

# The semileptonic $D$ and $D_s$ decays as the probe of the constituent quark-antiquark pairs in the light scalar mesons

**N.N. Achasov, A.V. Kiselev and G.N. Shestakov**

**Laboratory of Theoretical Physics,  
Sobolev Institute for Mathematics,  
Academician Koptiug Prospekt, 4,  
Novosibirsk, 630090, Russia**

# ABSTRACT

It is shown that the CLEO data on the  $D_s^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$  decay directly indicate the absence of the constituent  $s\bar{s}$  pairs in the  $f_0(500)$  and  $f_0(980)$  mesons.

It is shown also that the BES III data on the  $D^0 \rightarrow \pi^- \eta e^+ \nu_e$  and  $D^+ \rightarrow \pi^0 \eta e^+ \nu_e$  decays directly indicate the absence of the constituent  $d\bar{u}$  and  $d\bar{d}$  pairs in the  $a_0^-(980)$  and  $a_0^0(980)$  mesons respectively.

In addition, it is shown that the BESS III experiment on the  $D^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$  decay directly indicates the absence of the constituent  $d\bar{d}$  and  $d\bar{d}$  pairs in the  $f_0(500)$  and  $f_0(980)$  mesons.

A similar investigation program is proposed also for the semileptonic B decays.

# OUTLINE

The  $a_0(980)$  and  $f_0(980)$  mesons are well-established parts of the proposed light scalar meson nonet,

**M. Tanabashi *et al.* (Particle Data Group), Phys. Rev. D 98, 030001 (2018).**

From the beginning, the  $a_0(980)$  and  $f_0(980)$  mesons became one of the central problems of nonperturbative QCD, as they are important for understanding the way chiral symmetry is realized in the low-energy region and, consequently, for understanding confinement. Many experimental and theoretical papers have been devoted to this subject.

**There is much evidence that supports the four-quark model of light scalar mesons,**

**R.L. Jaffe, Phys. Rev. D 15, 267 (1977), Phys. Rev. D 15, 281 (1977),  
S. Weinberg, Phys. Rev. Lett. 110, 261601 (2013).**

# OUTLINE

The suppression of the  $a_0^0(980)$  and  $f_0(980)$  resonances in the  $\gamma\gamma \rightarrow \eta\pi^0$  and  $\gamma\gamma \rightarrow \pi\pi$  reactions, respectively, was predicted in 1982, **N.N. Achasov, S.A. Devyanin, and G.N. Shestakov, Phys. Lett. B 108, 134 (1982), Z. Phys. C 16, 55 (1982),**

$\Gamma_{a_0^0\gamma\gamma} \approx \Gamma_{f_0\gamma\gamma} \approx 0.27$  keV,  
and confirmed by experiment,

**M. Tanabashi et al. (Particle Data Group), Phys. Rev. D 98, 030001 (2018).**

The high quality Belle data,

**Uehara et al. (Belle Collaboration), Phys. Rev. D 78, 052004 (2008),  
Phys. Rev. D 80, 032001 (2009),**

allowed to elucidate the mechanisms of the  $\sigma(600)$ ,  $f_0(980)$ , and  $a_0^0(980)$  resonance production in  $\gamma\gamma$  collisions confirmed their four-quark structure.

# OUTLINE

Light scalar mesons are produced in  $\gamma\gamma$  collisions mainly via rescatterings, that is, via the four-quark transitions. As for  $a_2(1320)$  and  $f_2(1270)$  (the well-known  $q\bar{q}$  states), they are produced mainly via the two-quark transitions (direct couplings with  $\gamma\gamma$ ),

**N.N. Achasov and G.N. Shestakov, Z. Phys. C 41, 309 (1908), Phys. Rev. D 77, 074020 (2008), Phys. Rev. D 81, 094029 (2010), Usp. Fiz. Nauk 54, 799 (2011),**

**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 98, 096009 (2018).**

As a result the practically model-independent prediction of the  $q\bar{q}$  model  $g_{f_2\gamma\gamma}^2 : g_{a_2\gamma\gamma}^2 = 25 : 9$  agrees with experiment rather well.

As to the ideal  $q\bar{q}$  model prediction  $g_{f_0\gamma\gamma}^2 : g_{a_0\gamma\gamma}^2 = 25 : 9$ , it is excluded by experiment.

# OUTLINE

**Note also that the absence of**

**$J/\psi \rightarrow \gamma f_0(980), \rho a_0(980), \omega f_0(980)$  decays in the presence of the intense**

**$J/\psi \rightarrow \gamma f_2(1270), \gamma f'_2(1525), \rho a_2(1320), \omega f_2(1270)$  decays is at variance with the  $P$ -wave two-quark,  $q\bar{q}$ , structure of  $a_0(980)$  and  $f_0(980)$  resonances,**

**N.N. Achasov, Phys. Usp. 41, 1149 (1998), Phys. At. Nucl. 65, 546 (2002).**

# OUTLINE

The argument in favor of the four-quark nature of  $a_0(980)$  and  $f_0(980)$  is the fact that the  $\phi(1020) \rightarrow a_0^0 \gamma$  and  $\phi(1020) \rightarrow f_0 \gamma$  decays go through the kaon loop:  
 $\phi \rightarrow K^+ K^- \rightarrow a_0^0 \gamma$ ,  $\phi \rightarrow K^+ K^- \rightarrow f_0 \gamma$ , i.e., via the four-quark transition,

**N.N. Achasov and V.N. Ivanchenko, Nucl. Phys. B 315, 465 (1989),  
N.N. Achasov, Nucl. Phys. A 728, 425 (2003),  
N.N. Achasov and V.V. Gubin, Phys. Rev. D 63, 094007 (2001),  
Phys. Rev. D 56, 4084 (1997),  
N.N. Achasov and A.V. Kiselev, Phys. Rev. D 73, 054029 (2006),  
Phys. Rev. D 68, 014006 (2003).**

# OUTLINE

The kaon-loop model was suggested in Ref.

**N.N. Achasov and V.N. Ivanchenko, Nucl. Phys. B 315, 465 (1989)**

and confirmed by experiment ten years later,

**M.N. Achasov *et al.* (SND Collaboration), Phys. Lett. B 438, 441 (1998), Phys. Lett. B 479, 53 (2000), Phys. Lett. B 440, 442 (1998), Phys. Lett. B 485, 349 (2000),**

**R.R. Akhmetshin *et al.* (CMD-2 Collaboration) Phys. Lett. B 462, 380 (1999),**

**A.Aloisio *et al.* (KLOE Collaboration), Phys. Lett. B 536, 209 (2002), Phys. Lett. B 537, 21 (2002),**

**F. Ambrosino *et al.* (KLOE Collaboration), Phys. Lett. B 681, 5 (2009).**



# OUTLINE

It was shown in Ref.

**N.N. Achasov, Nucl. Phys. A 728, 425 (2003)**

that the production of  $a_0^0(980)$  and  $f_0(980)$  in  $\phi \rightarrow a_0^0 \gamma \rightarrow \eta \pi^0 \gamma$  and  $\phi \rightarrow f_0 \gamma \rightarrow \pi^0 \pi^0 \gamma$  decays is caused by the four-quark transitions, resulting in strong restrictions on the large- $N_C$  expansion of the decay amplitudes. The analysis showed that these constraints give new evidence in favor of the four-quark nature of the  $a_0(980)$  and  $f_0(980)$  mesons.

# OUTLINE

**In Refs.**

**N.N. Achasov, V.V. Gubin, and V.I. Shevchenko, Phys. Rev. D 56, 203 (1997),**

**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 76, 077501 (2007),  
Phys. Rev. D 78, 058502 (2008)**

**it was shown that the description of the**

**$\phi \rightarrow K^+ K^- \rightarrow \gamma a_0^0(980) / f_0(980)$  decays requires virtual momenta of  $K (\bar{K})$  greater than 2 GeV, while in the case of loose molecules with a binding energy about 20 MeV, they would have to be about 100 MeV. Besides, it should be noted that the production of scalar mesons in the pion-nucleon collisions with large momentum transfers also points to their compactness,**

**N.N. Achasov and G.N. Shestakov, Phys. Rev. D 58, 054011 (1998).**

# OUTLINE

It was also shown in Refs.

**N.N. Achasov and G.N. Shestakov, Phys. Rev. D 49, 5779 (1994),  
Phys. Rev. Lett. 99, 072001 (2007)**

that the linear  $S_L(2) \times S_R(2)$   $\sigma$  model,

**M. Gell-Mann and M. Levy, Nuovo Cimento 16, 705 (1960),**

contains a chiral shielding of the  $\sigma$  meson and reflects all of the main features of low-energy  $\pi\pi \rightarrow \pi\pi$  and  $\gamma\gamma \rightarrow \pi\pi$  reactions up to energy 0.8 GeV and agrees with the four-quark nature of the  $\sigma$  meson.

# OUTLINE

This allowed for the development of a phenomenological model with the right analytical properties in the complex  $s$  plane that took into account the linear  $\sigma$  model, the  $\sigma(600) - f_0(980)$  mixing and the background,

**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 83, 054008 (2011),  
Phys. Rev. D 85, 094016 (2012).**

This background has a left cut inspired by crossing symmetry, and the resulting amplitude agrees with results obtained using the chiral expansion, dispersion relations, and the Roy equation,

**I. Caprini, G. Colangelo and H. Leutwyler, Phys. Rev. Lett. 96,  
132001 (2006),**

and with the four-quark nature of the  $\sigma(600)$  and  $f_0(980)$  mesons as well. This model well describes the experimental data on  $\pi\pi \rightarrow \pi\pi$  scattering up to 1.2 GeV.

# OUTLINE

It is shown in Refs.

**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 97, 036015 (2018),  
Phys. Rev. D 98, 096009 (2018)**

that the recent data on the  $K_S^0 K^+$  correlation in Pb-Pb interactions Ref.

**S. Acharya *et al.* (ALICE Collaboration), Phys. Lett. B 774, 64 (2017)**

agree with the data on the  $\gamma\gamma \rightarrow \eta\pi^0$  and  $\phi \rightarrow \eta\pi^0\gamma$  reactions and support the four-quark model of the  $a_0(980)$  meson. It is shown that the data does not contradict the validity of the Gaussian assumption.

# OUTLOOK

**In Refs.**

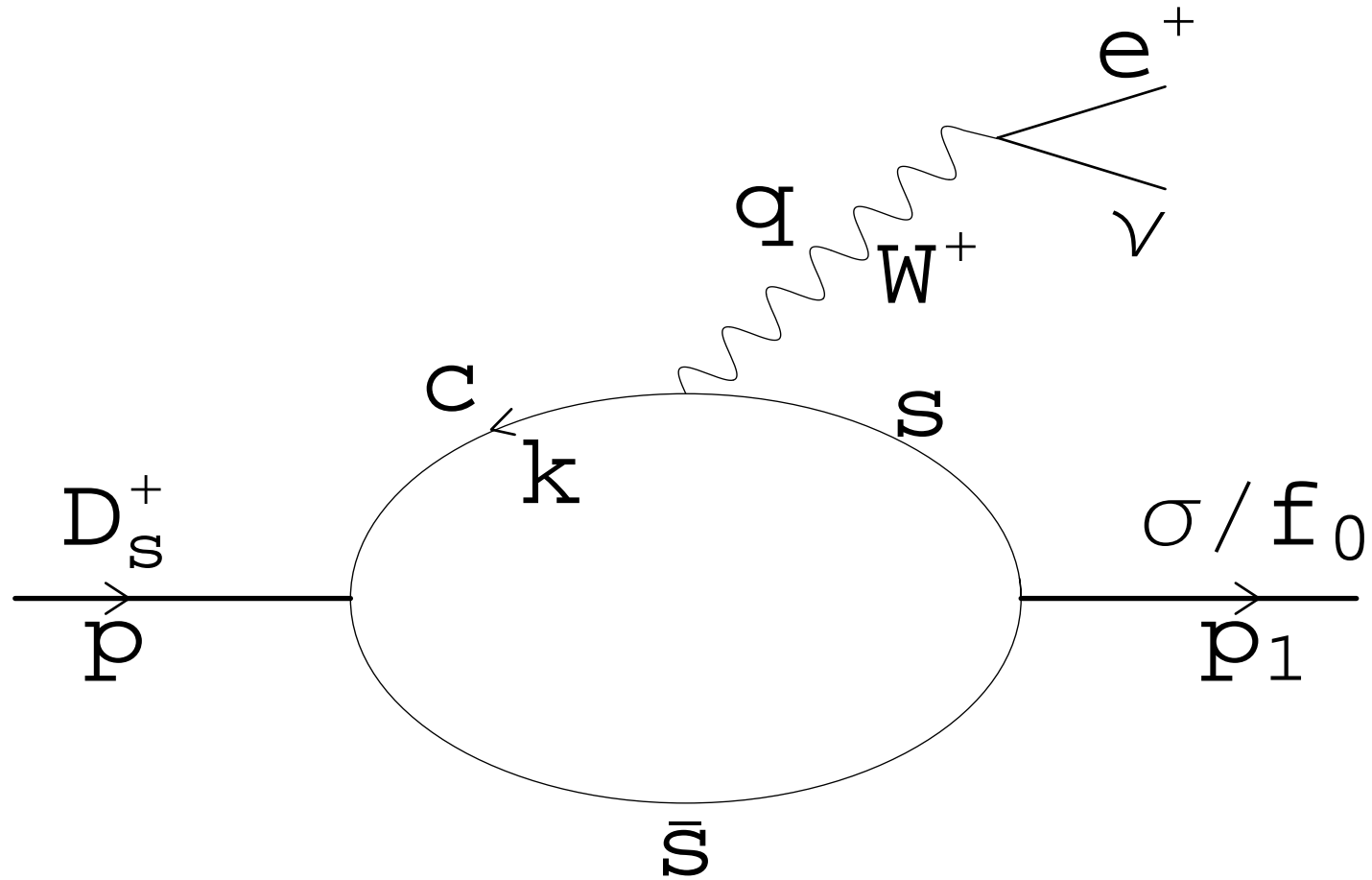
**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 86, 114010 (2012),  
Int. J. Mod. Phys. Conf. Ser. 35, 1460447 (2014)**

**it was suggested the program of studying light scalars in semileptonic  $D$  and  $B$  decays, which are the unique probe of the  $q\bar{q}$  constituent pair in the light scalars. The was studied the CLEO data about production of scalars  $\sigma(600)$  and  $f_0(980)$  in the  $D_s^+ \rightarrow s\bar{s} e^+ \nu_e \rightarrow \pi^+ \pi^- e^+ \nu$  decays, the conclusion was that the fraction of the  $s\bar{s}$  constituent components in  $\sigma(600)$  and  $f_0(980)$  is small. Unfortunately, the CLEO statistics**

**K.M Ecklund *et al.* (CLEO Collaboration), Phys. Rev. D 80, 052009 (2009)**

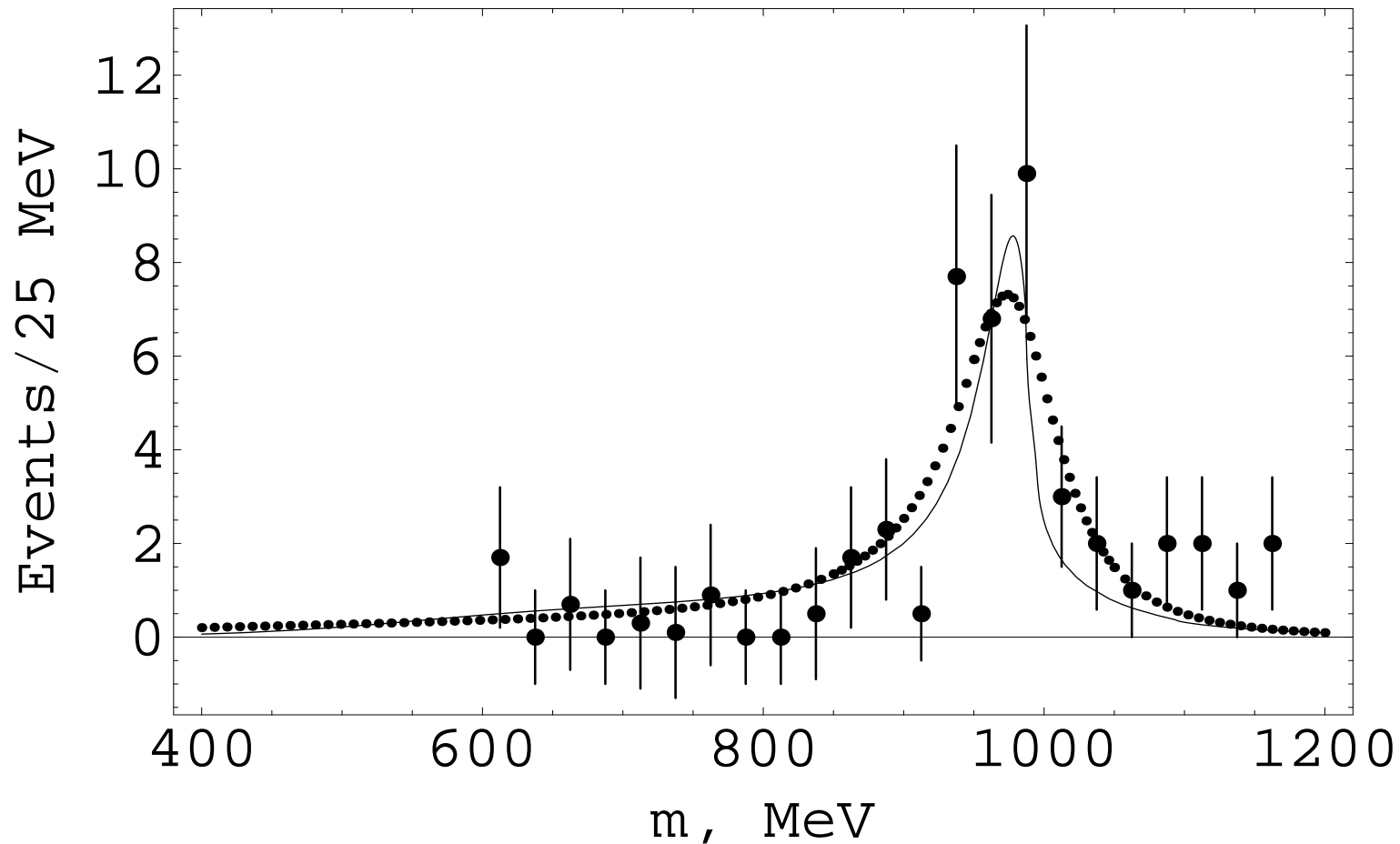
**is rather poor, and thus new high-statistics data are highly desirable.**

# OUTLOOK



# OUTLOOK

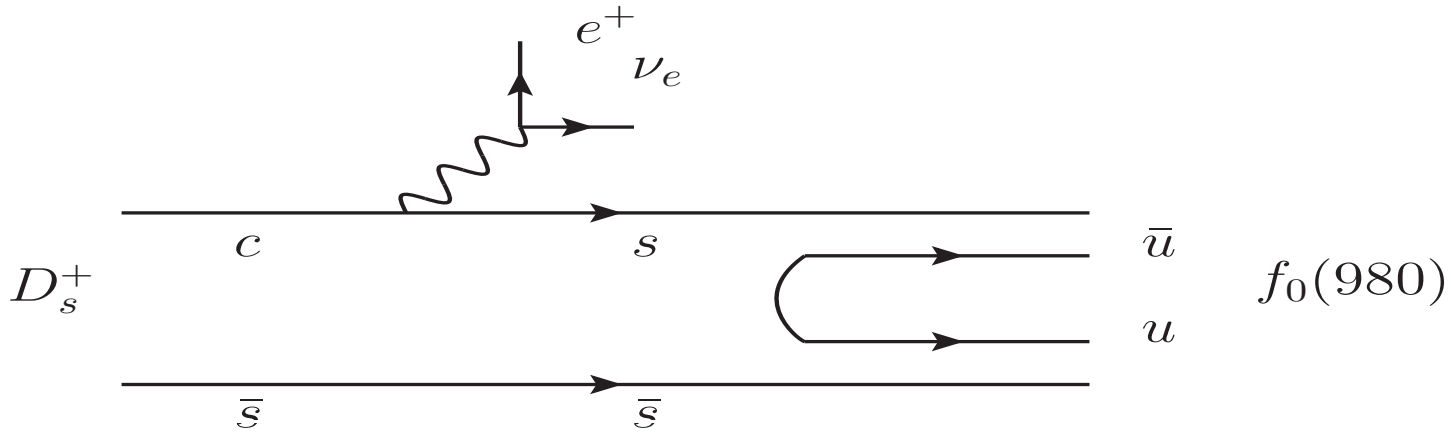
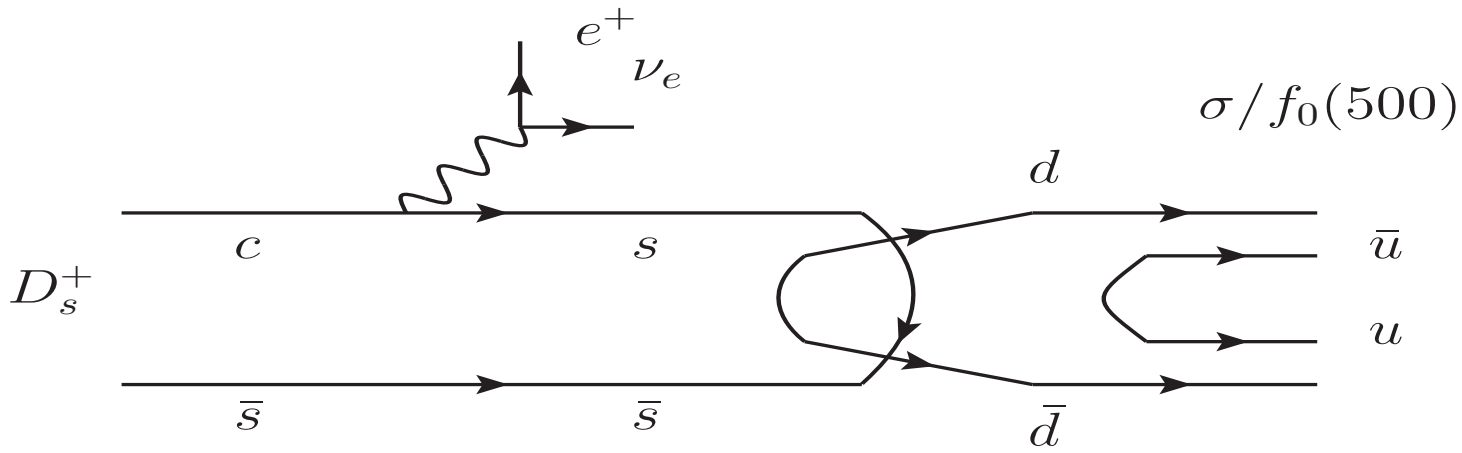
$$D_s^+ \rightarrow \pi^+ \pi^- e^+ \nu_e$$



N.N. Achasov and A.V. Kiselev, Phys. Rev. D 86, 114010 (2012)



# OUTLOOK



**OUR NEW WORK!**

# OUTLOOK

It was noted in Refs.

**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 86, 114010 (2012),  
Int. J. Mod. Phys. Conf. Ser. 35, 1460447 (2014)**

that no less interesting is the study of semileptonic decays of  $D^0$  and  $D^+$  mesons:

$$D^+ \rightarrow d\bar{d}e^+\nu_e \rightarrow [\sigma(600) + f_0(980)]e^+\nu_e \rightarrow \pi^+\pi^-e^+\nu_e,$$

$$D^0 \rightarrow d\bar{u}e^+\nu_e \rightarrow a_0^-e^+\nu_e \rightarrow \pi^-\eta e^+\nu_e \text{ and}$$

$$D^+ \rightarrow d\bar{d}e^+\nu_e \rightarrow a_0^0e^+\nu_e \rightarrow \pi^0\eta e^+\nu_e$$

or the charged-conjugated ones which had not been investigated.

# OUTLOOK

Recently BESIII Collaboration measured the decays

$$D^0 \rightarrow d\bar{u} e^+ \nu \rightarrow a_0^- e^+ \nu \rightarrow \pi^- \eta e^+ \nu \text{ and}$$

$$D^+ \rightarrow d\bar{d} e^+ \nu \rightarrow a_0^0 e^+ \nu \rightarrow \pi^0 \eta e^+ \nu \text{ for the first time}$$

**M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. 121, 081802 (2018).**

**In Ref.**

**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 98, 096009 (2018)**

**these measurements are discussed taking into account also contribution of  $a'_0$  meson with mass about 1400 MeV.**

# OUTLOOK

Below is presented a variant when  $a_0^-(980)$  and  $a_0^0(980)$  have not the  $d\bar{u}$  and  $d\bar{d}$  constituent components respectively at all.

That is,  $a_0^-(980)$  is produced as a result of mixing

$$a_0^{\prime-}(1400) \rightarrow a_0^-(980),$$

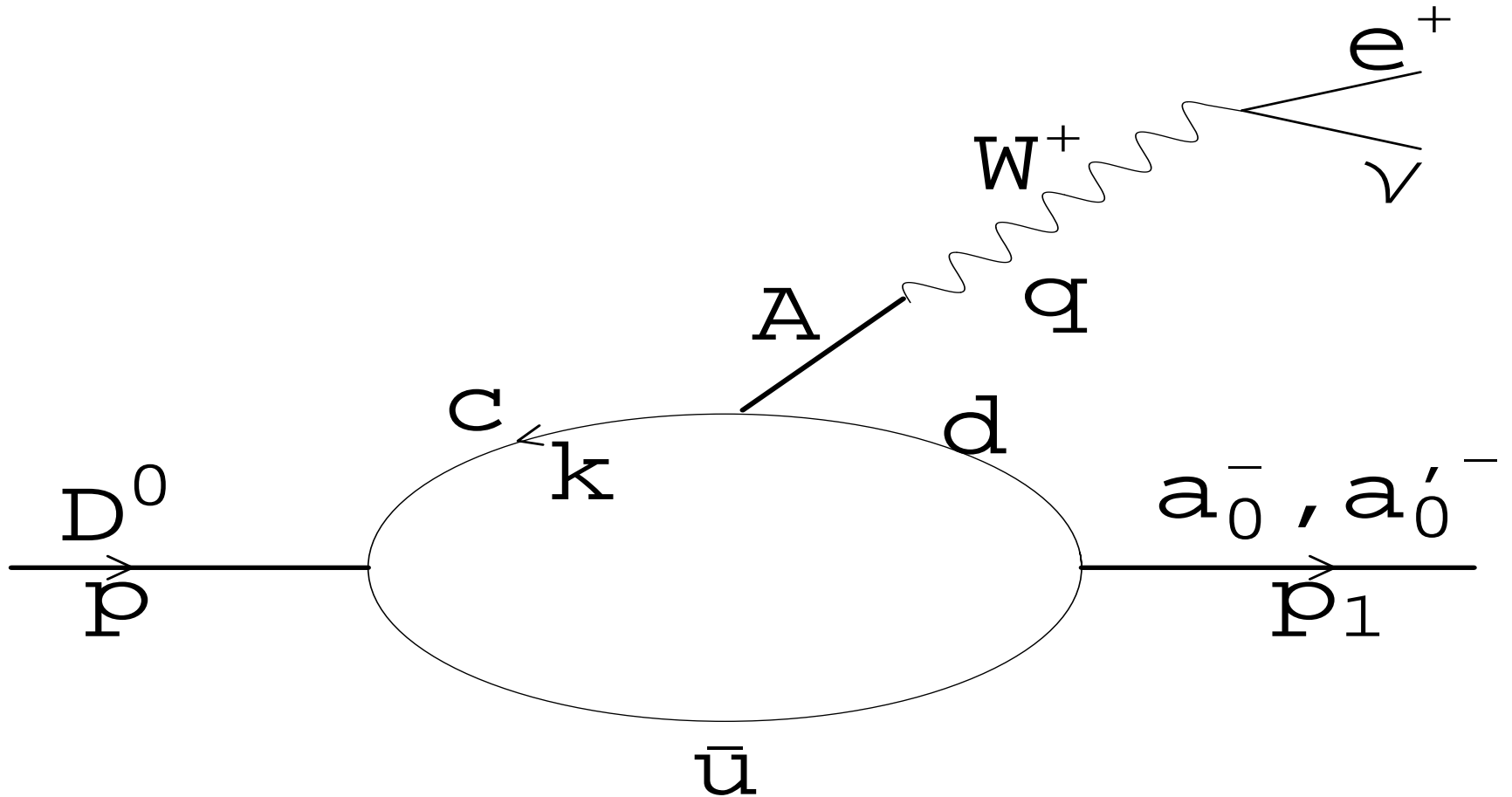
$$D^0 \rightarrow d\bar{u} e^+ \nu_e \rightarrow a_0^{\prime-} e^+ \nu_e \rightarrow a_0^- e^+ \nu_e \rightarrow \pi^- \eta e^+ \nu_e,$$

and  $a_0^0(980)$  is produced as a result of mixing

$$a_0^{\prime 0}(1400) \rightarrow a_0^0(980),$$

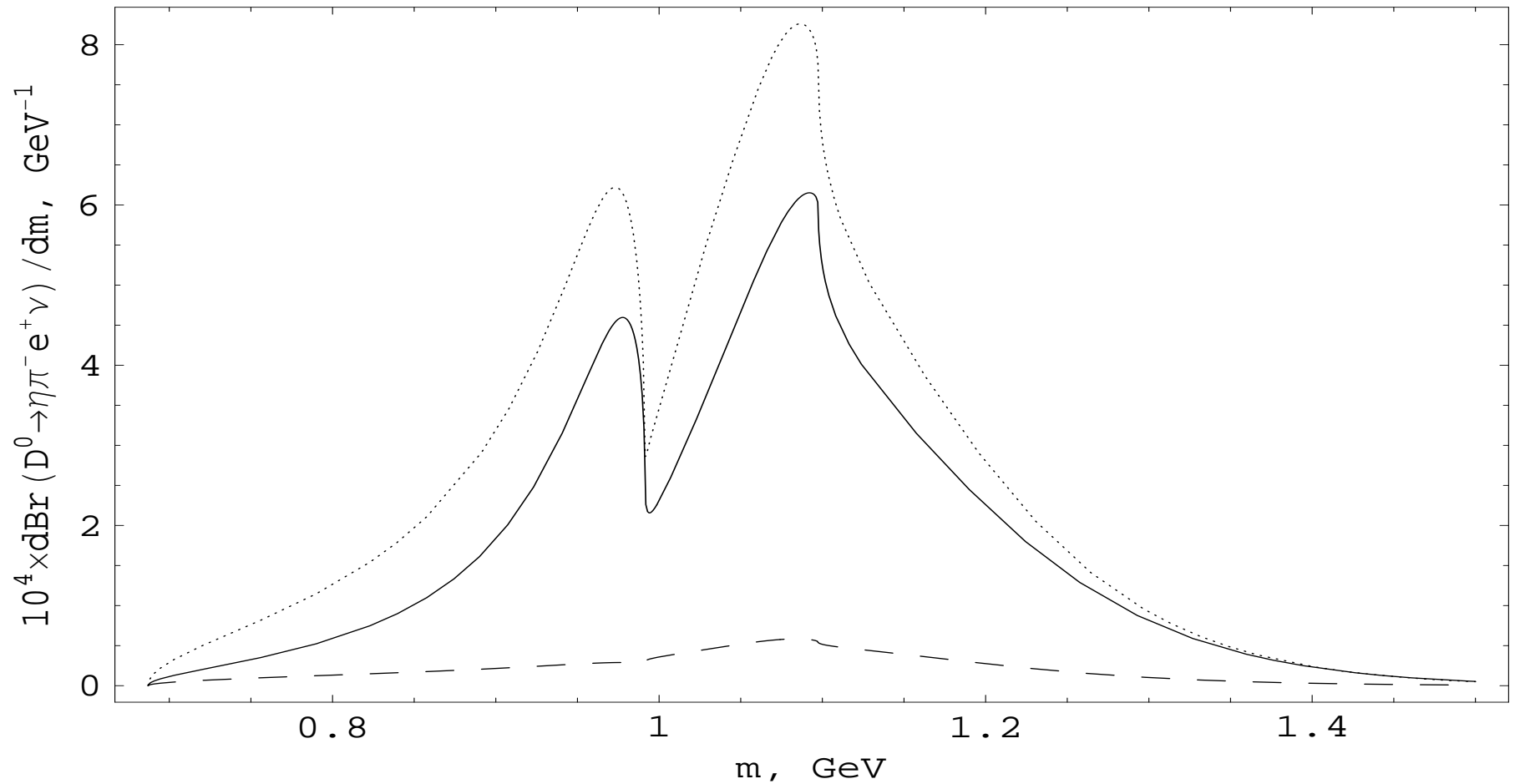
$$D^+ \rightarrow d\bar{d} e^+ \nu_e \rightarrow a_0^{\prime 0} e^+ \nu_e \rightarrow a_0^0 e^+ \nu_e \rightarrow \pi^0 \eta e^+ \nu_e.$$

# OUTLOOK



N.N. Achasov and A.V. Kiselev, Phys. Rev. D 98, 096009 (2018).

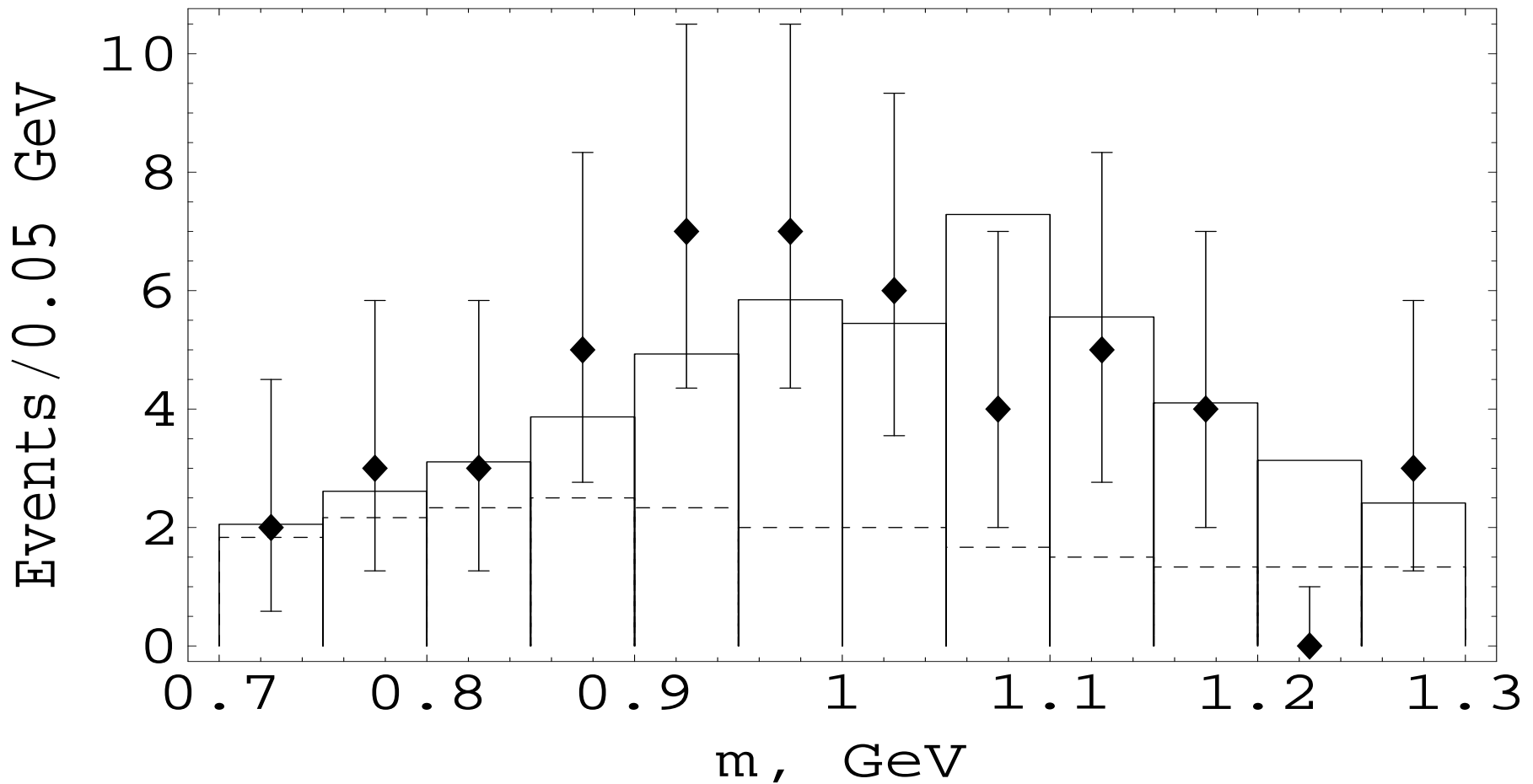
# OUTLINE



**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 98, 096009 (2018).**

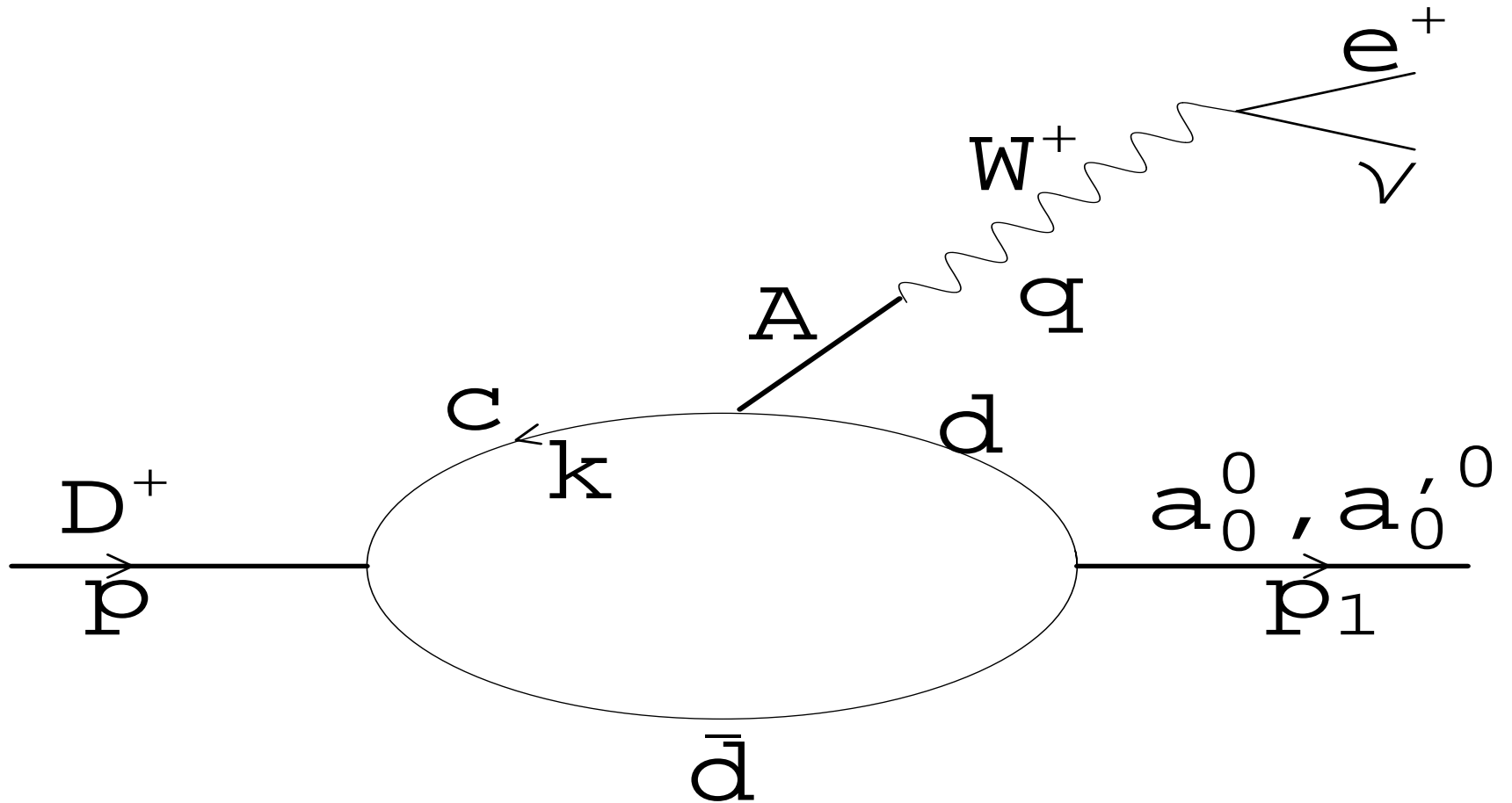
# OUTLOOK

$$D^0 \rightarrow a_0'^- \rightarrow a_0^- \rightarrow \eta \pi^- e^+ \nu_e$$



N.N. Achasov and A.V. Kiselev, Phys. Rev. D 98, 096009 (2018).

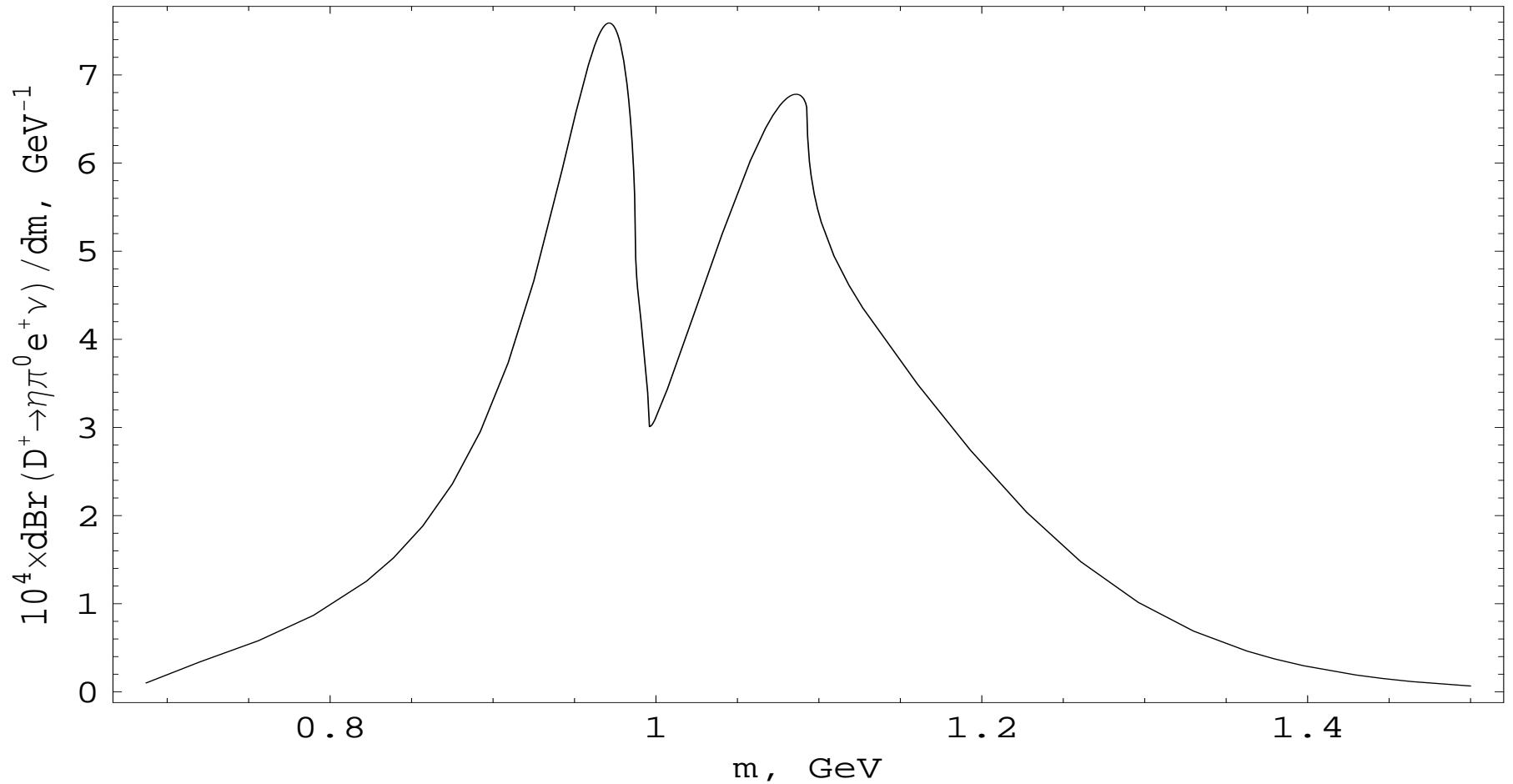
# OUTLOOK



N.N. Achasov and A.V. Kiselev, Phys. Rev. D 98, 096009 (2018).



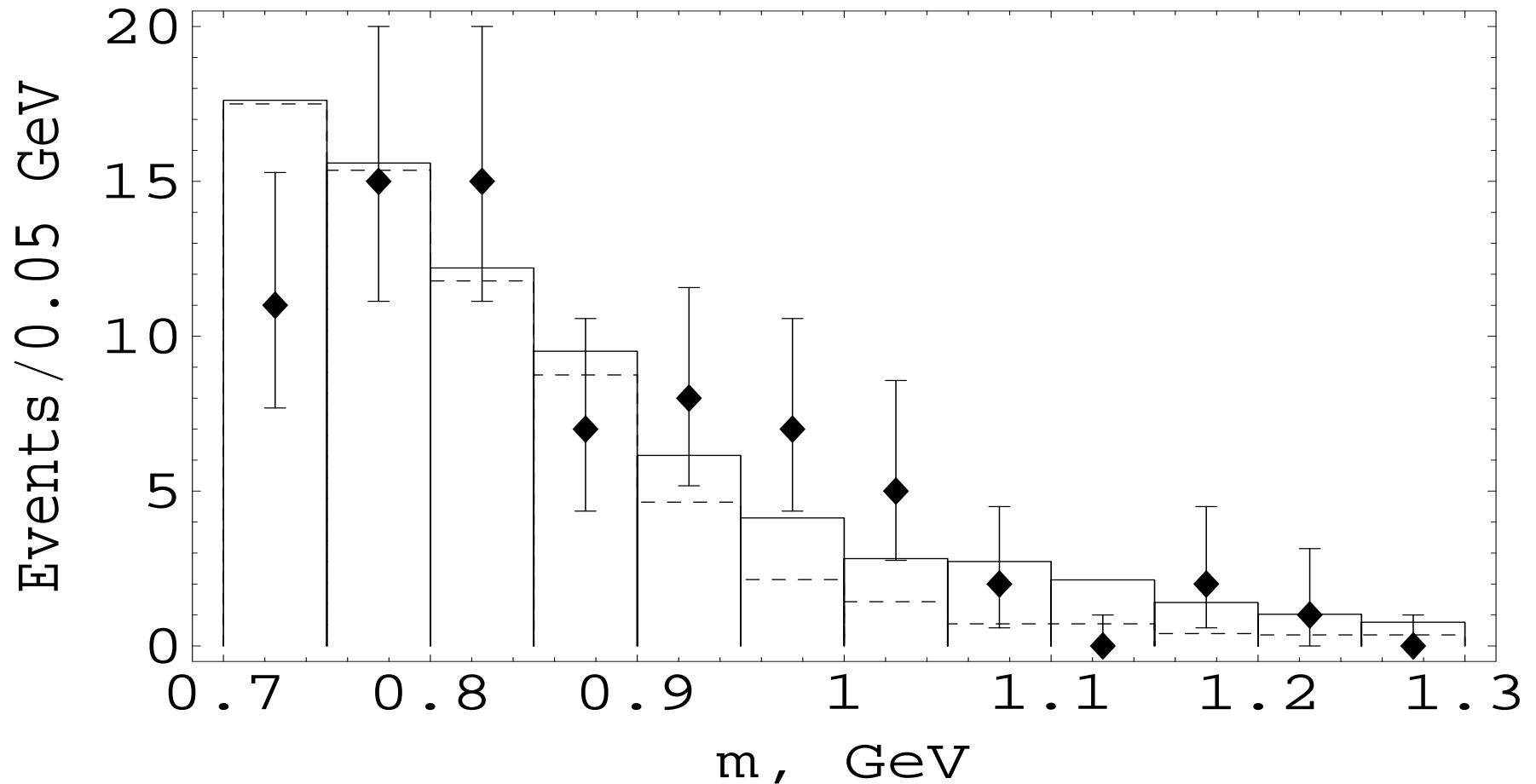
# OUTLINE



**N.N. Achasov and A.V. Kiselev, Phys. Rev. D 98, 096009 (2018).**

# OUTLOOK

$$D^+ \rightarrow a_0^{\prime 0} \rightarrow a_0^0 \rightarrow \eta \pi^- e^+ \nu_e$$



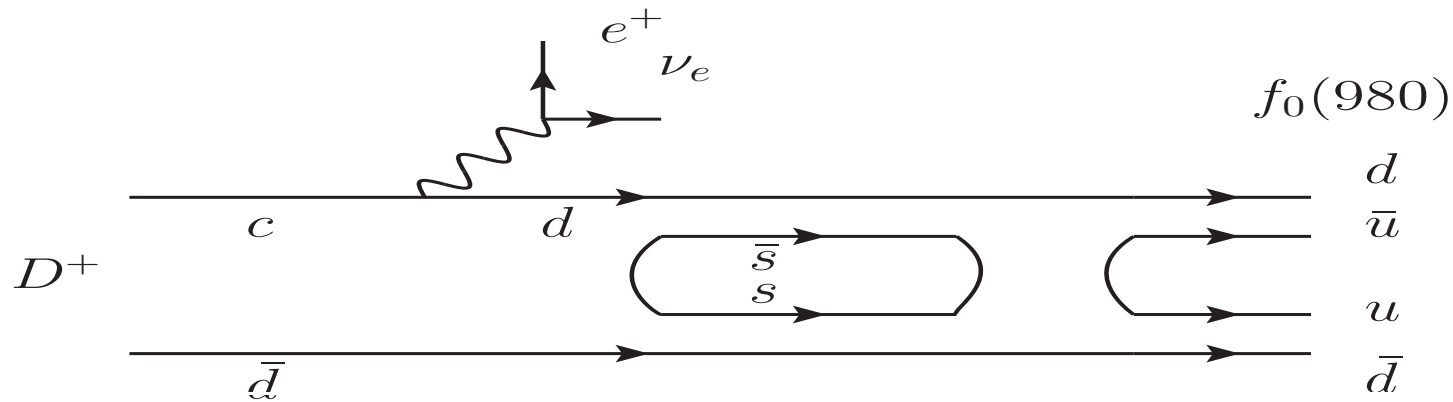
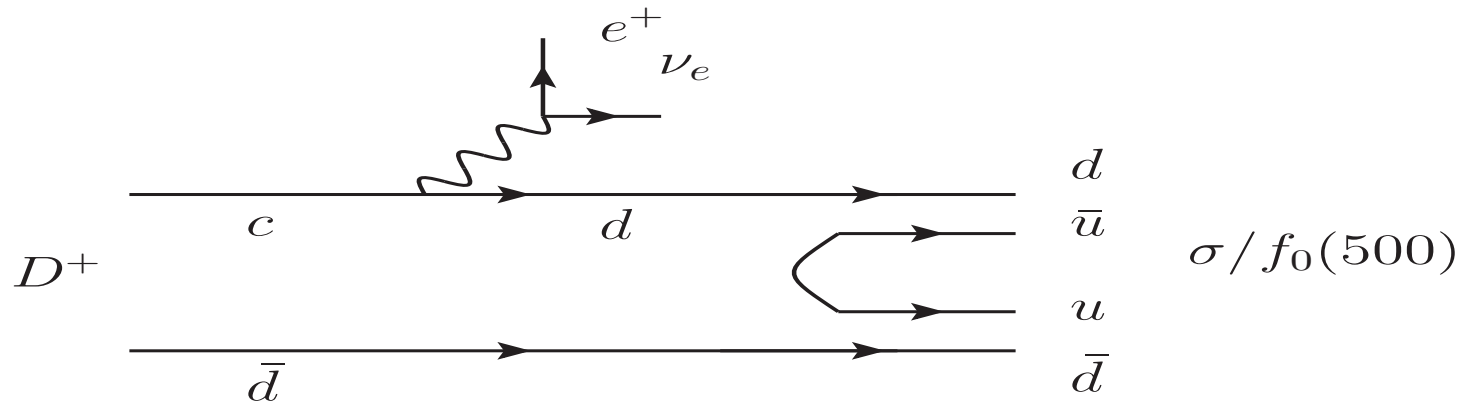
N.N. Achasov and A.V. Kiselev, Phys. Rev. D 98, 096009 (2018).

# OUTLOOK

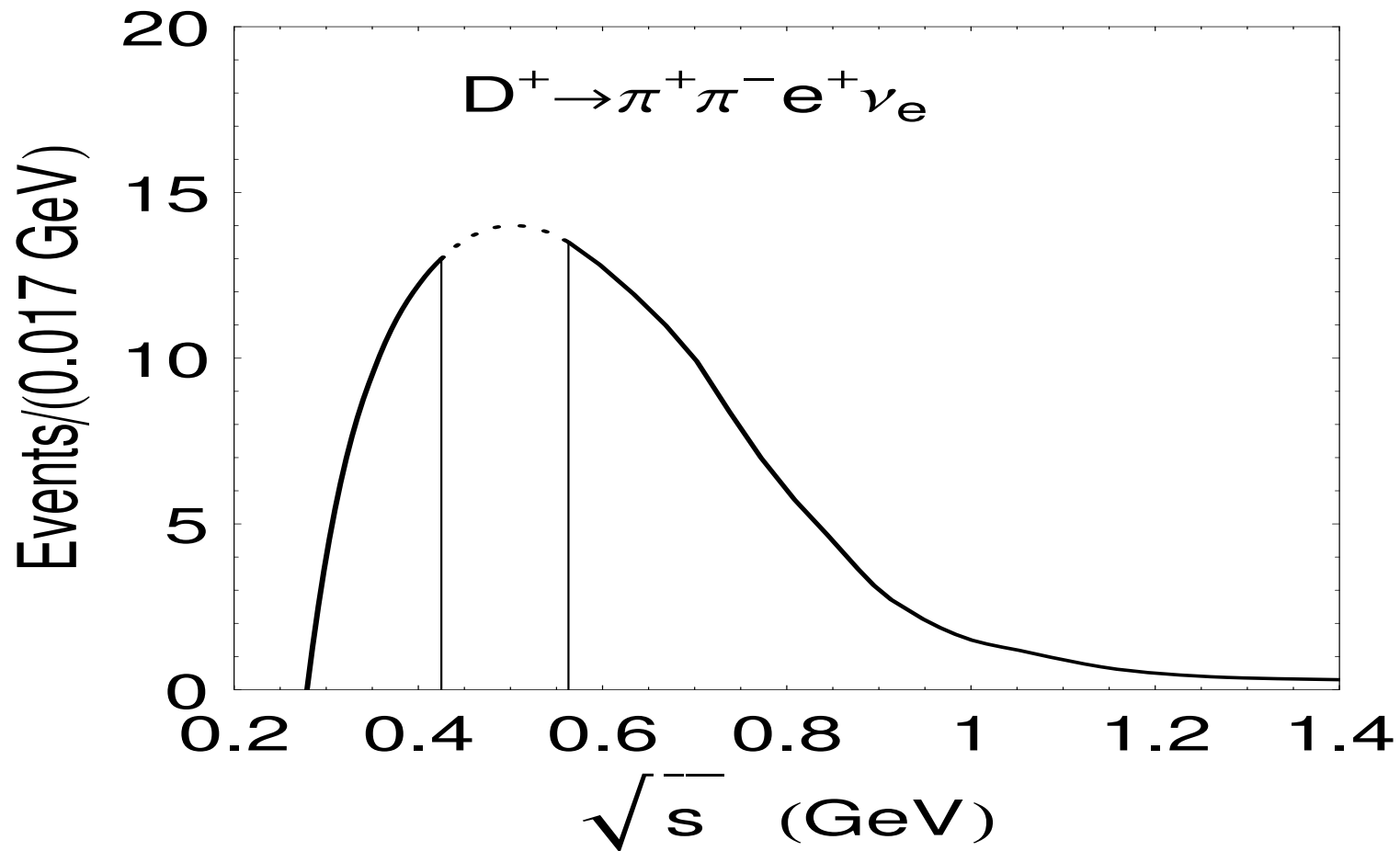
The first measurements of BESIII directly indicate the absence of the constituent  $d\bar{d}$  and  $d\bar{u}$  pairs in the  $a_0^0(980)$  and  $a_0^-(980)$  states respectively. But the the present the statistics is not adequate for the conclusions about details of the  $\pi\eta$  production.

# OUTLOOK

A half of year later BESIII Collaboration measured the decay  $D^+ \rightarrow d\bar{d}e^+\nu \rightarrow \pi^+\pi^-e^+\nu$  for the first time **M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. 122, 062001 (2019).**



# OUTLOOK



OUR NEW WORK!

# OUTLOOK

It is very tempting to study light scalar mesons in semileptonic decays of  $B$  mesons

**N.N. Achasov and A.V. Kiselev, Int. J. Mod. Phys. Conf. Ser. 35, 1460447 (2014):**

$$B^0 \rightarrow d\bar{u} e^+ \nu_e \rightarrow a_0^- e^+ \nu_e \rightarrow \pi^- \eta e^+ \nu_e,$$

$$B^+ \rightarrow u\bar{u} e^+ \nu_e \rightarrow a_0^0 e^+ \nu_e \rightarrow \pi^0 \eta e^+ \nu_e,$$

$$B^+ \rightarrow u\bar{u} e^+ \nu_e \rightarrow [\sigma(600) + f_0(980)] e^+ \nu_e \rightarrow \pi^+ \pi^- e^+ \nu_e$$

or the charged-conjugated ones.

# A LOT OF THANKS

**I am grateful Organizers for the kind Invitation.**

**The work was supported by the program of fundamental scientific researches of the SB RAS No. II.15.1., project No. 0314-2019-0021.**