

Recent results from SND detector at VEPP-2000 collider. Measurement of pion formfactor.

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on behalf of the SND collaboration

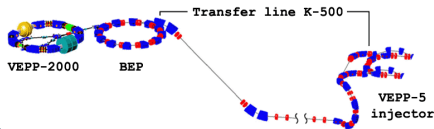
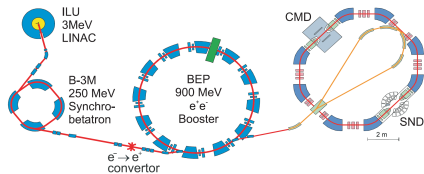
Tau and QCD physics at present and future electron-positron colliders.

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BINP, Novosibirsk



VEPP-2000 e^+e^- collider

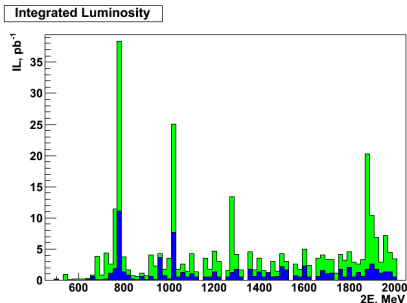


VEPP-2000 parameters

- c.m. energy $E=0.3-2.0$ GeV
- Luminosity at $E=1.8$ GeV
 $10^{32} \text{ cm}^{-2} \text{ sec}^{-1}$ (project)
 $4 \times 10^{31} \text{ cm}^{-2} \text{ sec}^{-1}$ (achieved)
- Beam energy spread - 0.6 MeV
at $E=1.8$ GeV

- 10 times more intense positron source
- Experiments at upgraded VEPP-2000 was restarted by the end of 2016





Timeline

2010-2013 – experiments, $70 pb^{-1}$

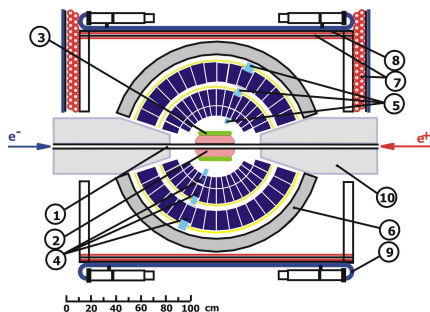
2013-2016 – upgrade, new injector

2016 - ... – experiments, $210 pb^{-1}$

15 hadronic processes are currently under analysis

- $e^+e^- \rightarrow \eta\pi^0\gamma$
- $e^+e^- \rightarrow \pi^+\pi^-\pi^0\eta$
- $e^+e^- \rightarrow n\bar{n}$
- $e^+e^- \rightarrow \pi^+\pi^-$
- $e^+e^- \rightarrow f_1(1285)$
- $e^+e^- \rightarrow \eta$





1-beam pipe, 2-tracking system, 3-aerogel Cherenkov counter, 4 - NaI(Tl) crystals, 5 - phototriodes, 6 - iron muon absorber, 7-9 - muon detector, 10 - focusing solenoids.

Main physics task of SND is study of all possible processes of e^+e^- annihilation into hadrons below 2 GeV.

- The total hadronic cross section, which is calculated as a sum of exclusive cross sections.
- Study of hadronization (dynamics of exclusive processes).

Analysis is based on the 4.6 pb^{-1} statistics, collected in 2012 – 2013, that corresponds to the 2.3×10^6 collinear events, with 10^6 $e^+e^- \rightarrow \pi^+\pi^-, \mu^+\mu^-$ and 1.3×10^6 $e^+e^- \rightarrow e^+e^-$

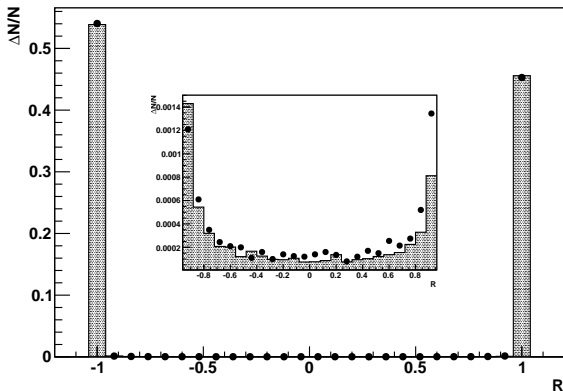


- 1 $N_{ch} \geq 2$. The events can contain neutral particles due to nuclear interactions of charged pions with detector material or due to electromagnetic showers splitting
- 2 $|\Delta\theta| = |180^\circ - (\theta_1 + \theta_2)| < 12^\circ$ and $|\Delta\phi| = |180^\circ - |\phi_1 - \phi_2|| < 4^\circ$, where ϕ is the particle azimuthal angle
- 3 $E_{1,2} > 40$ MeV, where E_i is the i th particle ($i = 1, 2$) energy deposition
- 4 $50^\circ < \theta_0 = (\theta_1 - \theta_2 + 180^\circ) \times 0.5 < 130^\circ$
- 5 $|d0_1| < 1$ cm , $|d0_2| < 1$ cm, where $|d0_i|$ is a distance between the i th particle track and the beam axis
- 6 $|z0_1| < 8$ cm , $|z0_2| < 8$ cm, where $|z0_i|$ is a distance from the center of the detector to the primary vertex of the i th particle track along the beam axis
- 7 The muon system $veto = 0$



The output signal of the trained BDT network R is a value in the interval from -1.0 to 1.0

The $e^+e^- \rightarrow e^+e^-$ events are located in the region $R < 0$, while $e^+e^- \rightarrow \pi^+\pi^-, \mu^+\mu^-$ events in $R > 0$.



$$N_{cosm} = N_{exp}[veto = 1] \times \frac{N_{cosm}[veto = 0]}{N_{cosm}[veto = 1]}$$

$N_{exp}[veto = 1]$ – number of data events selected with 2π cuts but with veto=1; $N_{cosm}[veto = 0(1)]$ – number of special cosmic events

Two types of cosmic events are used:

- Non-central ($|d0_1| > 0.5$ cm , $|d0_2| > 0.5$ cm, $|z0_1| > 5$ cm and $|z0_2| > 5$ cm) events from the same data sample.
- Events from special cosmic runs without beams

Both give the **same 2.5%** ratio between $N_{cosm}[veto = 0]$ and $N_{cosm}[veto = 1]$ in the **whole energy spectrum**



Background from the $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ is subtracted directly in the $\omega(782)$ region, with a number of background events estimated according to the formula:

$$N_{3\pi} = N^{\text{exp}}[3\pi] \times \frac{N_{3\pi}^{\text{mc}}[2\pi]}{N_{3\pi}^{\text{mc}}[3\pi]}$$

$N^{\text{exp}}[3\pi]$ – number of $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ events in the same data sample selected with a special 3π cuts:

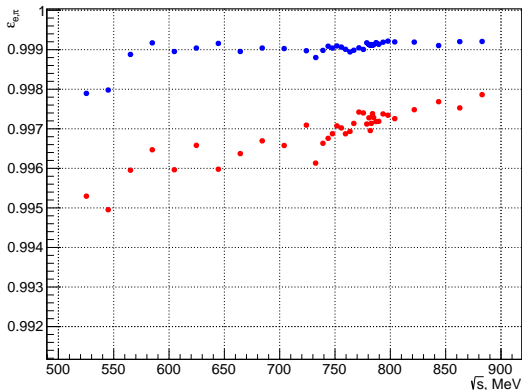
$$N_{cha} \geq 2, N_n \geq 2, |\Delta\theta| > 10^\circ, |\Delta\phi| > 10^\circ, \\ 40^\circ < \theta_i < 140^\circ, \chi_{\pi^+\pi^-2\gamma}^2 < 50, \chi_{\pi^+\pi^-\pi^0}^2 < 30$$

Contribution of this background to the total $e^+e^- \rightarrow \pi^+\pi^-$ cross section is **less than 0.15%**, due to the strong suppression by $|\Delta\theta|$ and $|\Delta\phi|$ cuts.



$$\varepsilon_e = \frac{N^{ee}(R \in [-1; 0])}{N^{ee}(R \in [-1; 1])}, \quad \varepsilon_\pi = \frac{N^{\pi\pi}(R \in [0; 1])}{N^{\pi\pi}(R \in [-1; 1])}$$

$N^{ee, \pi\pi}(R \in [a; b])$ are the numbers of $e^+e^- \rightarrow e^+e^-$ or $\pi^+\pi^-$ events with R in the interval $[a; b]$



Identification efficiencies for $e^+e^- \rightarrow e^+e^-$ and $e^+e^- \rightarrow \pi^+\pi^-$ simulated events



$$\delta_x = \frac{\epsilon_x^{exp}}{\epsilon_x^{mc}}$$

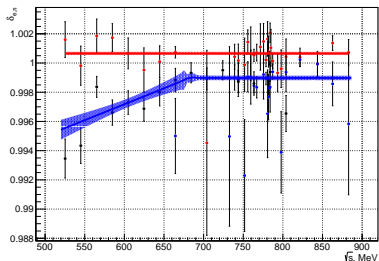
$x = e(\pi)$, ϵ_x^{exp} and ϵ_x^{mc} are identification efficiencies for experimental and simulated pseudoevents respectively. The δ_e does not depend on energy, and its average value is 1.0006 ± 0.0001

$$\delta_\pi(\sqrt{s}) = a \left(\sqrt{(\sqrt{s} - b)^2 + 10} - (\sqrt{s} - b) \right) + c$$

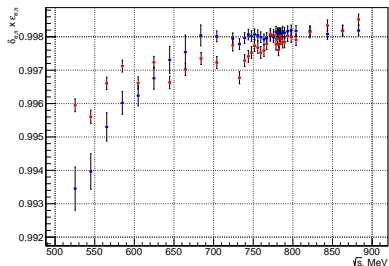
$\delta_\pi = 0.9990 \pm 0.0002$ at the energy region $\sqrt{s} > 0.65$ GeV and below δ_π changes upto 0.9950 ± 0.0006 at $\sqrt{s} = 0.52$ GeV



ID efficiency correction



Correction coefficients for ID efficiencies of the $e^+e^- \rightarrow e^+e^-$ and $e^+e^- \rightarrow \pi^+\pi^-$ events. δ_π obtained using pseudo $\pi\pi$ events constructed from $e^+e^- \rightarrow \pi^+\pi^-$ and $e^+e^- \rightarrow \omega, \phi \rightarrow \pi^+\pi^-\pi^0$ events. Lines are the fit results.



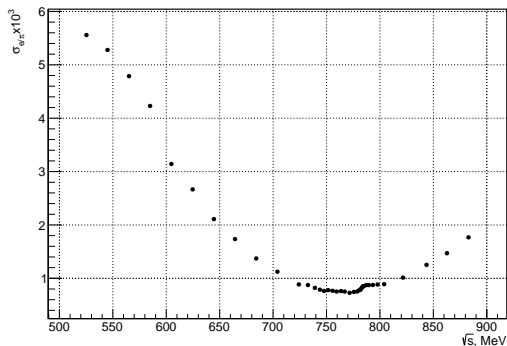
Corrected ID efficiencies for the $e^+e^- \rightarrow e^+e^-$ and $e^+e^- \rightarrow \pi^+\pi^-$ events

JINST T01002 (2017)



Contribution to the cross section uncertainty

Error	$\delta_e, \%$	δ_π	
		at $\sqrt{s} > 0.65$ GeV, %	at $\sqrt{s} < 0.65$ GeV, %
σ_{stat}	0.01	0.02	0.02 – 0.06
σ_{ID}	0.02	0.01	0.02
σ_{bkg}	0.02	0.02	–
σ_{tot}	0.03	0.03	0.03 – 0.06



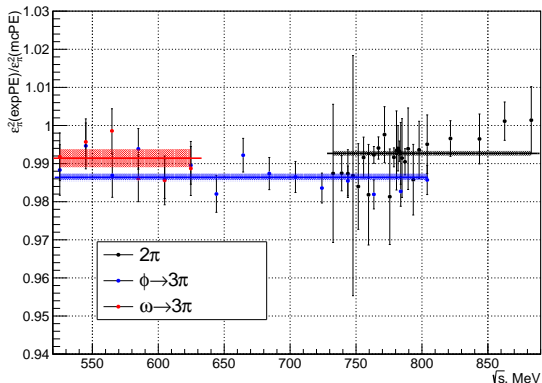
Contribution of the ID efficiencies to the relative error of $e^+e^- \rightarrow \pi^+\pi^-$ cross section is **less than 0.2%** for the most energy points.



$E_{1,2} > 40$ MeV efficiency

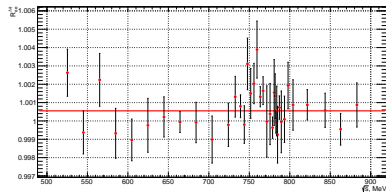
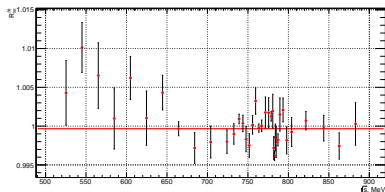
The pseudo- $\pi\pi$ events are used to check the validity of efficiency for the $E_{1,2} > 40$ MeV cut, derived from the simulation

Obtained average correction is equal to **0.992**. The maximum difference between corrections derived from the different types of pseudo-events is **0.5%**

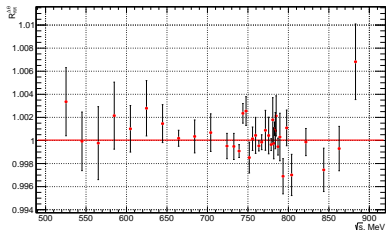


In order to study the differences between simulation and experimental data at each energy point, an efficiency correction is introduced:

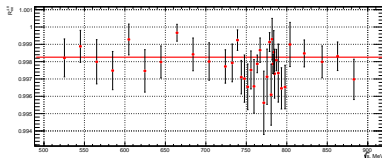
$$R_i(x) = \frac{\epsilon_i^{exp}(x)}{\epsilon_i^{mc}(x)} \epsilon_i^{exp} = \frac{N_i(x \in [A_x; B_x])}{N_i(x \in [C_x; D_x])} \epsilon_i^{mc} = \frac{M_i(x \in [A_x; B_x])}{M_i(x \in [C_x; D_x])}$$



Efficiency of the $|\Delta\phi| < 4^\circ$ and $|\Delta\theta| < 12^\circ$ cuts



$$e^+e^- \rightarrow \pi^+\pi^-$$



$$e^+e^- \rightarrow e^+e^-$$

The average values of $\delta_{\Delta\phi} = R_{\pi\pi}(\Delta\phi)/R_{ee}(\Delta\phi)$ and $\delta_{\Delta\theta} = R_{\pi\pi}(\Delta\theta)/R_{ee}(\Delta\theta)$ differ from 1 by 0.1 % and 0.2 %, respectively

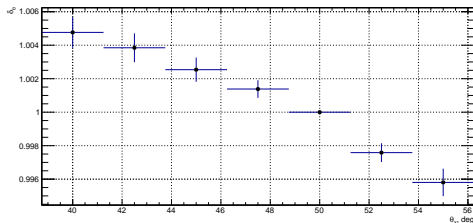
The overall contribution to the systematic uncertainty from the conditions on the $\Delta\phi$ and $\Delta\theta$ is equal to $0.001 \oplus 0.002 = 0.002$



Efficiency of the $50^\circ < \theta_0 < 130^\circ$ cut

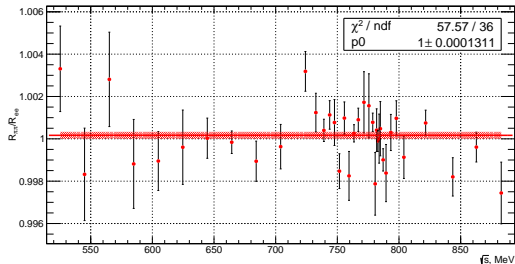
$$R_i(z) = \frac{\varepsilon_i^{exp}(z)}{\varepsilon_i^{mc}(z)} \quad \varepsilon_i^{exp}(z) = \frac{N_i(\theta_0 \in [x; 180^\circ - z])}{N_i(\theta_0 \in [50^\circ; 130^\circ])} \quad \varepsilon_i^{mc}(z) = \frac{M_i(\theta_0 \in [x; 180^\circ - z])}{M_i(\theta_0 \in [50^\circ; 130^\circ])}$$

The statistically significant deviation of $\delta_{\theta_0} = R_{\pi\pi}/R_{ee}$ from unity does not exceed 0.5 %



Probability of the π (e) track loss due reconstruction inefficiency is estimated from the $R_{\pi\pi}$ (R_{ee}):

the ratio of the number of events with one track, but the total number of particles > 1 and loosen $\Delta\phi$ and $\Delta\theta$ cuts, to the number of events with two or more tracks



The ratio of $R_{\pi\pi}$ to R_{ee} is taken as a correction to the measured cross section

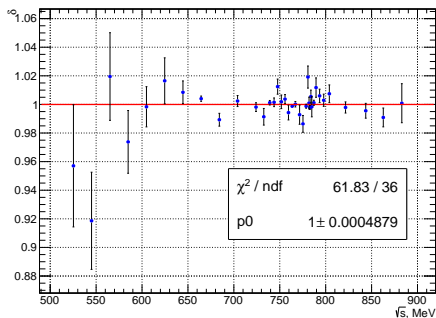
It does not show a significant deviation from unity



Muon system veto efficiency

$$\delta_{\text{veto}} = \frac{\sigma_{\pi\pi}((\phi_1 + \phi_2 - 180^\circ)/2 > 166^\circ \text{ or } < 14^\circ; \text{veto} \geq 0)}{\sigma_{\pi\pi}((\phi_1 + \phi_2 - 180^\circ)/2 > 166^\circ \text{ or } < 14^\circ; \text{veto} = 0)}$$

In case of the $\text{veto} \geq 0$ selection the certain number of the **residual cosmic background** events, derived from the fit of the $(z_{01} + z_{02})/2$ with a sum of uniform and normal distributions, is **subtracted** from the total number of the $e^+e^- \rightarrow \pi^+\pi^-$ events



δ_{veto} shows
no significant
energy
dependence

Averaged
value is
applied and it
is consistent
with 1



The main sources of systematic uncertainty

- $\Delta\theta, \Delta\phi, \theta_0$ cuts: $0.001 \oplus 0.002 \oplus 0.005 = 0.55\%$
- $E_{1,2} > 40$ MeV condition: 0.5 %
- e/π -separation for the $\sqrt{s} \leq 600$ MeV: 0.3 – 0.5%
- muon subtraction for the $\sqrt{s} \leq 600$ MeV: 0.3 – 0.7%

Additional sources of systematic uncertainty

- 0.2 % is taken as a systematic error from modeling of the pion loss due to nuclear interaction
- Contributions from the $N_{cha} \geq 2$ and $veto = 0$ cuts are considered to be negligible
- Calculation of the radiative correction gives 0.2 %
- 0.1 % from variation of the trigger cuts



Source	$\sqrt{s} > 600$ MeV	$\sqrt{s} \leq 600$ MeV
ID e/π	0.1-0.2	0.3-0.5
μ	0.0-0.2	0.3-0.7
$\Delta\theta$	0.1	
$\Delta\phi$	0.2	
θ_0	0.5	
$E_{1,2}$	0.5	
rad	0.2	
trig	0.1	
nucl	0.2	
total	0.8	0.9-1.2



Calculating $e^+e^- \rightarrow \pi^+\pi^-$ cross section

$$N_a = L(\sigma_{\pi\pi}\varepsilon_{\pi\pi}^a + \sigma_{\mu\mu}\varepsilon_{\mu\mu}^a + \sigma_{ee}\varepsilon_{ee}^a) + N_{nc}^a$$

$a = 1, 2$ correspond to the $R_{e/\pi} \in [0, 1]$ and $R_{e/\pi} \in [-1, 0]$ respectively; σ_{jj} and ε_{jj}^a , with $jj = \pi^+\pi^-, \mu^+\mu^-, e^+e^-$ in the final state; N_{nc}^a is the number of non-collinear and cosmic background events; L is the IL collected at s_i .

From these equations $e^+e^- \rightarrow \pi^+\pi^-$ cross section and L can be deduced:

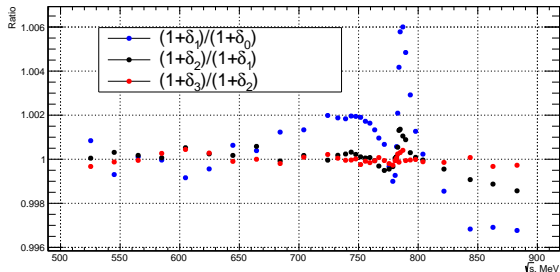
$$L(s_i) = \frac{(N_2 - N_{nc}^2)\varepsilon_{\pi\pi}^1 - (N_1 - N_{nc}^1)\varepsilon_{\pi\pi}^2}{\sigma_{ee}(\varepsilon_{ee}^2\varepsilon_{\pi\pi}^1 - \varepsilon_{ee}^1\varepsilon_{\pi\pi}^2) + \sigma_{\mu\mu}(\varepsilon_{\mu\mu}^2\varepsilon_{\pi\pi}^1 - \varepsilon_{\mu\mu}^1\varepsilon_{\pi\pi}^2)}$$

$$\sigma_{\pi\pi}(s_i) = \frac{N_1 - N_{nc}^1 - L(s_i)\sigma_{\mu\mu}\varepsilon_{\mu\mu}^1(s_i) - L(s_i)\sigma_{ee}\varepsilon_{ee}^1}{L(s_i)\varepsilon_{\pi\pi}^1}$$



$$\sigma_{\pi\pi}^0(s_i) = \frac{\sigma_{\pi\pi}(s_i)}{1 + \delta_{rad}(s_i)}$$

$1 + \delta_{rad}(s_i)$ is a **radiative correction**, that accounts for radiation from the initial and final states, calculated using the **MCGPJ** code.



JHEP 9710, 006 (1997)

$\delta_{rad}(s_i)$ has to be calculated **iteratively**, by fitting measured cross sections with a model from the MCGPJ



$$\sigma_{\pi\pi}(s) = \frac{2}{3} \frac{\alpha^2}{s^{5/2}} \mathbf{P}_{\pi\pi}(s) |\mathbf{A}_{\pi\pi}(s)|^2$$

$$\mathbf{P}_{\pi\pi}(s) = q_\pi^3(s), \quad \mathbf{q}_\pi(s) = \frac{1}{2} \sqrt{s - 4m_\pi^2}$$

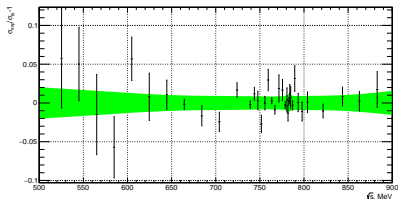
$$|\mathbf{A}_{\pi\pi}(s)|^2 = \left| \sqrt{\frac{3}{2}} \frac{1}{\alpha} \sum_{V=\rho,\omega,\rho'} \frac{\Gamma_V m_V^3 \sqrt{m_V \sigma(V \rightarrow \pi^+ \pi^-)}}{D_V(s)} \frac{e^{i\phi_{\rho V}}}{\sqrt{q_\pi^3(m_V)}} \right|^2$$

$$D_V(s) = m_V^2 - s - i\sqrt{s}\Gamma_V(s), \quad \Gamma_V(s) = \sum_f \Gamma(V \rightarrow f, s)$$

$$\Gamma_\omega(s) = \frac{m_\omega^2}{s} \frac{q_\pi^3(s)}{q_\pi^3(m_\omega)} \Gamma_\omega B_{\omega \rightarrow \pi^+ \pi^-} + \frac{q_{\pi\gamma}^3(s)}{q_{\pi\gamma}^3(m_\omega)} \Gamma_\omega B_{\omega \rightarrow \pi^0 \gamma} + \frac{W_{\rho\pi}(s)}{W_{\rho\pi}(m_\omega)} \Gamma_\omega B_{\omega \rightarrow 3\pi}$$

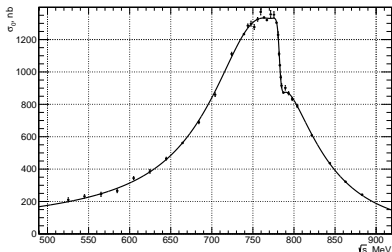
$$\Gamma_V(s) = \frac{m_V^2}{s} \frac{q_\pi^3(s)}{q_\pi^3(m_V)} \Gamma_V \quad (V = \rho, \rho')$$





The **relative difference** between the $e^+e^- \rightarrow \pi^+\pi^-$ cross section, measured by SND and fit of the SND experimental data. The **green bar** depicts **systematic** and **statistical** errors of the SND fit, folded quadratically.

Cross section values in the $\sqrt{s} = 352.02, 375.85$ and 389.36 MeV energy points shows **non-statistical** deviation from the fit

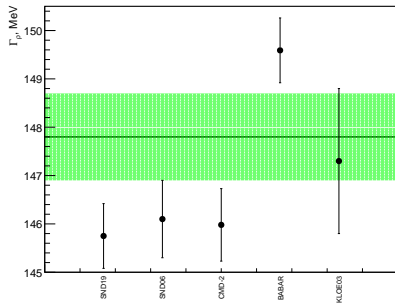
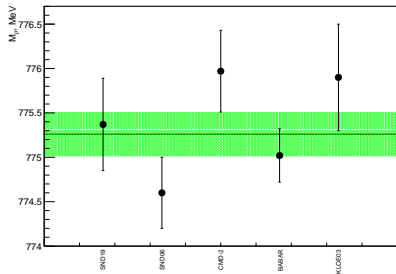


parameter	SND VEPP-2000	SND VEPP-2M
m_ρ , MeV	$775.4 \pm 0.5 \pm 0.4$	$774.6 \pm 0.4 \pm 0.5$
Γ_ρ , MeV	$145.8 \pm 0.7 \pm 1$	$146.1 \pm 0.8 \pm 1.5$
$\sigma(\rho \rightarrow \pi^+\pi^-)$, nb	$1189.25 \pm 4.6 \pm 9.5$	$1193 \pm 7 \pm 16$
$\sigma(\omega \rightarrow \pi^+\pi^-)$, nb	$31.3 \pm 1.3 \pm 0.3$	$29.3 \pm 1.4 \pm 1.0$
$\phi_{\rho\omega}$, deg.	$110.9 \pm 1.5 \pm 0.7$	$113.7 \pm 1.3 \pm 2.0$
$\sigma(\rho' \rightarrow \pi^+\pi^-)$, nb	2.3 ± 0.6	1.8 ± 0.2
χ^2/ndf	43/30	–

parameters	SND VEPP-2000	SND VEPP-2M
$B_{\rho \rightarrow e^+e^-} \times B_{\rho \rightarrow \pi^+\pi^-}$	$(4.888 \pm 0.02 \pm 0.04) \times 10^{-5}$	$(4.876 \pm 0.02 \pm 0.06) \times 10^{-5}$
$B_{\omega \rightarrow e^+e^-} \times B_{\omega \rightarrow \pi^+\pi^-}$	$(1.312 \pm 0.06 \pm 0.01) \times 10^{-6}$	$(1.225 \pm 0.06 \pm 0.04) \times 10^{-6}$



Fit results



$$\sigma_{\pi\pi}^{\text{bare}}(s) = \sigma_{\pi\pi}^0(s) \times |1 - \Pi(s)|^2 \times \left(1 + \frac{\alpha}{\pi} a(s)\right)$$

$$a(s) = \frac{1 + \beta^2}{\beta} \left[4 \text{Li}_2\left(\frac{1 - \beta}{1 + \beta}\right) + 2 \text{Li}_2\left(-\frac{1 - \beta}{1 + \beta}\right) - \right. \\ \left. 3 \ln \frac{2}{1 + \beta} \ln \frac{1 + \beta}{1 - \beta} - 2 \ln \beta \ln \frac{1 + \beta}{1 - \beta} \right] - 3 \ln \frac{4}{1 - \beta^2} - 4 \ln \beta + \frac{1}{\beta^3} \left[\frac{5}{4} (1 + \beta^2)^2 - 2 \right] \\ \times \ln \frac{1 + \beta}{1 - \beta} + \frac{3}{2} \frac{1 + \beta^2}{\beta^2}.$$

$$\text{Li}_2(x) = - \int_0^x dt \ln(1 - t)/t, \quad \beta = \sqrt{1 - \frac{4m_\pi^2}{s}}$$



$$a_\mu(\pi\pi, s_{\min} \leq \sqrt{s} \leq s_{\max}) = \left(\frac{\alpha m_\mu}{3\pi} \right)^2 \int_{s_{\min}}^{s_{\max}} \frac{R(s)K(s)}{s^2} ds$$

$K(s)$ is a known kernel ([J. Phys. G **38**, 085003 2011](#)) and

$$R(s) = \frac{\sigma_{\pi\pi}^{bare}}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}, \quad \sigma(e^+e^- \rightarrow \mu^+\mu^-) = \frac{4\pi\alpha^2}{3s}$$

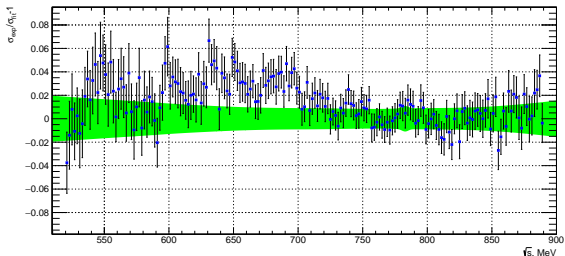
Trapezoid integration allows to compute a_μ using measured cross sections

	SND VEPP-2000	SND VEPP-2M	BaBar
$a_\mu(\pi\pi) \times 10^{10}$	$410.88 \pm 1.02 \pm 3.75$	$408.88 \pm 1.30 \pm 5.31$	$414.93 \pm 1.02 \pm 2.07$



The relative difference between the $e^+e^- \rightarrow \pi^+\pi^-$ cross section, measured by BABAR and fit of the SND experimental data

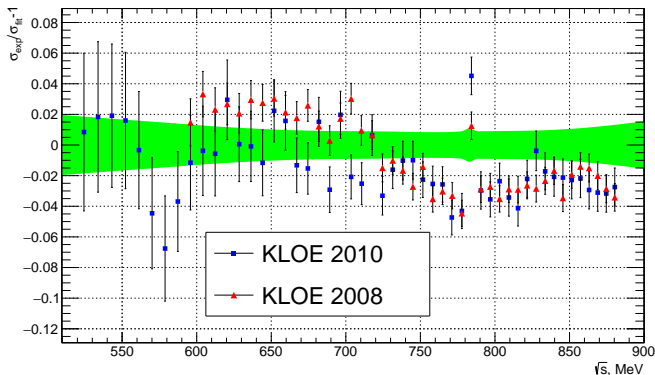
- $\sigma_{sys} \oplus \sigma_{stat}$ errors are shown for the BABAR data
- The green bar depicts systematic and statistical errors of the SND fit, folded quadratically



Phys. Rev. 2012.Vol. 86D.
3,032013



The relative difference between the $e^+e^- \rightarrow \pi^+\pi^-$ cross section, measured by KLOE and fit of the SND experimental data

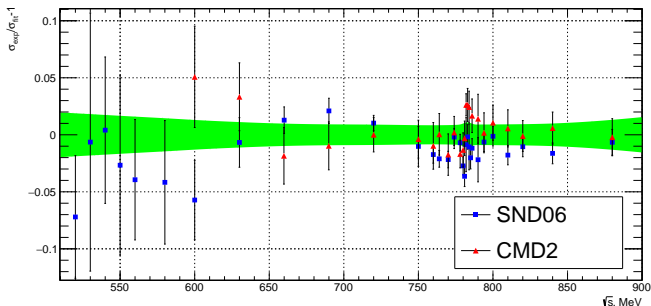


Phys. Lett. 2009. Vol. 670B 4-5, P.285-291

Phys. Lett. 2011. Vol. 700B 2. P.102-110



The relative difference between the $e^+e^- \rightarrow \pi^+\pi^-$ cross section, measured in experiments at VEPP-2M and fit of the SND experimental data

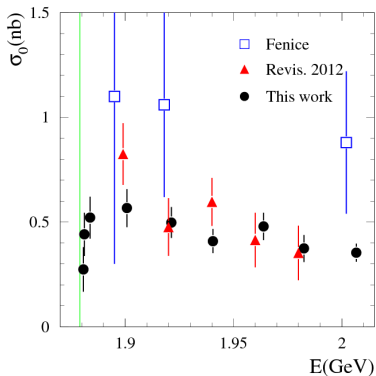


JETP (2006) vol. 103, N3, pp 380-384.
Phys. Lett. 2007 Vol.648B 5. P.28-38



- The difference between the value of $a_\mu(\pi\pi, 525\text{MeV} \leq \sqrt{s} \leq 883\text{MeV})$ obtained from the SND data, and ones derived from the previous measurements $< 1\sigma$
- The parameters of the ρ and ω mesons in this analysis are consistent with ones obtained by SND in experiments at VEPP-2M
- Comparison with VEPP-2M results indicates no significant contradictions in the whole energy spectrum
- In the $0.6 \leq \sqrt{s} \leq 0.7$ GeV energy range there is a 3% discrepancy between the SND and BABAR data, but for the rest of the spectrum SND data is in agreement with the BABAR results
- There is 1–3 % deviation between KLOE and SND data for $\sqrt{s} \geq 0.7$ GeV

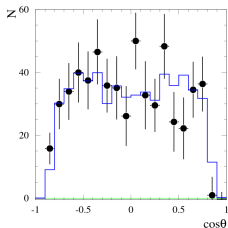
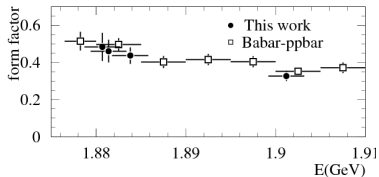
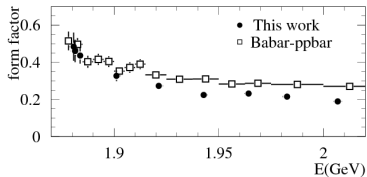




Cross Section measurement

- The new measurement is based on the 2017 dataset and uses a different method. The calorimeter-trigger-time distribution is analyzed.
- Our new result is lower than the previous SND measurement. The reasons are underestimated beam background and incorrect MC simulation.
- The systematic uncertainty on the cross section is estimated to be about 20%, mainly due to MC simulation.





Formfactor

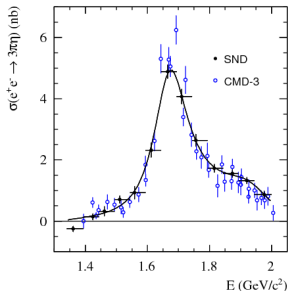
- The cross section depends on two form factors.
- From the measured cross section we determine the effective form factor
- Near threshold the proton and neutron effective form factors are close to each other. The neutron form factor become lower than the proton one with increase the energy.
- The ratio of the form factors can be determined from the analysis of the $\cos(\theta)$ distribution

G_E

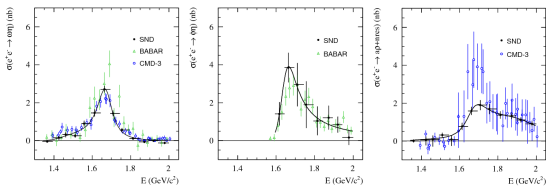
- The $\cos(\theta)$ distribution is well described by $1 + \cos(\theta)^2$, i.e. $G_E=0$.
- For proton $|G_E/G_M| \approx 1.5$ in this energy region.



$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\eta$$



The total $e^+e^- \rightarrow \pi^+\pi^-\pi^0\eta$ cross section measured by SND is, in general, consistent with the CMD-3 result. The $\approx 15\%$ difference in the cross section maximum is within the systematic uncertainties, which are 7% for SND and 11% for CMD-3.

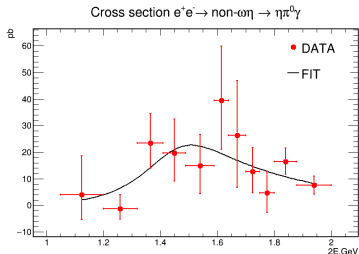
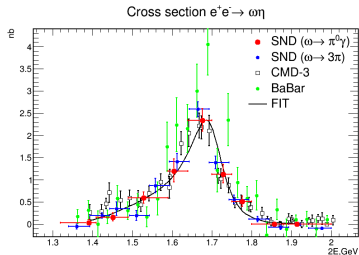


Exclusive chanel

- The obtained $\omega\eta$ cross section agrees with the CMD-3 measurement. Both the SND and CMD-3 results lie below the BABAR data.
- The SND and BABAR $\phi\eta$ measurements are in reasonable agreement.
- The significant difference between the SND and CMD-3 measurements is observed for the $a_0\rho$ +structureless final state.



$$e^+e^- \rightarrow \eta\pi^0\gamma$$



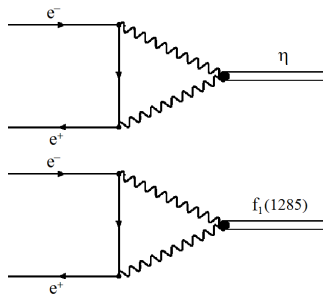
$$e^+e^- \rightarrow \omega\eta \rightarrow \eta\pi^0\gamma$$

The measured $e^+e^- \rightarrow \omega\eta$ cross section is in good agreement with the SND and CMD-3 measurements in the $\omega \rightarrow 3\pi$ decay mode.

- The radiative $e^+e^- \rightarrow \eta\pi^0\gamma$ process was studied previously only in the $\phi(1020)$ region.
- We perform the **first measurement** in the energy range 1.05-2.00 GeV.
- The value of the cross section is about 15-20 pb in the region 1.4-1.9 GeV.



$e^+e^- \rightarrow \eta$ and $e^+e^- \rightarrow f_1(1285)$



$e^+e^- \rightarrow \eta$

- The 650 nb^{-1} data sample was recorded in 2018 at $\sqrt{s} = m_\eta$.
- The decay mode $\eta \rightarrow 3\pi^0$ is used, in which the single photon annihilation background is absent.
- Zero signal events have been selected.
- The upper limit $B(\eta \rightarrow e^+e^-) < 7 \times 10^{-7}$ at 90% CL has been set.

$e^+e^- \rightarrow f_1(1285)$

- About 4 pb^{-1} of data were collected in the resonance maximum.
- The $f_1(1285) \rightarrow \pi^0\pi^0\eta \rightarrow 6\gamma$ decay mode is used.
- The main background sources are $e^+e^- \rightarrow \omega\pi^0 \rightarrow \pi^0\pi^0\gamma$, $e^+e^- \rightarrow \eta\gamma$ and $e^+e^- \rightarrow \pi^0\pi^0\omega$.
- After applying the selection criteria, two events have been observed at the peak.
- These two events correspond to $B(f_1(1285) \rightarrow e^+e^-) = 6.1^{+3.6}_{-2.6} \times 10^{-9}$



- The $e^+e^- \rightarrow \pi^+\pi^-$ cross section is measured with systematic uncertainty better than 1%
- The accuracy of $e^+e^- \rightarrow n\bar{n}$ measurement is significantly improved
- The $e^+e^- \rightarrow \pi^+\pi^-\pi^0\eta$ cross section has been measured
- Rare radiative process $e^+e^- \rightarrow \eta\pi^0\gamma$ have been measured for the first time in the energy range 1.05-2.00 GeV
- Search for production of C-even resonances, η and $f_1(1285)$, in e^+e^- annihilation is performed. The first indication of the process $e^+e^- \rightarrow f_1(1285)$ is obtained



\sqrt{s} , MeV	σ , nb	σ_0 , nb	$ F(s) ^2$	σ_{bare} , nb
525.3	203.3±12.3	210.3±12.7	4.4±0.3	209.6±12.7
545	223.5±10.1	231.7±10.4	5±0.2	231.2±10.4
565.1	235±12.3	244.4±12.8	5.5±0.3	243.9±12.8
584.9	254.7±10.7	265.8±11.2	6.2±0.3	265.5±11.1
604.8	328.5±8.7	344.4±9.1	8.3±0.2	344.5±9.1
624.7	366.5±11.1	386.2±11.7	9.7±0.3	386.7±11.7
644.6	438.2±8.2	464.5±8.7	12.1±0.2	465.8±8.8
664.4	526.4±3.5	561.5±3.7	15.3±0.1	564±3.7
684.2	642.1±8.4	689.4±9	19.5±0.3	693.1±9.1
704	797.3±10.2	859.8±11	25.4±0.3	864.6±11.1
724.1	1029.3±9.5	1111.2±10.3	34.2±0.3	1115.2±10.3
739.1	1146.5±5.6	1233.5±6	39.1±0.2	1233.7±6
743.8	1197.9±9.8	1285.8±10.5	41.1±0.3	1284.5±10.5
747.7	1212.1±14.4	1298.2±15.4	41.9±0.5	1295.3±15.4
751.7	1195.5±13.7	1277.2±14.6	41.5±0.5	1272.4±14.6
755.7	1243.9±10.8	1324.7±11.5	43.4±0.4	1318.2±11.4
759.5	1291.2±17.3	1370.7±18.4	45.3±0.6	1363.1±18.2



\sqrt{s} , MeV	σ , nb	σ_0 , nb	$ F(s) ^2$	σ_{bare} , nb
763.5	1263.7±5	1336.7±5.2	44.5±0.2	1328.9±5.2
767	1251.9±6.9	1320.2±7.3	44.3±0.2	1312.9±7.2
771.6	1289.8±22.2	1355.6±23.3	45.9±0.8	1350.9±23.2
775.6	1291.3±17.2	1353.9±18	46.2±0.6	1353.5±18
778.7	1251.6±5.3	1304.3±5.5	44.8±0.2	1300.7±5.5
780.7	1198.1±18.4	1229±18.9	42.4±0.7	1212.9±18.6
781.9	1105.1±11.2	1111.4±11.2	38.4±0.4	1081.6±10.9
782.8	1056.2±4.8	1041.3±4.7	36±0.2	1001.4±4.5
783.9	1000.8±11.6	967.2±11.2	33.5±0.4	917.7±10.6
784.9	957.3±12.8	915.3±12.2	31.8±0.4	862.6±11.5
787.1	911.3±5.1	872.1±4.8	30.4±0.2	818.7±4.5
789.5	933±14.1	901.8±13.6	31.6±0.5	849.8±12.8
793.4	891.7±10	868.5±9.7	30.7±0.3	823.3±9.2
797.8	856±10.1	833±9.8	29.7±0.4	792.8±9.3
804	818.3±10.4	789.9±10.1	28.5±0.4	754.1±9.6
821.6	654.4±5.6	608.4±5.2	22.7±0.2	582.6±5
843.6	496±5.8	436.9±5.1	17±0.2	419.5±4.9
862.7	383.4±4.6	322±3.9	13±0.2	309.8±3.8
882.9	303.2±6.7	242.3±5.3	10.2±0.2	233.7±5.1

