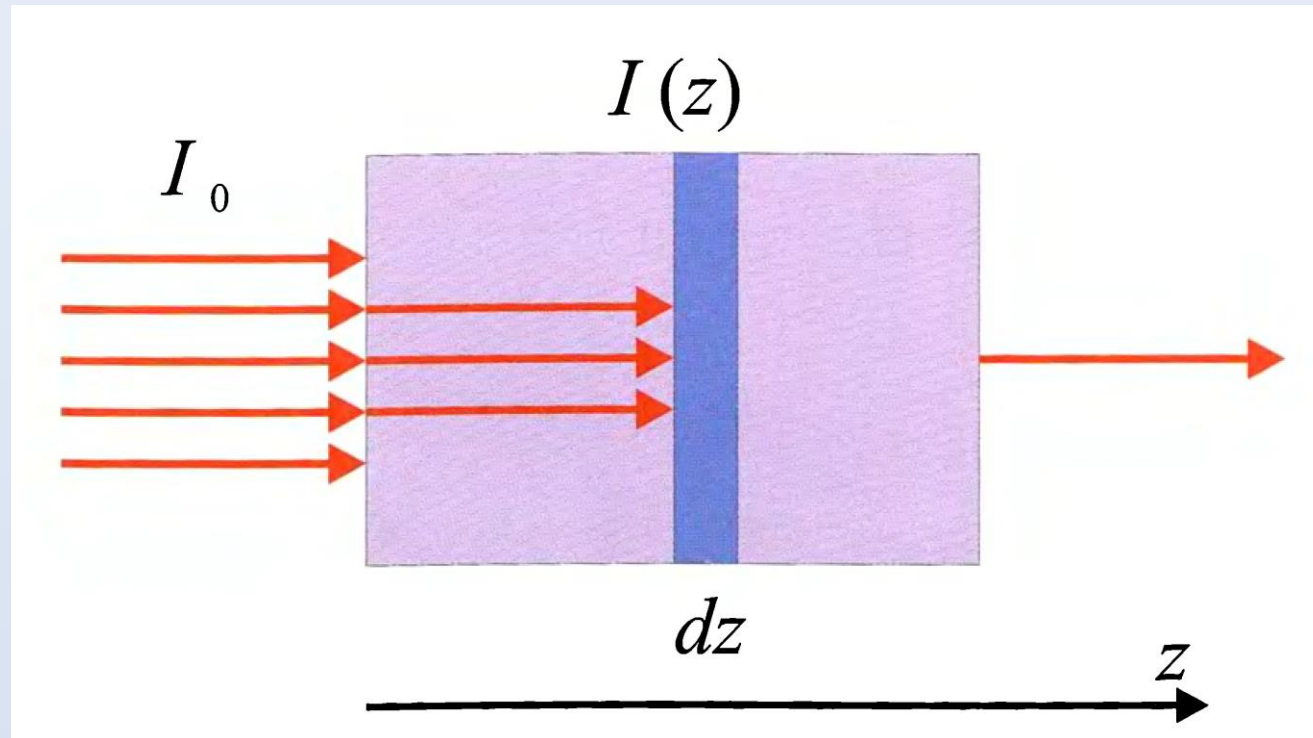


Mathematical modeling of thermal loads of x-ray adaptive optics materials

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The X-rays interaction physics with matter (heat release)

Photoelectric absorption

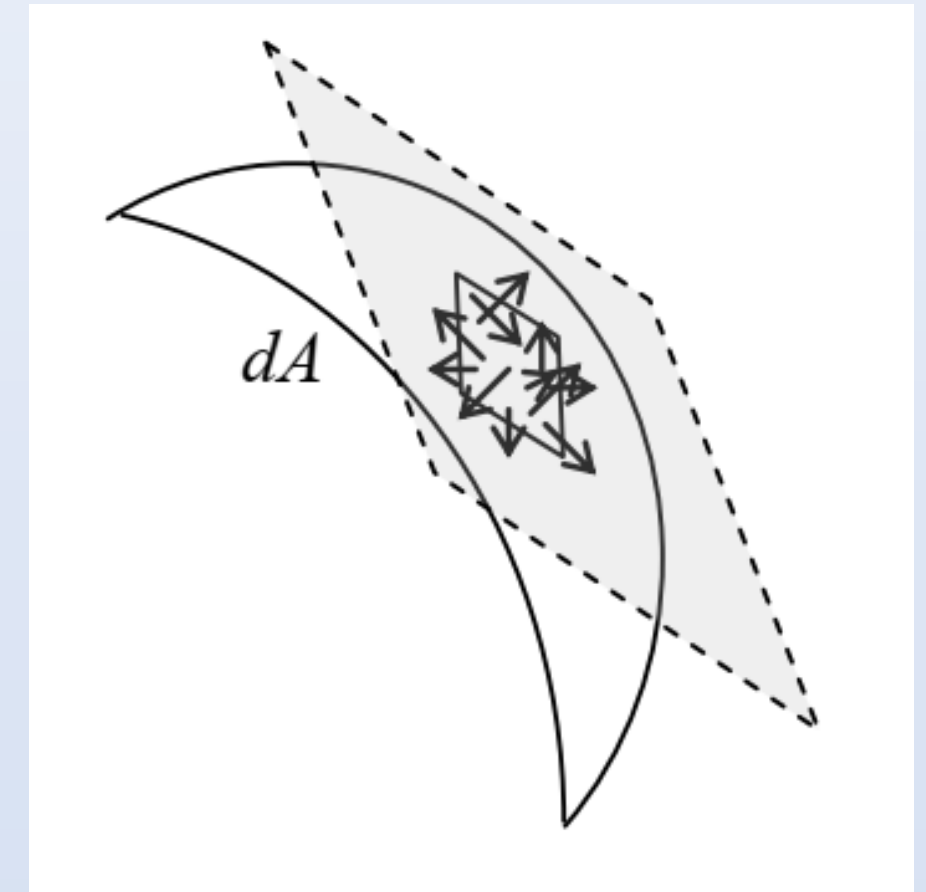


$$P = P_0 \exp(-\mu z)$$

$$P_{\text{abs}} = AP_{\text{init}} \exp\left(-\frac{x^2}{\sigma_x^2} - \frac{y^2}{\sigma_y^2}\right)$$

$$P_{\text{abs}} = AP_{\text{init}} \exp\left(-\frac{x^2}{\sigma_x^2} - \frac{y^2}{\sigma_y^2} - \mu z\right)$$

Radiative heat transfer



The mathematical formulation of the problem

Fourier heat equation

$$\lambda \nabla T = -AP_{\text{init}} \exp\left(-\frac{x^2}{\sigma_x^2} - \frac{y^2}{\sigma_y^2} - \mu z\right)$$

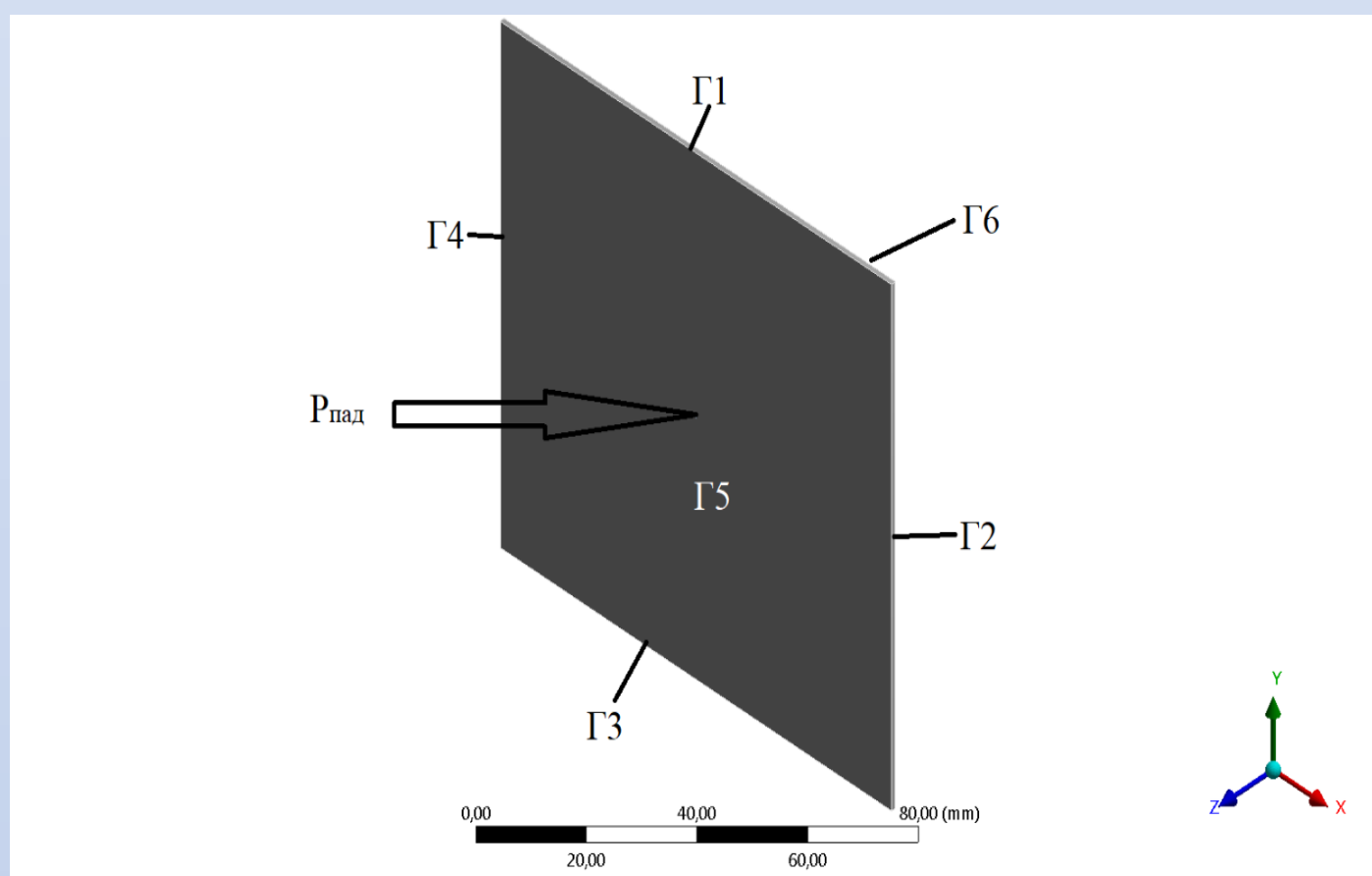
Initial condition

$$T|_{\Gamma_1} = T|_{\Gamma_2} = T|_{\Gamma_3} = T|_{\Gamma_4} = T|_{\Gamma_5} = T|_{\Gamma_6} = T_0 = 22 \text{ } ^\circ\text{C}$$

Boundary condition

$$P|_{\Gamma_1} = P|_{\Gamma_2} = P|_{\Gamma_3} = P|_{\Gamma_4} = P|_{\Gamma_5} = P|_{\Gamma_6} = 5 \cdot 10^{-6} \text{ W/mm}^2$$

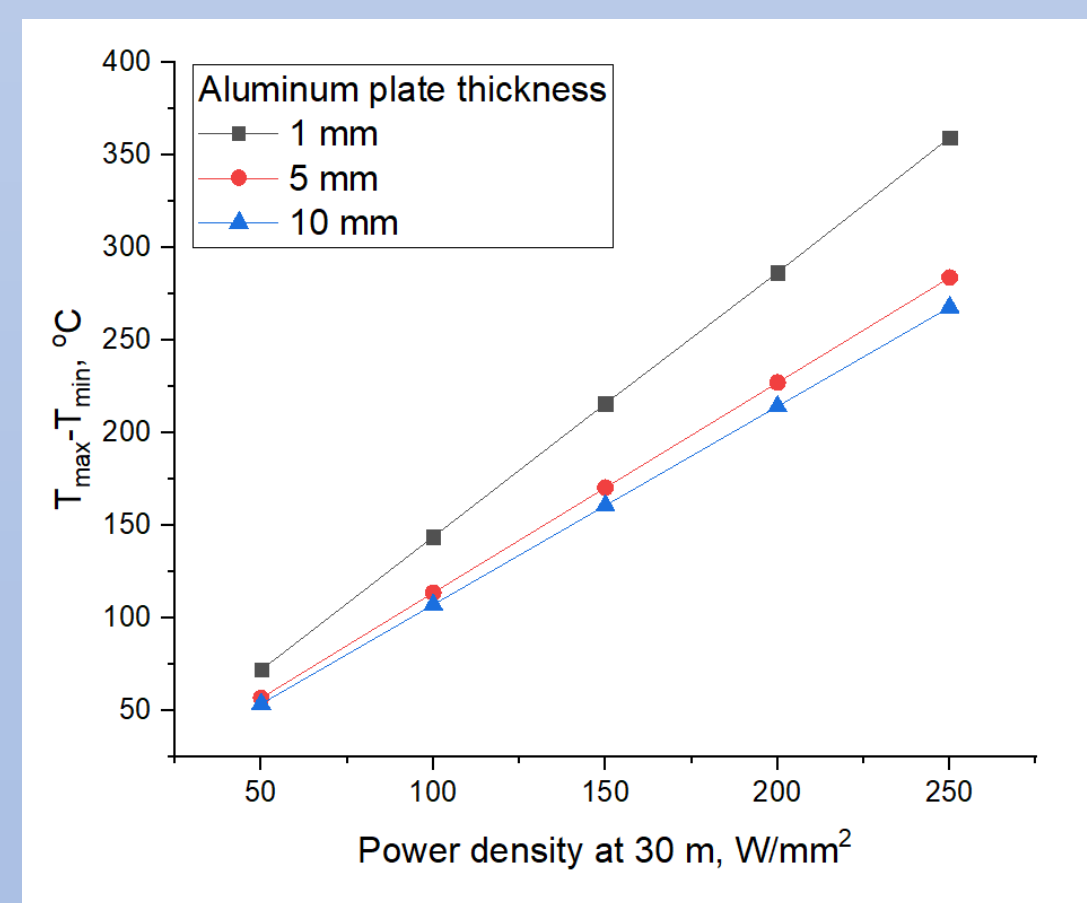
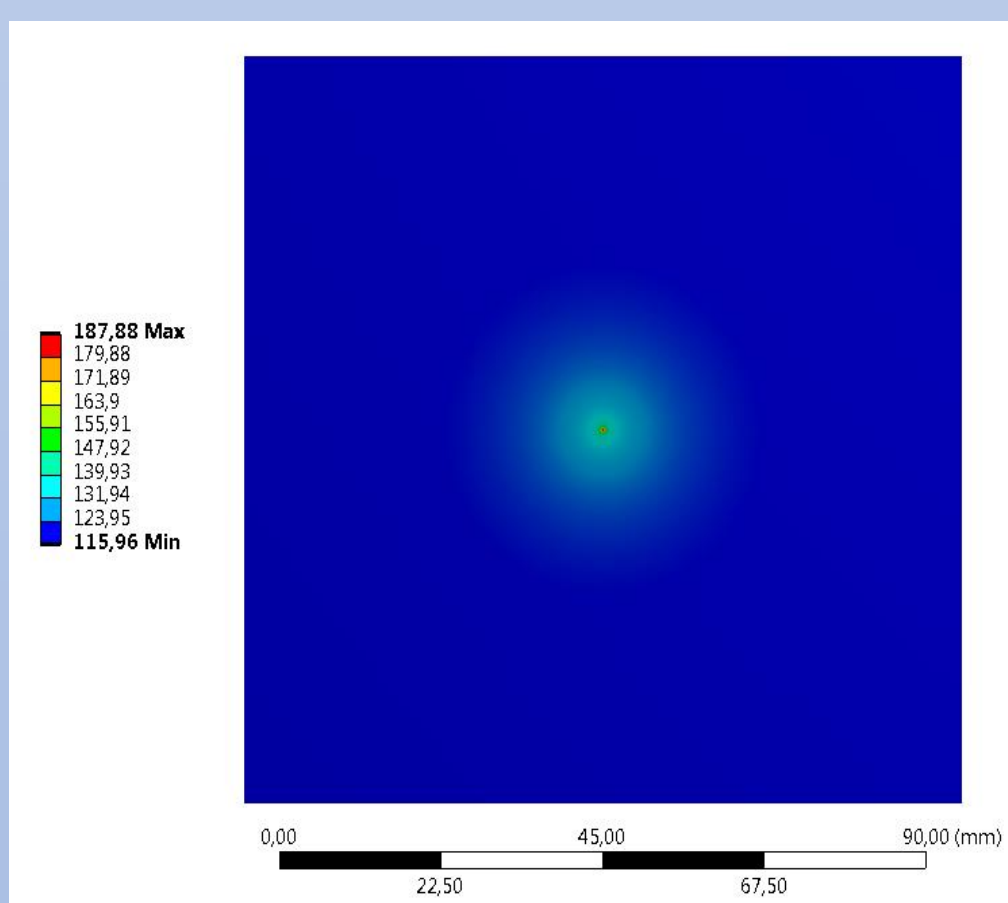
$$P|_{\Gamma_1} = P|_{\Gamma_2} = P|_{\Gamma_3} = P|_{\Gamma_4} = P|_{\Gamma_5} = P|_{\Gamma_6} = \sigma \cdot T^4 \text{ W/mm}^2$$



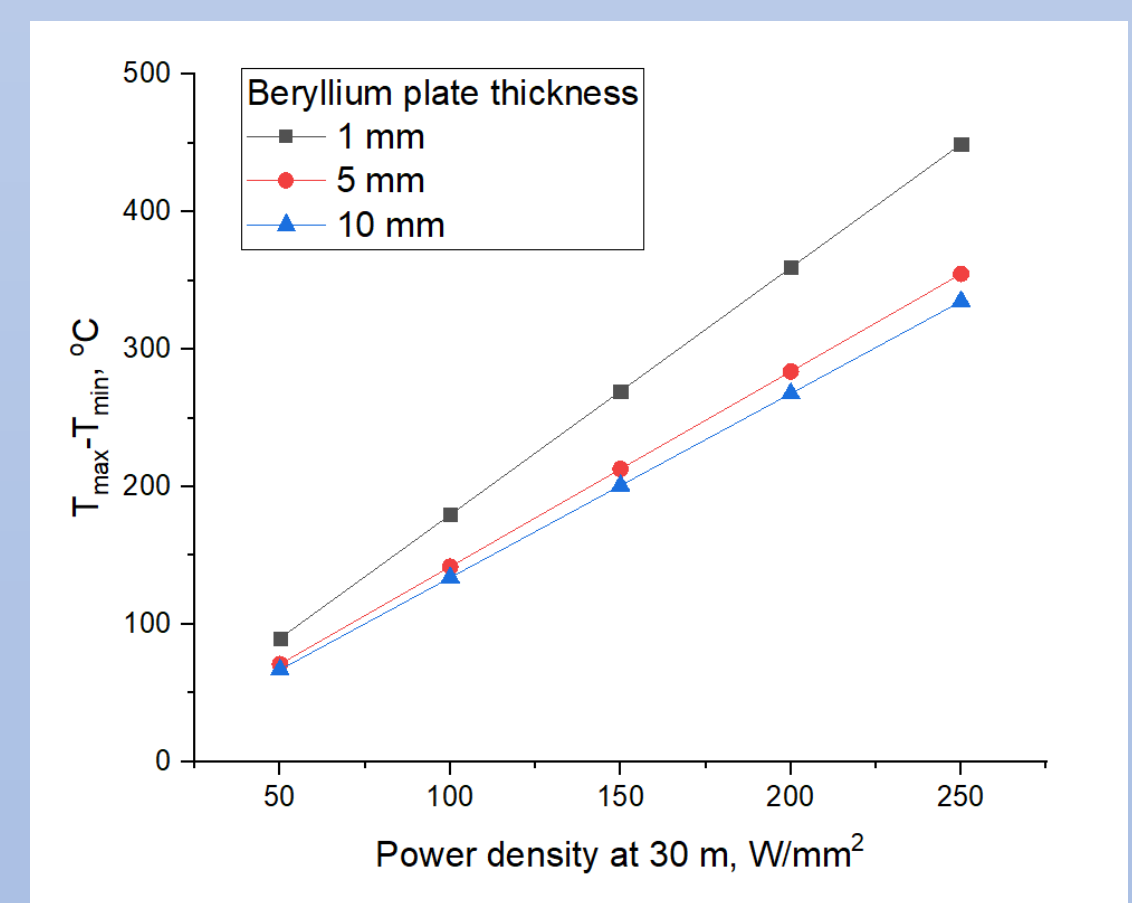
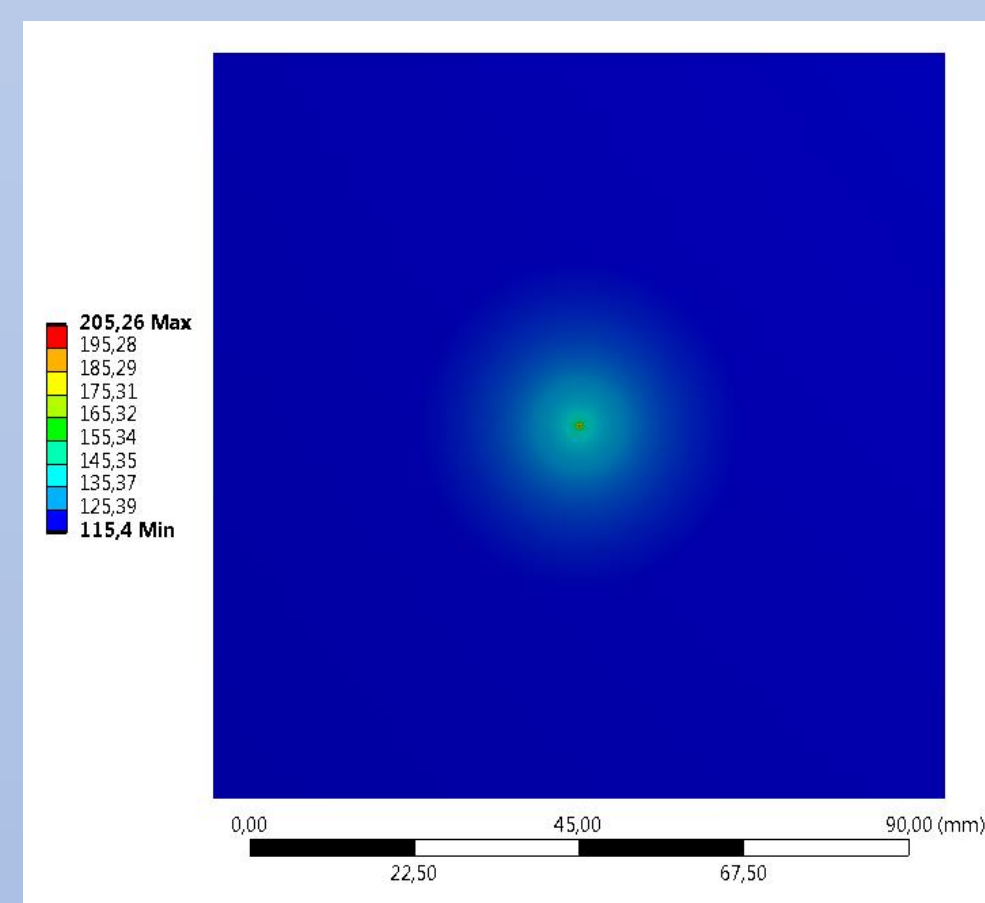
Material	Wavelength, A	Material absorption coefficient, mkm ⁻¹
Aluminum	1	3.5 * 10 ⁻³
	0.5	4.191 * 10 ⁻⁴
	0.25	4.718 * 10 ⁻⁵
Beryllium	1	3.992 * 10 ⁻⁵
	0.5	3.954 * 10 ⁻⁶
	0.25	3.646 * 10 ⁻⁷
Diamond	1	3.564 * 10 ⁻⁴
	0.5	3.460 * 10 ⁻⁵
	0.25	3.756 * 10 ⁻⁶
UHWPE	1	8.178 * 10 ⁻⁵
	0.5	7.935 * 10 ⁻⁶
	0.25	8.614 * 10 ⁻⁷

Results

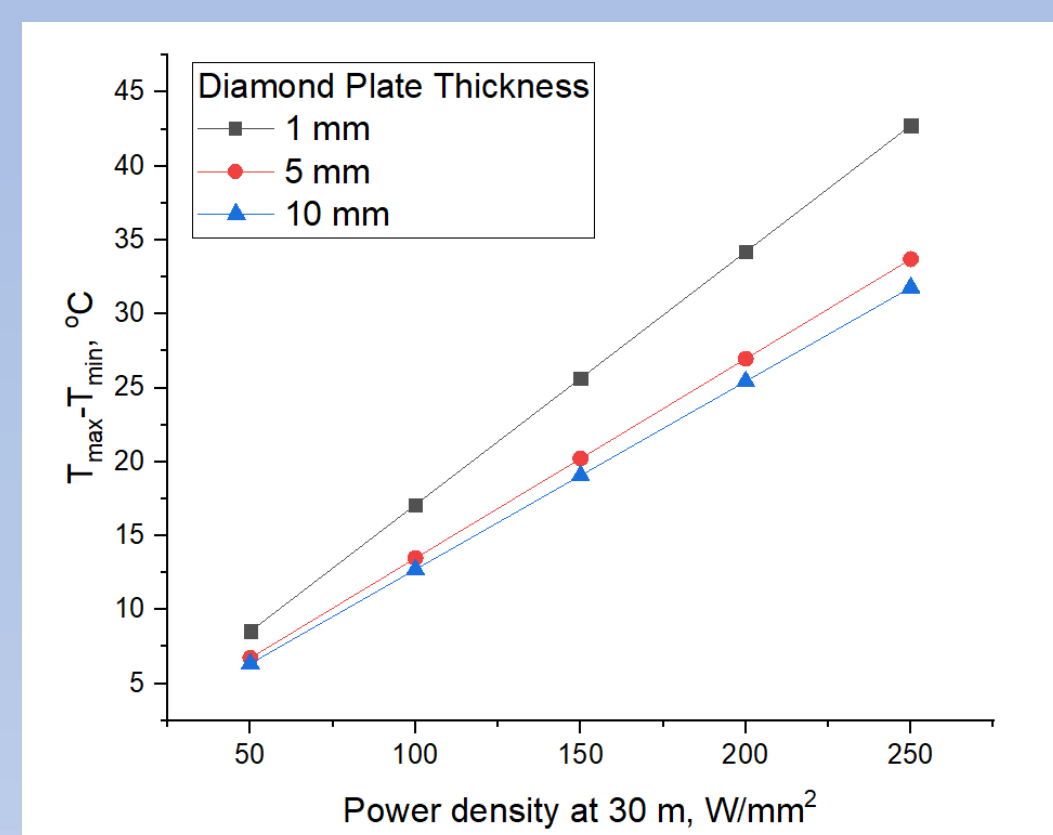
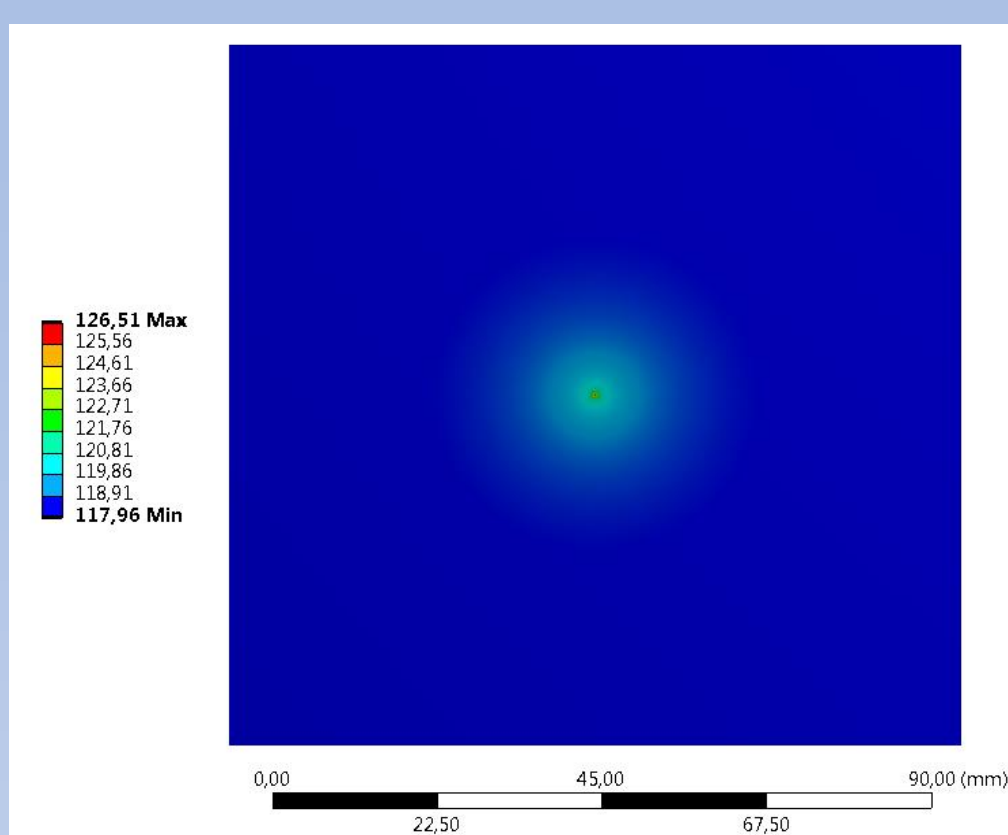
Aluminum



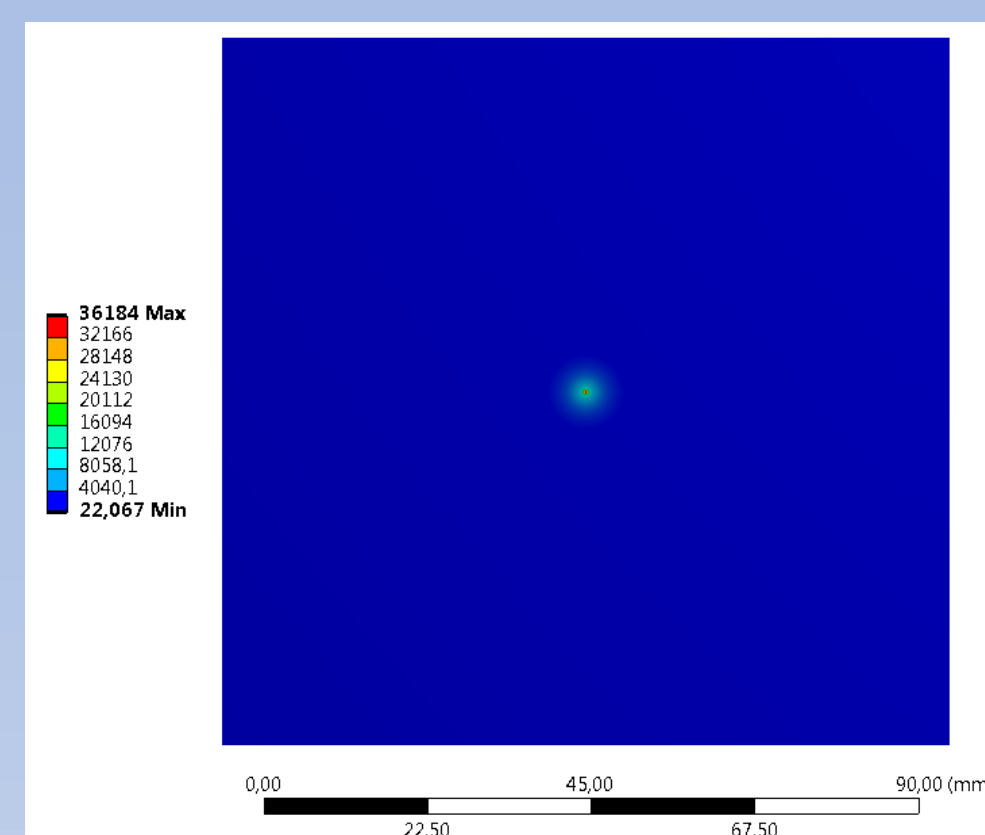
Beryllium



Diamond



UHMWPE



With this formulation of the problem and experimental conditions, the UHMWPE plate is burned through