

## Prospects of CKM elements $|V_{cs}|$ and decay constant $f_{D_s^+}$ in $D_s^+ \rightarrow l^+ \nu_l$ decay at STCF Jiajun Liu<sup>1</sup> Huijing Li<sup>2</sup> <sup>1</sup>helloliujiajun@163.com, University of South China

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## Introduction

## In the SM

•  $D_s$  pure leptonic decay:



Analysis of  $D_s^+ \rightarrow l^+ \nu_l$ 

 $e^+e^- \to D_s^+D_s^- 0.1 \text{ ab}^{-1} @4.009 \text{GeV}$ 



$$\Gamma(D_s^+ \to l^+ \nu_l) \propto \left| f_{D_s^+} \right|^2 \cdot |V_{cs}|^2$$

- □ Precise measurements of  $f_{D_s^+}$  and  $|V_{cs}|$  are essential to probe new physics beyond the Standard Model (SM).
- □ Up-to-date results of  $|V_{cs}|$  and  $f_{D_s^+}$  are still limited by statistics uncertainty in the measurement of  $D_s^+ \rightarrow l^+ \nu_l$ .
- □ Future precise measurement of  $D_s^+ \rightarrow l^+ v_l$  is critical to calibrate various theoretical calculations of  $f_{D_s^+}$  and test the unitarity of the CKM matrix.



• Analysis method is double tag method.

14 single tags are reconstructed, whose total Branch fraction is  $(30.57 \pm 1.05) \times 10^{-2}$ .

- The branch fraction is  $(5.61 \pm 0.05) \times 10^{-3}$  by  $D_s^+ \to \mu^+ \nu_{\mu}$ . The branch fraction is  $(5.49 \pm 0.06) \times 10^{-2}$  by  $D_s^+ \to \tau^+ \nu_{\tau}$ .
- Statistical sensitivity of BF is 2.7 times better than BESIII.

Results of  $D_s^+ \rightarrow l^+ \nu_l$ 

**Combined results from these BESIII measurements and PDG values** 



- > Optimized response of tracking efficiency for low momentum charged pion is 72.19% at  $p_T = 0.1 \text{GeV}/c$ .
- > Detection efficiency of photons is 97.32% at 0.2 GeV.

ETM(2+1+1) FMILC(2+1+1 FLAG19(2+1+	PRD91(2015)054507 ) PRD98(2018)074512 1) arXiv:1902.08191 [hep-lat]	247.2±4.1 ► 249.9±0.4 249.9±0.5	
HFLAV18	EPJC81(2021)226	254.5±3.2	
CLEO	PRD79(2009)052002, t <sub>e</sub> ∨	251.8±11.2±5.3	-#
CLEO	PRD80(2009)112004, $\tau_{p}V$	257.0±13.3±5.0	-
CLEO	PRD79(2009)052001, $t_{\pi}V$ PRD82(2010)091103 $\tau_{\pi}V$	277.1±17.5±4.0	
Babar Ballo	IHEP09(2013)139. T V	244.0 ±8.0 ±12.0	
BESHI 0 482 f	-1 PRD94(2016)072004. μV	245.5+17.8+5.1	-
CLEO	PRD79(2009)052001, µv	256.7±10.2±4.0	<u> </u>
BaBar	PRD82(2010)091103, µV	264.9±8.4±7.6	• •
Belle	JHEP09(2013)139, μν	248.8±6.6±4.8	
BESIII 3.19 fb	I PRL122(2019)071802, μν	253.0±3.7±3.6	E .
BESIII 6.32 fb	arXiv:2102.11734 [hep-ex], μν	249.8±3.0±3.8	
BESIII 6.32 fb	arXiv:2102.11734 [hep-ex], $\tau_{\pi}$	249.7±6.0±4.2 <b>H</b> ●	
BESIII 6.32 fb	arXiv:2105.07176 [nep-ex], 1,	251.6±5.9±4.9	
STCF 0.1 ab	arXiv:2100.00004v1 [hep-ex],	VeV 200.0 ±0.0	
SICF 0.1 ab	ar Arv. 2107.14707 [hep-ex], p	400.0 - 9.4	. P
I I E			i i s
0	100	200	300
0	100 f <sub>Ds</sub> * [Me'	200 V]	300
CKMFitter	100 f <sub>D<sup>+</sup><sub>s</sub></sub> [Me <sup>+</sup>	200 V]	300 
CKMFitter ETM(2+1+1)	100 f <sub>D<sup>+</sup></sub> [Me <sup>1</sup> PJC41(2005)1 PRD91(2015)054507	200 V] 0.973394±0.000096	300 300
O CKMFitter ETM(2+1+1) FMILC(2+1+1)	100 f <sub>D</sub> <sup>+</sup> [Me <sup>1</sup> PJC41(2005)1 PRD91(2015)054507 PRD98(2018)074512	200 V] 0.973394±0.000096 1.014±0.024 1.000±0.016±0.003	30C
CKMFitter ETM(2+1+1) FMILC(2+1+1) FLAG19(2+1+1)	100 f <sub>D</sub> <sup>+</sup> [Me <sup>1</sup> PJC41(2005)1 PRD91(2015)054507 PRD98(2018)074512 arXiv:1902.08191 [hep-lat]	<b>200</b> <b>V</b> ] 0.973394±0.000096 1.014±0.024 1.000±0.016±0.003 1.004±0.002±0.016	30C
CKMFitter ETM(2+1+1) FMILC(2+1+1) FLAG19(2+1+1) HFLAV18	100 f <sub>D<sub>s</sub></sub> [Me <sup>v</sup> PJC41(2005)1 PRD91(2015)054507 PRD98(2018)074512 arXiv:1902.08191 [hep-lat] EPJC81(2021)226	200 V] 0.973394±0.000096 1.014±0.024 1.000±0.016±0.003 1.004±0.002±0.016 0.969±0.01	300
0 CKMFitter ETM(2+1+1) FMILC(2+1+1) FLAG19(2+1+1) HFLAV18 CLEO-c	100 f <sub>D<sub>s</sub></sub> [Me <sup>×</sup> PJC41(2005)1 PRD91(2015)054507 PRD98(2018)074512 arXiv:1902.08191 [hep-lat] EPJC81(2021)226 PRD79(2009)052002, τ <sub>e</sub> V	200 V] 0.973394±0.000096 1.014±0.024 1.000±0.016±0.003 1.004±0.002±0.016 0.969±0.01 0.988±0.044±0.022	300
0 CKMFitter ETM(2+1+1) FMILC(2+1+1) FLAG19(2+1+1) HFLAV18 CLEO-c CLEO-c CLEO-c	100 f <sub>D</sub> <sup>+</sup> [Me <sup>N</sup> PJC41(2005)1 PRD91(2015)054507 PRD98(2018)074512 arXiv:1902.08191 [hep-lat] EPJC81(2021)226 PRD79(2009)052002, τ <sub>e</sub> V PRD80(2009)112004, τ <sub>ρ</sub> V	200 V] 0.973394±0.000096 1.014±0.024 1.000±0.016±0.003 1.004±0.002±0.016 0.969±0.01 0.988±0.044±0.022	300
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0 CKMFitter ETM(2+1+1) FMILC(2+1+1) FLAG19(2+1+1) HFLAV18 CLEO-c CLEO-c CLEO-c BaBar Belle	$\begin{array}{c} 100\\ f_{D_s^+} \text{[Me']}\\ \end{array}$	200 V] 0.973394±0.000096 1.014±0.024 1.014±0.024 1.000±0.016±0.003 1.004±0.002±0.016 0.969±0.01 0.988±0.044±0.022 1.009±0.052±0.021 1.088±0.069±0.018 0.956±0.036±0.056	
CKMFitter ETM(2+1+1) FMILC(2+1+1) FLAG19(2+1+1) HFLAV18 CLEO-c CLEO-c CLEO-c BaBar Belle BESIII 0.482 fb <sup>-1</sup>	100 $f_{D_s^+}$ [Me <sup>N</sup> PJC41(2005)1 PRD91(2015)054507 PRD98(2018)074512 arXiv:1902.08191 [hep-lat] EPJC81(2021)226 PRD79(2009)052002, τ <sub>e</sub> V PRD80(2009)112004, τ <sub>p</sub> V PRD80(2009)112004, τ <sub>p</sub> V PRD79(2009)052001, τ <sub>π</sub> V PRD79(2009)052001, τ <sub>π</sub> V PRD82(2010)091103, τ <sub>e,µ,π</sub> V JHEP09(2013)139, τ <sub>e,µ,π</sub> V PRD94(2016)072004, µV	200 V] 0.973394±0.000096 1.014±0.024 1.000±0.016±0.003 1.004±0.002±0.016 0.969±0.01 0.988±0.044±0.022 H 1.009±0.052±0.021 H 1.088±0.069±0.018 0.956±0.036±0.056 H 1.025±0.019±0.029 0.944±0.063±0.027 H	
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- $> \pi/k$  mis-identification rate of 1% with the PID performance.
- >  $\pi/\mu$  mis-identification rate of 3% with the MUD performance.
- > Detection efficiency for ST is increased by a factor of 1.1 to 1.2.
- > Efficiency for selecting  $D_s^+ \rightarrow \mu^+ \nu_{\mu}$  is increased by a factor of 1.3.

BESIII 6.32 fb STCF 1.0 ab<sup>-1</sup> STCF 0.1 ab<sup>-1</sup> -0.5 -1.5 - 1 0.5 0 1.5 -2  $|V_{cs}|$  $f_{D_s^+} = 255.8 \pm 0.4 \text{ MeV}$  $\tau^+ \nu_{\tau}$  $f_{D_s^+} = 256.3 \pm 0.5 \text{ MeV}$  $\mu^+ \nu_{\mu}$  $|V_{cs}| = 0.998 \pm 0.003$  $|V_{cs}| = 0.996 \pm 0.002$  $R_{\tau/\mu} = \frac{\overline{\Gamma} (D_s^+ \to \tau^+ \nu_{\tau})}{\overline{\Gamma} (D_s^+ \to \mu^+ \nu_{\mu})} = 9.79 \pm 0.05$ 

## Summary

- Unprecedented precision to be achieved at STCF will provide a precise calibration of QCD and a rigorous test of SM.
- Accuracy of LFU test can be improved obviously experimentally, which makes it promise to search for the new physics beyond SM.