

"Tau and QCD physics at present and future electron-positron colliders"

December 16-18, 2019

Study of electron-positron annihilation to hadrons with CMD-3 at VEPP-2000

Evgeny Kozyrev (on behalf of the CMD-3 collaboration)

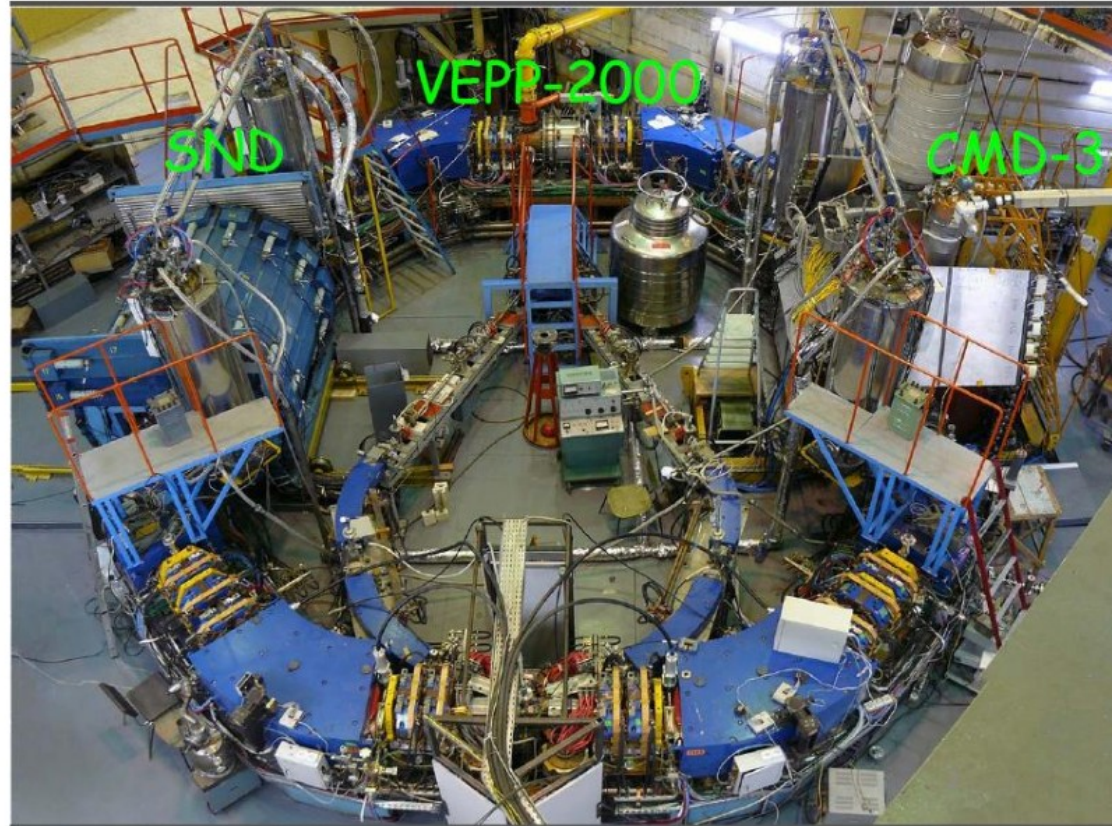
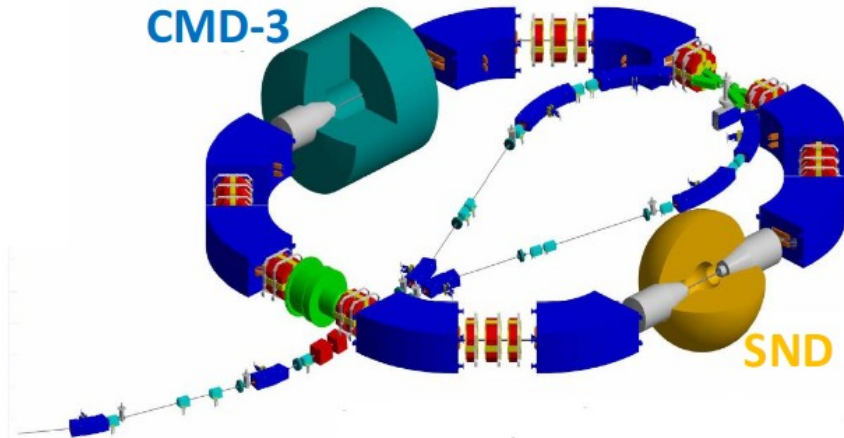
BINP, NSU

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18.12.2019

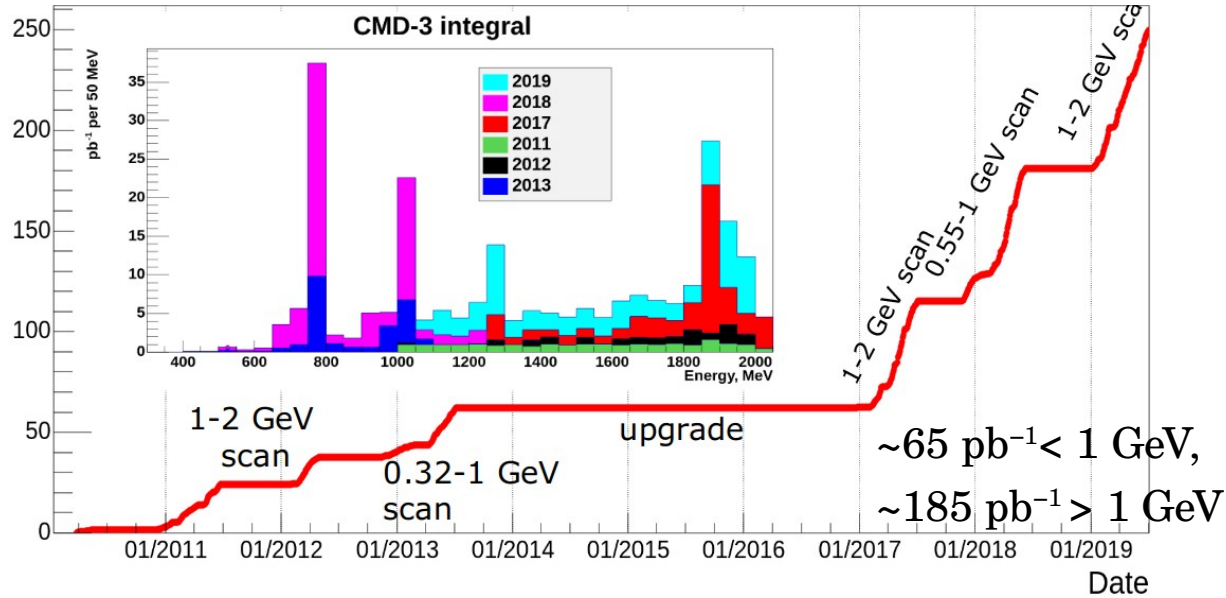
VEPP-2000

- VEPP-2000 (Novosibirsk, Russia) scans the $\sqrt{s}$ in the range from 0.32 to 2.01 GeV
- Beam energy is monitored by the Compton backscattering laser light system with ~ 50 keV precision
- Uses “round beams” technique (focusing solenoids)
- Maximum luminosity achieved - $4 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$
- CMD-3 and SND detectors placed at two beam interaction points



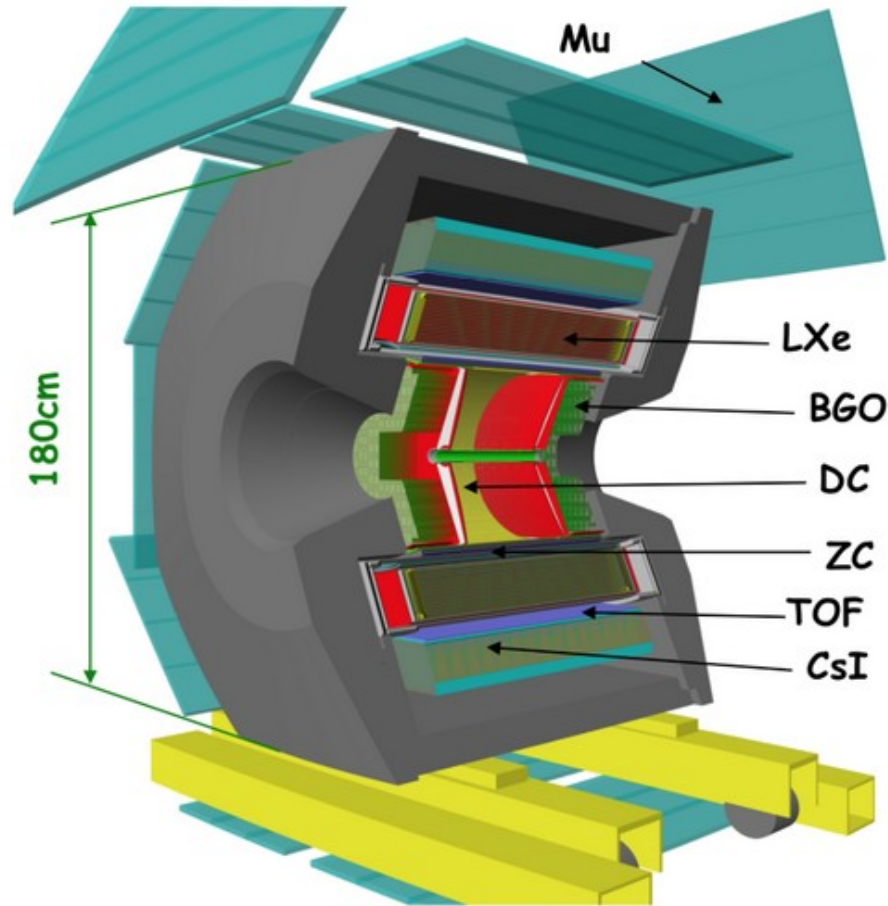
CMD-3 detector & physics program

Collected 1/pb



- ° Precise measurement of $R = \sigma(e+e- \rightarrow \text{hadrons}) / \sigma(e+e- \rightarrow \mu+\mu-)$ to achieve <1% systematic for major channels
- ° Study of the exclusive hadronic channels of $e+e-$ annihilation, test of the isotopic relations
- ° Study of the “excited” vector mesons: ρ' , ρ'' , ω' , ϕ' ...
- ° Study of GE/GM for nucleons and behavior of hadronic cross sections near nucleon-antinucleon threshold
- ° CVC tests: comparison of isovector part of $\sigma(e+e- \rightarrow \text{hadrons})$ with τ -decays spectra
- ° Two-photon physics (e.g. η' production)

Detector CMD-3



Tracking:

- × Drift Chamber in 1.3 T magnetic field

$$\sigma_{R\phi} \sim 100 \mu\text{m}, \sigma_Z \sim 2.5\text{mm}$$

$$\sigma_p/P \sim \sqrt{0.6^2 + (4.4 \cdot p[\text{GeV}])^2}, \%$$

Calorimetry:

- × Combined EM calorimeter (LXe, CsI, BGO)
13.4 X_0 in barrel part

$$\sigma_E/E \sim 0.034/\sqrt{E[\text{GeV}]} \oplus 0.020 - \text{barrel}$$

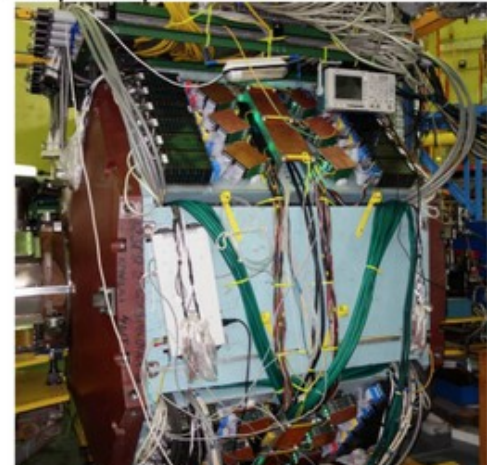
$$\sigma_E/E \sim 0.024/\sqrt{E[\text{GeV}]} \oplus 0.023 - \text{endcap}$$

- × LXe calorimeter with 7 ionization layers
with strip readout

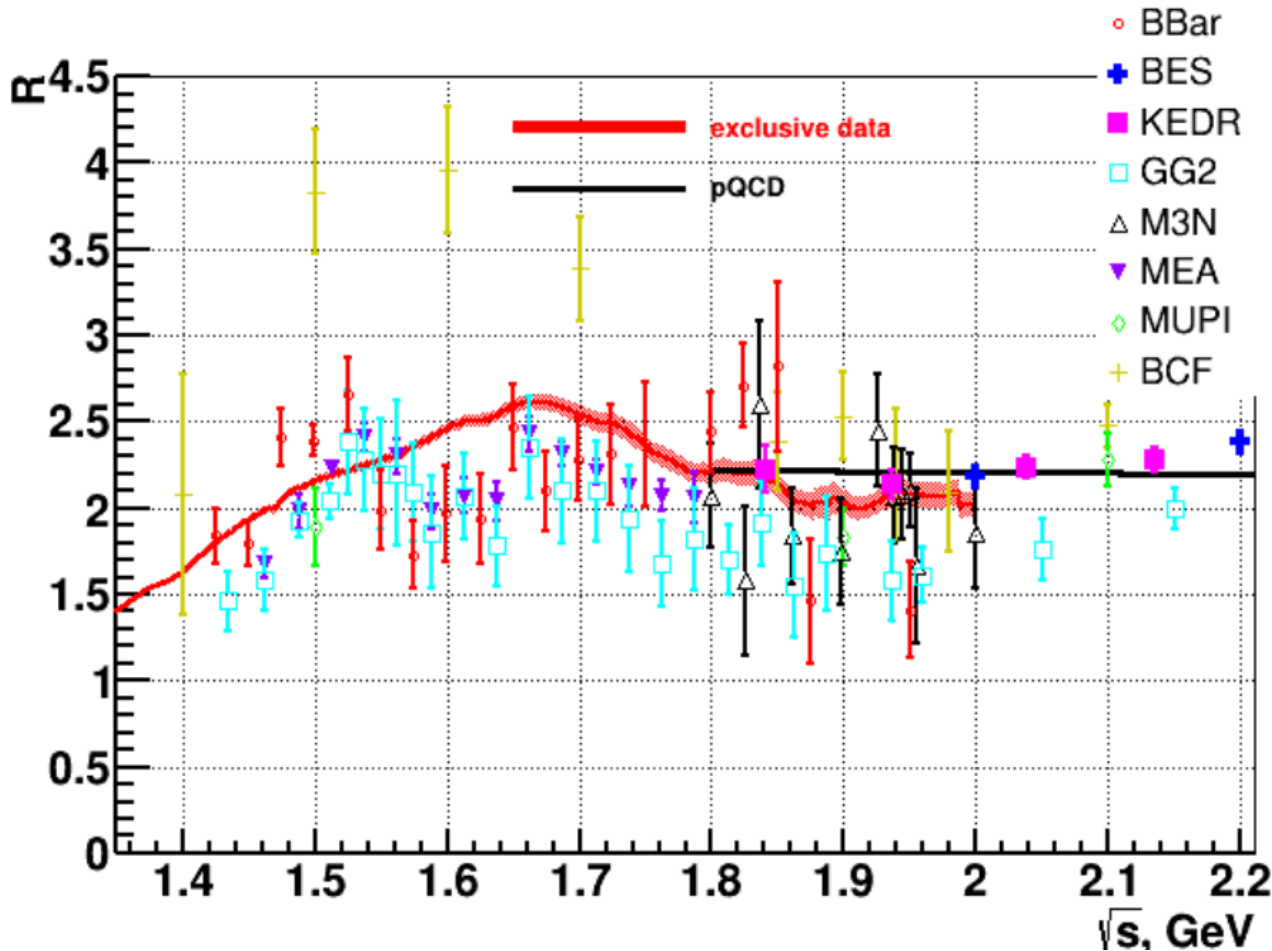
~2mm measurement of conversion point,
tracking capability,
shower profile (from 7 layers + CsI)

PID:

- × TOF system ($\sigma_T < 1\text{nsec}$)
particle id mainly for p, n
- × Muon system



CMD-3 Motivation

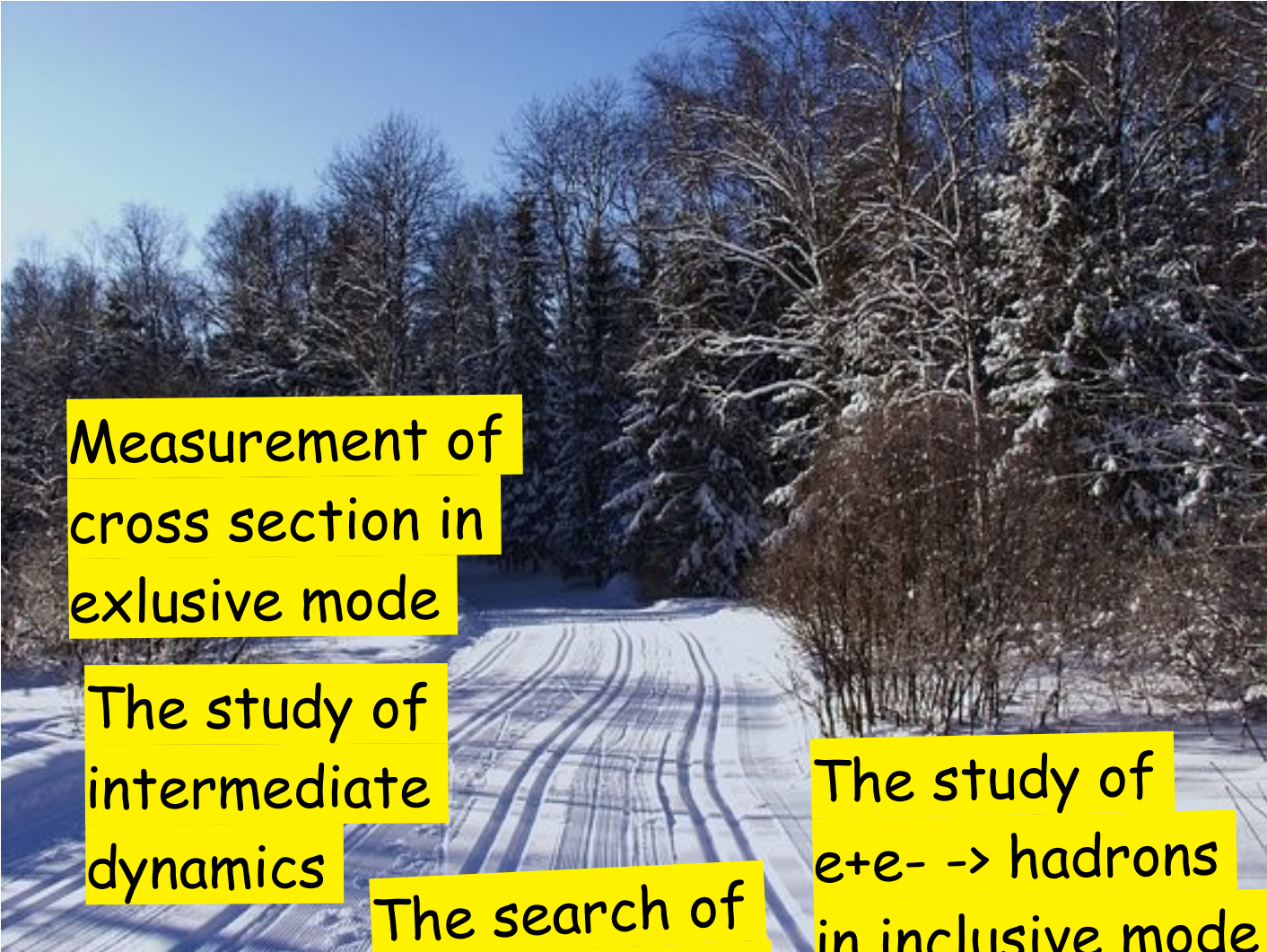


- Indication:
The sum of exclusive measurements disagree with pQCD as well as with inclusive data
- More precise data is needed
- There is still unmeasured exclusive processes

Exclusive channels of $e^+e^- \rightarrow hadrons$

Event signature	Final state (published/submitted, in progress)
2 charged	$\pi^+\pi^-$ K^+K^- $K_S K_L$ $p\bar{p}$ $\pi^+\pi^-\gamma$
2 charged + γ 's	$\pi^+\pi^-\pi^0$ $\pi^+\pi^-2\pi^0$ $\pi^+\pi^-3\pi^0$ $\pi^+\pi^-4\pi^0$ $\pi^+\pi^-\eta$ $\pi^+\pi^-\pi^0\eta$ $\pi^+\pi^-2\pi^0\eta$ $K^+K^-\pi^0$ $K^+K^-2\pi^0$ $K^+K^-\eta$ $K_S K_L \pi^0$ $K_S K_L \eta$ $\eta'(958)$
4 charged	$2\pi^+2\pi^-$ $K^+K^-\pi^+\pi^-$ $K_S K^\pm \pi^\mp$
4 charged + γ 's	$2\pi^+2\pi^-\pi^0$ $2\pi^+2\pi^-2\pi^0$ $\pi^+\pi^-\eta$ $\pi^+\pi^-\omega$ $2\pi^+2\pi^-\eta$ $K^+K^-\omega$ $K_S K^\pm \pi^\mp \pi^0$ $D^{*0}(2007)$
6 charged	$3\pi^+3\pi^-$ $K_S K_S \pi^+\pi^-$
6 charged + γ 's	$3\pi^+3\pi^-\pi^0$
Fully neutral	$\pi^0\gamma$ $2\pi^0\gamma$ $3\pi^0\gamma$ $\eta\gamma$ $\pi^0\eta\gamma$ $2\pi^0\eta\gamma$
Other	$n\bar{n}$ $\pi^0 e^+e^-$ ηe^+e^-

Published/submitted results:
 $3\pi^+3\pi^-$: PLB 723 (2013) 82-89
 η' : PLB 740 (2015) 273-277
 $p\bar{p}$: PLB 759 (2016) 634-640
 $K^+K^-\pi^+\pi^-$: PLB 756 (2016)
 $K^+K^-(at\ \phi(1020))$: PLB 760 (2016) 314-319
 $2\pi^+2\pi^-$ (near $\phi(1020)$):PLB 768 (2017) 345-350
 $\omega\eta$, $\eta\pi^+\pi^-\pi^0$: PLB 773 (2017)
 $K_S K_L$ (at $\phi(1020)$): PLB 779 (2018) 64-71
 $3\pi^+3\pi^-\pi^0$: PLB 792 (2019)
 $K^+K^-\eta$: PLB 798, (2019)134946
Observation of a fine structure ...: PLB-D-19-00534R1

A photograph of a snowy forest path. The path is covered in snow and has several dark, curved tracks from a vehicle or sled. The trees are mostly bare, with some evergreens visible on the right side. The sky is a clear, pale blue. Overlaid on the image are four yellow rectangular boxes containing black text.

Measurement of
cross section in
exclusive mode

The study of
intermediate
dynamics

The search of
rare processes

The study of
 $e^+e^- \rightarrow \text{hadrons}$
in inclusive mode



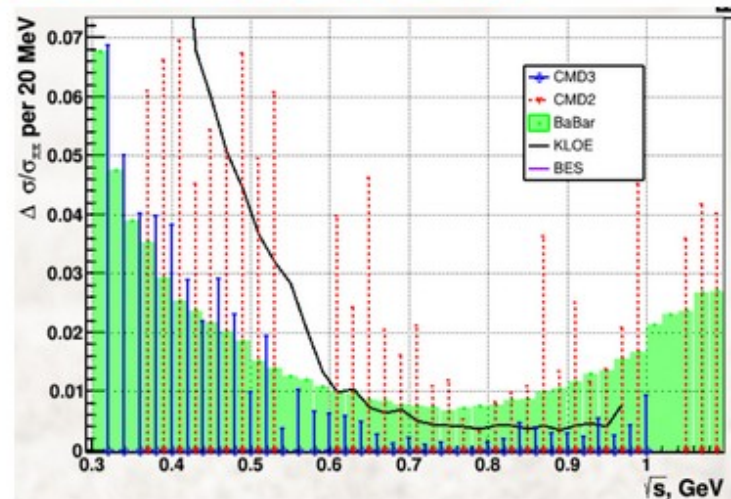
The search of
rare processes, like, $e^+e^- \rightarrow \eta'(950), f_1(1285), D^{*0}(2007)$

$e^+e^- \rightarrow \pi^+\pi^-$: pion formfactor measurement

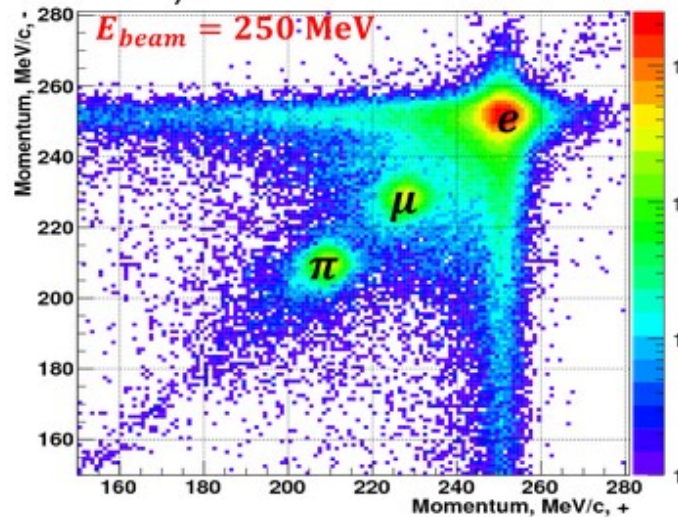
- It is a main contributor to the $a^{\text{had,LO}}_\mu$ ($\sim 73\%$)
- The CMD-3's goal is to measure the $|F_\pi|^2$ with 0.4-0.5% systematics uncertainty
- CMD-3's 2013 & 2018 statistics for $\pi^+\pi^-$ a few times larger than in other experiments
- To control systematics, two independent approaches for determination of the number of $\pi^+\pi^-$ events are used:

momentum-based and energy deposition-based

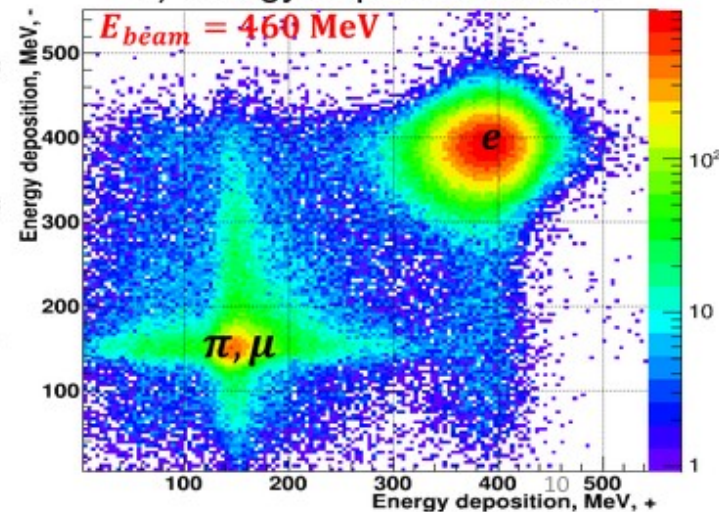
- Momentum-based approach works better at low c.m. energies (< 0.8 GeV), energy-based – at large energies (> 0.6 GeV). Using both methods in the middle allows to control systematics
- In both cases 2D-likelihood function is constructed, its minimization gives $N_{\pi\pi}/N_{ee}$



1) momentum-based



2) energy deposition-based

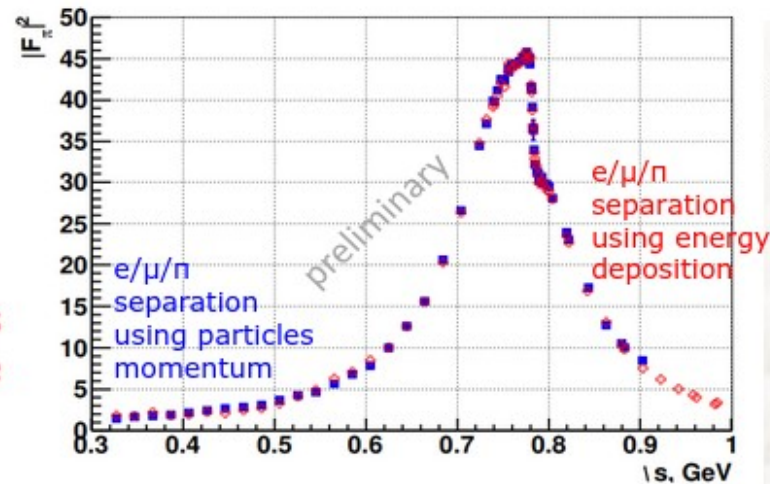
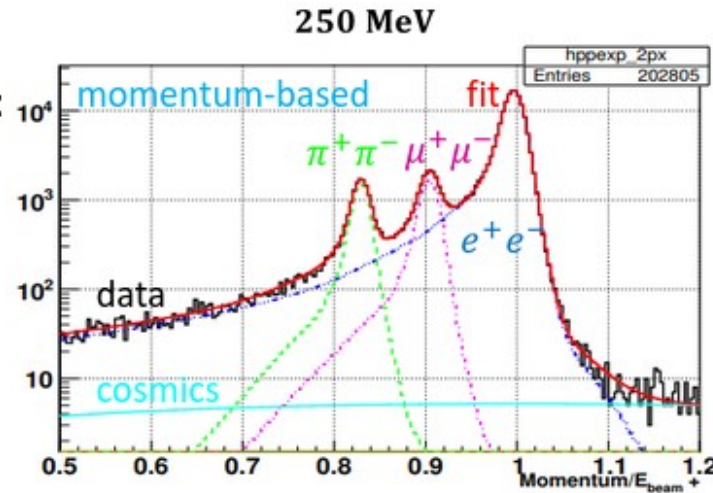


$e^+e^- \rightarrow \pi^+\pi^-$: pion formfactor measurement

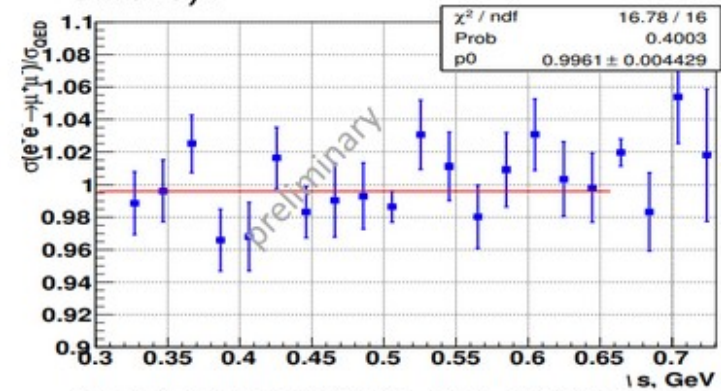
- The projection of the fitting functions after minimization:

The list of sources of systematics:

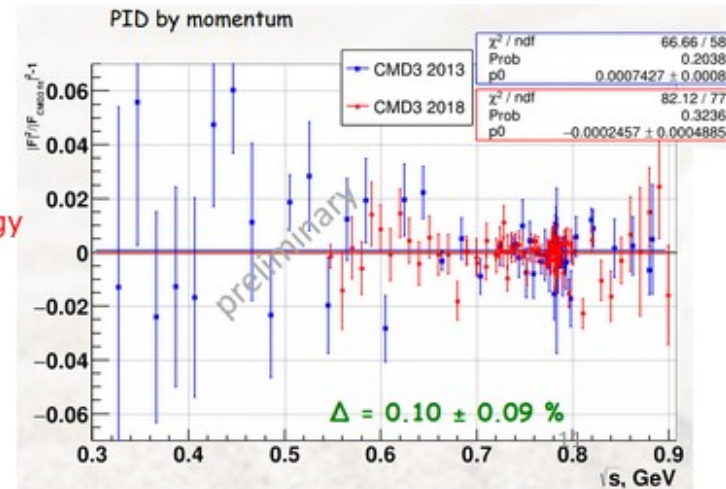
- Radiative corrections
- $e/\mu/\pi$ separation
- Uncertainty of fiducial volume
- Beam energy
- Electron bremsstrahlung loss
- Pion specific corrections
- Currently the systematics is estimated to be 0.6-0.9% (momentum-based)



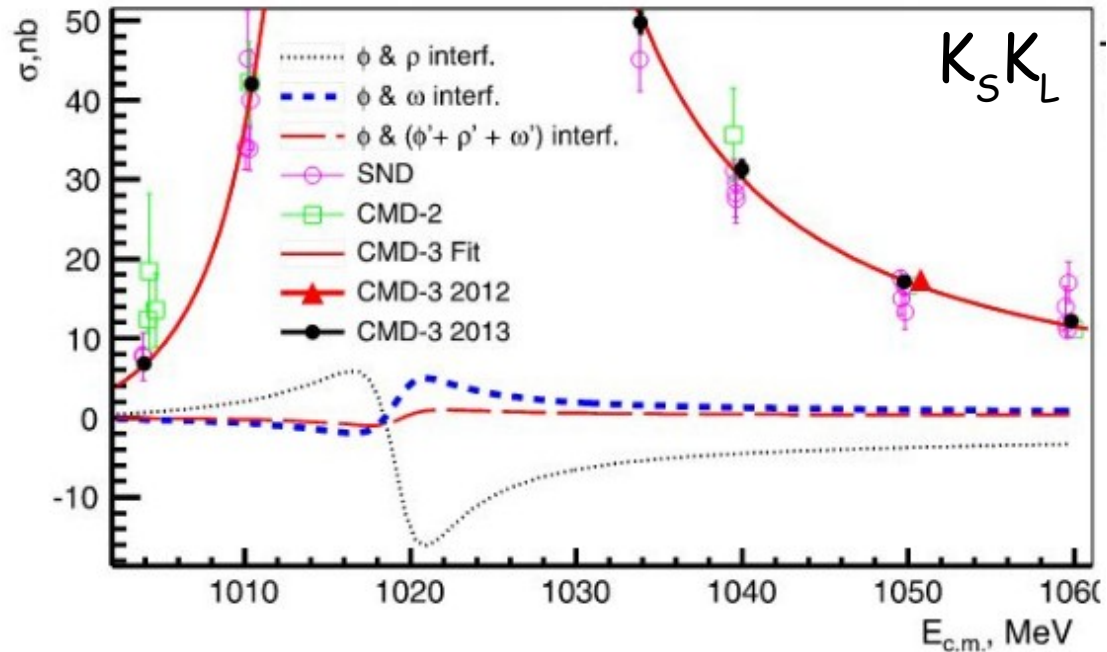
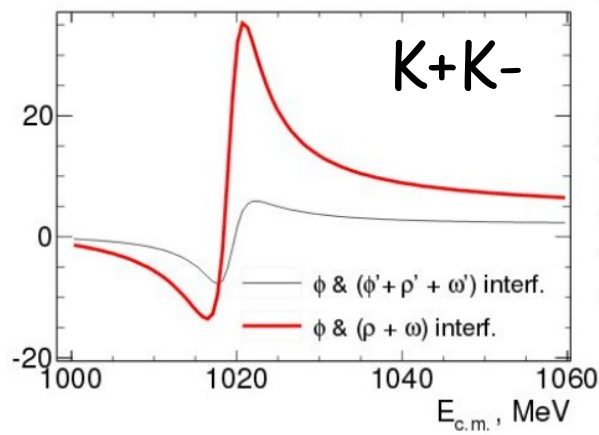
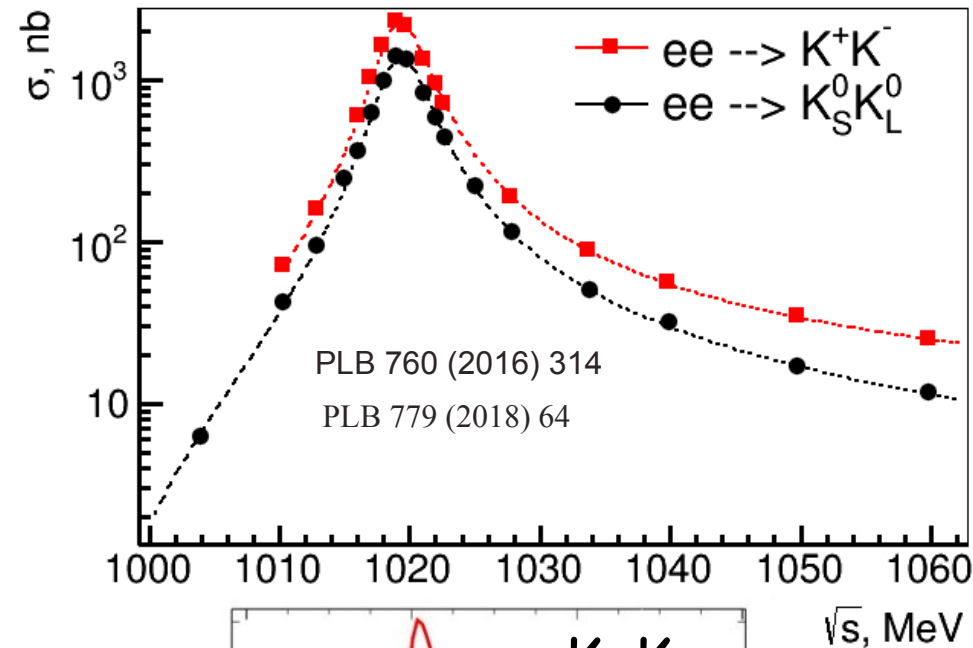
- Additional test - $\sigma(e^+e^- \rightarrow \mu^+\mu^-)$ measurement (compatible with QED at $\sim 0.25\%$):



- The results of 2013 and 2018 are consistent within $\sim 0.1\%$:



$e^+e^- \rightarrow K \text{ anti}K$



$$m_\phi = 1019.464 \pm 0.061 \text{ MeV}/c^2$$

$$\Gamma_\phi = 4.250 \pm 0.015 \text{ MeV}$$

$$\Gamma_{\phi \rightarrow ee} B_{\phi \rightarrow K^+ K^-} = 0.671 \pm 0.020 \text{ keV}$$

$$\Gamma_{\phi \rightarrow ee} B_{\phi \rightarrow K_S^0 K_L^0} = 0.428 \pm 0.009 \text{ keV}$$

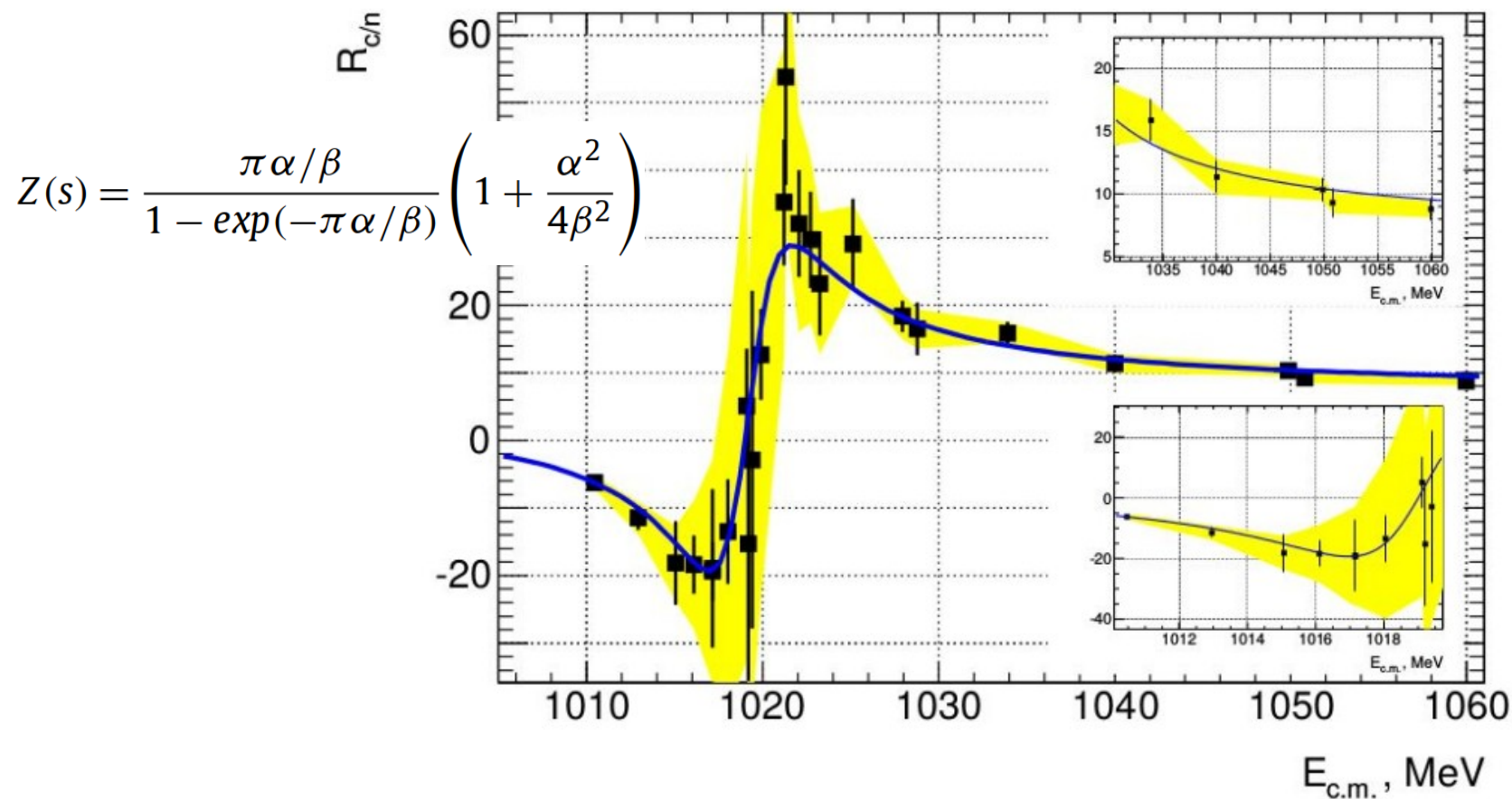
$$R_{c/n} = \sigma_{e^+e^- \rightarrow K^+K^-} \times \frac{p_{K^0}^3(s)}{p_{K^\pm}^3(s)} \times \frac{1}{Z(s)} - \delta_{K_S^0 K_L^0} \times \sigma_{e^+e^- \rightarrow K_S^0 K_L^0}$$

$$r_{\rho/\omega} = 0.91 \pm 0.04$$

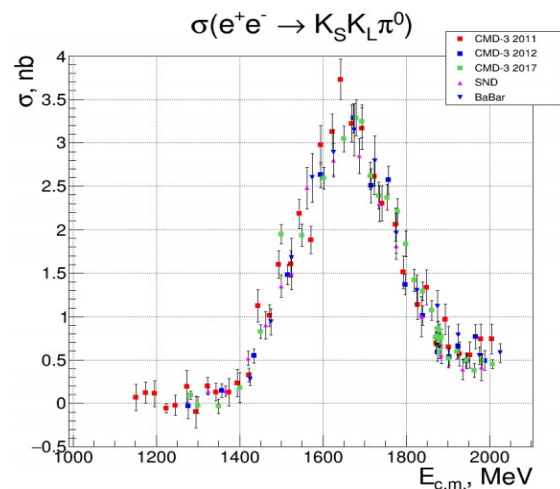
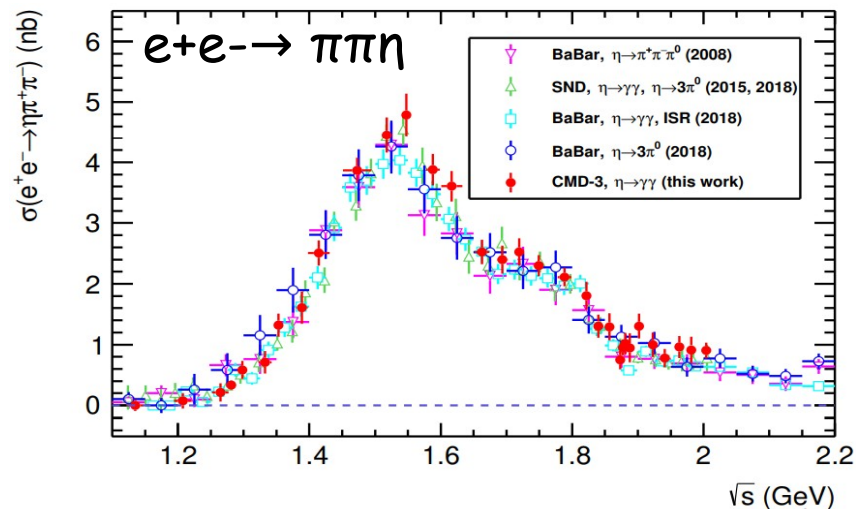
$$\delta_{K_S^0 K_L^0} = 0.989 \pm 0.003$$

$$\chi^2/ndf = 10/22$$

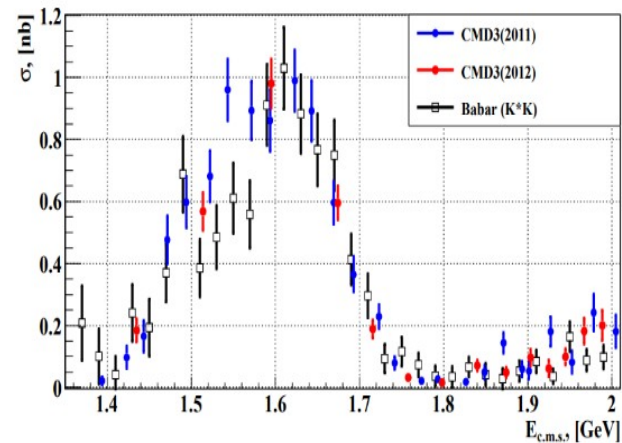
Two floating
parameters



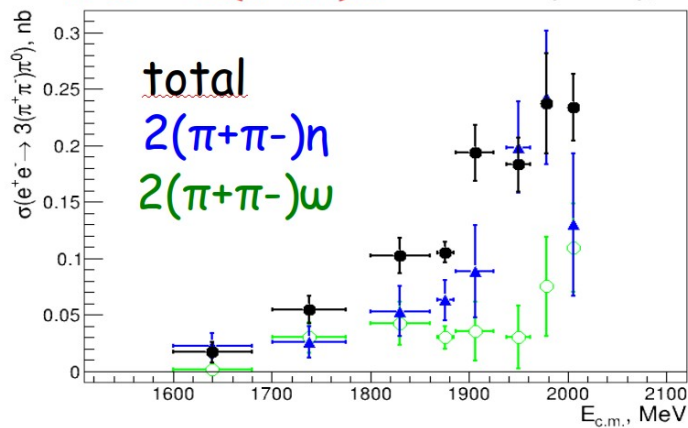
Other processes



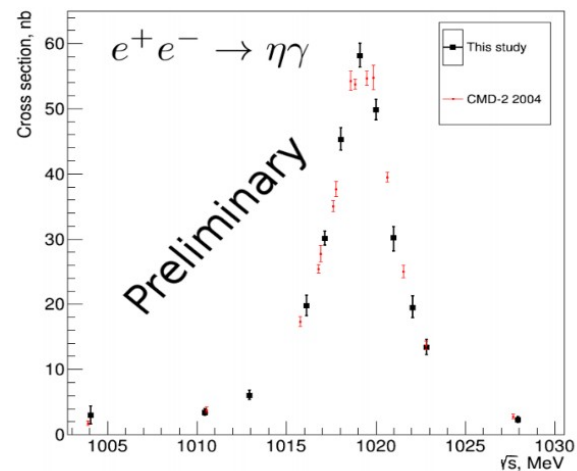
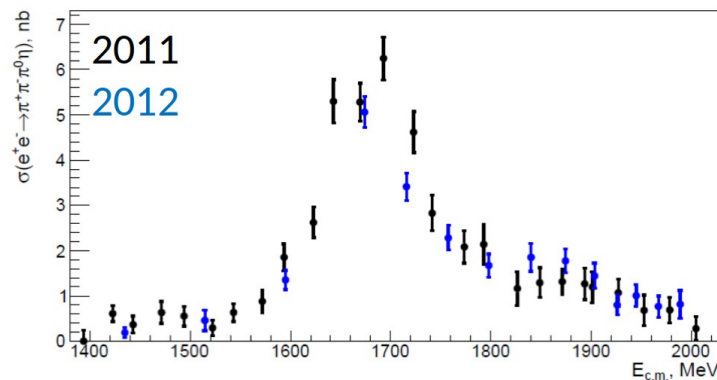
• Study of $e^+e^- \rightarrow K^+K^-\pi^0$:



• $e^+e^- \rightarrow 3(\pi^+\pi^-)\pi^0$: PLB 792 (2019), 419-423

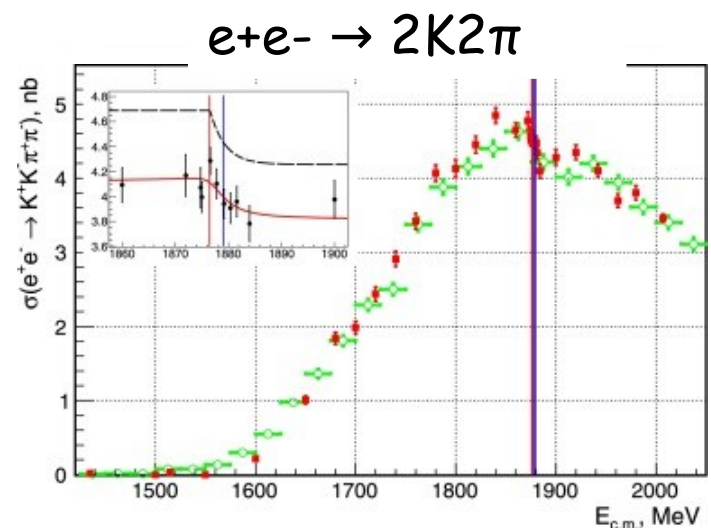
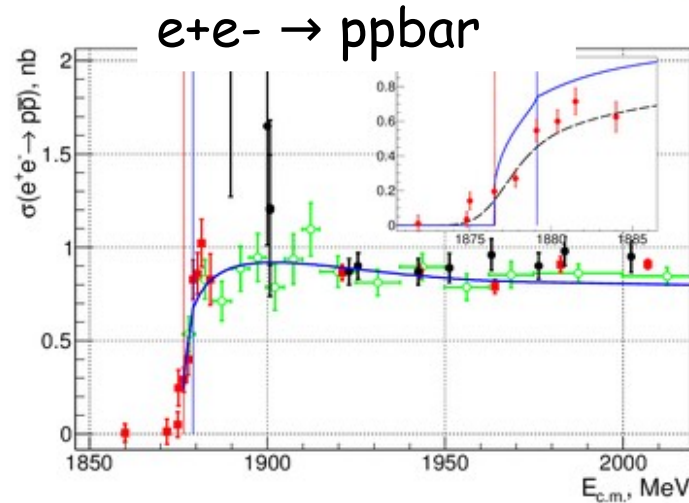
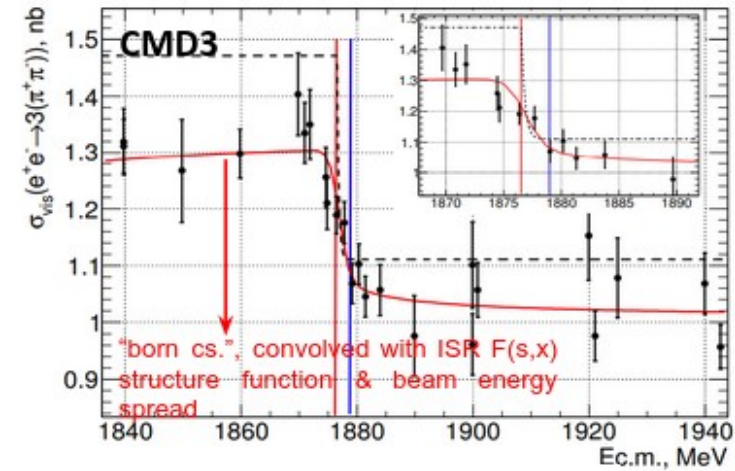
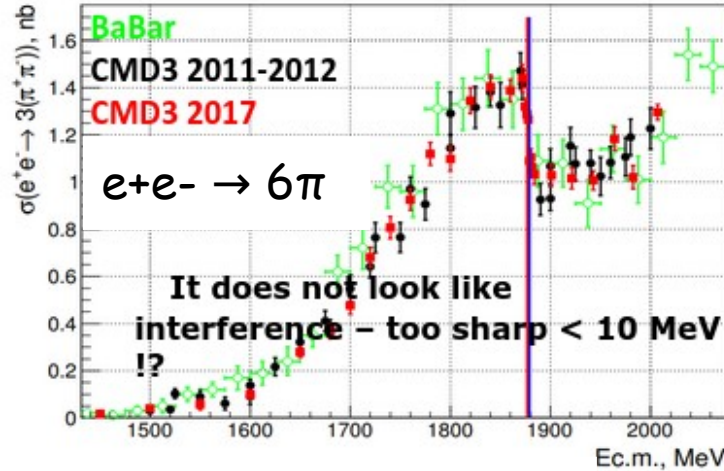


• $e^+e^- \rightarrow \pi^+\pi^-\pi^0\eta$: PLB 773 (2017) 150-158



Multihadron production @ $N\bar{N}$ threshold

- In 2017 we did the detailed scan of $N\bar{N}$ threshold region with the step 0.8 MeV ($\sim$ beam energy spread)
- Several dip structures with ~ 1 MeV width are seen in multihadron production!
(see details in PLB 794 (2019) 64-68)
- Effect can be described via optical nucleon-antinucleon potentials ("Milstein-Salnikov" parametrization, see Nuc. Phys. A 977 (2018) 60-68)



Results of the fit to the exponentially rising function. Only statistical uncertainties are shown.

Reac.	A, nb	B, nb	E _{thr} , MeV	σ _{thr} , MeV	χ ² /ndf
<i>p</i> $\bar{p}$	0 – fxd	0.91±0.02	1877.1±0.2	0.18±0.27	29/26
<i>p</i> $\bar{p}$	0 – fxd	0.91±0.02	1876.54-fxd	0.76±0.28	31/27
6π	1.55±0.02	−0.42±0.03	1875.8±0.2	0.18±0.67	17/20
6π	1.54±0.02	−0.41±0.03	1876.54-fxd	0.0±2.5	18/21
2K2π	4.69±0.08	−0.44±0.12	1878.8±0.2	0.35±2.69	7/10
2K2π	4.70±0.08	−0.45±0.12	1876.54-fxd	2.36±2.01	8/11

$$\sigma_{\text{Born}}(\text{E}_{\text{c.m.}}) = \text{A} + \text{B} \left[1 - \exp \left(-\frac{(\text{E}_{\text{c.m.}} - \text{E}_{\text{thr}})}{\sigma_{\text{thr}}} \right) \right]$$

Multihadron production @ $N\bar{N}$ threshold

- However, some questions still remain: why no "dip" structure in $e^+e^- \rightarrow 2\pi^+2\pi^-, \pi^+\pi^-4\pi^0$?

$e^+e^- \rightarrow 2(\pi^+\pi^-)$

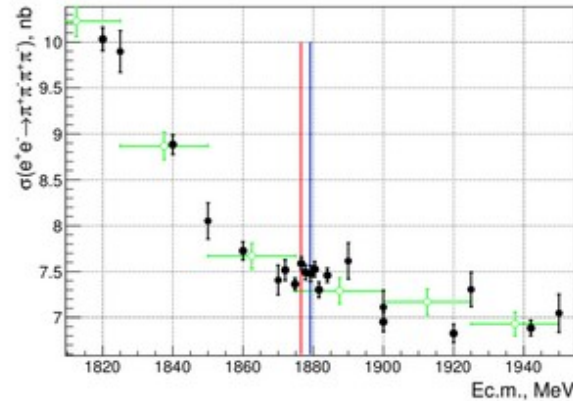
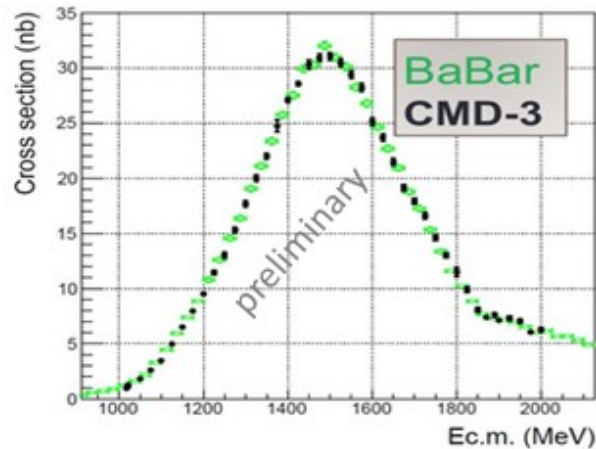
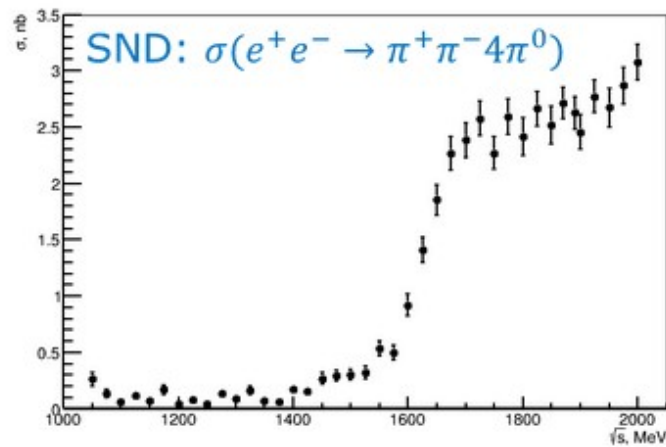
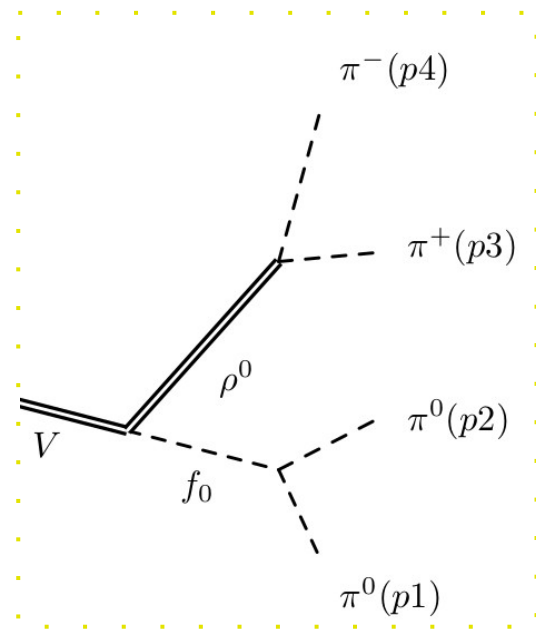
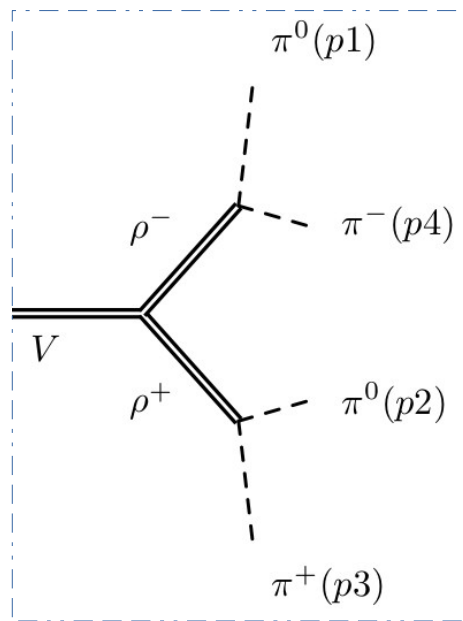
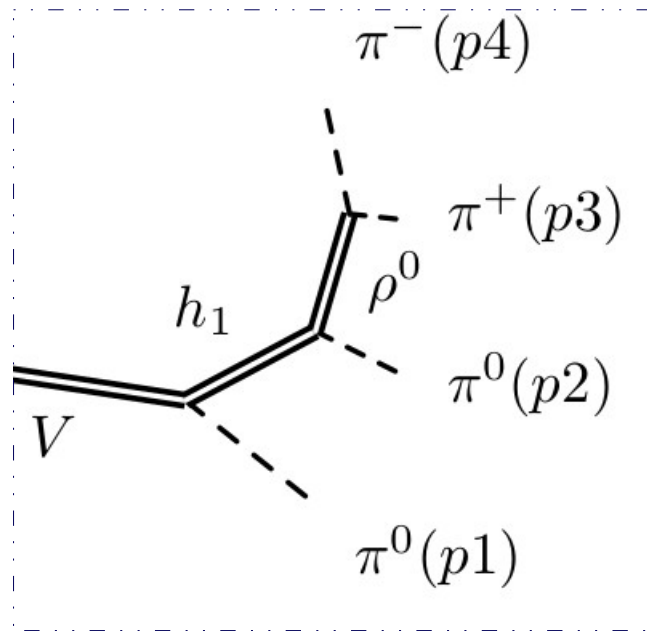
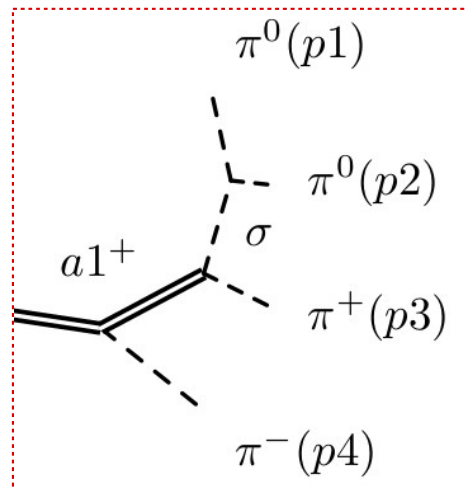
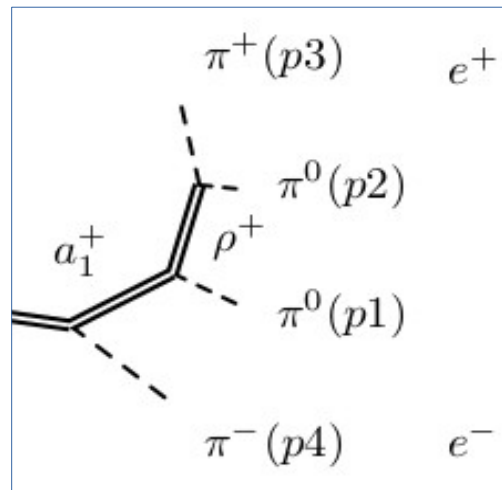
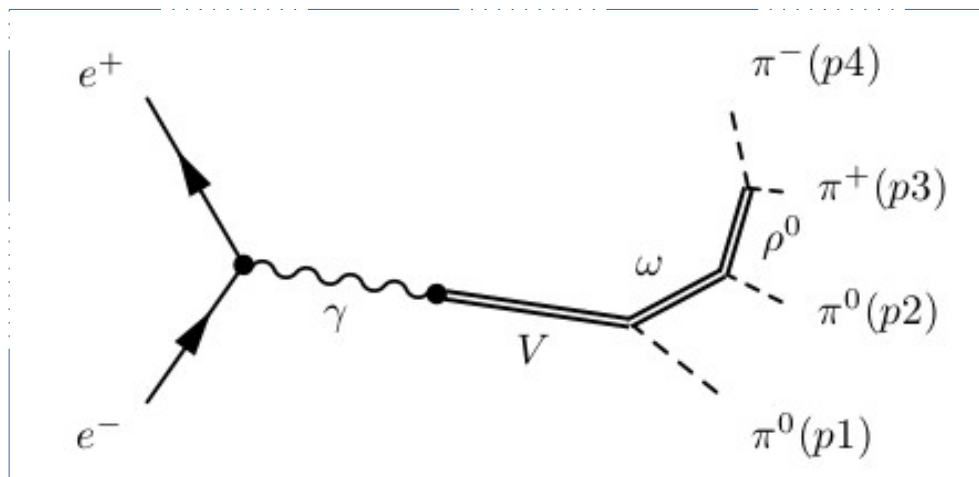


Figure 4: The $e^+e^- \rightarrow 2(\pi^+\pi^-)$ cross section measured with the CMD-3 detector. Lines show the $p\bar{p}$ and $n\bar{n}$ thresholds.

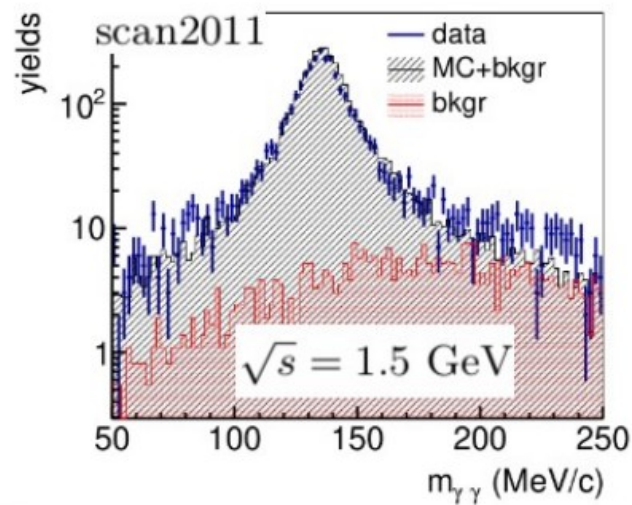




Event selection

($ee \rightarrow \pi^+\pi^-\pi^0$) 43 kevents

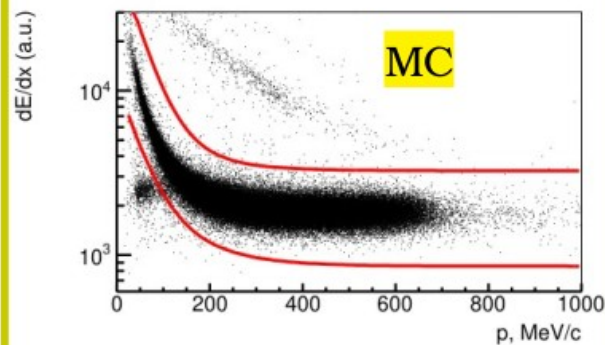
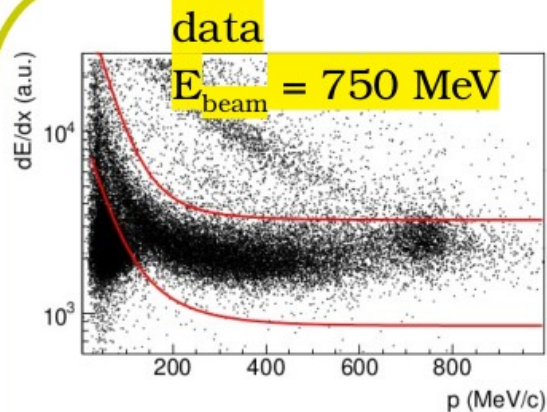
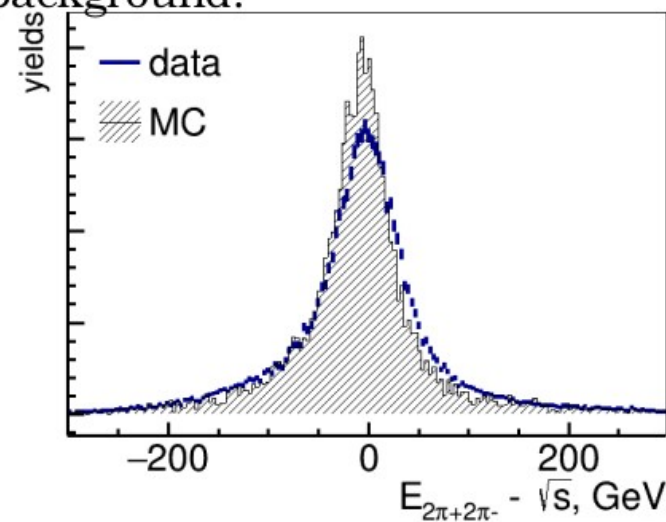
- $0.75 < \theta_{\pi,\gamma} < \pi - 0.75$ rad
- Total $E - \sqrt{s}$ and $P < 150$ MeV/(c)
- Two candidates for π^0
- 6C kinematic fit
- The **invariant mass** spectrum of 3rd and 4th **photons** is used for the estimation of the contribution of background:



Event selection

($ee \rightarrow 2\pi^+2\pi^-$) 83 kevents

- $0.75 < \theta_{\pi} < \pi - 0.75$ rad
- $|Total E - \sqrt{s}|$ and $P < 150$ MeV/(c)
- 4C kinematic fit
- The spectrum of **total energy of four tracks** ($E - \sqrt{s}$) is used for the estimation of the contribution of background:



dE/dx vs momentum

Amplitude analysis

The production of 4π system can proceed via a list of intermediate states:

- $\omega[1^{--}]\pi^0[0^{-+}]$ (only $2\pi^0 2\pi^\pm$)
- $a_1(1260)[1^+]\pi[0^-]$
- $\rho[1^{--}]f_0/\sigma[0^{++}]$
- $\rho f_2(1270)[2^{++}]$
- $\rho^+\rho^-$ (only $2\pi^0 2\pi^\pm$)
- $a_2(1320)[2^{++}]\pi$
- $h_1(1170)[1^{+-}]\pi^0$ (only $2\pi^0 2\pi^\pm$)
- $\pi'(1300)(0^{-+})\pi$

The likelihood for model under test is

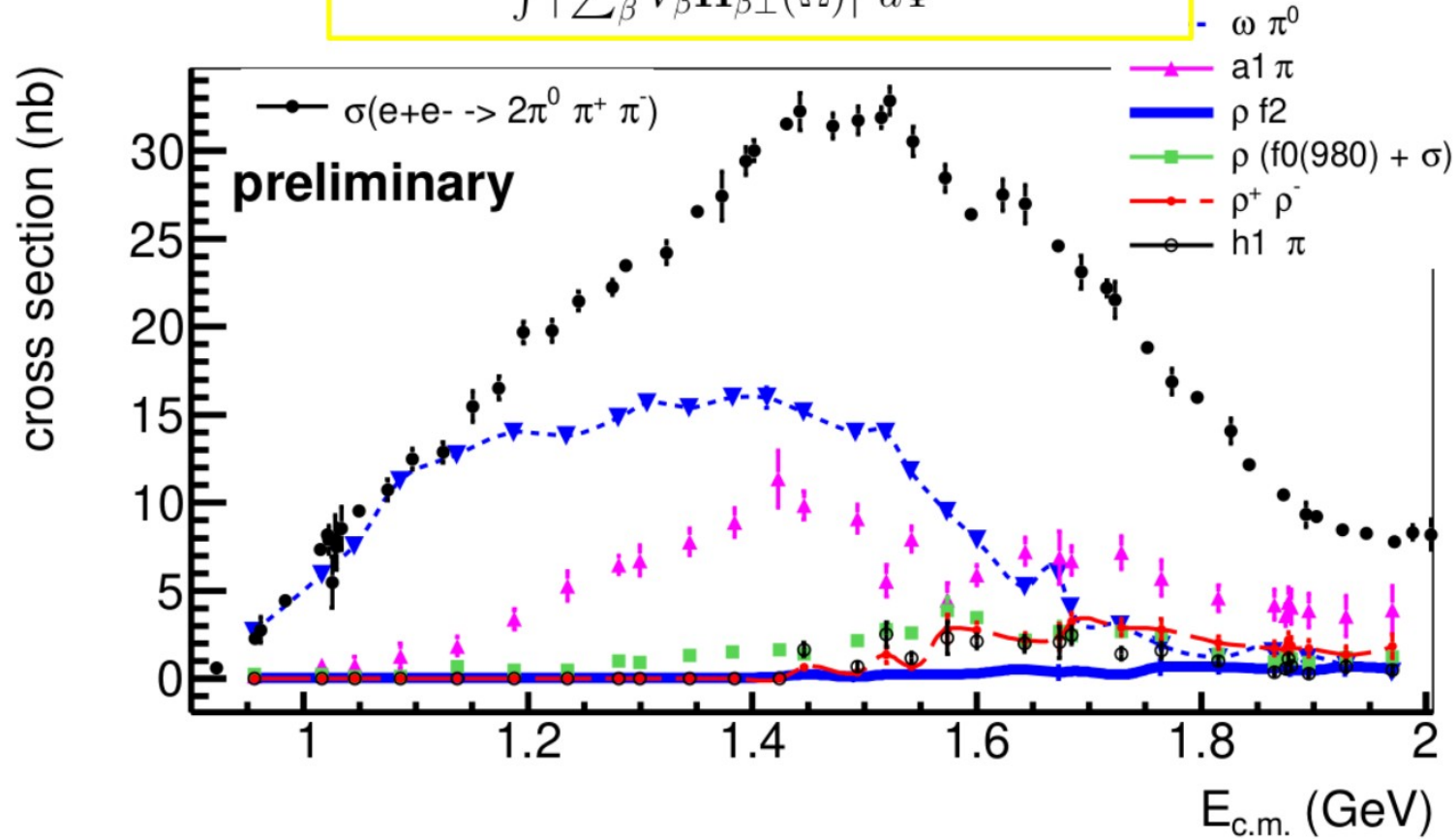
$$L = -\ln \prod_i \frac{|\sum_{\alpha} \mathbf{V}_{\alpha} A_{\alpha}^0(\Omega_i)|^2}{\frac{1}{N_{\text{MC}}^{\text{gen}}} \sum_k |\sum_{\alpha} \mathbf{V}_{\alpha} A_{\alpha}^0(\Omega_k)|^2} - \\ - \ln \prod_j \frac{|\sum_{\alpha} \mathbf{V}_{\alpha} A_{\alpha}^{\pm}(\Omega_j)|^2}{\frac{1}{N_{\text{MC}}^{\text{gen}}} \sum_k |\sum_{\alpha} \mathbf{V}_{\alpha} A_{\alpha}^{\pm}(\Omega_k)|^2},$$

The relative number of events I at a particular point Ω in phase space can be represented as

$$I(\Omega) = |\sum_{\alpha} V_{\alpha} A_{\alpha}(\Omega)|^2$$

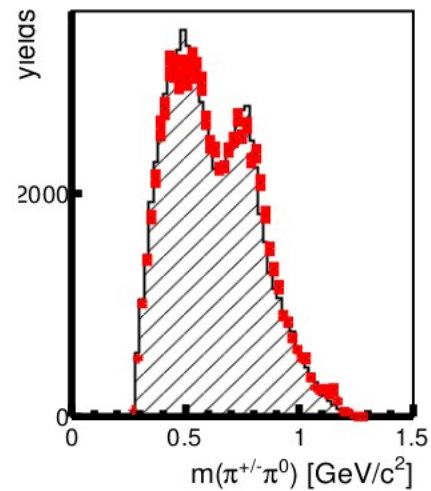
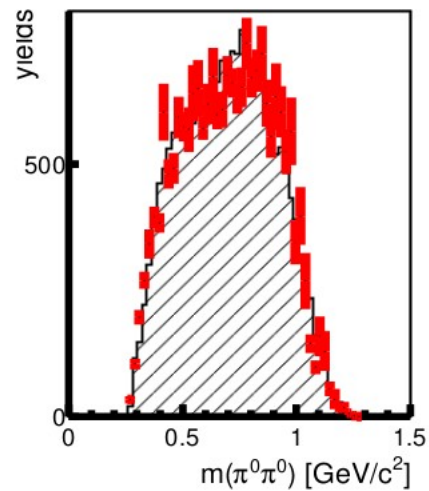
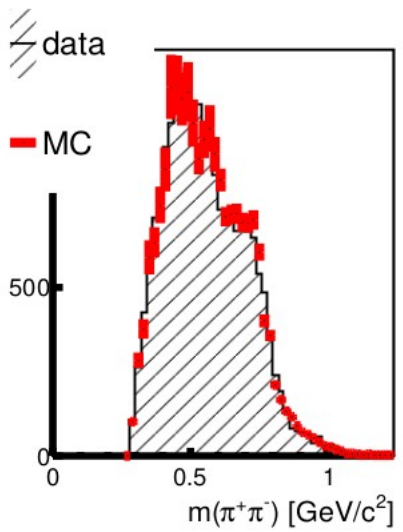
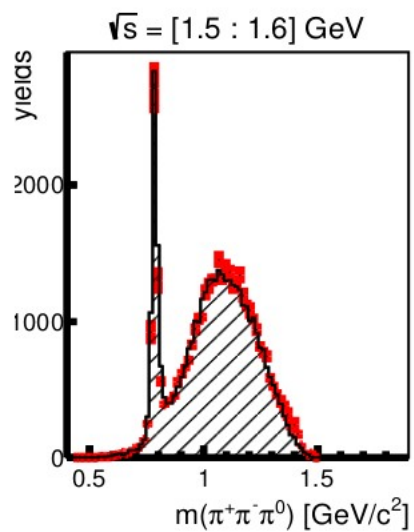
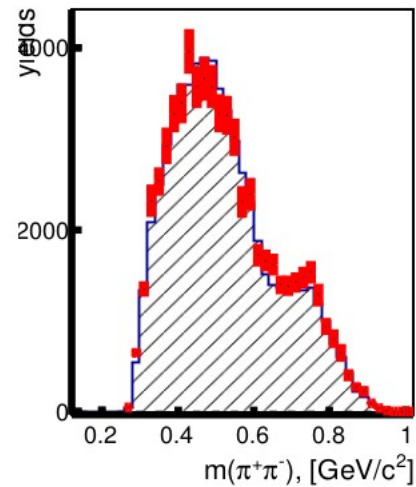
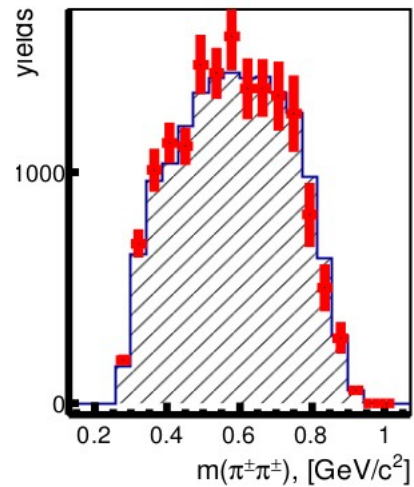
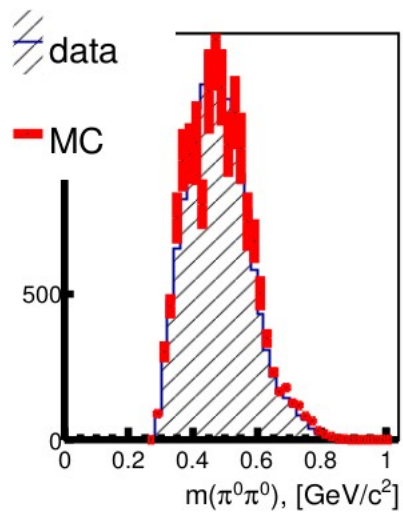
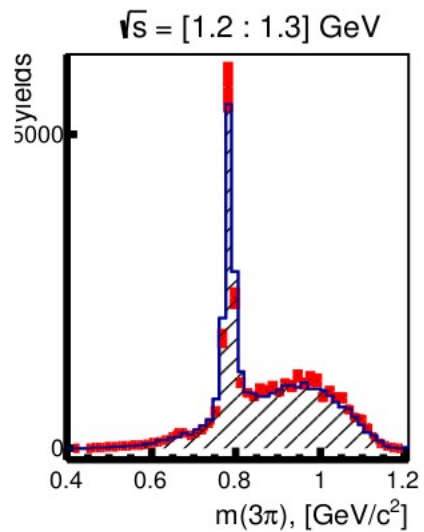
where the sum runs over all intermediate states, V_{α} - the complex production amplitude (the free parameter) and $A_{\alpha}(\Omega)$ - the amplitude at a particular point in phase space.

$$R_i(s) = \frac{\int |V_i \cdot \mathbf{H}_{i\perp}(\Omega)|^2 d\Phi}{\int |\sum_{\beta} V_{\beta} \mathbf{H}_{\beta\perp}(\Omega)|^2 d\Phi} \cdot \sigma_{2\pi^0\pi^+\pi^-}(s)$$

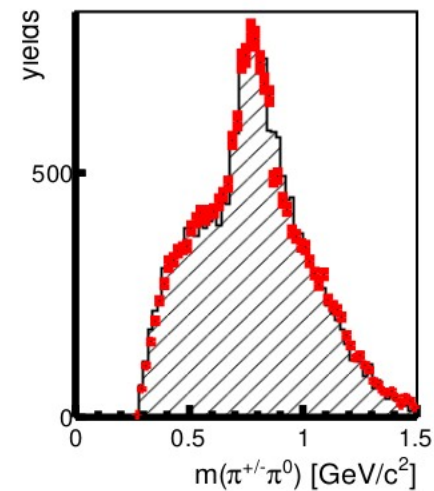
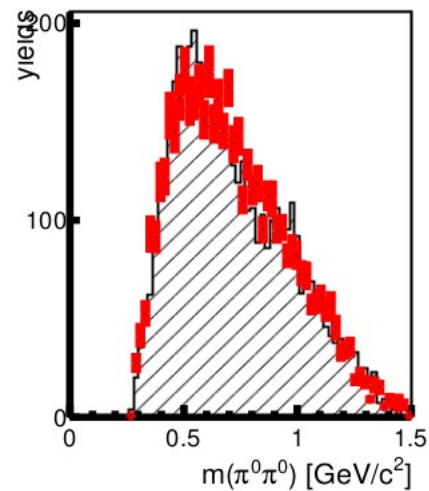
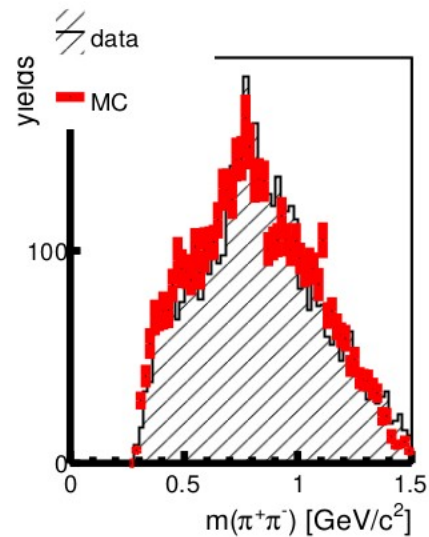
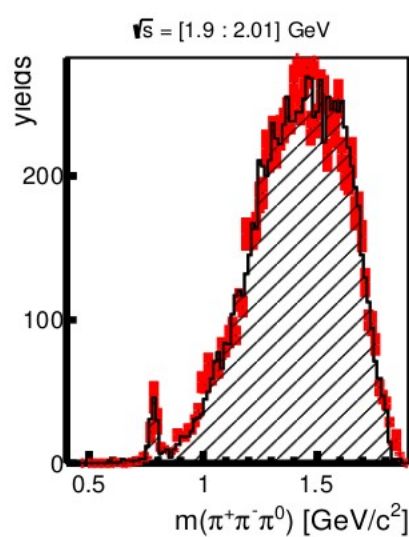
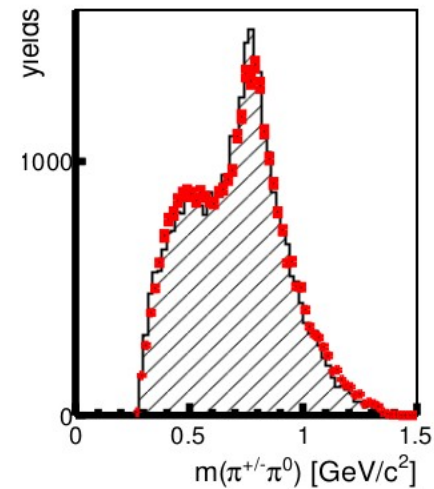
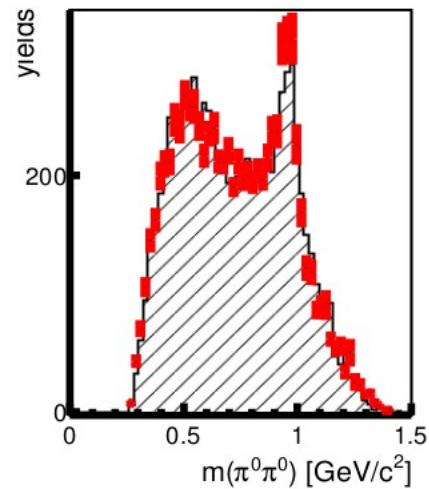
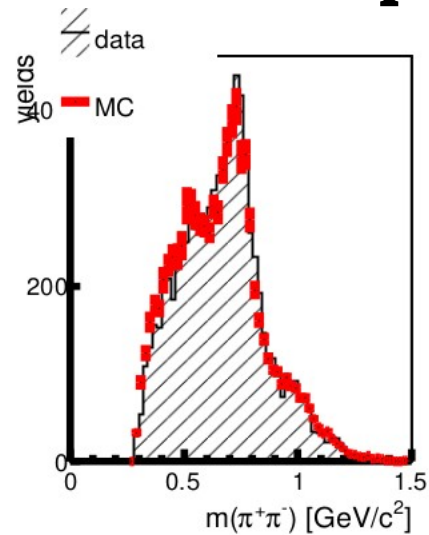
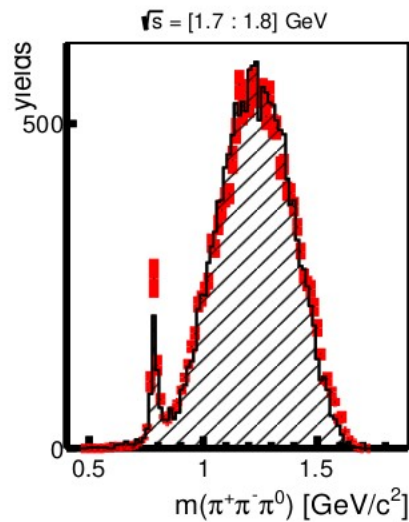


Obtained amplitudes can be used for the prediction of $W \rightarrow 4\pi$, ex., $\tau \rightarrow \omega\pi^-$,
 $\tau \rightarrow a_1(1260)\pi$, $\tau \rightarrow \rho^- [\sigma(500) + f_0(980)]$, $\tau \rightarrow \rho^- f_2(1270)$, $\tau \rightarrow \rho^- \rho^0$, $\tau \rightarrow h_1(1170)\pi^0$ 20

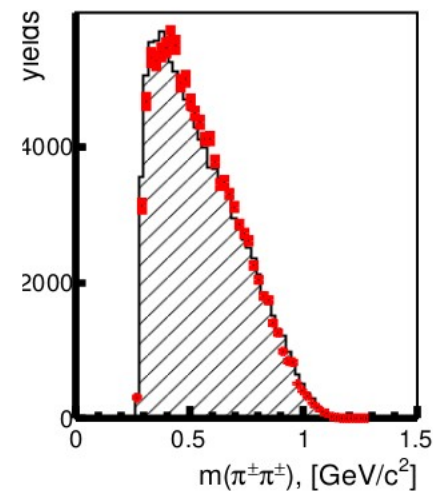
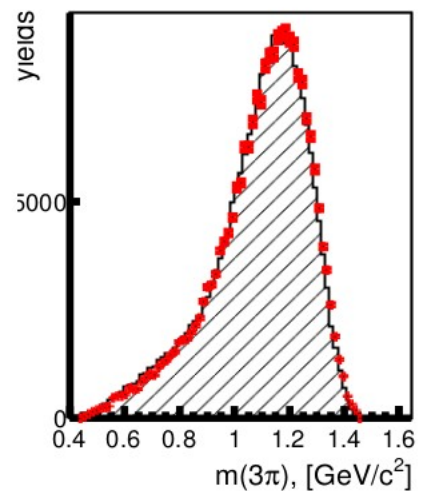
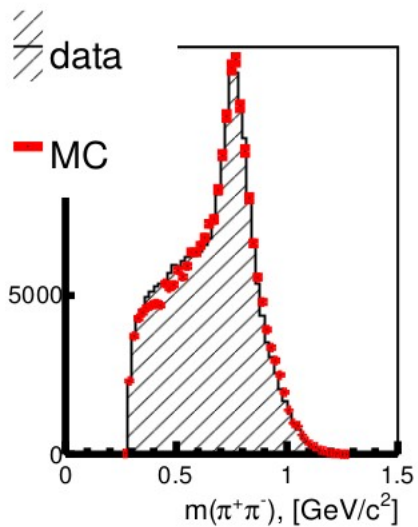
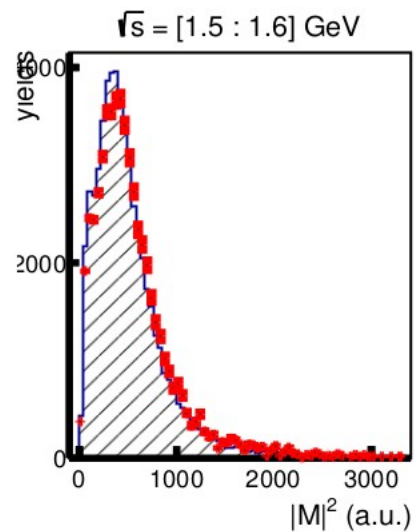
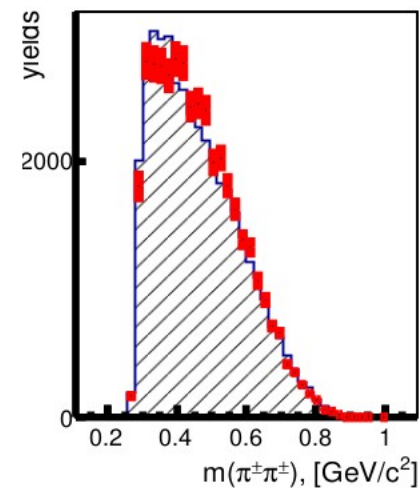
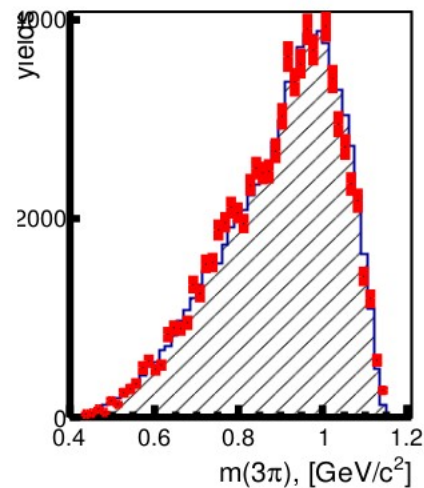
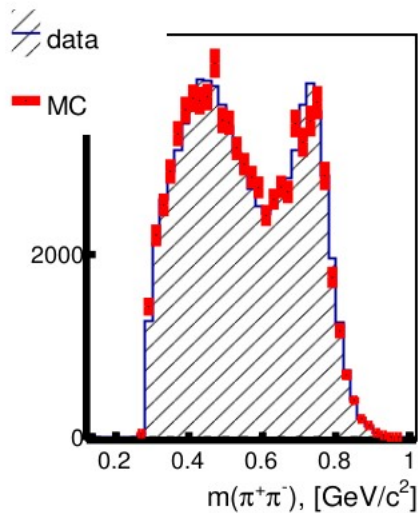
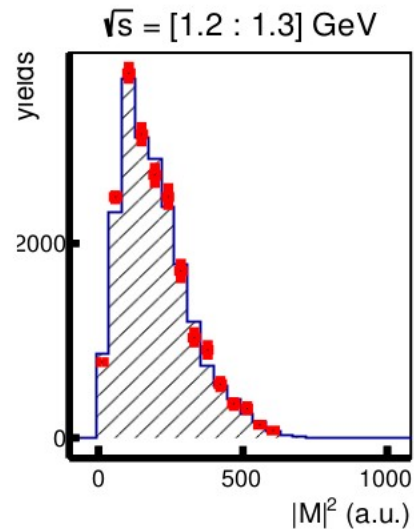
$ee \rightarrow \pi^+\pi^-\pi^0$



$ee \rightarrow \pi^+\pi^-\pi^0$



$ee \rightarrow 2\pi^+2\pi^-$

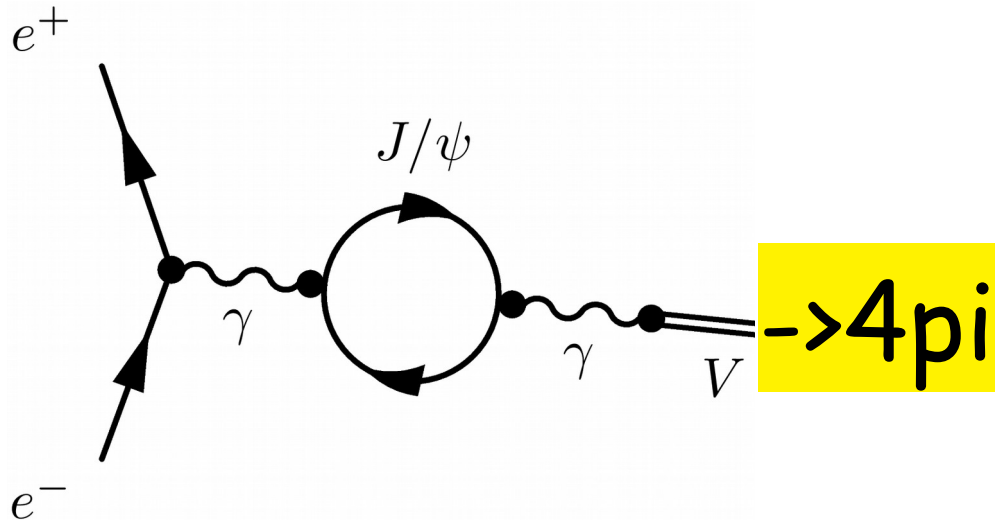


There are three different options to study dynamics (measure cross section) at BESIII

1. Using ISR events in data sets at charmonium and other resonances
2. Using data from R-scans
3. Huge BESIII data at, ex., J/ψ allows to study the dynamics of J/ψ decays into hadrons as well as continuum dynamics

There are three different options to study dynamics (measure cross section) at BESIII

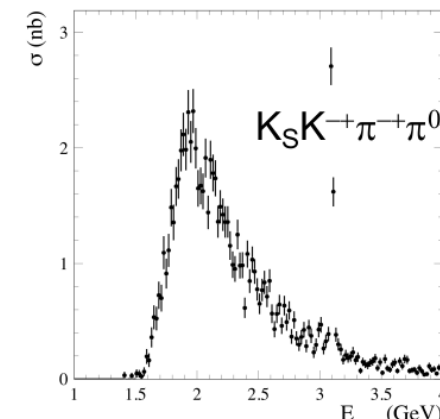
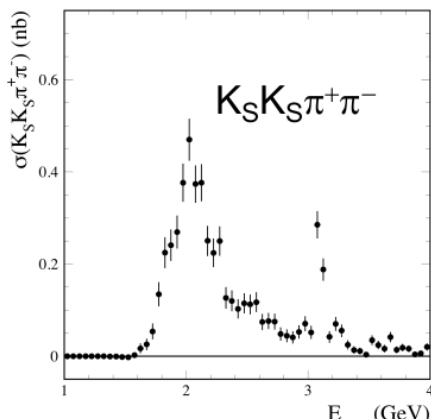
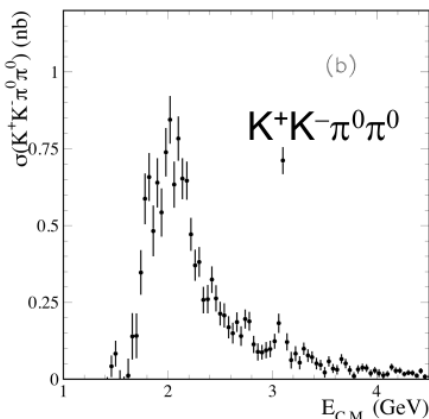
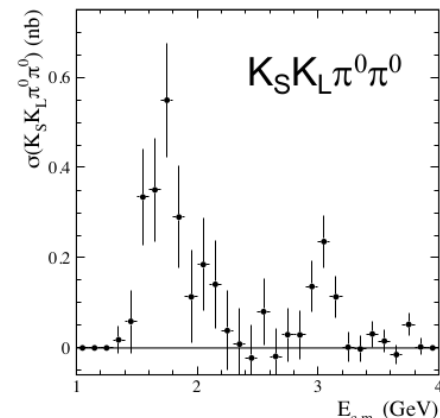
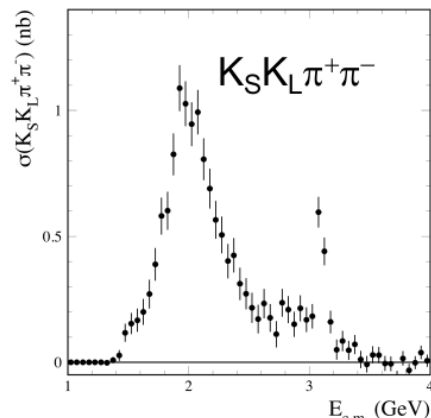
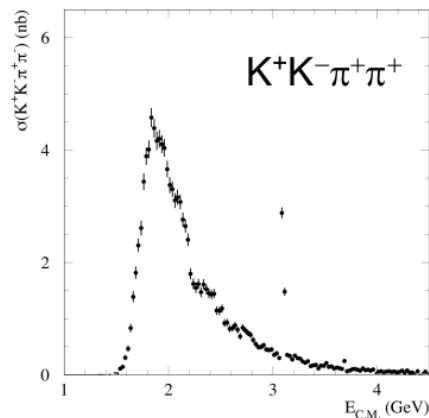
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$$B(J/\psi \rightarrow \pi^+\pi^-2\pi^0) \sim 5 \times 10^{-3}$$

$$10 \times 10^9 \times B(J/\psi \rightarrow \pi^+\pi^-2\pi^0) = 5 \times 10^6$$

All possible $KK\pi\pi$ combinations are measured – BaBar data



Contribution to $(g-2)_\mu$: (10^{-10} units)

BaBar data only !

using iso-spin

$1.35 \pm 0.09 \pm 0.38 \pm 0.03$

direct

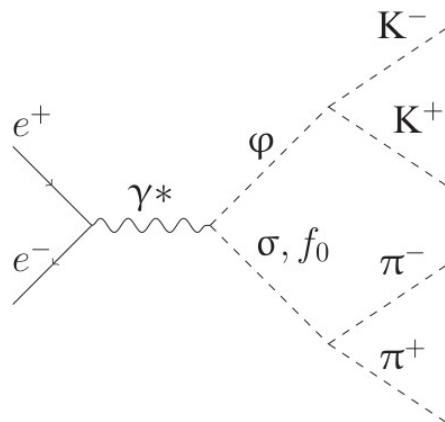
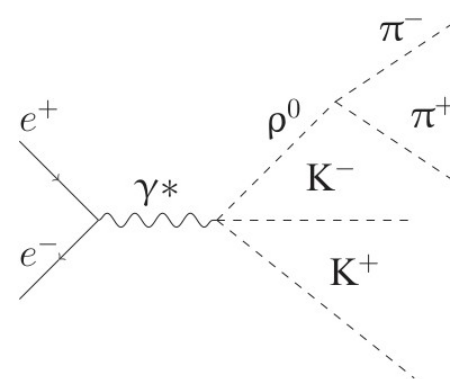
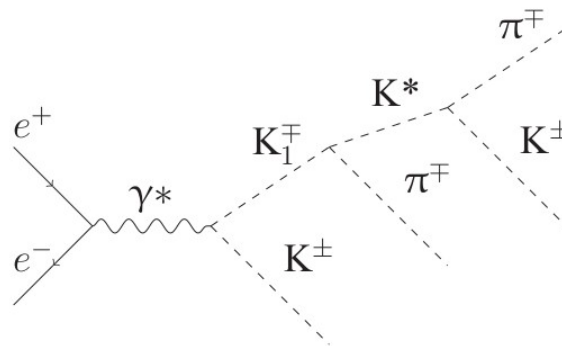
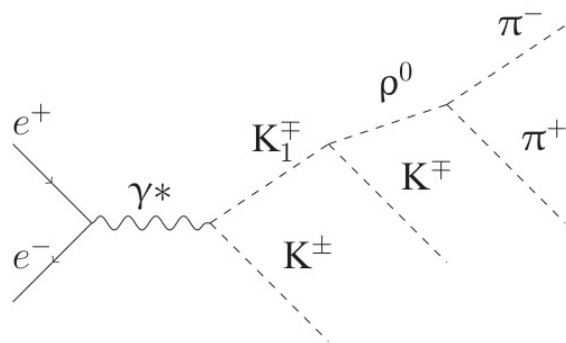
2.41 ± 0.11

$\sqrt{s} < 2.0$ GeV

26

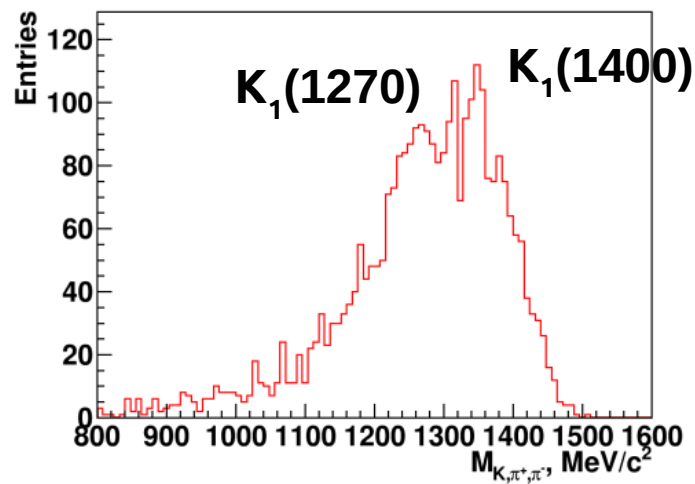
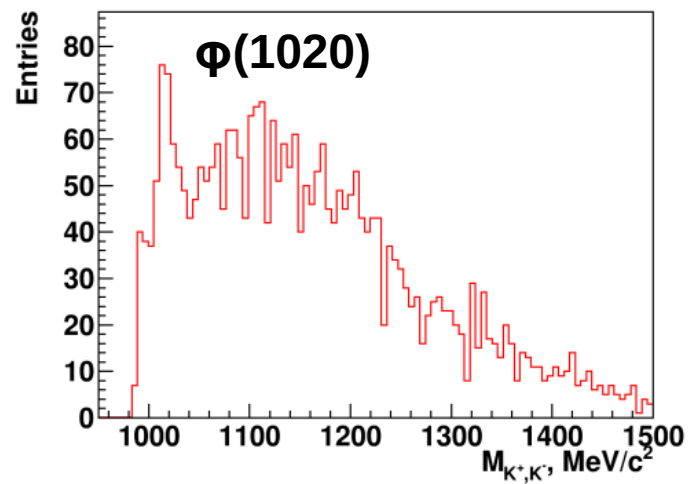
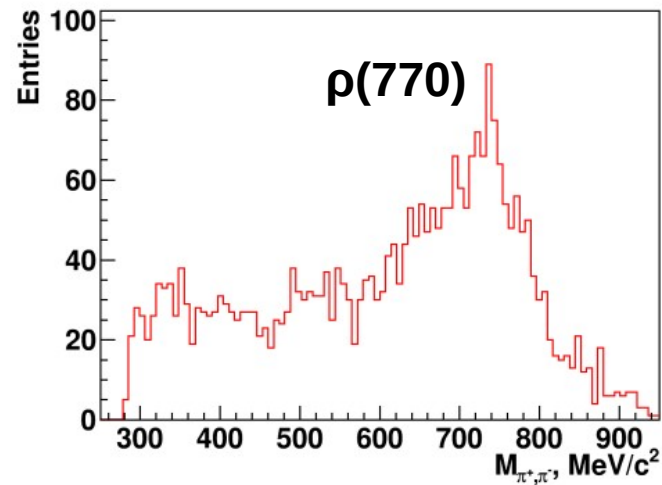
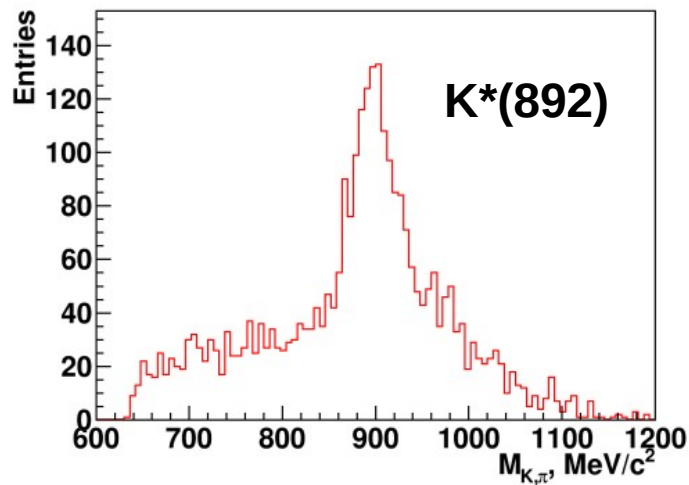
$$\sigma(K\bar{K}\pi\pi) = 9[\sigma(K^+K^-2\pi^0) - \sigma(\phi 2\pi^0)] + \frac{9}{4}\sigma(K^{*0}K^\pm\pi^\mp) + \frac{3}{2}\sigma(\phi\pi^+\pi^-) + 4\sigma(K^+K^-\rho^0).$$

The most important diagrams for the analysis of $e^+e^- \rightarrow K^+K^-\pi^+\pi^-$

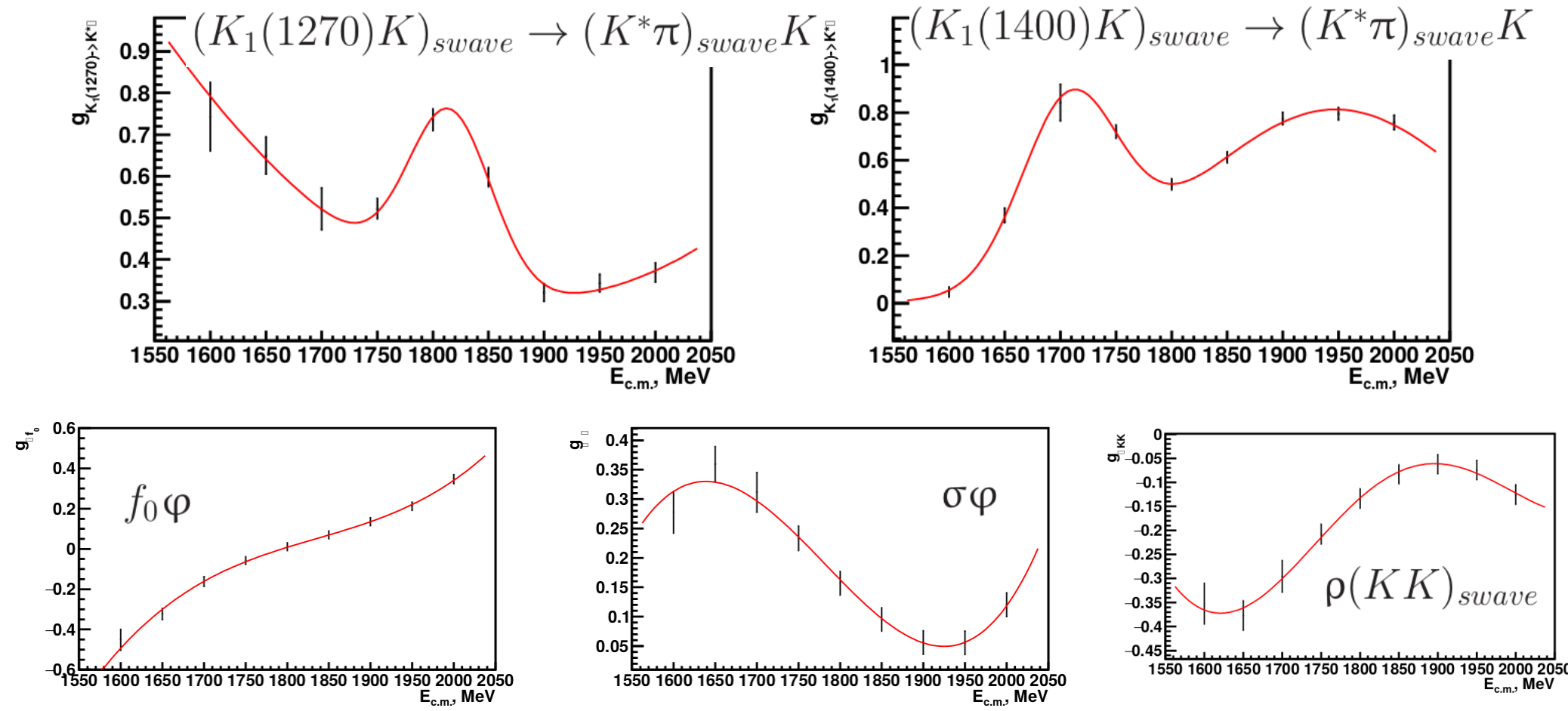


- $e^+e^- \rightarrow (K_1(1270)K)_{swave} \rightarrow (K^*\pi)_{swave}K \rightarrow K\pi\pi K$
- $e^+e^- \rightarrow (K_1(1400)K)_{swave} \rightarrow (K^*\pi)_{swave}K \rightarrow K\pi\pi K$
- $e^+e^- \rightarrow (K_1(1270)K)_{swave} \rightarrow (\rho K)_{swave}K \rightarrow \pi\pi K K$
- $e^+e^- \rightarrow f_0\phi \rightarrow \pi\pi K K$
- $e^+e^- \rightarrow \sigma\phi \rightarrow \pi\pi K K$
- $e^+e^- \rightarrow \rho(KK)_{swave}$

Invariant mass spectra for $e^+e^- \rightarrow K^+K^-\pi^+\pi^-$ (10 kevents)



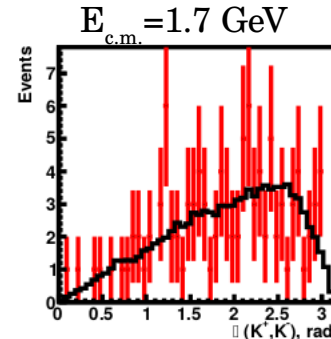
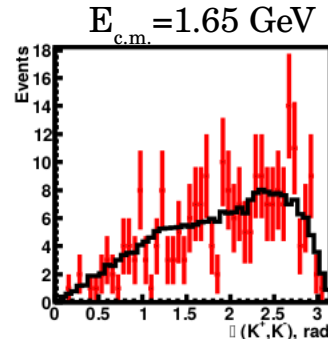
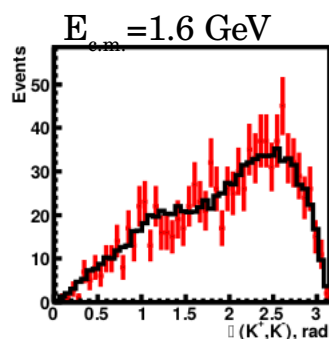
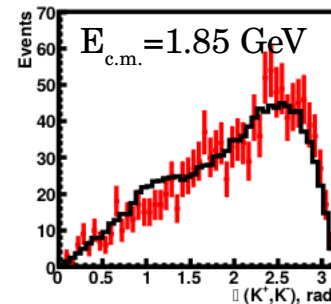
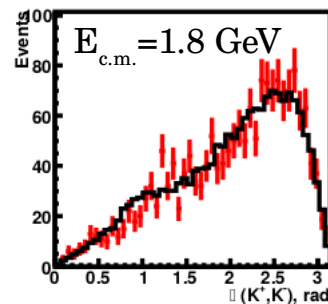
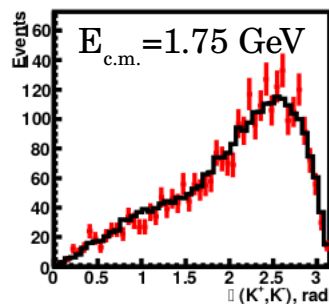
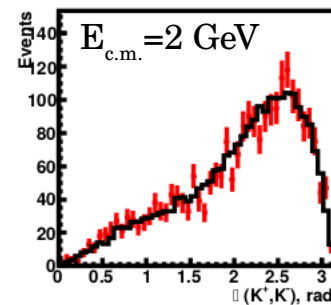
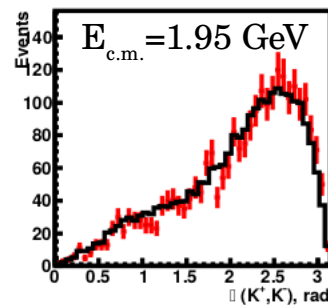
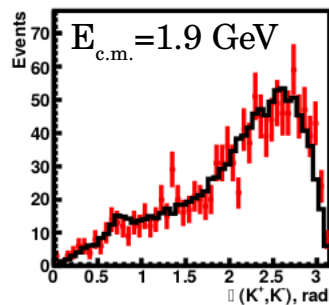
The constant of the amplitudes relatively to $e^+e^- \rightarrow (K_1(1270)K)_{swave} \rightarrow (\rho K)_{swave} K \rightarrow KK\pi\pi$



The angle between kaons

EXP

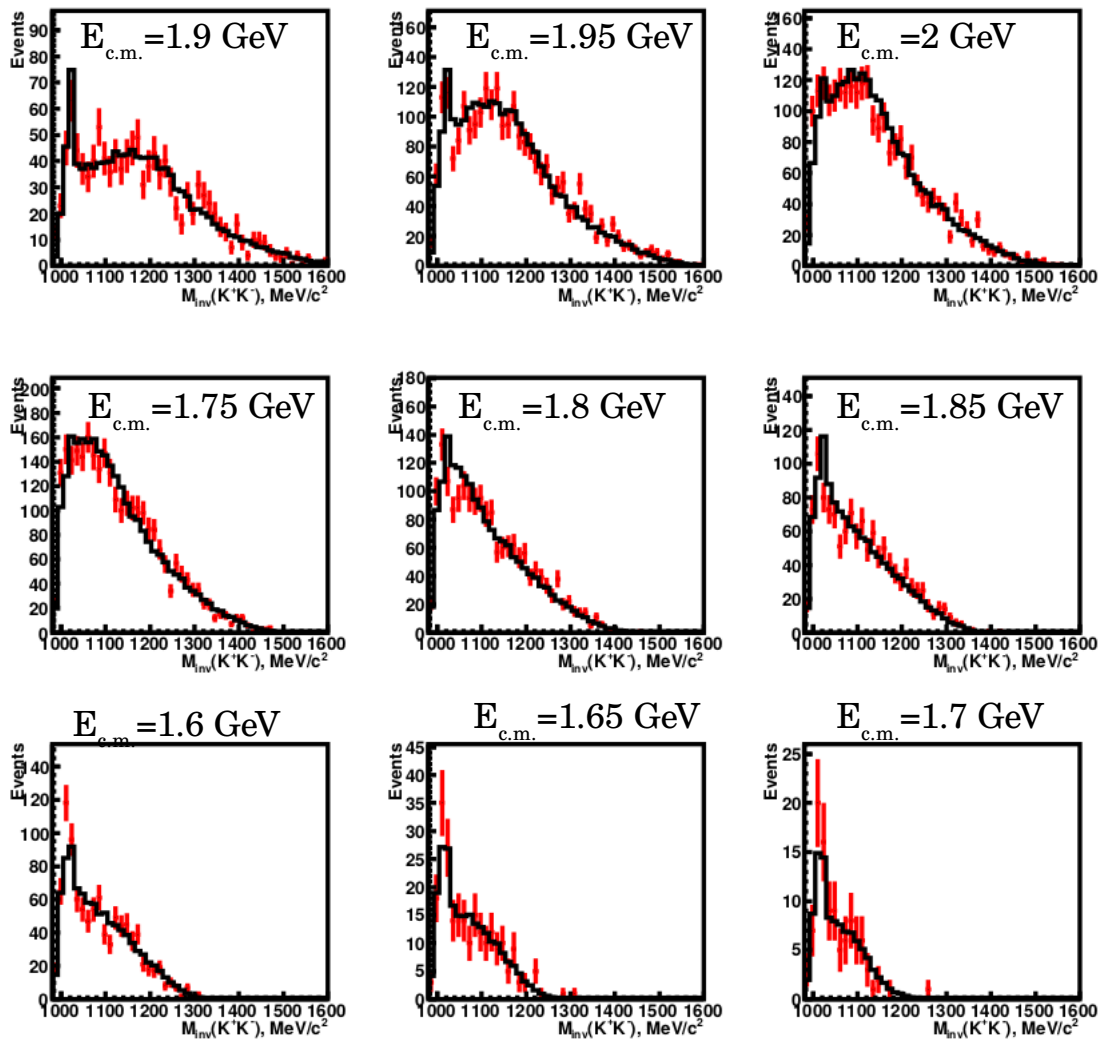
MC



Invariant mass of K+K-

EXP

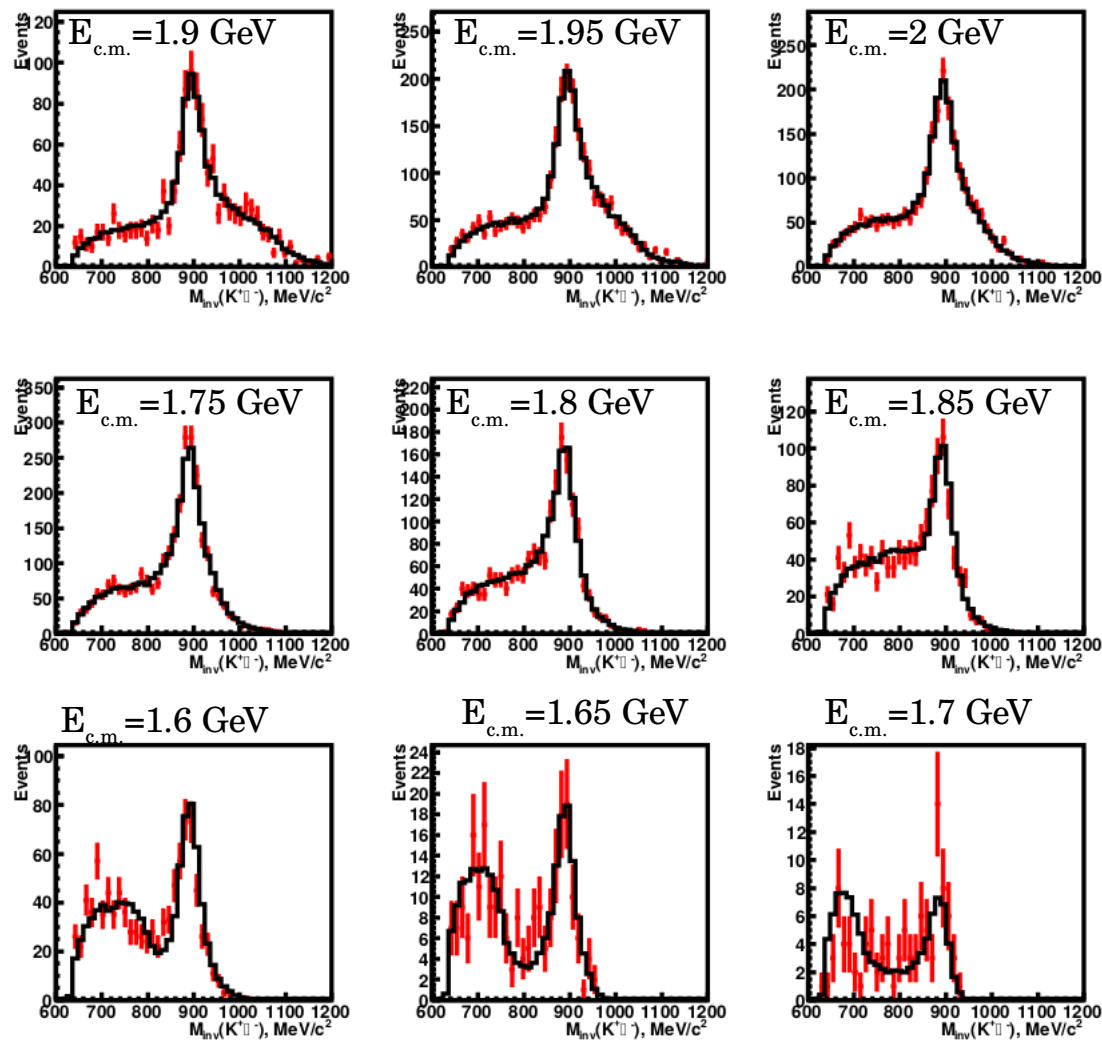
MC



Invariant mass of πK

EXP

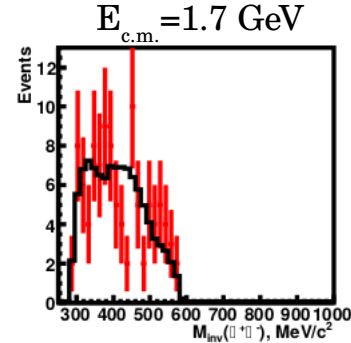
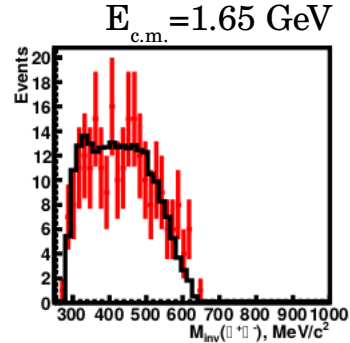
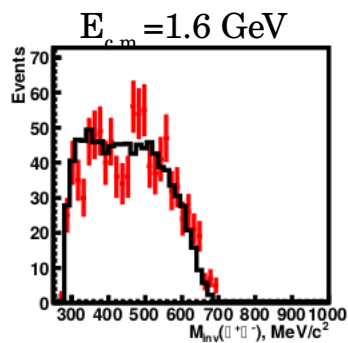
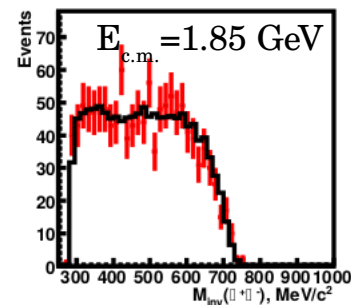
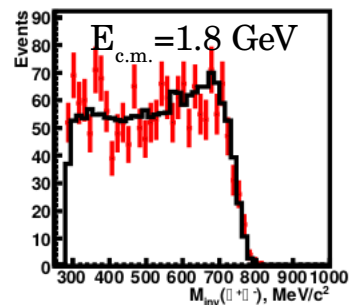
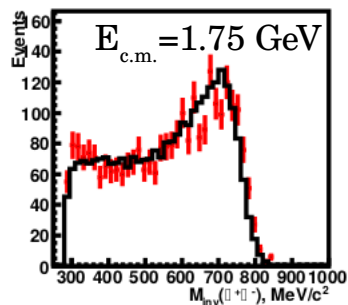
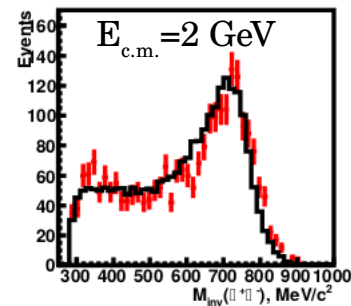
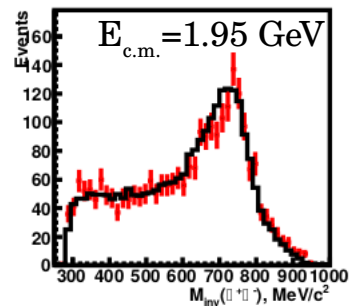
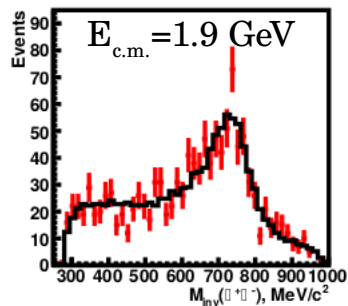
MC



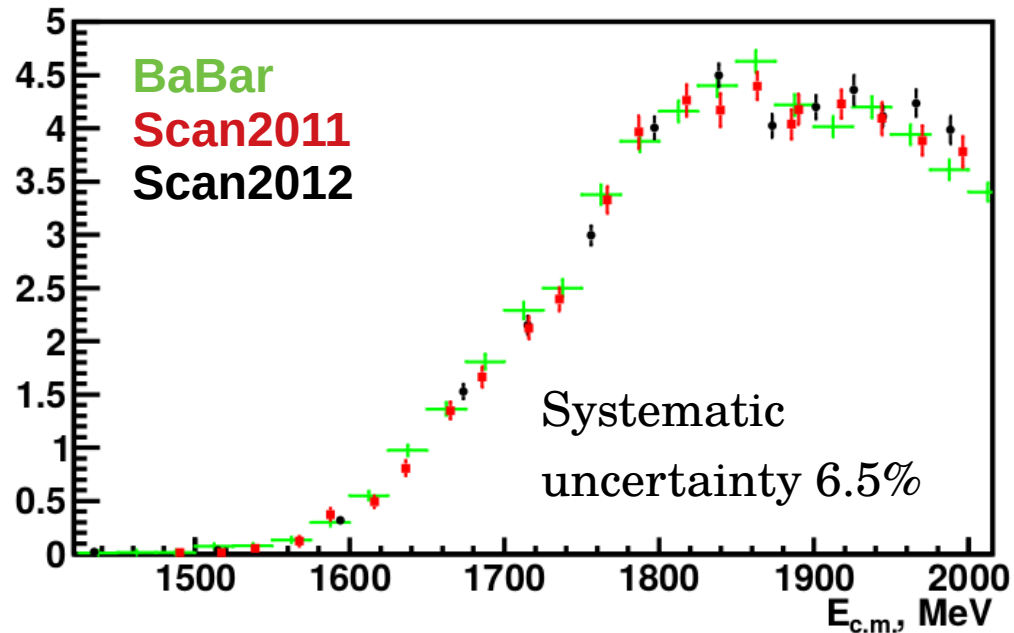
Invariant mass of 2π

EXP

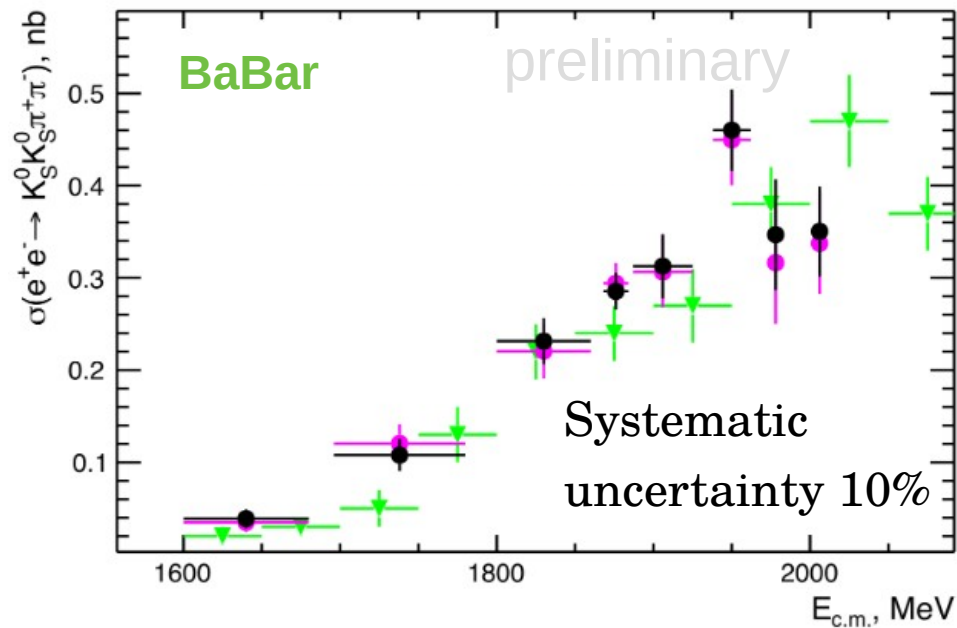
MC



Cross section of $e^+e^- \rightarrow K^+K^-\pi^+\pi^-$



Cross section of $e^+e^- \rightarrow K_S K_S \pi^+ \pi^-$



This reaction is dominated by $K^{*+}(892)K^{*-}(892)$ production

- Simultaneous analysis of all $e^+e^- \rightarrow KK\pi\pi$ channels is required for comprehensive meson spectroscopy and the test of isospin relations

Summary

- CMD-3 has taken $\sim 250 \text{ pb}^{-1}$ of data in the whole energy range GeV and is going to take $\sim 1 \text{ fb}^{-1}$ in the next ~ 5 years.
- Many analyses have been published. Many others are in progress.
- The dominance of the channels $\omega\pi$ and $a_1\pi$ below 2 GeV is confirmed in the $e^+e^- \rightarrow 4\pi$.
- The perspectives of the analysis of $e^+e^- \rightarrow KK\pi\pi$ is shown
- It looks that the production of two ground-state vectors ($\rho^-\rho^+$, $K^*(890)\bar{K}^*(890)$) is suppressed relatively to the emission of pseudoscalar ($\omega\pi$, $a_1\pi$, K_1K).
- If you are interesting in the analysing of the CMD-3 data you are more than welcome.
- BES-III and CMD-3 physics programs are strongly overlapping. We can be useful to each other.