

Feasibility study of measuring $b \rightarrow s\gamma$ photon polarization in $D^0 \rightarrow K_1(1270)^- e^+ \nu_e$ at STCF

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Workshop on future Super c-tau factories 2021
Nov. 15th ~ 17th, 2021



arXiv:2107.06118v3

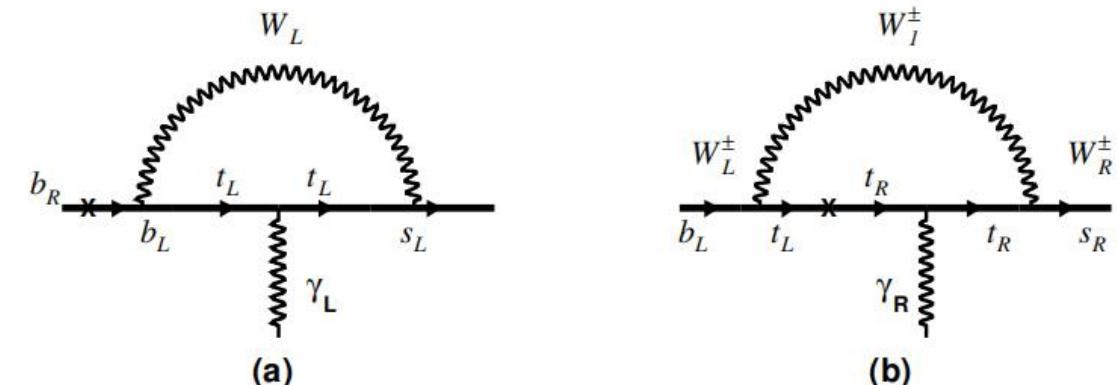
Outline

- **Motivation**
- **MC Sample**
- **Event Selection and Analysis**
- **Optimization of Detector Response**
- **Statistical Analysis**
- **Summary**

Photon Polarization In $b \rightarrow s\gamma$

➤ Sensitivity to BSM

- In SM, right-handed vs. left-handed $\sim \frac{m_s}{m_b}$
 - In LRSM, right-handed vs. left-handed $\sim \frac{m_t}{m_b}$

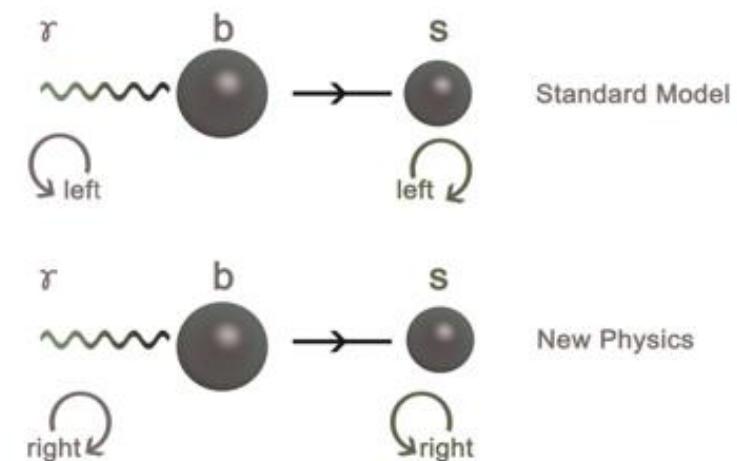


$$\mathcal{H}_{eff} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* (C_{7L} \mathcal{O}_{7L} + C_{7R} \mathcal{O}_{7R})$$

- In SM, left-(right-)handed photon predominate in \bar{B} (B) decays.

for B decay : $|C_{7L}|^2 \ll |C_{7R}|^2$

for \bar{B} decays : $|C_{7L}|^2 \gg |C_{7R}|^2$



- Picture taken from report of Fu-Sheng Yu

Photon Polarization In $b \rightarrow s\gamma$

➤ Have never been measured at a high precision

- CP asymmetry in time dependent decays $B(t) \rightarrow X_{s/d}^{CP}\gamma$ [1]
- $b \rightarrow sl^+l^-$ transition [2] (l^+l^- come from a virtual photon)
- $\Lambda_b \rightarrow \Lambda\gamma$ [3] (forward-upward asymmetry)

➤ Hadronic state helicity in $B \rightarrow K_{res}(\rightarrow K\pi\pi)\gamma$ [4]

$$\lambda_\gamma = \frac{|C_{7R}|^2 - |C_{7L}|^2}{|C_{7R}|^2 + |C_{7L}|^2} \quad \text{In SM,} \quad \lambda_\gamma \simeq -1 \text{ for } b \rightarrow s\gamma \text{ and } \lambda_\gamma \simeq +1 \text{ for } \bar{b} \rightarrow \bar{s}\gamma.$$

$$A_{UD} = \frac{\Gamma_{K_{res}}\gamma[\cos \theta_K > 0] - \Gamma_{K_{res}}\gamma[\cos \theta_K < 0]}{\Gamma_{K_{res}}\gamma[\cos \theta_K > 0] + \Gamma_{K_{res}}\gamma[\cos \theta_K < 0]} \\ = \lambda_\gamma \frac{3 \operatorname{Im}[\vec{n} \cdot (\vec{J} \times \vec{J}^*)]}{4 |\vec{J}|^2}.$$

$M_{K\pi\pi}$ in (1.1,1.3) GeV, $A_{UD} = (6.9 \pm 1.7) \times 10^{-2}$

Observation of photon polarization !

R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 112, 161801 (2014).

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- [1]. F. Muheim, Y. Xie and R. Zwicky, Phys. Lett. B 664 174 (2008). [2]. F. Kruger and J. Matias, Phys. Rev. D 71 094009 (2005).
 - [3]. T. Mannel and S. Recksiegel, Acta Phys. Pol. B 28, 2489 (1997); G. Hiller and A. Kagan, Phys. Rev. D 65, 074038 (2002)
 - [4]. M. Gronau, Y. Grossman, D. Pirjol, and A. Ryd, Phys. Rev. Lett. 88, 051802 (2002); Gronau, Michael and Pirjol, Dan, Phys. Rev. D 66, 054008 (2002)

A'_{UD} of D semileptonic decay

➤ To extract λ_γ

a ratio of Up-Down Asymmetry in semi-leptonic decay $D \rightarrow K_1 l^+ \bar{\nu}_l \sim A'_{UD}$

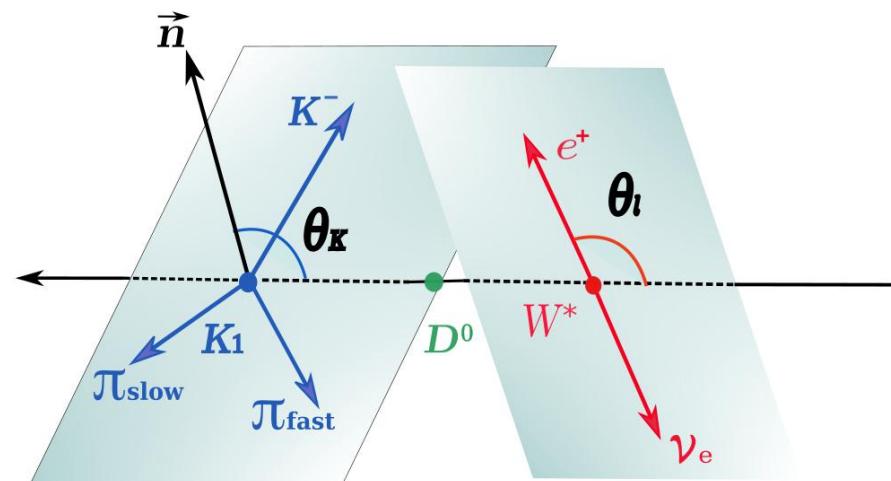
➤ Combining $B \rightarrow K_{res}(\rightarrow K\pi\pi)\gamma$ and $D \rightarrow K_{res}(\rightarrow K\pi\pi)l\nu_l$

W. Wang, F. S. Yu, and Z. X. Zhao,
Phys. Rev. Lett. 125, 051802 (2020).

$$\begin{aligned} A'_{UD} &= \frac{\Gamma_{K_1^- e^+ \bar{\nu}_e}[\cos \theta_K > 0] - \Gamma_{K_1^- e^+ \bar{\nu}_e}[\cos \theta_K < 0]}{\Gamma_{K_1^- e^+ \bar{\nu}_e}[\cos \theta_l > 0] - \Gamma_{K_1^- e^+ \bar{\nu}_e}[\cos \theta_l < 0]} \\ &= \frac{\text{Im}[\vec{n} \cdot (\vec{J} \times \vec{J}^*)]}{|\vec{J}|^2}. \end{aligned}$$

$$\lambda_\gamma = \frac{4 A_{UD}}{3 A'_{UD}}$$

➤ Kinematics for $D^0 \rightarrow K_1(1270)^- e^+ \bar{\nu}_e \rightarrow K^- \pi^+ \pi^- e^+ \bar{\nu}_e$



$$B(D^0 \rightarrow K_1(1270)^- e^+ \bar{\nu}_e) = (1.09 \pm 0.13^{+0.09}_{-0.16} \pm 0.12) \times 10^{-3}$$

Statistically limited to measure the A'_{UD}

M. Ablikim et al. (BESIII Collaboration),
Phys. Rev. Lett 127, 131801, (2021)

MC Simulation

➤ Fast simulation tool for STCF [1]

- Resolution and efficiency responses for tracking of final state particles, PID system ; kinematic fit related to variables.
- Functions for adjust performance of each sub-system.

➤ MC simulated samples 1ab^{-1} @ $\sqrt{s} = 3.773 \text{ GeV}$

charmed hadron pairs near the charm threshold allow for measuring A'_{UD} in with very low background level

- 1ab^{-1} @ $\sqrt{s} = 3.773 \text{ GeV}$
 $e^+e^- \sim D\bar{D}, \text{ non - } D\bar{D}, \gamma_{ISR}J/\psi, \gamma_{ISR}\psi(3686)$
- $D^0 \rightarrow K_1(1270)^- e^+ \nu_e$
ISGW2 [2] , BF[3]
The mass , width[3,4]
and ratio of subdecays of $K_1(1270)$ [4] (fit2)

Mass (GeV/c^2)	1.253 ± 0.007
Width (MeV)	90 ± 20
Decay mode	Decay ratio (%)
$K\rho$	54.8 ± 4.3
$K_0^*(1430)\pi$	2.01 ± 0.64
$K^*(892)\pi$	17.1 ± 2.3
$K\omega$	22.5 ± 5.2

[1]. X.-D. Shi *et al.* JINST 16 P03029 (2021)

[2]. D. Scora and N. Isgur, Phys. Rev. D 52 2783 (1995).

[3]. P.A.Zyla et.al.(ParticleDataGroup),Prog.Theor.Exp. Phys. 2020 083C01 (2020)

[4]. H. Guler *et al.* (Belle Collaboration), Phys. Rev. D 83 032005 (2011).

Event Selection

- **Single tags (ST)** $\bar{D}^0 \rightarrow K^+ \pi^-$, $K^+ \pi^- \pi^0$, $K^+ \pi^- \pi^+ \pi^-$
- **Good charged tracks** $|\cos\theta| < 0.93$, $|dr| < 1\text{cm}$, $|dz| < 10\text{cm}$

➤ Particle identification of charged tracks

Kaon: $CL_K > 0.001$, $CL_K > CL_\pi$ Pion: $CL_\pi > 0.001$, $CL_\pi > CL_K$

electron: $\frac{E}{p} > 0.8$, $\frac{CL_e}{CL_e + CL_K + CL_\pi} > 0.8$, $CL_e > 0.001$

➤ Neutral pion

$M_{\gamma\gamma}(0.115, 0.150)\text{GeV}/c^2$

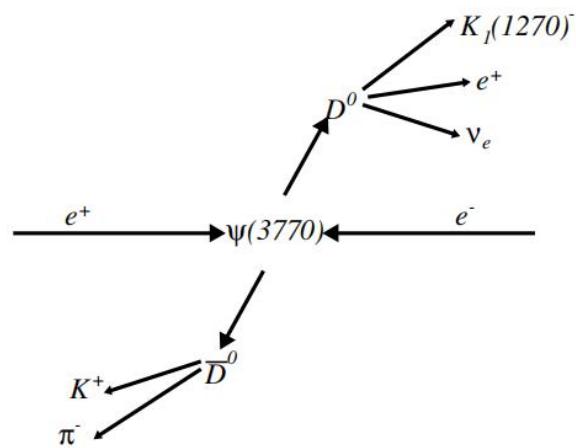
1-C mass kinematic fit on $\pi^0 \rightarrow \gamma\gamma$, $\chi^2_{\text{KMFIT}} < 200$

➤ ST D mesons

$$\Delta E = E_{Kn\pi} - E_{beam} \quad \sim (29, 27), (-69, 38), (-31, 28) \text{ MeV}$$

$$M_{BC} = \sqrt{E_{beam}^2 - |\vec{P}_{Kn\pi}|^2} \quad \sim (1.858, 1.874) \text{ GeV}/c^2$$

- **Charge conjugation, Double tag (DT) method**

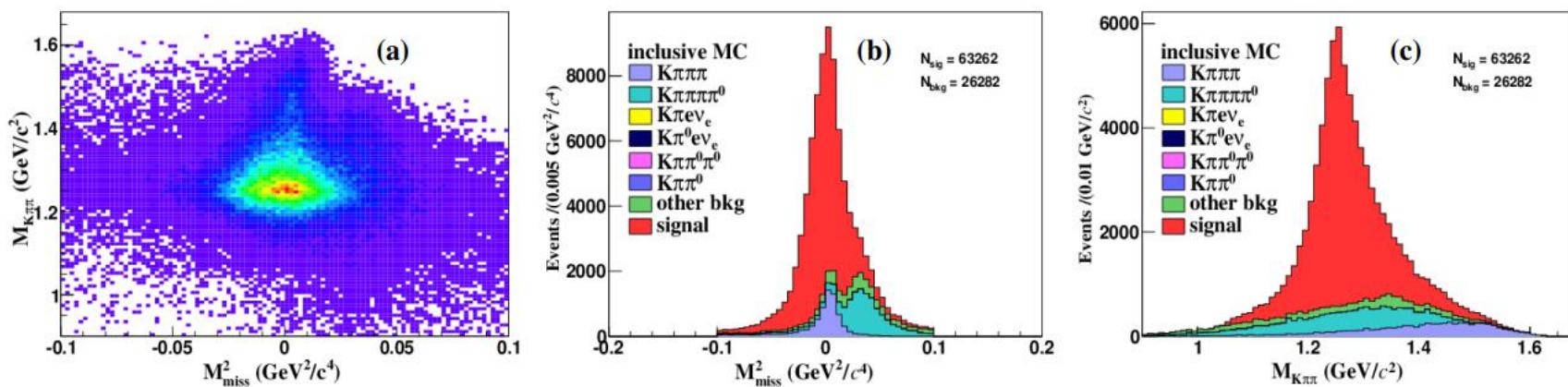


- **Singal candidates** $D^0 \rightarrow K_1(1270)^- e^+ \nu_e$
 $K_1(1270)^- \rightarrow K^- \pi^+ \pi^-$

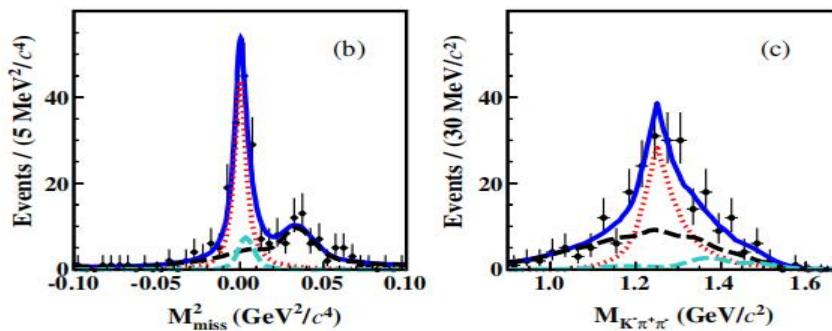
- only four good unused charged tracks
- charge(lepton) = charge(Kaon in tag side)
- other three charged tracks are identified as a Kaon and two pions.
- charge(Kaon) = -charge(lepton)

DT Candidates

- Main peaking backgrounds $e \leftrightarrow \pi$,
most criteria are same as M. Ablikim et al. (BESIII Collaboration), Phys. Rev. Lett 127,131801,(2021)
- Accepted $D^0 \rightarrow K^-\pi^+\pi^-e^+\nu_e$ candidate events



➤ 2-D fit of BESIII results $\sim 109 \pm 12.5$



➤ Selection efficiencies

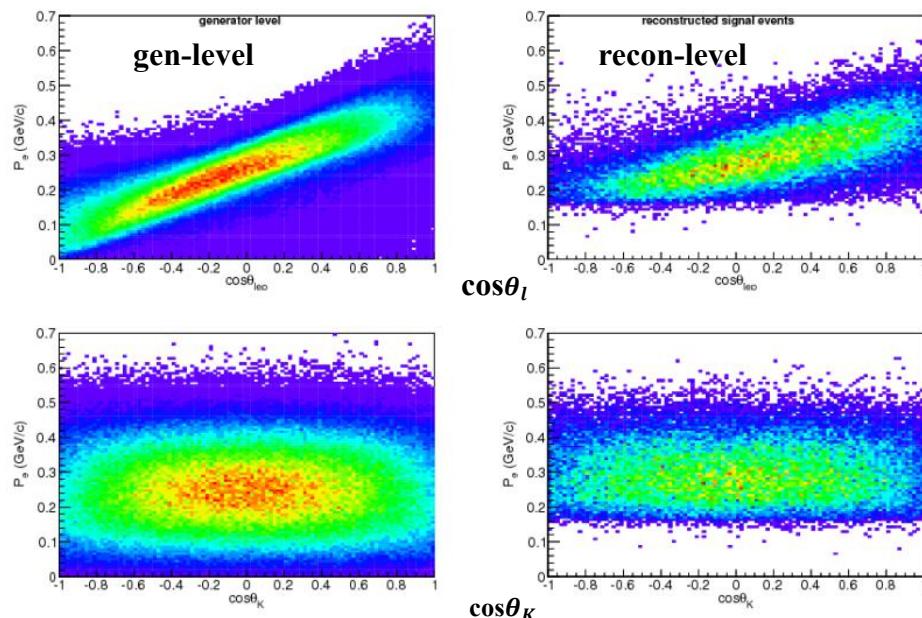
12.11% for $\bar{D}^0 \rightarrow K^-\pi^+$
6.93% for $\bar{D}^0 \rightarrow K^-\pi^+\pi^0$
6.25% for $\bar{D}^0 \rightarrow K^-\pi^+\pi^-\pi^+$

Dependence of DT Efficiency on $\cos\theta_l$

➤ Electron Momentum Dependence

$\cos\theta_l$

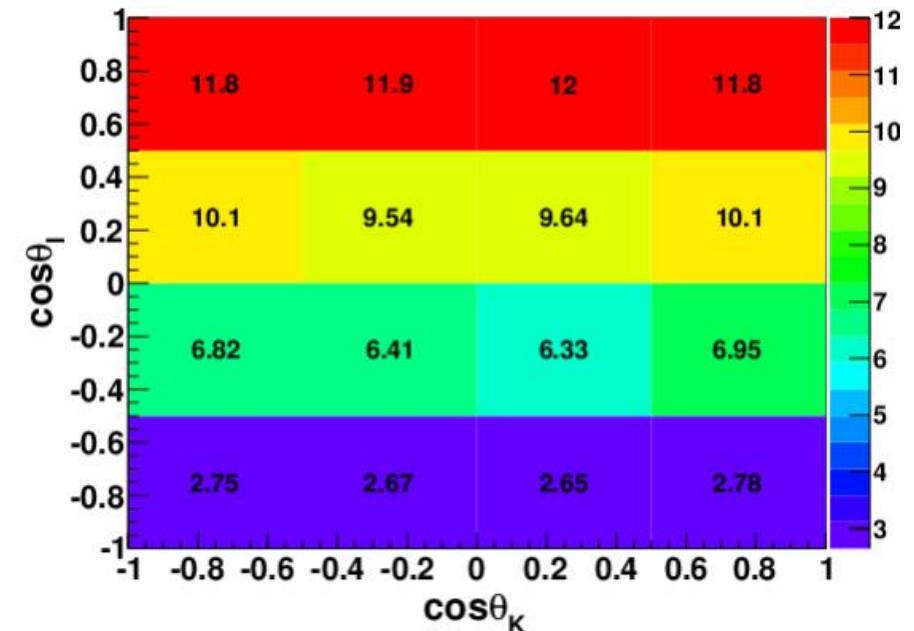
- ~ low momentum electron
- ~ tracking & PID efficiencies



➤ Singal reconstruction efficiencies in bins of $\cos\theta_K$ vs. $\cos\theta_l$

$$\varepsilon_{DT}^j = \frac{\sum_i \mathcal{B}_{ST}^i \varepsilon_{DT}^{ij}}{\sum_i \mathcal{B}_{ST}^i}$$

tag mode i
angular bin j



Angular Fit to Extract A'_{UD}

➤ Fit to M_{miss}^2 and $M_{K\pi\pi}$ to obtain signal yields

- 2-D unbin-maximum likelihood fit
- extracted signal yields in each ($\cos \theta_K$ vs. $\cos \theta_l$) bin

➤ Bin migration

- full width at half maximum(FWHM) :

$$\sigma(\cos \theta_l) \sim 0.12$$

$$\sigma(\cos \theta_K) \sim 0.05$$
- bin width : 0.5
- expected to be negligible

➤ Fit function [1]

$$\begin{aligned}
 f(\cos \theta_K, \cos \theta_l; A'_{UD}, d_+, d_-) = & \\
 & (4 + d_+ + d_-)[1 + \cos^2 \theta_K \cos^2 \theta_l] \\
 & + 2(d_+ - d_-)[1 + \cos^2 \theta_K] \cos \theta_l \\
 & + 2A'_{UD}(d_+ - d_-) \cos \theta_K [1 + \cos^2 \theta_l] \\
 & + 4A'_{UD}(d_+ + d_-) \cos \theta_K \cos \theta_l \\
 & - (4 - d_+ - d_-)[\cos^2 \theta_K + \cos^2 \theta_l].
 \end{aligned}$$

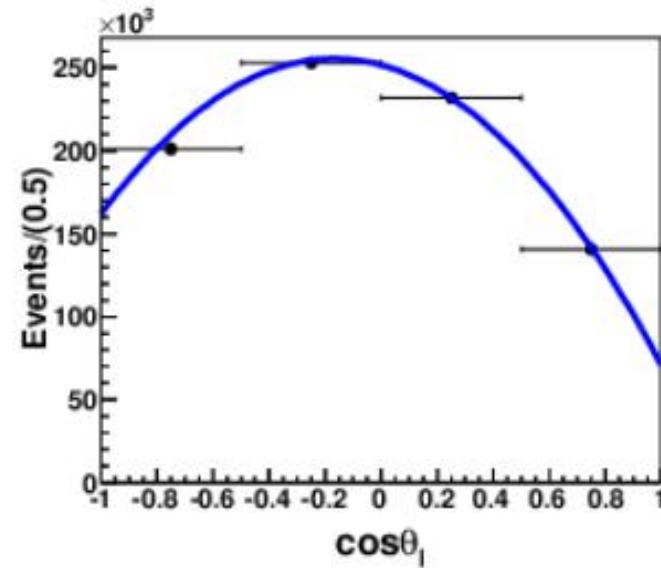
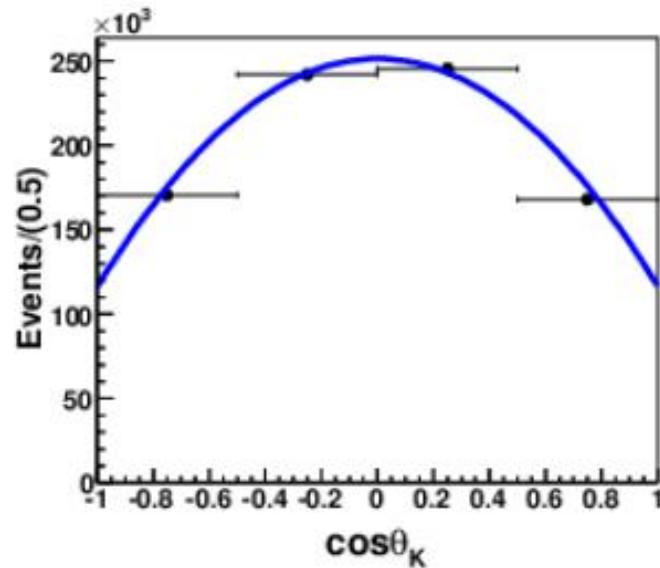
$$d_+ = \frac{|c_+|^2}{|c_0|^2}, d_- = \frac{|c_-|^2}{|c_0|^2}$$

$c_\pm \sim$ transverse polarization of K_1
 $c_0 \sim$ longitudinal polarization of K_1

[1]. W. Wang, F. S. Yu, and Z. X. Zhao, Phys. Rev. Lett. 125, 051802 (2020).

Angular Fit to Extract A'_{UD}

- 2-D χ^2 fit to efficiency corrected signal yields in each ($\cos \theta_K$ vs. $\cos \theta_l$)



statistical sensitivity 1.8×10^{-2} @ $1 ab^{-1}$ MC sample

Optimization of Detector Responses

➤ Optimization factors for different sub-detector responses

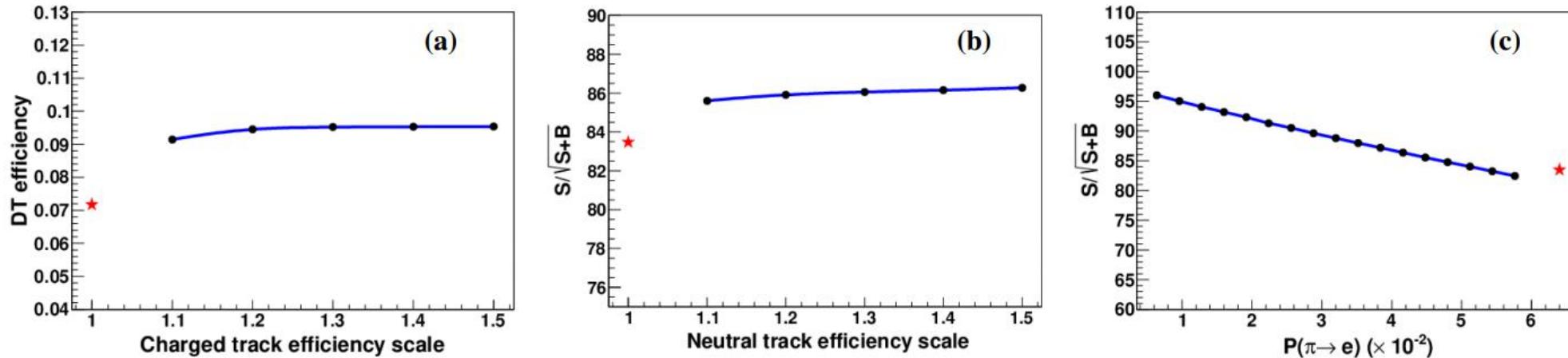
- **charged tracking selection** (detection efficiency, momentum and position resolution)
 - <1>. detection efficiency (p_T , $\cos\theta$) : increasing **from 10% to 50%** ✓
 - <2>. σ_{xy} (resolution of tracking system in xy plane): **ranging from 150 μm to 30 μm .**
 - <3>. σ_z (resolution of tracking system in z direction): **ranging from 2500 μm to 500 μm .**
- **neutral selection** (detection efficiency, energy and position resolution)
 - <1>. detection efficiency : increasing **from 10% to 50%** ✓
 - <2>. energy resolution : increasing **from 10% to 50%**
 - <3>. position resolution : increasing **from 10% to 50%**
- **identification of electron at low momentum** (misidentify a pion as electron in $p < 0.6 \text{ GeV}/c$)
 - <1>. misidentification rate for π/e ranging **from 5.7% to 0.64% @ 0.2GeV/c** ✓
(can be reduced from 6.4% to 3.2% at 0.2GeV/c in STCF)

➤ Characterization of the detector performance

- figure-of-merit ($\frac{S}{\sqrt{S+B}}$)
- DT efficiencies

Optimization of Detector Responses

➤ Optimization



- reconstruction efficiency for charged track: in 1.1(10%) improved by 27%
- reconstruction efficiency for neutral track: in 1.1(10%) improved by 4%
- misidentification rate of π/e : in 3.2% @ 0.2 GeV improved by 7%

➤ Sensitivity

- signal selection efficiency ~ improved by 33%
- $\sigma_{stat}(A'_{UD}) \sim 1.5 \times 10^{-2}$ (~improved by 17%)

Dependence of Wilson Coefficiency on A'_{UD}

➤ Dependence of Wilson coefficient on A'_{UD}

$$\frac{|C_{7L}|^2}{|C_{7R}|^2} = \frac{3A'_{UD} - 4A_{UD}}{3A'_{UD} + 4A_{UD}}$$

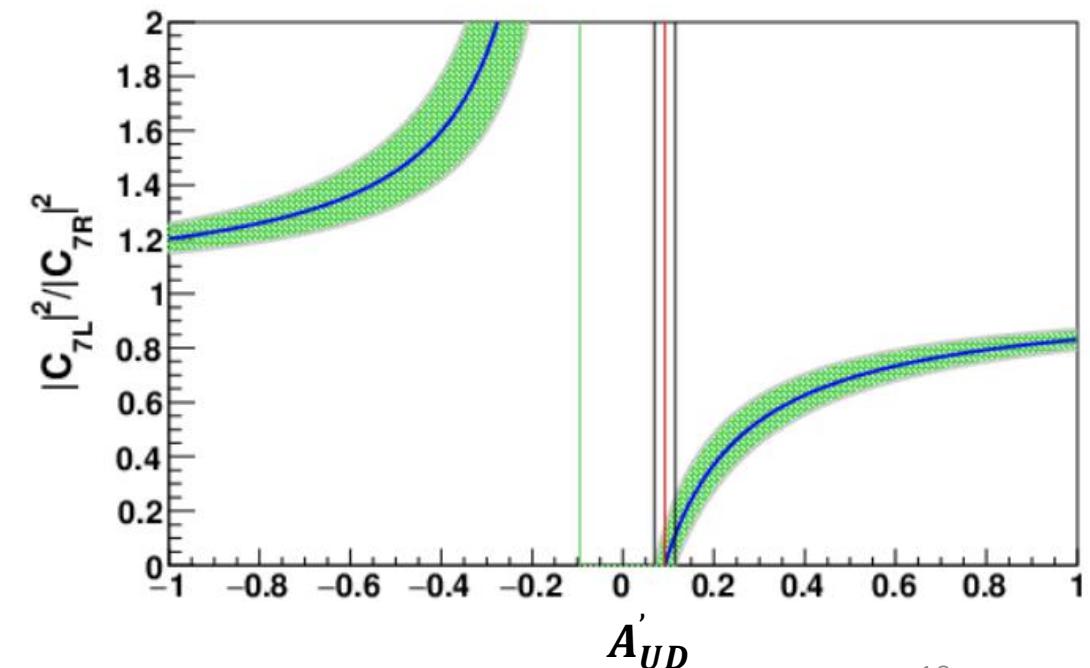
input of $A_{UD} = (6.9 \pm 1.7) \times 10^{-2}$ $M_{K\pi\pi} \sim (1.1, 1.3) \text{ GeV}$

(R. Aaij et al. (LHCb Collaboration). Phys. Rev. Lett. 112, 161801 (2014)).

In SM, $A'_{UD} = (9.2 \pm 2.3) \times 10^{-2}$

➤ Potential sources of systematic uncertainties

- electron tracking and PID efficiencies ✓
- bin migration
- signal and background shape modeling ✓
- non-resonance contribution
- $K_1(1400)$ contribution ✓



Summary

➤ **Statistical sensitivity of A'_{UD}**

[arXiv:2107.06118v3](#)

$\mathcal{L} = 1 \text{ ab}^{-1}$ @ $\sqrt{s} = 3.773 \text{ GeV}$ + optimized efficiency with the fast simulation

statistical sensitivity of a ratio of up-down asymmetry A'_{UD} @ STCF in $D^0 \rightarrow K_1(1270)^- e^+ \nu_e$

$\sim 1.5 \times 10^{-2}$

➤ **Probing for new physics**

Combining the A'_{UD} in STCF and A_{UD} measured in $B^+ \rightarrow K_1^+(\rightarrow K^+\pi^-\pi^+)\gamma$ from B factories photon polarization in $b \rightarrow s\gamma$ can be measured model-independently with high precision.

Back Up

- Counting method to calculate A'_{UD}

$$A'_{UD} = \frac{N'(cos\theta_K > 0, cos\theta_l < 0) + N'(cos\theta_K > 0, cos\theta_l > 0) - N'(cos\theta_K < 0, cos\theta_l < 0) - N'(cos\theta_K < 0, cos\theta_l > 0)}{N'(cos\theta_K > 0, cos\theta_l > 0) + N'(cos\theta_K < 0, cos\theta_l > 0) - N'(cos\theta_K < 0, cos\theta_l < 0) - N'(cos\theta_K > 0, cos\theta_l < 0)}$$

statistical sensitivity 5.2×10^{-2}
@ $1 ab^{-1}$ MC sample

$$\mathcal{A}'_{ud} = \frac{\frac{N_{KpLm}}{\epsilon_{KpLm}} + \frac{N_{KpLp}}{\epsilon_{KpLp}} - \frac{N_{KmLm}}{\epsilon_{KmLm}} - \frac{N_{KmLp}}{\epsilon_{KmLp}}}{\frac{N_{KpLp}}{\epsilon_{KpLp}} + \frac{N_{KmpL}}{\epsilon_{KmLp}} - \frac{N_{KmLm}}{\epsilon_{KmLm}} - \frac{N_{KpLm}}{\epsilon_{KpLm}}}$$