pm 0.9$
$D^+ \rightarrow K^0_S K^+$	$3.35 \pm 0.06 \pm 0.07$	$0.306 \pm 0.005 \pm 0.007 \pm 0.007$	$-0.2 \pm 1.5 \pm 0.9$
$D^+ \rightarrow \pi^+ \pi^0$	$1.29 \pm 0.04 \pm 0.05$	$0.118 \pm 0.003 \pm 0.005 \pm 0.003$	$2.9 \pm 2.9 \pm 0.3$
$D^+ \rightarrow K^0_S \pi^+$	$16.82 \pm 0.12 \pm 0.37$	$1.537 \pm 0.011 \pm 0.034 \pm 0.033$	$-1.3 \pm 0.7 \pm 0.3$
$D^+ \rightarrow K^+ \pi^0$	$0.19 \pm 0.02 \pm 0.01$	$0.0172 \pm 0.0018 \pm 0.0007 \pm 0.0004$	$-3.5 \pm 10.7 \pm 0.9$
$D^+ \rightarrow K^+ \eta$	<0.15 (90% C.L.)	<0.013 (90% C.L.)	
$D^+ o \pi^+ \eta$	$3.87 \pm 0.09 \pm 0.19$	$0.354 \pm 0.008 \pm 0.018 \pm 0.008$	$-2.0 \pm 2.3 \pm 0.3$
$D^+ \rightarrow K^+ \eta'$	<0.20 (90% C.L.)	<0.019 (90% C.L.)	
$D^+ o \pi^+ \eta'$	$5.12 \pm 0.17 \pm 0.25$	$0.468 \pm 0.016 \pm 0.023 \pm 0.010$	$-4.0 \pm 3.4 \pm 0.3$
		$+ D_s$ modes	

Belle, "Search for CP violation in the $D^+ \to \pi^+ \pi^0$ decay at Belle," PRD 97, 011101(R) (2018)

But D. Improvement over CLEO is only ×2...

Strengths of CLEO/BES/tc-Factory

(1) Quantum-correlated pairs of D-mesons

 \Rightarrow complementary to other mixing and CP studies (*and input for B* \rightarrow *DK*)

(2) Leptonic decays

 \Rightarrow precision QCD and tests of lepton-flavor universality

(3) Special hadronic decays (*e.g.* $D^+ \rightarrow \pi^+ \pi^0$)

 \Rightarrow CP asymmetries and absolute branching fractions

(4) Charmed baryons

 \Rightarrow absolute branching fractions and features of production

(5) Rare decays (also from charmonium)

 \Rightarrow complementary searches

Terminology/Formulae/Definitions:

Amplitudes to a final state i:

$$A_i \equiv A(D^0 \to i)$$

$$\bar{A}_i \equiv A(\bar{D}^0 \to i)$$

Ratio of amplitudes:

$$r_i \equiv \frac{|\bar{A}_i|}{|A_i|}$$

Strong phase between A_i and \bar{A}_i :

$$R_i e^{-i\delta_i} \equiv \frac{\int \bar{A}_i A_i^* dx_i}{|A_i| |\bar{A}_i|}$$

For the 2-body case:

$$R_{i} = 1; \quad r_{i}e^{-i\delta_{i}} = \frac{\bar{A}_{i}}{A_{i}}$$

For $e^{+}e^{-} \rightarrow \psi(3770) \rightarrow D^{0}\bar{D}^{0} \rightarrow (i,j)$:
$$\Gamma(i,j) = \frac{1}{\sqrt{2}} \int |A_{i}\bar{A}_{j} - \bar{A}_{i}A_{j}|^{2} dx_{i} dx_{j}$$
$$= |A_{i}|^{2}|A_{j}|^{2} \left[r_{i}^{2} + r_{j}^{2} - 2\operatorname{Re}(r_{i}R_{i}e^{i\delta_{i}}r_{j}R_{j}e^{-i\delta_{j}})\right]$$
$$B_{i} \equiv B(D^{0} \rightarrow i) = |A_{i} + \bar{A}_{i}A(D^{0} \rightarrow \bar{D}^{0})|^{2}$$
$$= |A_{i}|^{2} \left[1 + r_{i}R_{i}(y\cos\delta_{i} + x\sin\delta_{i})\right]$$

Exploit quantum correlations in $\psi(3770)$ decays:

$$|\psi\rangle \rightarrow \frac{1}{\sqrt{2}}(|D^0\rangle_1 |\bar{D}^0\rangle_2 - |\bar{D}^0\rangle_1 |D^0\rangle_2)$$

Measure many different pairs of final states (i,j):

$$\frac{\Gamma(i,j)}{B_i B_j} = f_{ij}(B_i, B_j, r_i, r_j, R_i, R_j, \delta_i, \delta_j, x, y) \propto \frac{N(i,j)}{B_i B_j}$$

Different (i,j) produce different parameter dependences:

_						
-	Final State	r_i	δ_i	$R_i \cos \delta_i$	$R_i \sin \delta_i$	$\mathcal{B}_{\overline{\imath}}/\mathcal{B}_i$
_	$K^{\mp}\pi^{\pm}$	r	δ	$\cos \delta$	$\sin \delta$	$R_{\rm WS}$
$(K_S\pi^+\pi^-)$) $Y_k/ar{Y}_k$	$ ho_k$	•	c_k	s_k	Q_k
(CP+)	S_+	1	π	-1	0	1
(CP-)	S_{-}	1	0	+1	0	1
(semilep.) ℓ^{\pm}	0				0

Create an overconstrained system and fit.

CLEO: 261 measurements; 51 free parameters; no external dependencies

CLEO (legacy), "Updated measurement of the strong phase in $D^0 \to K^+\pi^$ decay using quantum correlations in $e^+e^- \to D^0\bar{D}^0$ at CLEO," PRD 86, 112001 (2012)

Exploit	Correlated	Mode
	$1 + R_{\rm WS}$	$K^{-}\pi^{+}$
	2	S_+
· · · · · · · · · · · · · · · · · · ·	2	S_{-}
	$1+Q_k$	Y_k
Measur	$R_{\rm M}[(1+R_{\rm WS})^2 - 4r\cos\delta(r\cos\delta + y)]$	$\pi^{+}, K^{-}\pi^{+}$
Ivicasui	$(1+R_{\rm WS})^2 - 4r\cos\delta(r\cos\delta + y)$	$\pi^{+}, K^{+}\pi^{-}$
	$1 + R_{\rm WS} + 2r\cos\delta + y$	$K^{-}\pi^{+}, S_{+}$
$\frac{1}{(l)}$	$1 + R_{\rm WS} - 2r\cos\delta - y$	$K^{-}\pi^{+}, S_{-}$
B_i	$1 - ry\cos\delta - rx\sin\delta$	$K^-\pi^+, \ell^-$
	$r^2(1 - ry\cos\delta - rx\sin\delta)$	$K^-\pi^+,\ell^+$
	$(1 + R_{\rm WS})(1 + Q_i) - r^2 - \rho_i^2$	$K^-\pi^+$ \bar{Y}_i
Differe	$-2(r\cos\delta + y)(\rho_i c_i + y) + 2r\sin\delta\rho_i s_i$	· · · · · · · · · · · · · · · · · · ·
	$(1 + R_{\rm WS})(1 + Q_i) - 1 - r^2 \rho_i^2$	$K^-\pi^+ Y_i$
	$-2(r\cos\delta + y)(\rho_i c_i + y) - 2r\sin\delta\rho_i s_i$	i <i>n</i> , <i>i i</i>
	0	S_+, S_+
$(K_{\alpha}\pi^{+}\tau)$	0	S, S
(R_{SU})	4	S_{+}, S_{-}
(<i>CP</i> -	1+y	S_+, ℓ^-
(semile	1-y	S, ℓ^-
	$1 + Q_i + 2\rho_i c_i + y$	S_+, Y_i
	$1 + Q_i - 2\rho_i c_i - y$	S_{-}, Y_{i}
Create	$1 - \rho_i y c_i - \rho_i x s_i$	Y_i, ℓ^-
	$\rho_i^2(1-\rho_i y c_i - \rho_i x s_i)$	Y_i,ℓ^+
	$(1+Q_i)(1+Q_j) - \rho_i^2 - \rho_j^2$	$Y_{\dot{a}}, \bar{Y}_{\dot{a}}$
$D^0 \rightarrow K$	$-2(\rho_i c_i + y)(\rho_j c_j + y) + 2\rho_i s_i \rho_j s_j$	• <i>i</i> , • <i>j</i>
$PRD 86 11^{\circ}$	$(1+Q_i)(1+Q_j) - 1 - \rho_i^2 \rho_j^2$	V_{\cdot} V_{\cdot}

(1) Quantum Correlations – a global fit

Exploit quantum correlations in $\psi(3770)$ decays:

$$\psi > \rightarrow \frac{1}{\sqrt{2}} (|D^0 >_1 |\bar{D}^0 >_2 - |\bar{D}^0 >_1 |D^0 >_2)$$

Measure many different pairs of final states (i,j):

$$\frac{\Gamma(i,j)}{B_i B_j} = f_{ij}(B_i, B_j, r_i, r_j, R_i, R_j, \delta_i, \delta_j, x, y) \propto \frac{N(i,j)}{B_i B_j}$$

Different (i,j) produce different parameter dependences:

_						
-	Final State	r_i	δ_i	$R_i \cos \delta_i$	$R_i \sin \delta_i$	$\mathcal{B}_{\overline{\imath}}/\mathcal{B}_i$
-	$K^{\mp}\pi^{\pm}$	r	δ	$\cos \delta$	$\sin \delta$	$R_{\rm WS}$
$(K_S\pi^+\pi^-)$) Y_k/\bar{Y}_k	$ ho_k$	•	c_k	s_k	Q_k
(CP+)	S_+	1	π	-1	0	1
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Terminology/Formulae/Definiti	Parameter	Standard Fit	-	Parameter	Standard Fit	e	cays:
Amplitudes to a final state i :	$\mathcal{N}~(10^6)$	$3.092 \pm 0.050 \pm 0.040$		$\mathcal{B}(K^-\pi^+)$ (%)	$3.77 \pm 0.06 \pm 0.05$		
Amplitudes to a mai state i.	y~(%)	$4.2\pm2.0\pm1.0$		$\mathcal{B}(K^-K^+) \ (10^{-3})$	$3.99 \pm 0.07 \pm 0.08$		
$A_i \equiv A(D^0 \to i)$	$r^2~(\%)$	$0.533 \pm 0.107 \pm 0.045$		$\mathcal{B}(\pi^{-}\pi^{+}) \ (10^{-3})$	$1.36 \pm 0.03 \pm 0.04$	ľ	$>_{2})$
$\bar{A}_i \equiv A(\bar{D}^0 \rightarrow i)$	$\cos\delta$	$0.81\substack{+0.22+0.07\\-0.18-0.05}$		$\mathcal{B}(K^0_S \pi^0 \pi^0)$ (%)	$0.99 \pm 0.02 \pm 0.06$		
	$\sin \delta$	$-0.01 \pm 0.41 \pm 0.04$		$\mathcal{B}(K_L^0\pi^0)$ (%)	$0.94 \pm 0.03 \pm 0.03$		
Ratio of amplitudes:	x^2 (%)	$0.06 \pm 0.23 \pm 0.11$		$\mathcal{B}(K_{L}^{0}\eta)$ (10 ⁻³)	$3.36 \pm 0.30 \pm 0.17$	5	(i,j):
$ \overline{A} $	$ ho_0^2$	$0.337 \pm 0.030 \pm 0.006$		$\mathcal{B}(K_{I}^{0}\omega)$ (%)	$0.90 \pm 0.05 \pm 0.03$		
$r_i \equiv \frac{ T_i }{ A_i }$	$ ho_1^2$	$0.270 \pm 0.044 \pm 0.005$		$\mathcal{B}(K_{c}^{0}\pi^{0})$ (%)	$1.17 \pm 0.02 \pm 0.03$		$\mathbf{\Lambda} \mathbf{T} (\cdot \cdot \cdot)$
$ A_i $	$ ho_2^2$	$0.235 \pm 0.028 \pm 0.003$		$\mathcal{B}(K_{c}^{0}n) (10^{-3})$	$4.95 \pm 0.14 \pm 0.36$	p	$(u) \propto \frac{N(i,j)}{2}$
Strong phase between A_i and \bar{A}_j	$ ho_3^2$	$0.399 \pm 0.066 \pm 0.005$		$\mathcal{B}(K^0_{\mathcal{G}}(\omega))$ (%)	$1.00 \pm 0.11 \pm 0.00$ $1.15 \pm 0.02 \pm 0.04$		$, g \rightarrow a B_i B_i$
Strong phase setween 11, and 11	$ ho_4^2$	$0.592 \pm 0.067 \pm 0.010$		$\mathcal{B}(K_{2}^{0}\pi^{0}\pi^{0})$ (%)	$0.95 \pm 0.06 \pm 0.05$		c J
$\int \bar{A}_i A_i^* dx_i$	$ ho_5^2$	$0.343 \pm 0.044 \pm 0.000$		$\mathcal{B}(K^{-}e^{+}\mu) (\%)$	$0.59 \pm 0.00 \pm 0.00$ $3.54 \pm 0.05 \pm 0.08$		
$R_i e^{-i \sigma_i} \equiv \frac{1}{ A_i \bar{A}_i }$	$ ho_6^2$	$0.146 \pm 0.023 \pm 0.000$		$\mathcal{B}(K^{-}u^{+}u) (\%)$	$3.34 \pm 0.05 \pm 0.08$ $3.38 \pm 0.05 \pm 0.08$		
	$ ho_7^2$	$0.445 \pm 0.039 \pm 0.002$		$\mathcal{B}(K \mid \mu^{-} \nu_{\mu}) (70)$ $\mathcal{B}(V) (10^{-3})$	$3.30 \pm 0.00 \pm 0.00$	(sependences
For the 2-body case:	c_0	$-0.76 \pm 0.06 \pm 0.01$		$\mathcal{B}(I_0)$ (10) $\mathcal{B}(V)$ (10 ⁻³)	$4.30 \pm 0.10 \pm 0.12$		
-	c_1	$-0.75 \pm 0.11 \pm 0.00$		$\mathcal{D}(Y_1) (10^{-3})$ $\mathcal{P}(V) (10^{-3})$	$1.03 \pm 0.10 \pm 0.04$		$\frac{1}{n}$
$R_i = 1$: $r_i e^{-i\delta_i} = \frac{A_i}{2}$	c_2	$0.00 \pm 0.10 \pm 0.01$		$\mathcal{B}(Y_2) \ (10^{-3})$	$3.43 \pm 0.10 \pm 0.10$	Ĺ	${\mathcal{S}}_{\overline{\imath}}/{\mathcal{B}}_i$
A_i	c_3	$0.45 \pm 0.15 \pm 0.01$		$\mathcal{B}(Y_3) (10^{-5})$	$0.99 \pm 0.08 \pm 0.03$		$R_{ m WS}$
Even $a^+a^- \rightarrow a/(2770) \rightarrow D^0 \overline{D}^0$	c_4	$0.95 \pm 0.07 \pm 0.01$		$\mathcal{B}(Y_4) \ (10^{-3})$	$1.70 \pm 0.11 \pm 0.05$		Q_k
For $e \cdot e \rightarrow \psi(3770) \rightarrow D^{\circ}D^{\circ}$	C_5	$0.79 \pm 0.09 \pm 0.01$		$\mathcal{B}(Y_5)$ (10 ⁻³)	$2.11 \pm 0.13 \pm 0.07$		1
1 (c_6	$-0.20 \pm 0.13 \pm 0.02$		$\mathcal{B}(Y_6) \ (10^{-3})$	$3.15 \pm 0.15 \pm 0.08$		1
$\Gamma(i,j) = \frac{1}{\sqrt{2}} \int A_i A_j - A_i A_j $	c_7	$-0.41 \pm 0.07 \pm 0.01$		$\mathcal{B}(Y_7) \ (10^{-3})$	$3.68 \pm 0.16 \pm 0.09$		1
$\sqrt{2} J$	s_0	$0.55 \pm 0.16 \pm 0.00$					0
$= A_i ^2 A_j ^2 \left[r_i^2 + r_j^2 - \right]$	s_1	$0.53 \pm 0.28 \pm 0.00$					
$B_i \equiv B(D^0 \to i) = A_i + i $	s_2	$0.93 \pm 0.15 \pm 0.00$					
$- A ^{2}[1+r \cdot B \cdot (u \cos \theta)]$	s_3	$0.47 \pm 0.30 \pm 0.00$					
$= \mathcal{I}_i [\mathbf{I} + \mathcal{I}_i] \mathcal{U}_i (\mathcal{G} \cup \mathcal{G})$	s_4	$0.55 \pm 0.24 \pm 0.00$					
	s_5	$-0.71 \pm 0.24 \pm 0.00$					
	s_6	$-0.42 \pm 0.27 \pm 0.06$					
CLEO (legacy), "Updated meas	s_7	$-0.30 \pm 0.18 \pm 0.04$	_			- L	",
decay using quantum correlations	$\chi^2_{\rm fit}/{ m ndof}$	193.2/210	:				5;
(2012)					по ехієтна	<u>r aepen</u>	dencies



CLEO (legacy), "Updated measurement of the strong phase in $D^0 \to K^+\pi^$ decay using quantum correlations in $e^+e^- \to D^0\bar{D}^0$ at CLEO," PRD 86, 112001 (2012) CLEO: 261 measurements; 51 free parameters; no external dependencies

Terminology/Formulae/Definitions:

Amplitudes to a final state i:

$$A_i \equiv A(D^0 \to i)$$

$$\bar{A}_i \equiv A(\bar{D}^0 \to i)$$

Ratio of amplitudes:

$$r_i \equiv \frac{|\bar{A}_i|}{|A_i|}$$

Strong phase between A_i and \bar{A}_i :

$$R_i e^{-i\delta_i} \equiv \frac{\int \bar{A}_i A_i^* dx_i}{|A_i| |\bar{A}_i|}$$

For the 2-body case:

$$R_{i} = 1; \quad r_{i}e^{-i\delta_{i}} = \frac{\bar{A}_{i}}{A_{i}}$$

For $e^{+}e^{-} \rightarrow \psi(3770) \rightarrow D^{0}\bar{D}^{0} \rightarrow (i,j)$:
$$\Gamma(i,j) = \frac{1}{\sqrt{2}} \int |A_{i}\bar{A}_{j} - \bar{A}_{i}A_{j}|^{2} dx_{i} dx_{j}$$
$$= |A_{i}|^{2}|A_{j}|^{2} \left[r_{i}^{2} + r_{j}^{2} - 2\operatorname{Re}(r_{i}R_{i}e^{i\delta_{i}}r_{j}R_{j}e^{-i\delta_{j}})\right]$$
$$B_{i} \equiv B(D^{0} \rightarrow i) = |A_{i} + \bar{A}_{i}A(D^{0} \rightarrow \bar{D}^{0})|^{2}$$
$$= |A_{i}|^{2} \left[1 + r_{i}R_{i}(y\cos\delta_{i} + x\sin\delta_{i})\right]$$

Exploit quantum correlations in $\psi(3770)$ decays:

$$|\psi\rangle \rightarrow \frac{1}{\sqrt{2}}(|D^0\rangle_1 |\bar{D}^0\rangle_2 - |\bar{D}^0\rangle_1 |D^0\rangle_2)$$

Measure many different pairs of final states (i,j):

$$\frac{\Gamma(i,j)}{B_i B_j} = f_{ij}(B_i, B_j, r_i, r_j, R_i, R_j, \delta_i, \delta_j, x, y) \propto \frac{N(i,j)}{B_i B_j}$$

Different (i,j) produce different parameter dependences:

_						
-	Final State	r_i	δ_i	$R_i \cos \delta_i$	$R_i \sin \delta_i$	$\mathcal{B}_{\overline{\imath}}/\mathcal{B}_i$
_	$K^{\mp}\pi^{\pm}$	r	δ	$\cos \delta$	$\sin \delta$	$R_{\rm WS}$
$(K_S\pi^+\pi^-)$) $Y_k/ar{Y}_k$	$ ho_k$	•	c_k	s_k	Q_k
(CP+)	S_+	1	π	-1	0	1
(CP-)	S_{-}	1	0	+1	0	1
(semilep.) ℓ^{\pm}	0				0

Create an overconstrained system and fit.

CLEO: 261 measurements; 51 free parameters; no external dependencies

CLEO (legacy), "Updated measurement of the strong phase in $D^0 \to K^+\pi^$ decay using quantum correlations in $e^+e^- \to D^0\bar{D}^0$ at CLEO," PRD 86, 112001 (2012)

Strengths of CLEO/BES/\tau cF: (1) *Quantum Correlations — the (S,K\pi) piece*

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$$B_{i} \equiv B(D^{0} \rightarrow i) = |A_{i} + \bar{A}_{i}A(D^{0} \rightarrow \bar{D}^{0})|^{2}$$
$$= |A_{i}|^{2} \left[1 + r_{i}R_{i}(y\cos\delta_{i} + x\sin\delta_{i})\right]$$

BESIII looked specifically at final states (K- π +, S[±]) to determine $\delta_{K\pi}$:

$$A_{K\pi}^{CP} \equiv \frac{B(D^{S-} \to K^{-}\pi^{+}) - B(D^{S+} \to K^{-}\pi^{+})}{B(D^{S-} \to K^{-}\pi^{+}) + B(D^{S+} \to K^{-}\pi^{+})}$$
$$= \frac{2r\cos\delta_{K\pi} + y}{1 + R_{WS}}$$

Final states included:

Туре	Mode
Flavored S+ S–	$K^{-}\pi^{+}, K^{+}\pi^{-}$ $K^{+}K^{-}, \pi^{+}\pi^{-}, K^{0}_{S}\pi^{0}\pi^{0}, \pi^{0}\pi^{0}, \rho^{0}\pi^{0}$ $K^{0}_{S}\pi^{0}, K^{0}_{S}\eta, K^{0}_{S}\omega$

Use external r, y, R_{WS} as input to extract $\delta_{K\pi}$:

 $\cos \delta_{K\pi} = 1.02 \pm 0.11 \pm 0.06 \pm 0.01$

BESIII, "Measurement of the $D \to K^- \pi^+$ strong phase difference in $\psi(3770) \to D^0 \bar{D}^0$," PLB 734, 227 (2014)

Strengths of CLEO/BES/\tau cF: (1) *Quantum Correlations — the (S,K\pi) piece*



BESIII, "Measurement of the $D \to K^- \pi^+$ strong phase difference in $\psi(3770) \to D^0 \bar{D}^0$," PLB 734, 227 (2014)

Strengths of CLEO/BES/τcF: (1) *Quantum Correlations — the* (*S*,*l*) *piece*

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For the 2-body case:

$$R_i = 1; \quad r_i e^{-i\delta_i} = \frac{\bar{A}_i}{A_i}$$

For
$$e^+e^- \to \psi(3770) \to D^0 \overline{D}{}^0 \to (i, j)$$
:

$$\begin{split} \Gamma(i,j) &= \frac{1}{\sqrt{2}} \int |A_i \bar{A}_j - \bar{A}_i A_j|^2 dx_i dx_j \\ &= |A_i|^2 |A_j|^2 \left[r_i^2 + r_j^2 - 2 \text{Re}(r_i R_i e^{i\delta_i} r_j R_j e^{-i\delta_j}) \right] \\ B_i &\equiv B(D^0 \to i) = |A_i + \bar{A}_i A(D^0 \to \bar{D}^0)|^2 \\ &= |A_i|^2 \left[1 + r_i R_i (y \cos \delta_i + x \sin \delta_i) \right] \end{split}$$

BESIII also looked specifically at final states (l^{\pm}, S^{\pm}) to determine y_{CP}:

$$y_{CP} \approx \frac{1}{4} \left(\frac{B(D^{S-} \to l)}{B(D^{S+} \to l)} - \frac{B(D^{S+} \to l)}{B(D^{S-} \to l)} \right)$$

Final states included:

Туре	Mode
CP+	$K^{+}K^{-}, \pi^{+}\pi^{-}, K^{0}_{S}\pi^{0}\pi^{0}$
CP–	$K^{0}_{S}\pi^{0}, K^{0}_{S}\omega, K^{0}_{S}\eta$
Semileptonic	$K^{\mp}e^{\pm}v, K^{\mp}\mu^{\pm}v$

Directly extract y_{CP} (no external parameters):

$$y_{CP} = (-2.0 \pm 1.3 \pm 0.7)\%$$

BESIII, "Measurement of y_{CP} in $D^0 - \bar{D}^0$ oscillation using quantum correlations in $e^+e^- \rightarrow D^0\bar{D}^0$ at $\sqrt{s} = 3.773$ GeV," PLB 744, 339 (2015) (clean, but less precise than other methods: HFLAV 2016: $(0.835 \pm 0.155)\%$)

Strengths of CLEO/BES/τcF: (1) *Quantum Correlations — the* (*S*,*l*) *piece*



Strengths of CLEO/BES/tcF: (2) *Leptonic decays* $-D^+ \rightarrow \mu^+ \nu_{\mu}$



ETM 11A ETM 09

180 200 220 240

212.15(1.45) MeV

BESIII has the most precise measurement of $D^+ \rightarrow \mu^+ \nu_{\mu}$:



 $f_{D^+} = (203.2 \pm 5.3 \pm 1.8) \text{ MeV}$

(still statistics limited)

BESIII, "Precision measurements of $B(D^+ \to \mu^+ \nu_{\mu})$, the pseudoscalar decay constant f_{D^+} , and the quark mixing matrix element $|V_{cd}|$," PRD 89, 051104(R) (2014)

230 250 270 MeV

248.83(1.27) MeV



Strengths of CLEO/BES/\tau cF: (2) *Leptonic decays* $- D_{s^+} \rightarrow \mu^+ \nu_{\mu}$



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= 2 + 1

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 $N_f = 2$



BESIII has the most precise measurement of $D_{s^+} \rightarrow \mu^+ \nu_{\mu}$:



 $f_{D_s} = (249.1 \pm 3.6 \pm 3.8) \text{ MeV}$

BESIII, "Measurement of $D_s^+ \to \mu^+ \nu_{\mu}$," preliminary (2017)

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Strengths of CLEO/BES/tcF: (4) *Charmed baryons — absolute BF's*

With 567 pb⁻¹ of data at 4.6 GeV (200k Λ_c), measure absolute BF's with double-tags:



$$B(\Lambda_c^+ \to pK^-\pi^+) = (5.84 \pm 0.27 \pm 0.23)\%$$

But compare to the Belle measurement: $B(\Lambda_c^+ \rightarrow pK^-\pi^+) = (6.84 \pm 0.24^{+0.21}_{-0.27})\%$ [Belle, PRL 113, 042002 (2014)]

(A reminder that it is important to measure the same quantities with different techniques.)

With higher energies, access absolute BF's for other charmed baryons.

BESIII, "Measurements of absolute hadronic branching fractions of the Λ_c^+ baryon," PRL 116, 052001 (2016)

Strengths of CLEO/BES/ τcF : (4) *Charmed baryons* $-\sigma(e^+e^- \rightarrow \Lambda_c^+\Lambda_c^-)$

Also study the production of charmed baryons...



\sqrt{s} (MeV)	$\mathcal{L}_{int}~(pb^{-1})$	$f_{\rm ISR}$	σ (pb)
4574.5	47.67	0.45	$236 \pm 11 \pm 46$
4580.0	8.54	0.66	$207\pm17\pm13$
4590.0	8.16	0.71	$245\pm19\pm16$
4599.5	566.93	0.74	$237\pm3\pm15$

(interesting results even with small data sets)

Scanning in E_{CM} would be an important tool at a τ -charm factory.

BESIII, "Precision measurement of the $e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$ cross section near threshold," PRL 120, 132001 (2018)

Strengths of CLEO/BES/\tau cF: (5) *Rare decays* $- J/\psi \rightarrow D^0 e^+ e^-$

Besides the usual open charm decays, J/ψ decays might provide a complementary approach...



$$B(J/\psi \to D^0 e^+ e^-) < 8.5 \times 10^{-8} (90\% \text{ C.L.})$$

BESIII, "Search for the rare decays $J/\psi \rightarrow D^0 e^+ e^- + \text{c.c.}$ and $\psi(3686) \rightarrow D^0 e^+ e^- + \text{c.c.}$," PRD 96, 111101(R) (2017)

UL is factor of $10^2 - 10^4$ above SM expectations (*but c.f.* $B(D^0 \rightarrow \gamma \gamma)$, $10^1 - 10^2$ above SM) \Rightarrow might be competitive

Strengths of CLEO/BES/\tau cF: (5) *Rare decays* – *LFV*

Other ideas to probe new physics with quarkonia decays...



 \dots a τ -charm factory would be ideally suited for this.

Strengths of CLEO/BES/tc-Factory

(1) Quantum-correlated pairs of D-mesons

 \Rightarrow complementary to other mixing and CP studies (*and input for B* \rightarrow *DK*)

(2) Leptonic decays

 \Rightarrow precision QCD and tests of lepton-flavor universality

(3) Special hadronic decays (*e.g.* $D^+ \rightarrow \pi^+ \pi^0$)

 \Rightarrow CP asymmetries and absolute branching fractions

(4) Charmed baryons

 \Rightarrow absolute branching fractions and features of production

(5) Rare decays (also from charmonium)

 \Rightarrow complementary searches

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(5) Rare decays (also from charmonium)

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The statistics of LHCb and Belle II will be formidable... ... a super τ-charm factory would be formidable in a complementary way!