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Novel aspects of baryon-antibaryon production in e^+e^- annihilation

Andrzej Kupsc (UU)

$$e^+e^- \rightarrow J/\psi \rightarrow \Lambda \bar{\Lambda}:$$

G.Fäldt, AK PLB772 (2017) 16

Observation of Λ transverse polarization
 $\Rightarrow$ Determination of Λ decay parameter and CP test



arXiv:1808.08917

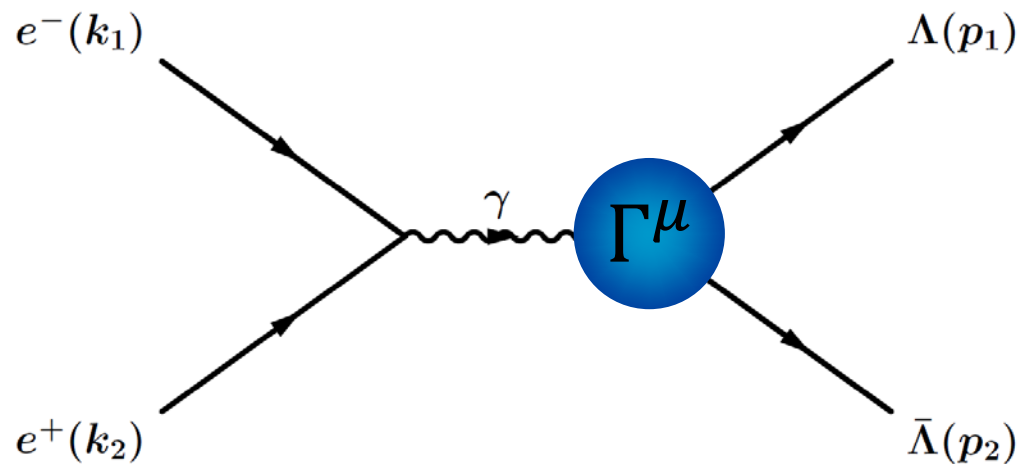
Outlook $\rightarrow$ general formalism:

$$e^+e^- \rightarrow J/\psi \rightarrow \Xi \bar{\Xi}$$

- decay parameters
- CP tests
- polarization tagging

E.Perotti, G.Fäldt, AK, S.Leupold, JJ.Song arXiv:1809.04038 $\rightarrow$ PRD

$$e^+ e^- \rightarrow \gamma^* \rightarrow B \bar{B} \text{ (spin } 1/2)$$



$$s = (p_1 + p_2)^2$$

$$q = p_1 - p_2$$

$$\Gamma^\mu(p_1, p_2) = -ie \left[\gamma^\mu F_1(s) + i \frac{\sigma^{\mu\nu}}{2M_B} q_\nu F_2(s) \right]$$

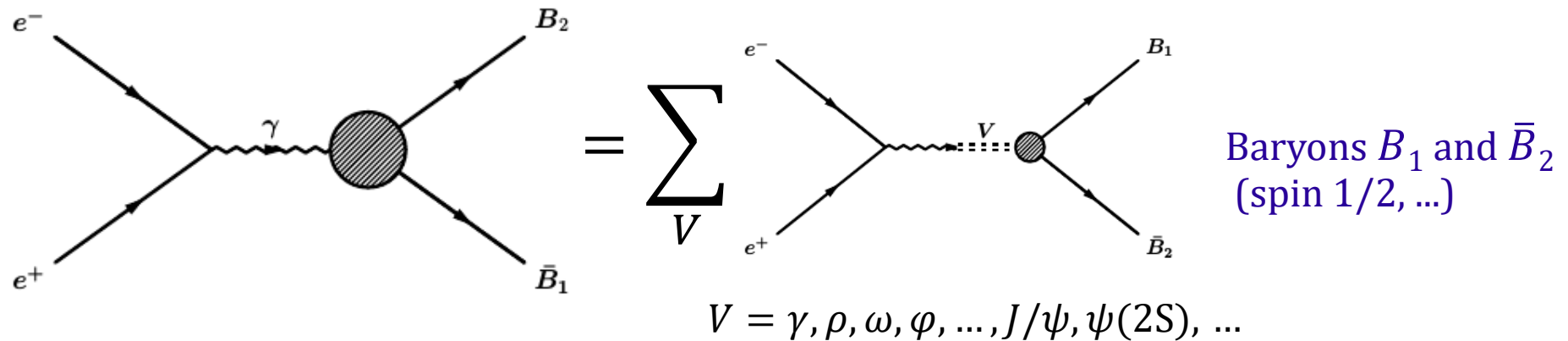
F_1 (Dirac) and F_2 (Pauli) Form Factors (complex)

Sachs Form Factors (FFs) $\Leftrightarrow$ helicity amplitudes:

$$G_M(s) = F_1(s) + F_2(s), \quad G_E(s) = F_1(s) + \tau F_2(s)$$

$$\tau = \frac{s}{4M_B^2}$$

Baryon FFs (continuum):



Cabibbo, Gatto PR124 (1961)1577

Time like spin 1/2 baryon FFs:

Dubnickova, Dubnicka, Rekaló

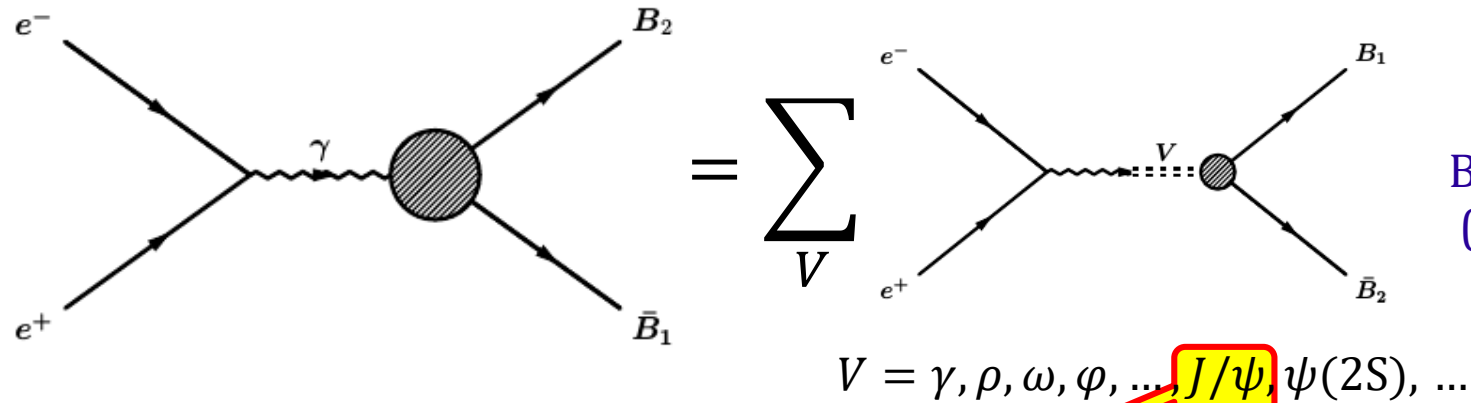
Nuovo Cim. A109 (1996) 241

Gakh, Tomasi-Gustafsson Nucl.Phys. A771 (2006) 169

Czyz, Grzelinska, Kuhn PRD75 (2007) 074026

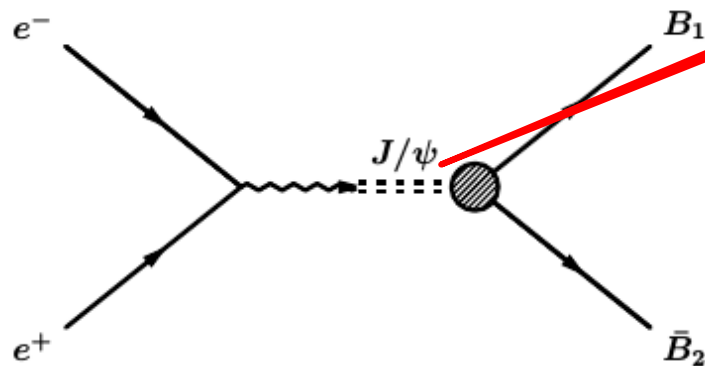
Fäldt EPJ A51 (2015) 74; EPJ A52 (2016)141

Baryon FFs (continuum):



Baryons B_1 and $\bar{B}_2$
(spin 1/2, ...)

vs J/ψ decay:



Both processes described by two
complex FFs: relative phase $\Delta\Phi$

Cabibbo, Gatto PR124 (1961)1577

Time like spin 1/2 baryon FFs:

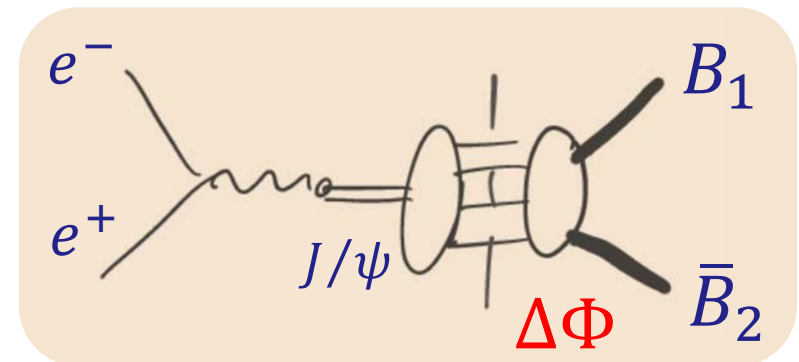
Dubnickova, Dubnicka, Rekaló

Nuovo Cim. A109 (1996) 241

Gakh, Tomasi-Gustafsson Nucl.Phys. A771 (2006) 169

Czyz, Grzelinska, Kuhn PRD75 (2007) 074026

Fäldt EPJ A51 (2015) 74; EPJ A52 (2016)141



Charmonia decays:

Fäldt, Kupsc PLB772 (2017) 16

$$e^+ e^- \rightarrow \gamma^* \rightarrow B\bar{B}$$

For spin $\frac{1}{2}$ $B\bar{B}$ production two complex FFs: $G_M(s)$, $G_E(s)$

$\Rightarrow$ process described by three parameters at fixed $\sqrt{s}$:

- ☐ cross section (σ)
- ☐ FFs ratio R or angular distribution parameter α_ψ
- ☐ relative phase between FFs ($\Delta\Phi$)

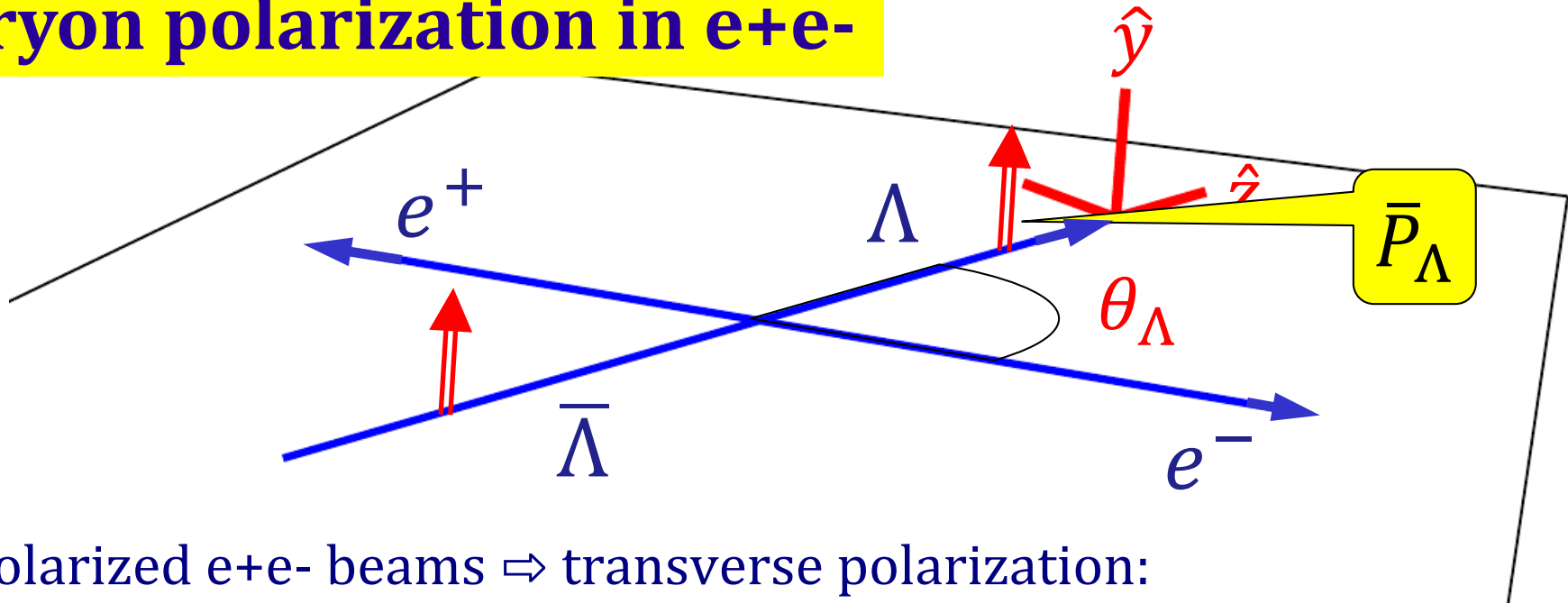
$$R = \left| \frac{G_E}{G_M} \right| \quad \left(\alpha_\psi = \frac{\tau - R^2}{\tau + R^2} \right) \quad G_E = R G_M e^{i\Delta\Phi}$$

Angular distribution:

$$\frac{d\Gamma}{d\Omega} \propto 1 + \alpha_\psi \cos^2\theta \quad -1 \leq \alpha_\psi \leq 1$$

Phase $\Delta\Phi$ expected/predicted for continuum
but neglected/not expected for the decays

Baryon polarization in e+e-

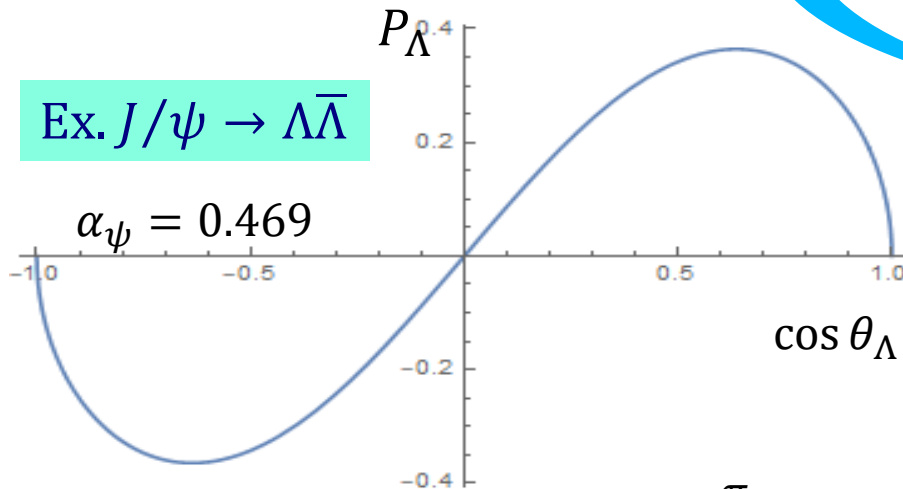


Unpolarized e+e- beams $\Rightarrow$ transverse polarization:

$$P_\Lambda(\cos \theta_\Lambda) = \frac{\sqrt{1 - \alpha_\psi^2} \cos \theta_\Lambda \sin \theta_\Lambda}{1 + \alpha_\psi \cos^2 \theta_\Lambda} \sin(\Delta\Phi)$$

Ex. $J/\psi \rightarrow \Lambda \bar{\Lambda}$

$\alpha_\psi = 0.469$



Max $P_\Lambda = 36.4\%$

if $\Delta\Phi = \frac{\pi}{2}$

$\Delta\Phi \neq 0$

Spin 1/2 baryon octet

$n(udd)$

$p(uud)$

$\Lambda(uds)$

$\Sigma^0(uds)$

$\Sigma^+(uus)$

$\Xi^-(dss)$

$\Xi^0(uss)$

hyperon	Mass [GeV/c ²]	$c\tau$ [cm]	decay (BF)
$\Lambda(uds)$	1.116	7.9	$p\pi^-$ (63.9%) $n\pi^0$ (35.8%)
$\Sigma^-(dds)$	1.197	4.4	$n\pi^-$ (99.8%)
$\Sigma^+(uus)$	1.189	2.4	$p\pi^0$ (51.6%) $n\pi^+$ (48.3%)
$\Xi^0(uss)$	1.315	8.7	$\Lambda\pi^0$ (99.5%)
$\Xi^-(dss)$	1.321	5.1	$\Lambda\pi^-$ (99.8%)

Weak hadronic two body decays

$$Y \rightarrow B\pi: \quad 1/2 \rightarrow 1/2 + 0$$

s wave parity violating

p wave parity conserving

$$\alpha_Y = \frac{2\text{Re}(s^*p)}{|s|^2 + |p|^2}, \quad \beta_Y = \frac{2\text{Im}(s^*p)}{|s|^2 + |p|^2} = \sqrt{1 - \alpha_Y^2} \sin \phi_Y$$

$$\gamma_Y = \frac{|s|^2 - |p|^2}{|s|^2 + |p|^2} = \sqrt{1 - \alpha_Y^2} \cos \phi_Y$$

α_-

hyperon	decay (BF)	α	ϕ
$\Lambda(uds)$	$p\pi^-$ (63.9%)	0.642 ± 0.013	$-6.5^\circ \pm 3.5^\circ$
	$n\pi^0$ (35.8%)		
$\bar{\Lambda}(\bar{u}\bar{d}\bar{s})$	$\bar{p}\pi^+$ (63.9%)	-0.71 ± 0.08	—
$\Sigma^-(dds)$	$n\pi^-$ (99.8%)	-0.068 ± 0.008	$10^\circ \pm 15^\circ$
$\Sigma^+(uus)$	$p\pi^0$ (51.6%)	-0.980 ± 0.017	$36^\circ \pm 34^\circ$
	$n\pi^+$ (48.3%)	-0.068 ± 0.013	$167 \pm 20^\circ$
$\Xi^0(uss)$	$\Lambda\pi^0$ (99.5%)	-0.406 ± 0.085	$21^\circ \pm 12^\circ$
$\Xi^-(dss)$	$\Lambda\pi^-$ (99.8%)	-0.458 ± 0.012	$-2.1^\circ \pm 0.8^\circ$

α_0

α_+

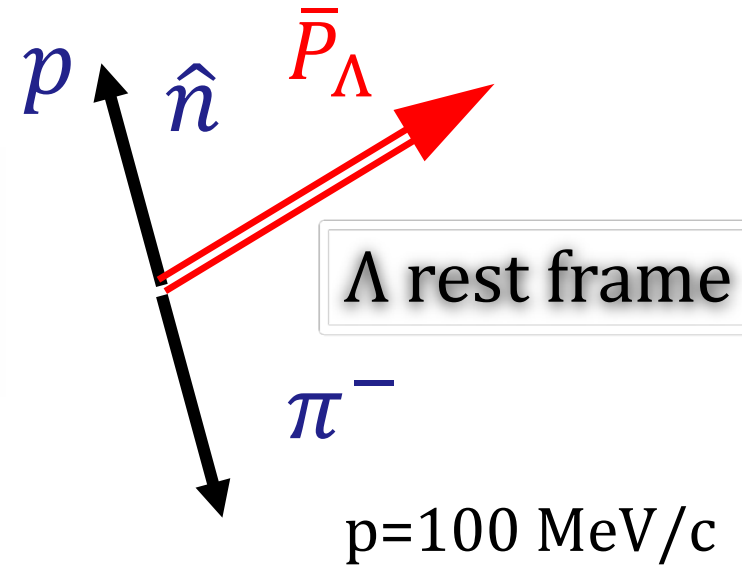
Weak decay $\Lambda \rightarrow p\pi^-$

Polarization of Λ is determined using this decay in all experiments.

Relies on:

$$\alpha_- = 0.642 \pm 0.013$$

Value in PDG unchanged since 1978: average based on 1963-75 experiments



$$\frac{d\Gamma}{d\Omega} = \frac{1}{4\pi} (1 + \alpha_- \hat{n} \cdot \bar{P}_\Lambda)$$

CP odd asymmetries

Compare partial decay widths

$$\frac{\Gamma - \bar{\Gamma}}{\Gamma + \bar{\Gamma}}$$

$$A_{CP} = \frac{\alpha + \bar{\alpha}}{\alpha - \bar{\alpha}}$$

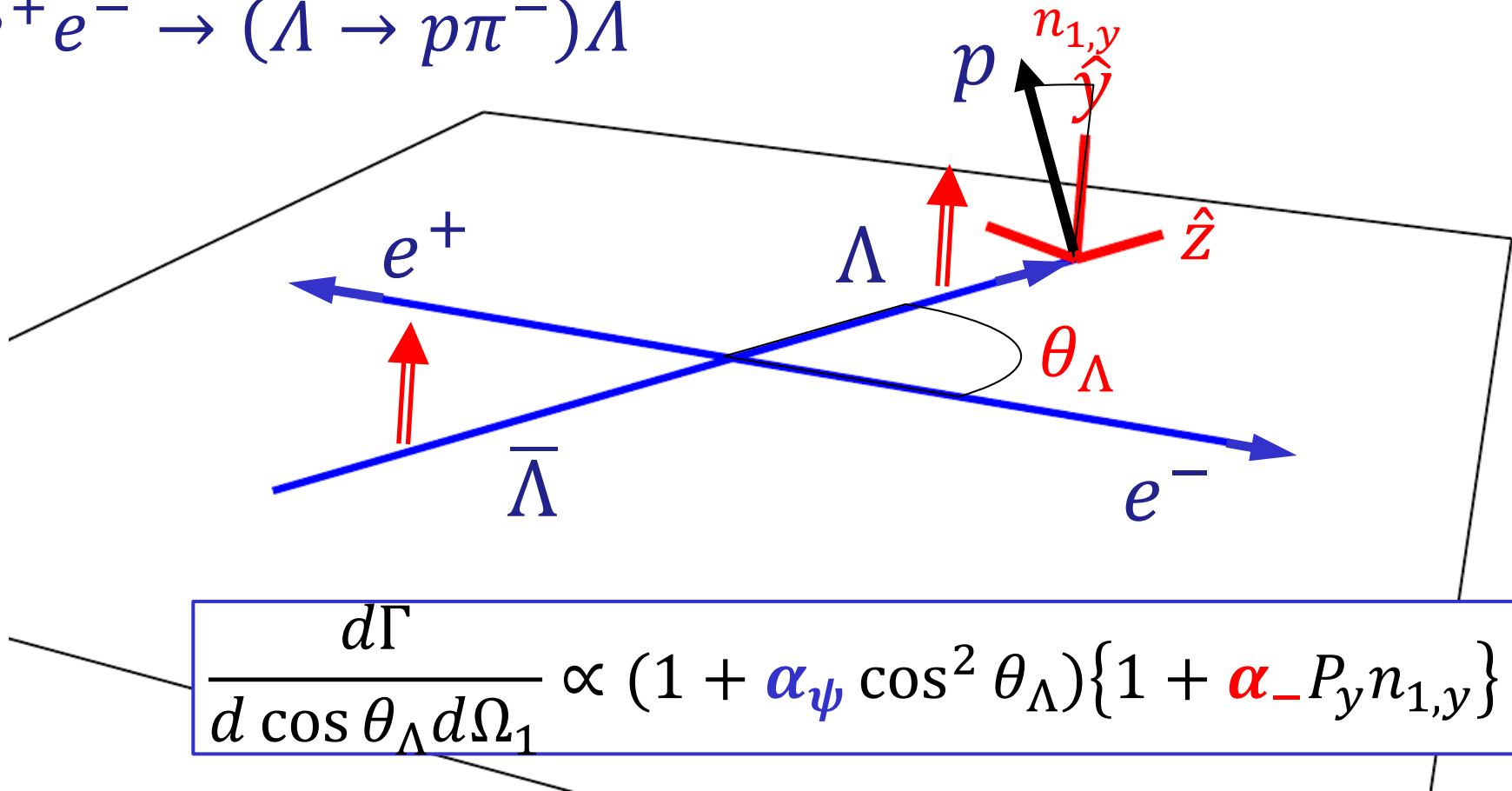
For sequential decays: ϕ (β) is accessible

$$\beta = \sqrt{1 - \alpha^2} \sin \phi$$

$$B_{CP} = \frac{\beta + \bar{\beta}}{\beta - \bar{\beta}}$$

Inclusive angular distribution

$$e^+e^- \rightarrow (\Lambda \rightarrow p\pi^-)\bar{\Lambda}$$



$$\Lambda \rightarrow p\pi^-: \hat{\mathbf{n}}_1 \rightarrow \Omega_1 = (\cos \theta_1, \phi_1) : \alpha_-$$

$\Rightarrow$ Determine product: $\alpha_- \cdot \sin(\Delta\Phi)$

Exclusive joint angular distribution

$$e^+ e^- \rightarrow (\Lambda \rightarrow p\pi^-)(\bar{\Lambda} \rightarrow \bar{p}\pi^+)$$

$$\Lambda \rightarrow p\pi^-: \hat{\mathbf{n}}_1 \rightarrow (\cos \theta_1, \phi_1) : \alpha_- \quad \bar{\Lambda} \rightarrow \bar{p}\pi^+: \hat{\mathbf{n}}_2 \rightarrow (\cos \theta_2, \phi_2) : \alpha_+$$

$$\xi : (\cos \theta_\Lambda, \hat{\mathbf{n}}_1, \hat{\mathbf{n}}_2) \quad \text{5D PhSp}$$

$$d\Gamma \propto W(\xi; \alpha_\psi, \Delta\Phi, \alpha_-, \alpha_+) =$$

$$1 + \alpha_\psi \cos^2 \theta_\Lambda \quad \text{Cross section}$$

$$+ \alpha_- \alpha_+ \left\{ \sin^2 \theta_\Lambda (n_{1,x} n_{2,x} - \alpha_\psi n_{1,y} n_{2,y}) + (\cos^2 \theta_\Lambda + \alpha_\psi) n_{1,z} n_{2,z} \right\} \quad \text{Spin correlations}$$

$$+ \alpha_- \alpha_+ \sqrt{1 - \alpha_\psi^2} \cos(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda (n_{1,x} n_{2,z} + n_{1,z} n_{1,x})$$

$$+ \sqrt{1 - \alpha_\psi^2} \sin(\Delta\Phi) \sin \theta_\Lambda \cos \theta_\Lambda (\alpha_- n_{1,y} + \alpha_+ n_{2,y}) \quad \text{Polarization}$$

$\Delta\Phi \neq 0 \Rightarrow$ independent determination of α_- and α_+

$J/\psi, \psi(2S) \rightarrow B\bar{B}$

decay mode	events			$\mathcal{B}(\text{units } 10^{-4})$
$J/\psi \rightarrow \Lambda\bar{\Lambda}$	440675	$\pm$	670	$19.43 \pm 0.03 \pm 0.33$
$\psi(2S) \rightarrow \Lambda\bar{\Lambda}$	31119	$\pm$	187	$3.97 \pm 0.02 \pm 0.12$
$J/\psi \rightarrow \Sigma^0\bar{\Sigma}^0$	111026	$\pm$	335	$11.64 \pm 0.04 \pm 0.23$
$\psi(2S) \rightarrow \Sigma^0\bar{\Sigma}^0$	6612	$\pm$	82	$2.44 \pm 0.03 \pm 0.11$
$J/\psi \rightarrow \Xi^0\bar{\Xi}^0$	134846	$\pm$	437	11.65 ± 0.04
$\psi(2S) \rightarrow \Xi^0\bar{\Xi}^0$	10839	$\pm$	123	2.73 ± 0.03
$J/\psi \rightarrow \Xi^-\bar{\Xi}^+$	42811	$\pm$	231	10.40 ± 0.06
$\psi(2S) \rightarrow \Xi^-\bar{\Xi}^+$	5337	$\pm$	83	2.78 ± 0.05

PRD 93, 072003 (2016)

PLB770,217 (2017)

PRD 95, 052003 (2017)

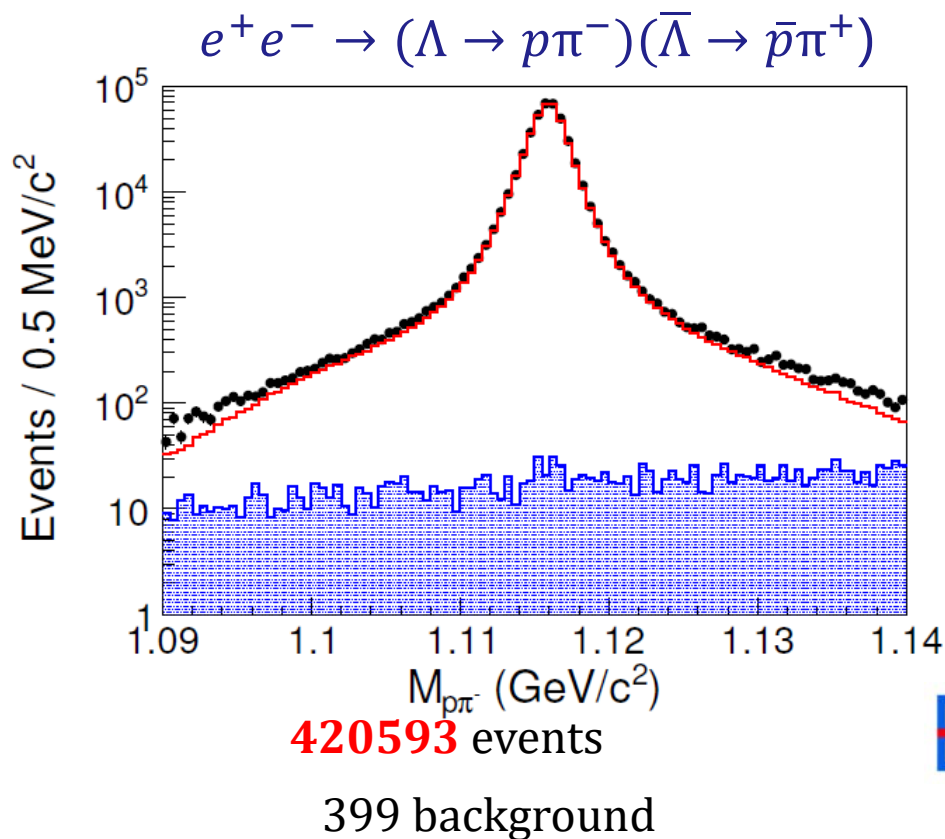
BESIII

$1.31 \times 10^9 J/\psi$

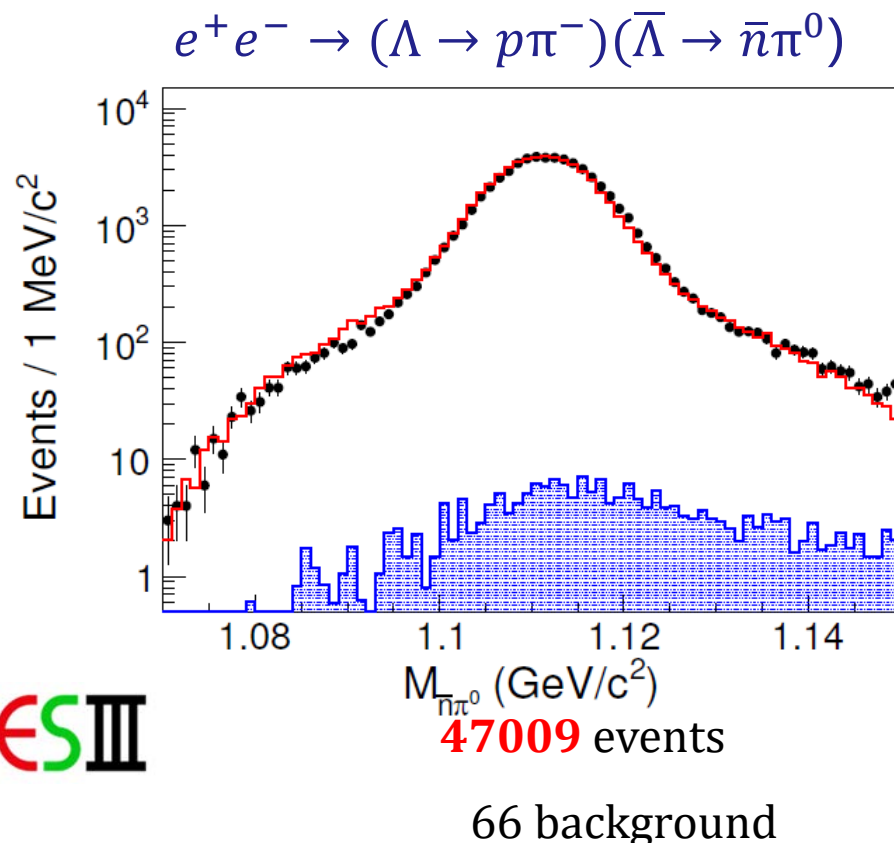
and $(4.48) \times 10^8 \psi(2S)$

$0.223 \times 10^9 J/\psi$

Now (Feb 2019): $10^{10} J/\psi$



BESIII



Global unbinned maximum log likelihood fit to the two data sets with the likelihood function constructed from probability function:

$$\mathcal{C}(\alpha_\psi, \Delta\Phi, \alpha_-, \alpha_2) \mathcal{W}(\xi_i; \alpha_\psi, \Delta\Phi, \alpha_-, \alpha_2)$$

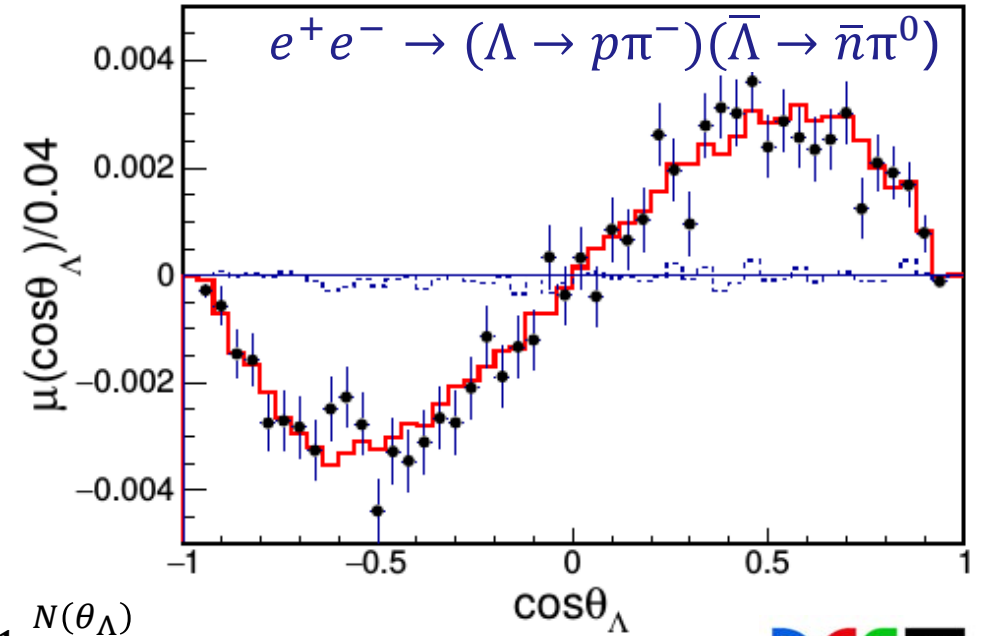
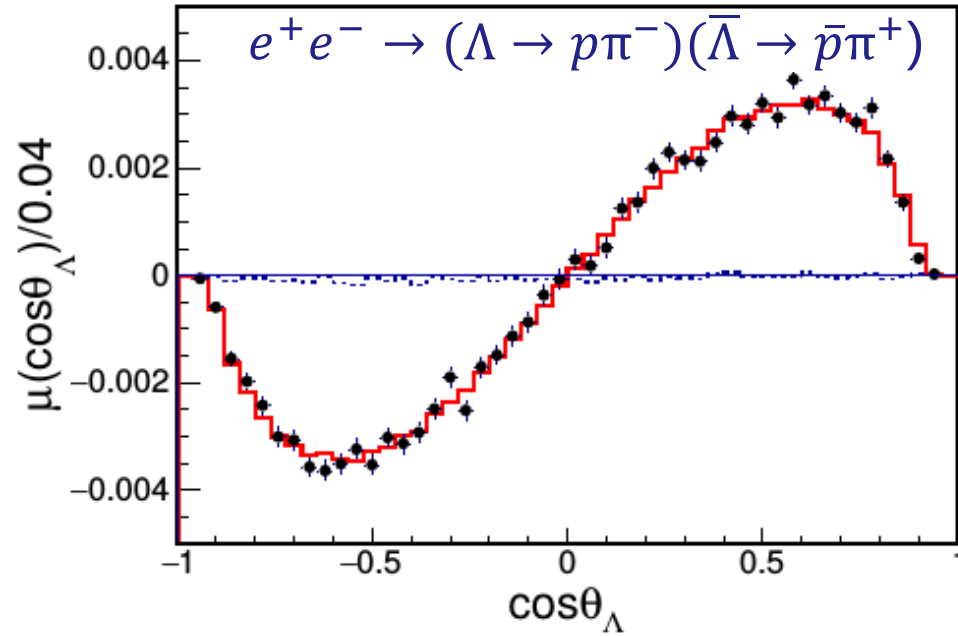
Where $\mathcal{C}(\alpha_\psi, \Delta\Phi, \alpha_-, \alpha_2)$ is the normalization factor obtained from $\mathcal{W}(\xi_i; \alpha_\psi, \Delta\Phi, \alpha_-, \alpha_2)$ weighted sum for flat phase space model MC events after detector reconstruction.

(1.31x10⁹ J/ψ)

arXiv:1808.08917

Fit results

$$\Delta\Phi = 42.3^\circ \pm 0.6^\circ \pm 0.5^\circ$$



moment:

$$\mu(\cos \theta_\Lambda) = \frac{1}{N} \sum_{i=1}^{N(\theta_\Lambda)} \left(n_{1,y}^{(i)} - n_{2,y}^{(i)} \right)$$

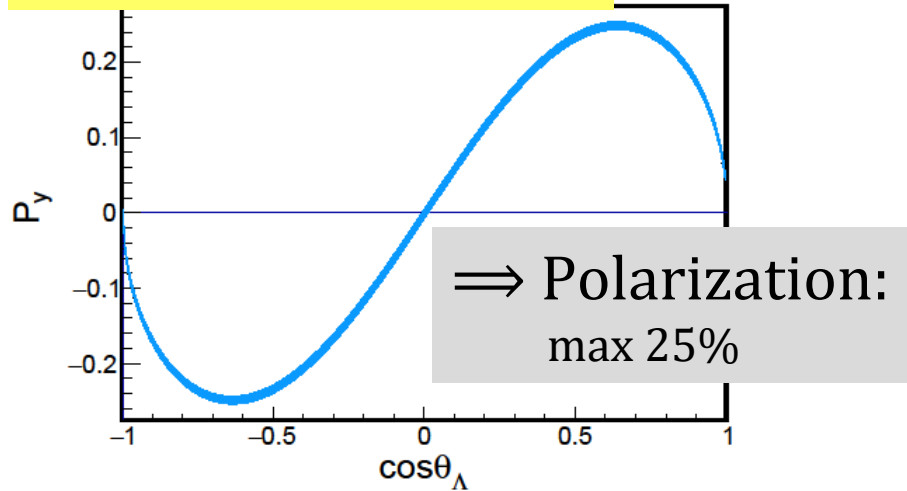
(uncorrected for acceptance)

BESIII

Parameters	This work	Previous results
α_ψ	$0.461 \pm 0.006 \pm 0.007$	0.469 ± 0.027 BESIII
$\Delta\Phi$ (rad)	$0.740 \pm 0.010 \pm 0.008$	—
α_-	$0.750 \pm 0.009 \pm 0.004$	0.642 ± 0.013 PDG
α_+	$-0.758 \pm 0.010 \pm 0.007$	-0.71 ± 0.08 PDG
$\bar{\alpha}_0$	$-0.692 \pm 0.016 \pm 0.006$	—

Implications of the $J/\psi \rightarrow \Lambda \bar{\Lambda}$ analysis

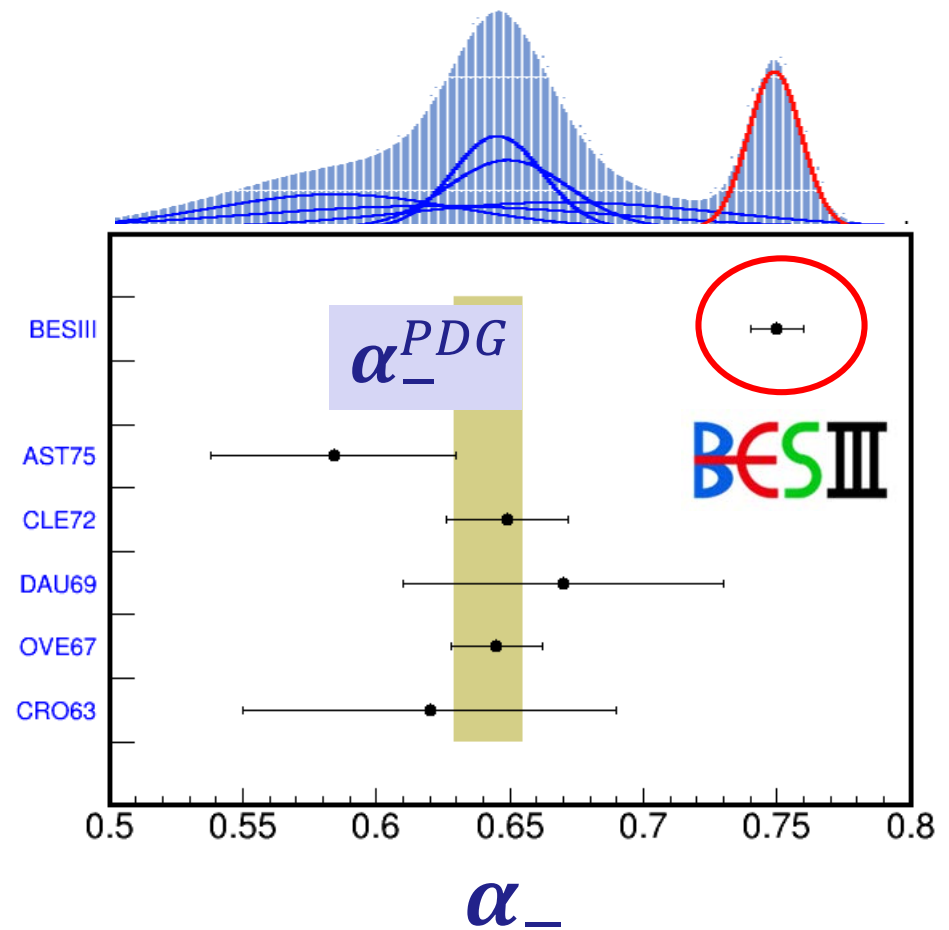
$$\Delta\Phi = 42.3^\circ \pm 0.6^\circ \pm 0.5^\circ$$



$\Rightarrow$ New value for e.g.
 $\alpha(\Omega \rightarrow \Lambda K)$, $\alpha(\Xi \rightarrow \Lambda \pi)$,
 $\alpha(\Lambda_c \rightarrow \Lambda K)$

$\Rightarrow$ Calls for reinterpretation of **all**
 Λ polarization measurements

$$\Lambda \rightarrow p\pi^-: \alpha_- = 0.750 \pm 0.009 \pm 0.004$$



17(3)% larger than α_-^{PDG}

Can one observe strange baryon CPV?

CP test: $A_{\Lambda} = \frac{\alpha_- + \alpha_+}{\alpha_- - \alpha_+}$

$A_{\Lambda} = -0.006 \pm 0.012 \pm 0.007$

BESIII

$J/\psi \rightarrow \Lambda \bar{\Lambda}$

Previous result (using αP product):

$A_{\Lambda} = 0.013 \pm 0.021$
PS185 PRC54(96)1877

	Events	Error A_{Λ}	
BESIII(2018)	$4.2 \cdot 10^5$	$1.2 \cdot 10^{-2}$	$1.31 \cdot 10^9 J/\psi$
BESIII	$3 \cdot 10^6$	$5 \cdot 10^{-3}$	$10^{10} J/\psi$ $L=0.47 \cdot 10^{33} \Delta\sqrt{s} = 0.9 \text{ MeV}$
SCTF	$6 \cdot 10^8$	$3 \cdot 10^{-4}$	$L=10^{35} \text{ cm}^{-2}\text{s}^{-1}$ $2 \cdot 10^{12} J/\psi$
SCTF+ ΔE ?	$3 \cdot 10^9$	$1.4 \cdot 10^{-4}$	$10^{12} J/\psi$

a guess

CKM $A_{\Lambda} \sim (1-5) \cdot 10^{-5}$

$$e^+e^- \rightarrow \Xi^- \bar{\Xi}^+ \rightarrow \Lambda \pi^- \bar{\Lambda} \pi^+ \rightarrow p \pi^- \pi^- \bar{p} \pi^+ \pi^+$$

$$d\Gamma \propto W(\xi; \boldsymbol{\pi}) \quad \xi \quad 9 \text{ kinematical variables } 9\text{D PhSp}$$

Parameters: 2 production + 6 decay chains

$$\boldsymbol{\pi} = (\alpha_\psi, \Delta\Phi, \overbrace{\alpha(\Xi^-), \phi(\Xi^-), \alpha_-, \alpha(\bar{\Xi}^+), \phi(\bar{\Xi}^+), \alpha_+})$$

Variables and parameters
factorize:

$$W(\xi; \boldsymbol{\pi}) = \sum_{k=1}^M f_k(\boldsymbol{\pi}) T_k(\xi)$$

$$\Delta\Phi \neq 0 \Rightarrow M = 72 \quad \begin{matrix} \Xi^- \bar{\Xi}^+ & \Lambda \bar{\Lambda} \end{matrix} \quad (7)$$

$$\Delta\Phi = 0 \Rightarrow M = 56 \quad (5)$$

$\Delta\Phi \neq 0$ is not necessary!

but $\Delta\Phi \neq 0$ increases sensitivity...

Can one observe strange baryon CPV?

$$\Xi^- \rightarrow \Lambda \pi^- \rightarrow p \pi^- \pi^-$$

$$A_{\Xi\Lambda} = (0.0 \pm 5.1 \pm 4.4) \times 10^{-4} \quad 1.2 \times 10^8 \Xi^- \quad 4.1 \times 10^7 \bar{\Xi}^+$$

$$\frac{[\alpha(\Xi^-)\alpha_-(\Lambda) - \alpha(\bar{\Xi}^+)\alpha_+(\bar{\Lambda})]}{[\alpha(\Xi^-)\alpha_-(\Lambda) + \alpha(\bar{\Xi}^+)\alpha_+(\bar{\Lambda})]}$$

present best limit...

HyperCP PRL 93 (2004) 262001

$$e^+ e^- \rightarrow J/\psi \rightarrow \Xi^- \bar{\Xi}^+ \rightarrow \Lambda \pi^- \bar{\Lambda} \pi^+ \rightarrow p \pi^- \pi^- \bar{p} \pi^+ \pi^+$$

$$\{1 + \alpha(\Xi^-)\alpha_-(\Lambda) \cos \theta_p\} \{1 + \alpha(\bar{\Xi}^+)\alpha_+(\bar{\Lambda}) \cos \theta_{\bar{p}}\}$$

...just (random) 4 terms out of 72 ...

4.3×10^4 BESIII PRD93,072003 ($0.223 \times 10^9 J/\psi$) $\Rightarrow$ 2×10^6 (BESIII $10^{10} J/\psi$)

STCF ($200 \times$): $4 \times 10^8 \Rightarrow \text{Error } A_{\Xi\Lambda} \sim 1.6 \times 10^{-4}$

primitive
guess

$$\begin{aligned} -3 \times 10^{-5} &\leq A_{\Lambda} \leq 4 \times 10^{-5} \\ -2 \times 10^{-5} &\leq A_{\Xi} \leq 1 \times 10^{-5} \\ -5 \times 10^{-5} &\leq A_{\Xi\Lambda} \leq 5 \times 10^{-5} \end{aligned}$$

CKM

Tandean, Valencia PRD67 (2003) 056001

s/p amplitude ratio

Λ

Ξ

PDG

0.368(11)

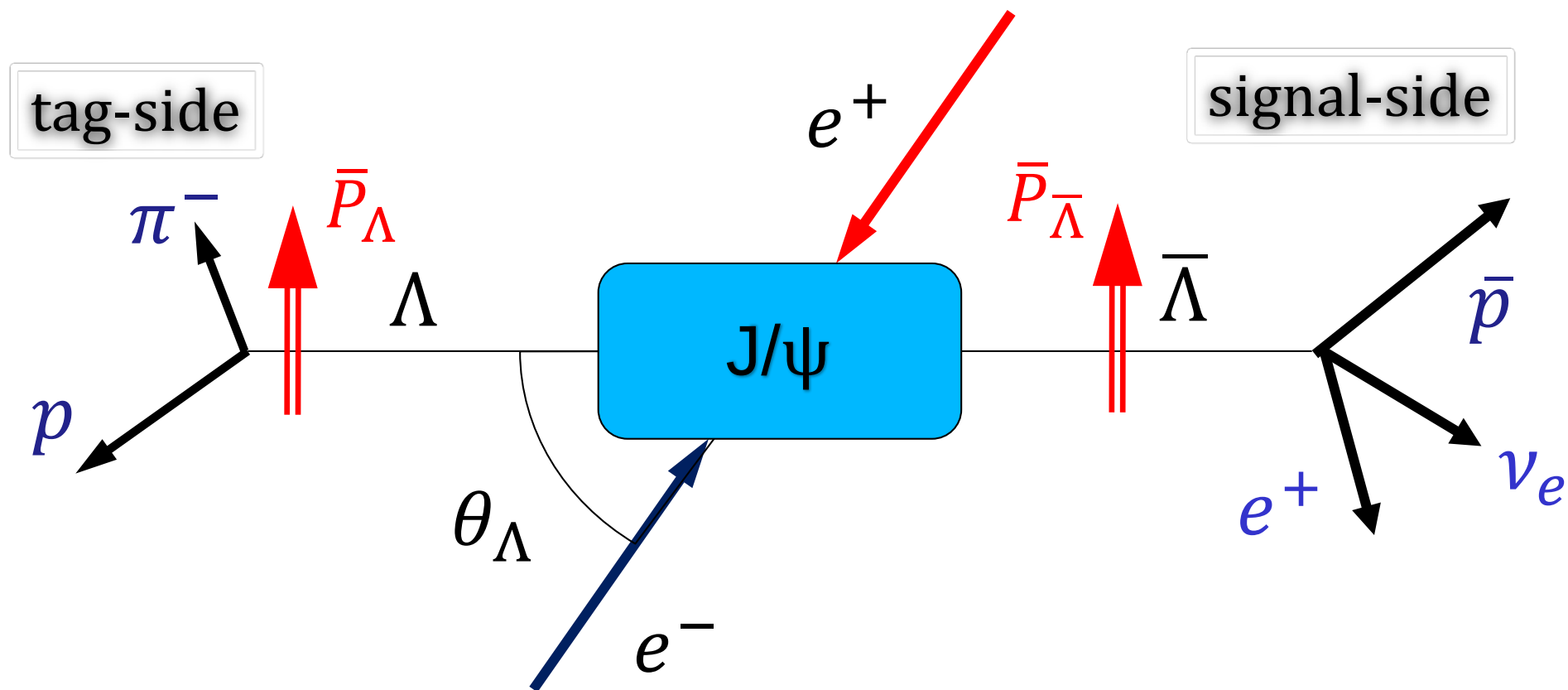
0.243(13)

BESIII

0.455(10)

0.204(10)

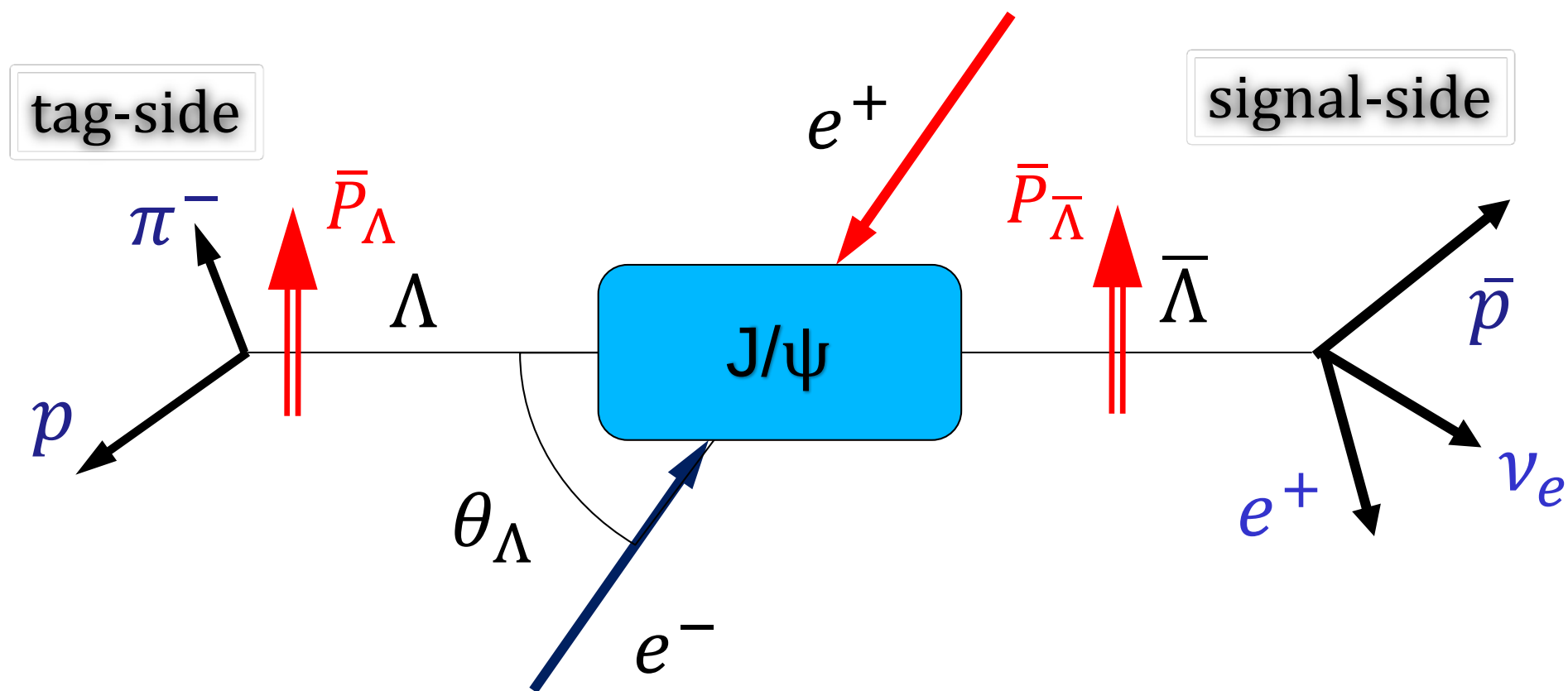
Double tag: polarization + spin correlations ...



"Byproduct" of BESIII and STCF run at $J/\psi, \psi'$:

$10^6 \div 10^9$ $B\bar{B}$ data samples: rare decays,
decay parameters

Double tag: polarization + spin correlations ...

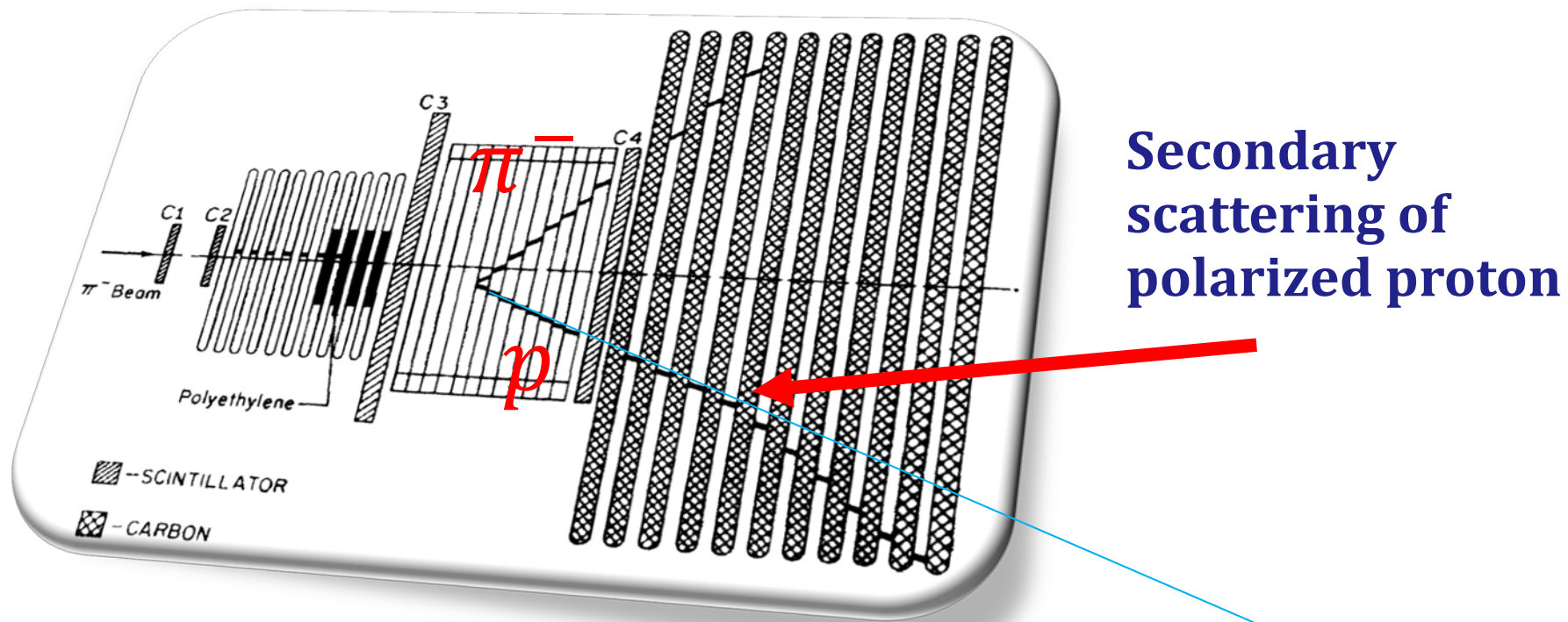


"Byproduct" of BESIII and STCF run at $J/\psi, \psi'$:

$10^6 \div 10^9$ $B\bar{B}$ data samples: rare decays,
decay parameters

Thank you!

$$\Lambda \rightarrow p\pi^-$$



Principle of previous α_- measurements

Cronin, Overseth Phys. Rev. 129, 1795 (1963)

Overseth, Roth Phys. Rev. Lett. 19, 391 (1967)